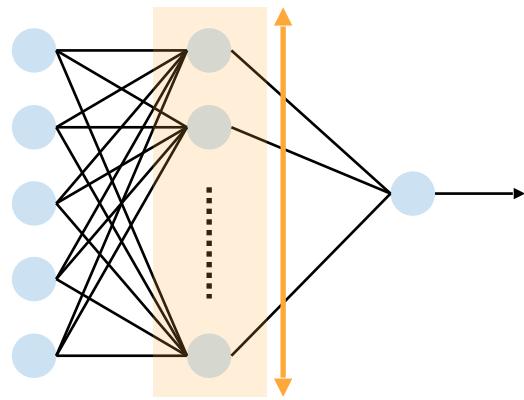


합성곱 신경망

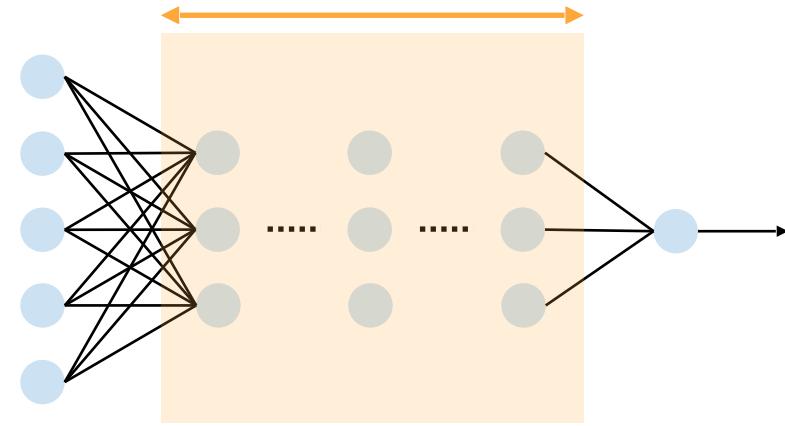
Convolutional Neural Network

정우일

5.1 합성곱 신경망의 발달 배경



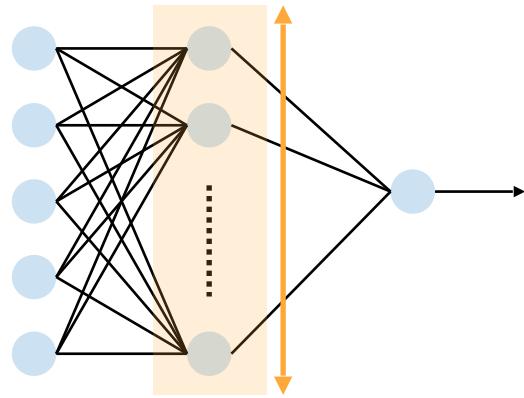
Single Hidden Layer Perceptron



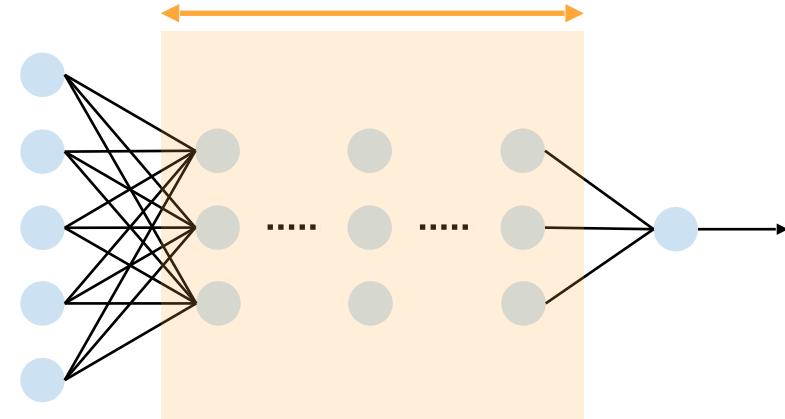
Multi Hidden Layer Perceptron

보편 근사 정리 (Universal Approximation Theorem)

5.1 합성곱 신경망의 발달 배경



Single Hidden Layer Perceptron

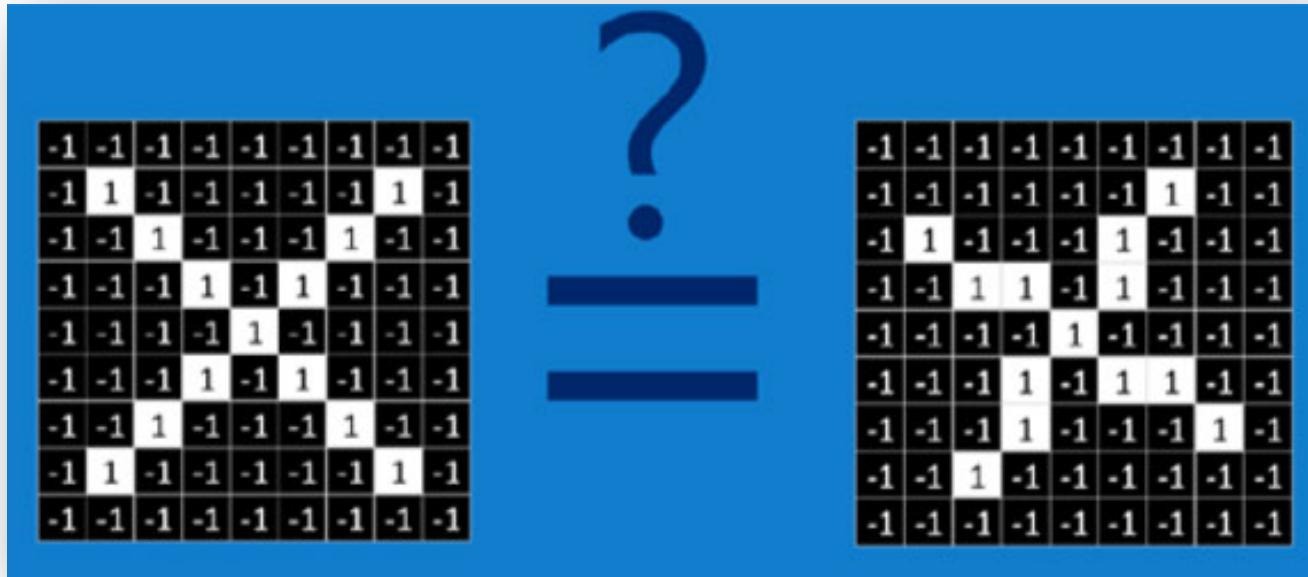


Multi Hidden Layer Perceptron

인공 신경망은 실수 공간에서 연속하는 모든 함수를 근사 가능

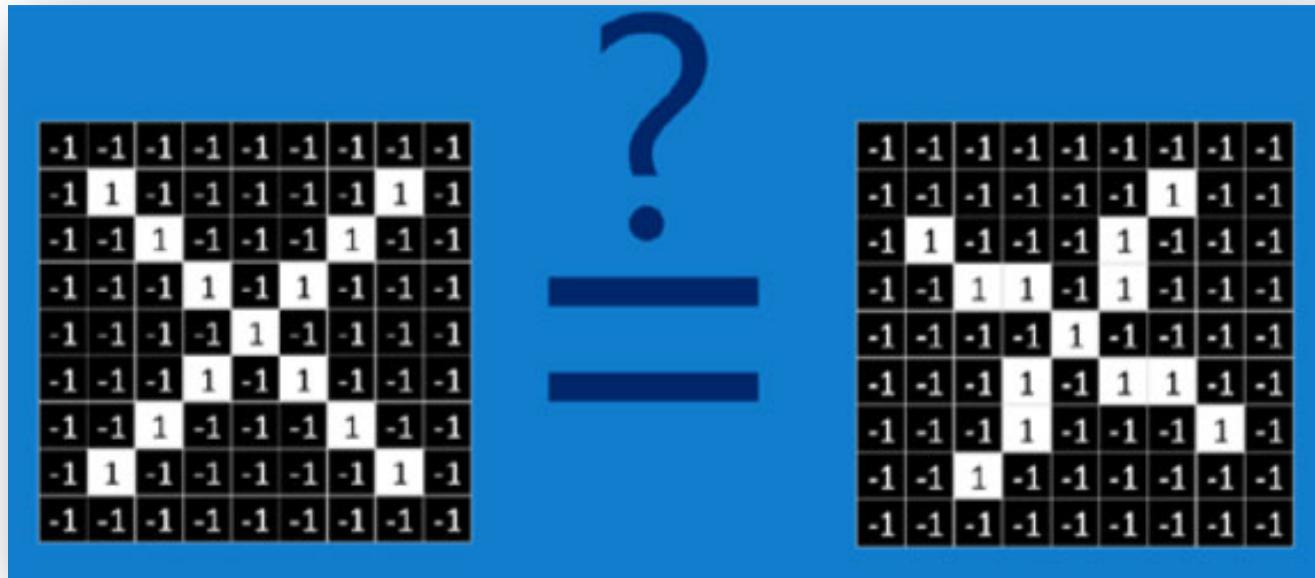
5.1 합성곱 신경망의 발달 배경

인공 신경망만으로 이미지를 분류할 수 있을까?



5.1 합성곱 신경망의 발달 배경

인공 신경망만으로 이미지를 분류할 수 있을까?



같은 위치의 픽셀 값이 서로 일치하지 않으면, 다른 이미지로 인식

5.1 합성곱 신경망의 발달 배경

동물의 시각 뉴런 연구와 CNN의 탄생

- [Kunihiko Fukushima](#)
- [Yann LeCun](#)



국소적인 영역을 보고
단순한 패턴에 자극을 받음.



넓은 영역을 보고
복잡한 패턴에 자극을 받음.

동물의 시각 체계는 단순 세포와 복잡 세포의 레이어로 이루어짐

5.1 합성곱 신경망의 발달 배경

동물의 시각 뉴런 연구와 CNN의 탄생

- [Kunihiko Fukushima](#)
- [Yann LeCun](#)



국소적인 영역을 보고
단순한 패턴에 자극을 받음.



넓은 영역을 보고
복잡한 패턴에 자극을 받음.

즉, 점이 아닌 영역을 보고, 패턴을 인식하는 과정의 연속

5.1 합성곱 신경망의 발달 배경

LeNet-5의 구조

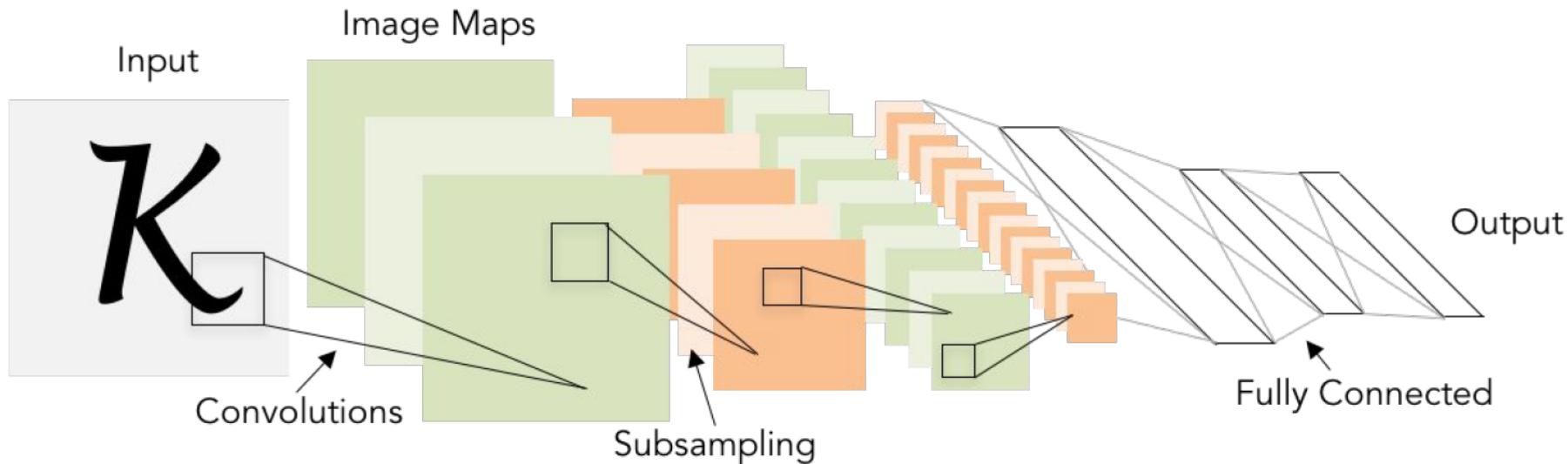


Illustration of LeCun et al. 1998 from CS231n 2017 Lecture 1

[Gradient-based learning applied to document recognition](#)
[LeCun, Bottou, Bengio, Haffner 1998]

[CS231n\(2017\)](#)

5.2 합성곱 연산 과정

-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1	-1
-1	-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1



1	-1	-1
-1	1	-1
-1	-1	1

=

0.77	-0.11	0.11	0.33	0.55	-0.11	0.33
-0.11	1.00	-0.11	0.33	-0.11	0.11	-0.11
0.11	-0.11	1.00	-0.33	0.11	-0.11	0.55
0.33	0.33	-0.33	0.55	-0.33	0.33	0.33
0.55	-0.11	0.11	-0.33	1.00	-0.11	0.11
-0.11	0.11	-0.11	0.33	-0.11	1.00	-0.11
0.33	-0.11	0.55	0.33	0.11	-0.11	0.77

5.2 합성곱 연산 과정

이미지

-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1

필터

1	-1	-1
-1	1	-1
-1	-1	1

피처 맵

0.77	-0.11	0.11	0.33	0.55	-0.11	0.33
-0.11	1.00	-0.11	0.33	-0.11	0.11	-0.11
0.11	-0.11	1.00	-0.33	0.11	-0.11	0.55
0.33	0.33	-0.33	0.55	-0.33	0.33	0.33
0.55	-0.11	0.11	-0.33	1.00	-0.11	0.11
-0.11	0.11	-0.11	0.33	-0.11	1.00	-0.11
0.33	-0.11	0.55	0.33	0.11	-0.11	0.77



=

$$O = \text{floor}\left(\frac{I - F}{S} + 1\right)$$

O : Output Size

I : Input Size

F : Filter Size

S : Stride

9×9

Input Size = 9

3×3

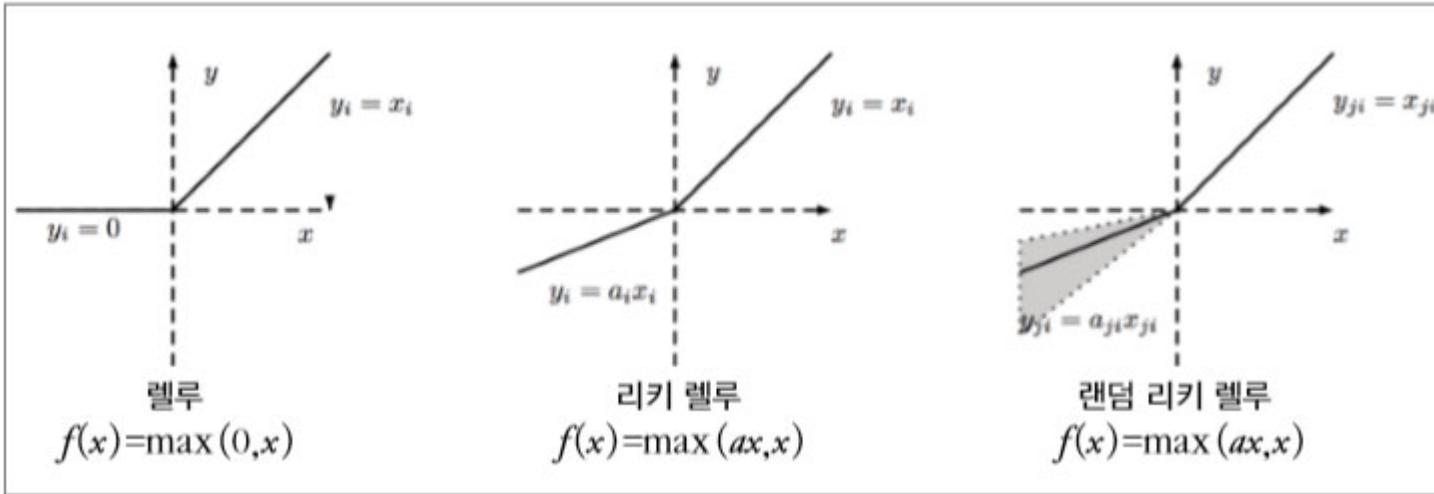
Filter Size = 3

7×7

Output Size = 7

5.2 합성곱 연산 과정

다양한 ReLU 함수

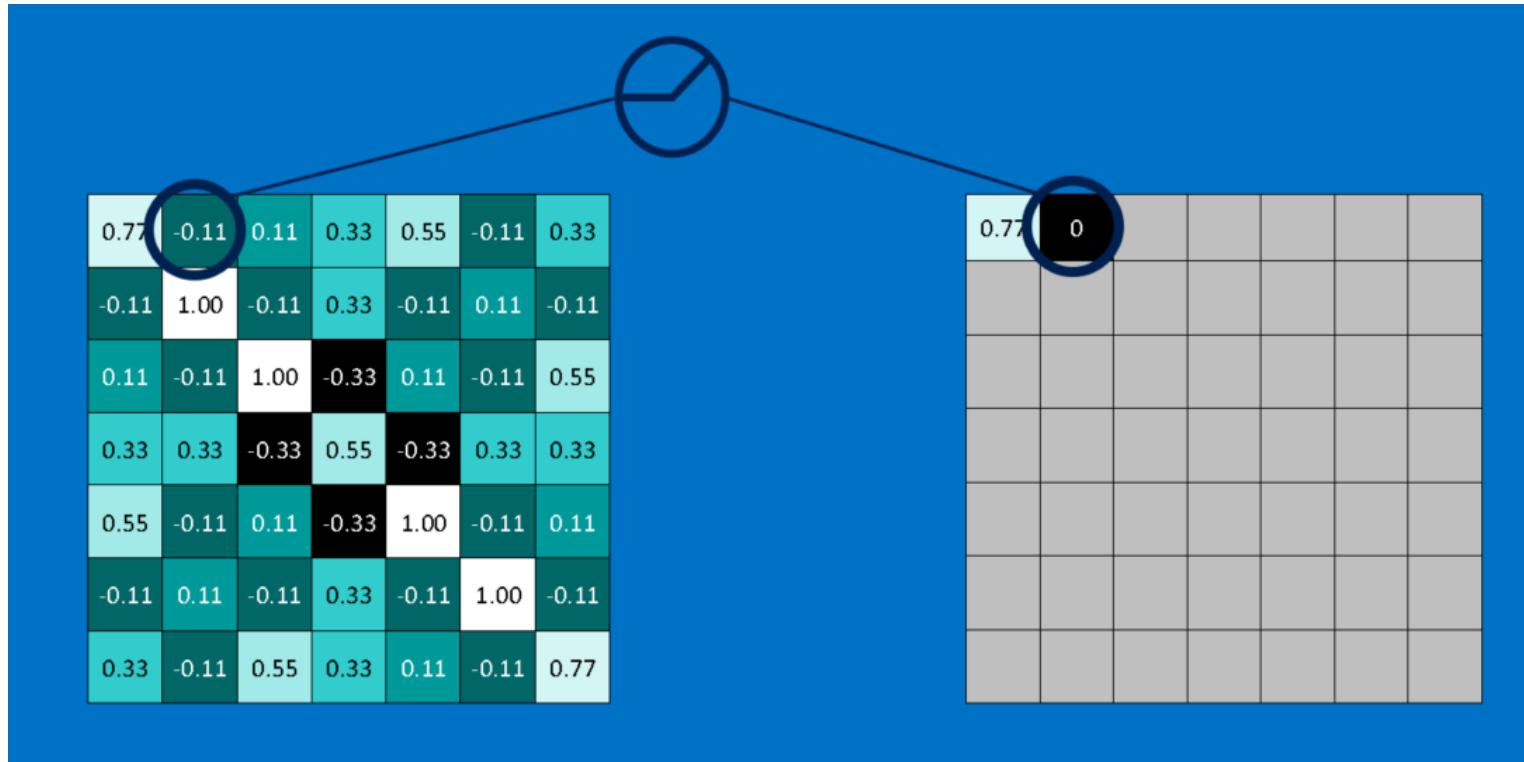


*다잉뉴런(Dying Neuron) : 어떠한 입력값이 들어와도 활성화 값이 0이 되는 현상.

예) 입력값(X)이 $-1 \sim 1$ 사이로 정규화되어 있고, $W = -3, b = -5$ 일 경우
 $WX+b$ 는 $-2 \sim -8$ 로 음수값을 가지게 되어, 활성화 값은 0이 됨.

5.2 합성곱 연산 과정

피처 맵에 ReLU 함수 적용



5.3 패딩과 풀링

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

3x3 filter, applied with stride 1

pad with 1 pixel border => what is the output?

7x7 output!

$$O = \text{floor}\left(\frac{I - F}{S} + 1\right) \rightarrow$$

O : Output Size

I : Input Size

F : Filter Size

S : Stride

$$O = \text{floor}\left(\frac{I - F + 2P}{S} + 1\right)$$

O : Output Size

I : Input Size

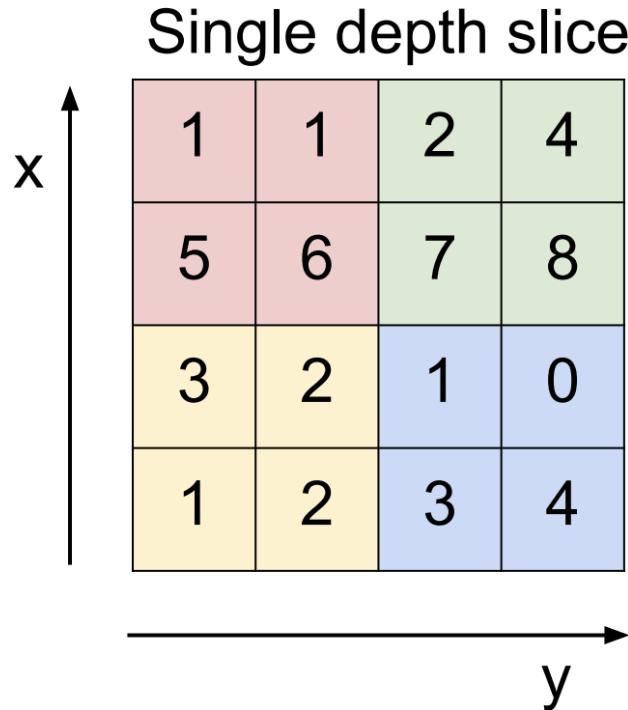
F : Filter Size

P : Padding Size

S : Stride

5.3 패딩과 풀링

MAX POOLING



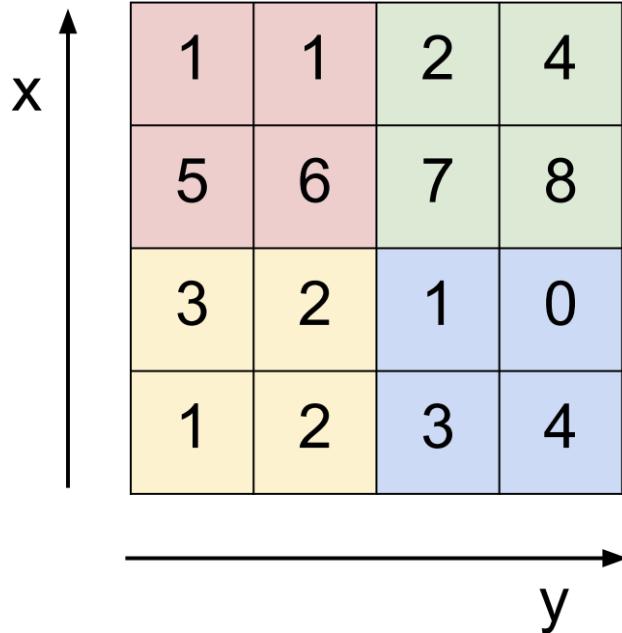
max pool with 2x2 filters
and stride 2

6	8
3	4

5.3 패딩과 풀링

AVERAGE POOLING

Single depth slice

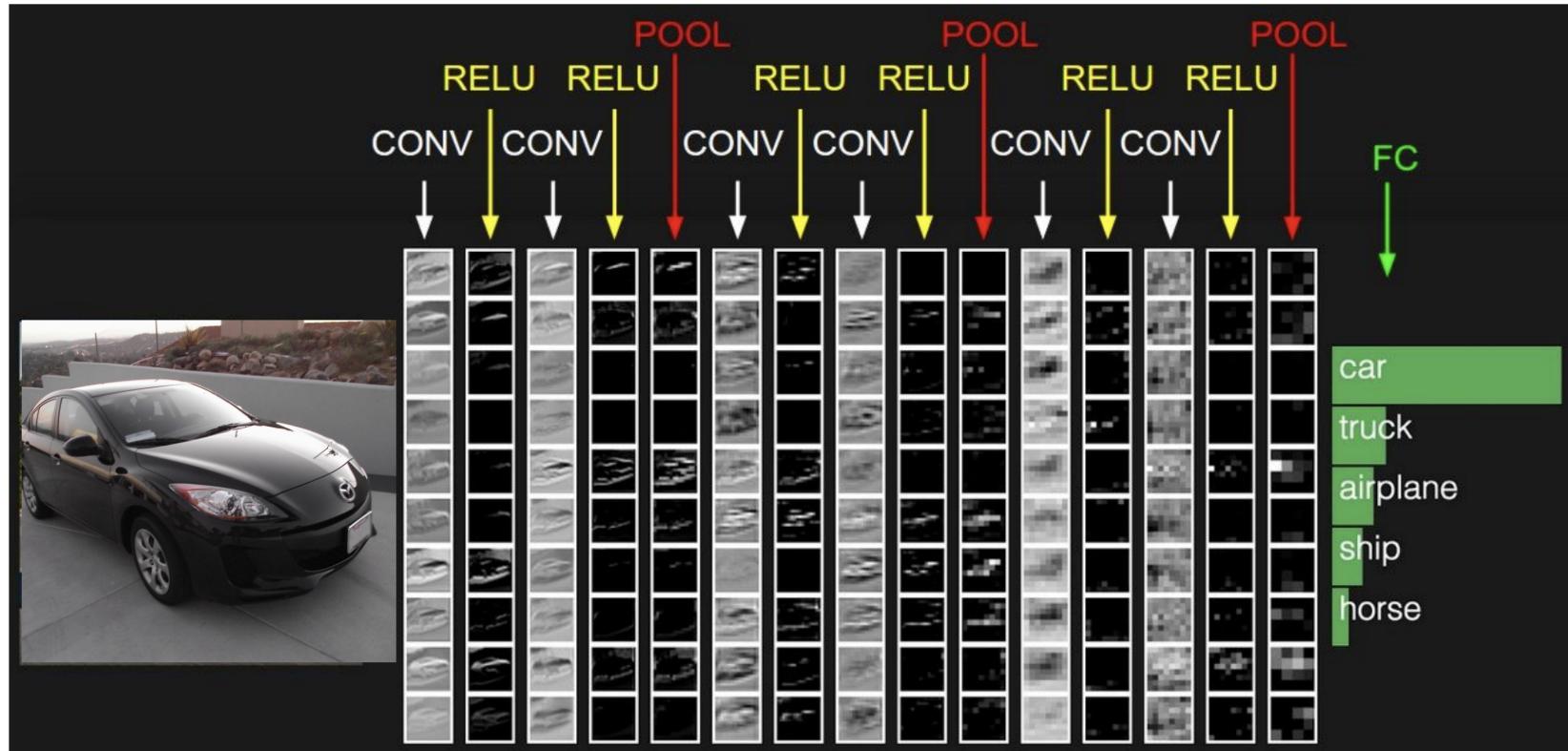


average pool with
2x2 filters and stride 2

The result of the average pooling operation is a 2x2 output tensor. The values are calculated as the average of the 2x2 input blocks:

3.25	5.25
2	2

5.3 패딩과 풀링



5.4 모델의 3차원적 이해

0	0	0	0	0	0	...
0	156	155	156	158	158	...
0	153	154	157	159	159	...
0	149	151	155	158	159	...
0	146	146	149	153	158	...
0	145	143	143	148	158	...
...

Input Channel #1 (Red)

0	0	0	0	0	0	...
0	167	166	167	169	169	...
0	164	165	168	170	170	...
0	160	162	166	169	170	...
0	156	156	159	163	168	...
0	155	153	153	158	168	...
...

Input Channel #2 (Green)

0	0	0	0	0	0	...
0	163	162	163	165	165	...
0	160	161	164	166	166	...
0	156	158	162	165	166	...
0	155	155	158	162	167	...
0	154	152	152	157	167	...
...

Input Channel #3 (Blue)

-1	-1	1
0	1	-1
0	1	1

Kernel Channel #1



308

1	0	0
1	-1	-1
1	0	-1

Kernel Channel #2



-498

0	1	1
0	1	0
1	-1	1

Kernel Channel #3



164

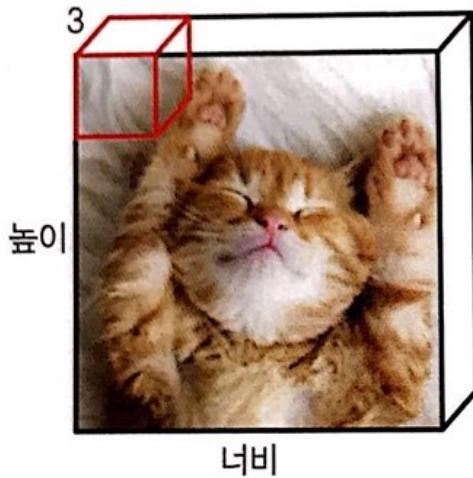
$$+ \quad + 1 = -25$$

$$\begin{array}{c} \uparrow \\ \text{Bias} = 1 \end{array}$$

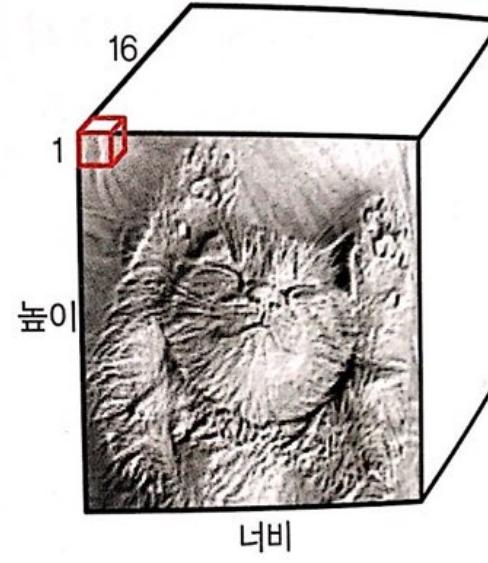
Output

-25					...
					...
					...
					...
...

5.4 모델의 3차원적 이해



합성곱
→
3x3 필터
스트라이드 1
패딩 1
채널 16

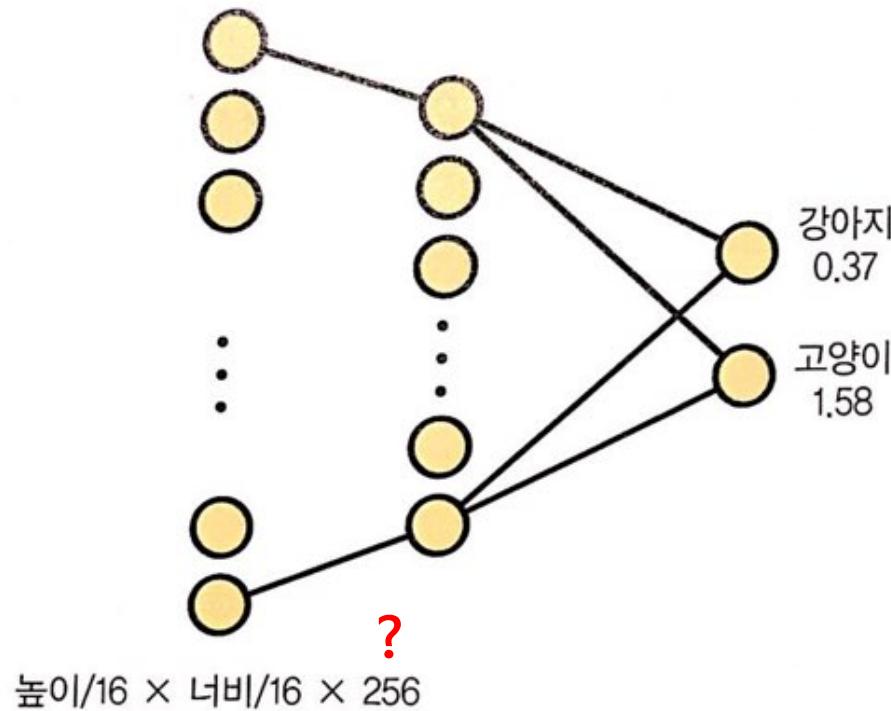
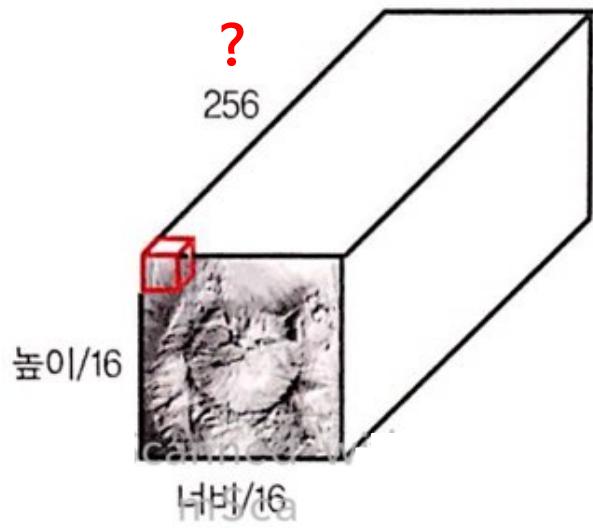


5.4 모델의 3차원적 이해



5.4 모델의 3차원적 이해

Q. 풀링 4회 수행 후 채널이 증가한 이유?



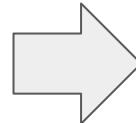
5.5 소프트맥스 함수

One-Hot Encoding

Target	Dog	Cat
Dog	1	0
Cat	0	1

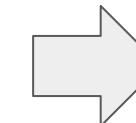


Softmax Function



Feed Forward Output

Dog	Cat
2	7



Softmax Output

Dog	Cat
0.01	0.99

```
import numpy as np  
  
y = np.array([2, 7])  
exp_y = np.exp(y)  
exp_y/exp_y.sum()
```

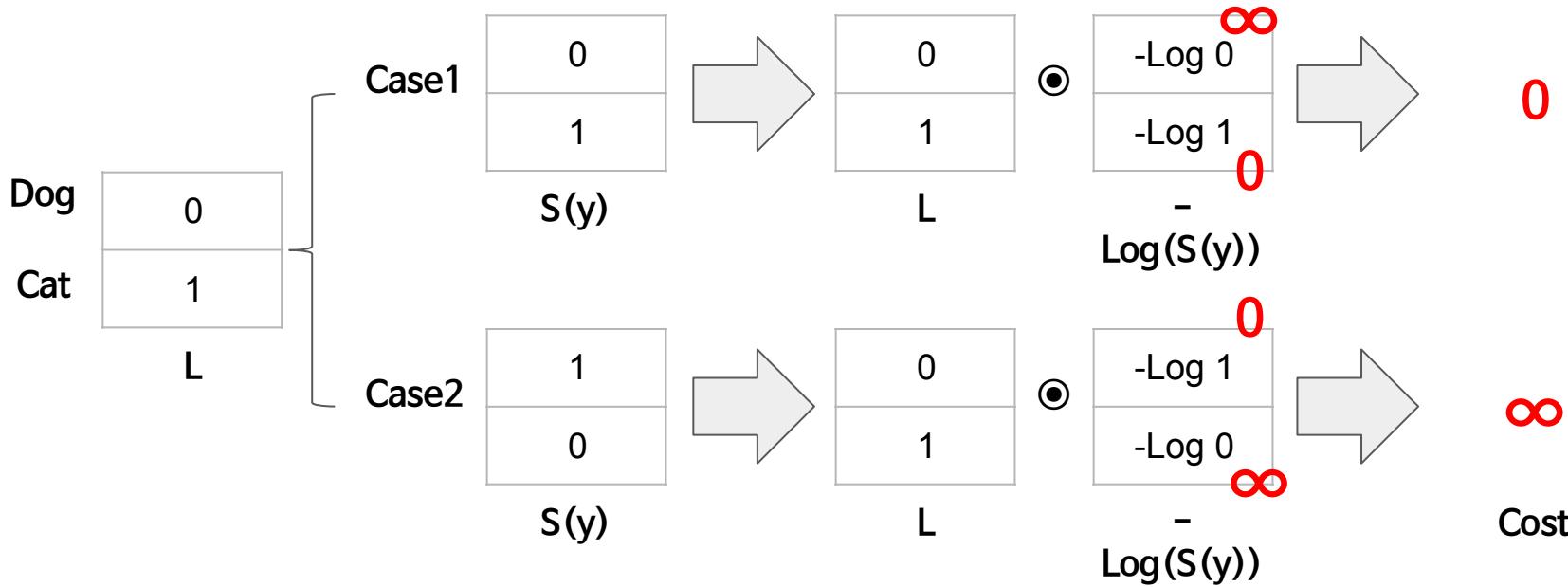
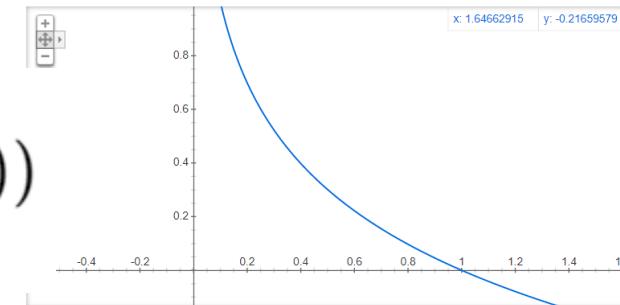
```
array([0.00669285, 0.99330715])
```

5.5 소프트맥스 함수

Cross Entropy

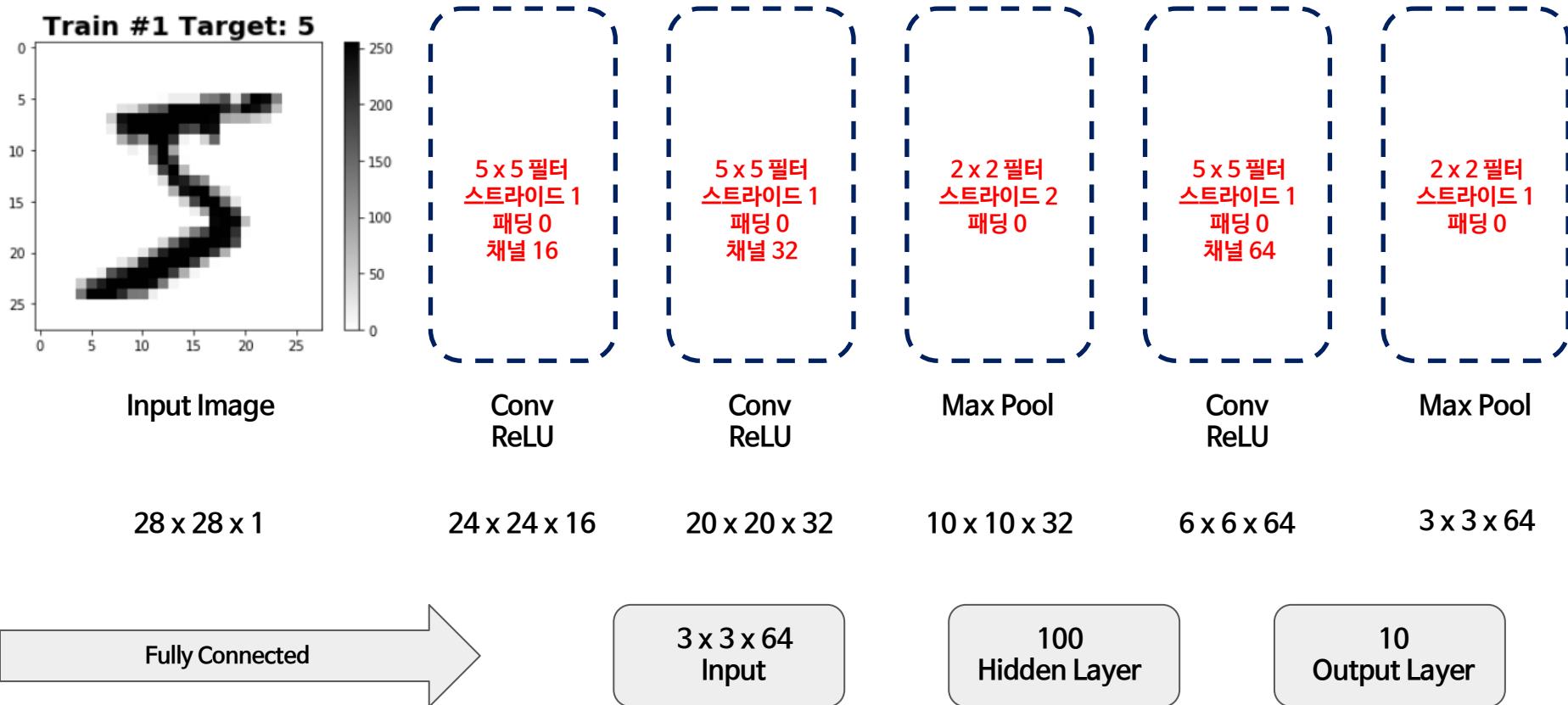
$$D(S, L) = - \sum_{j=1}^n L_j \log(S(y_j))$$

-log(x) 그래프



5.6 모델 구현, 학습 및 결과 확인

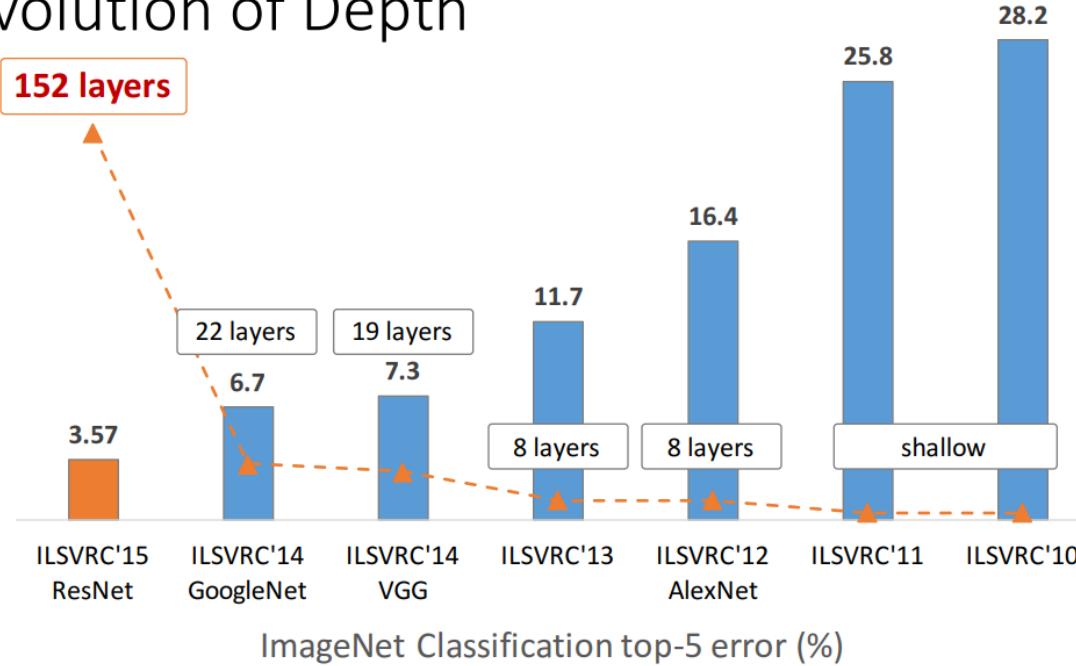
[Code](#)



5.7 유명한 모델들과 원리



Revolution of Depth



Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". CVPR 2016.

[https://icml.cc/2016/tutorials/
icml2016_tutorial_deep_residual_networks_kaiminghe.pdf](https://icml.cc/2016/tutorials/icml2016_tutorial_deep_residual_networks_kaiminghe.pdf)

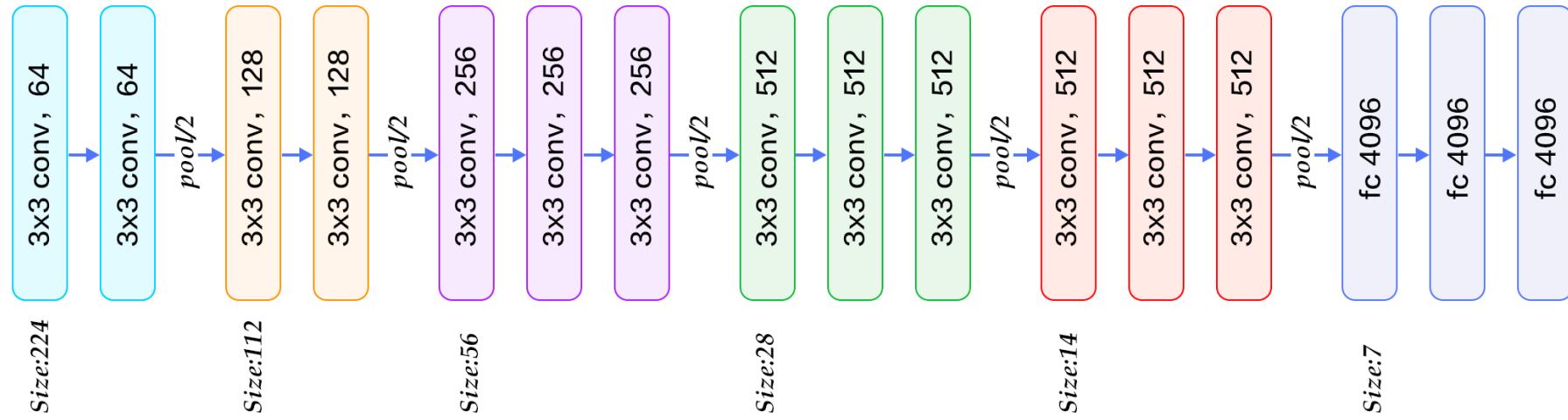
5.7 유망한 모델들과 원리

Code

VGGNet

<https://arxiv.org/pdf/1409.1556.pdf>

*2014 ILSVRC 2nd place



3x3 Conv, 2x2 MaxPool, 1 Padding, 1 Stride

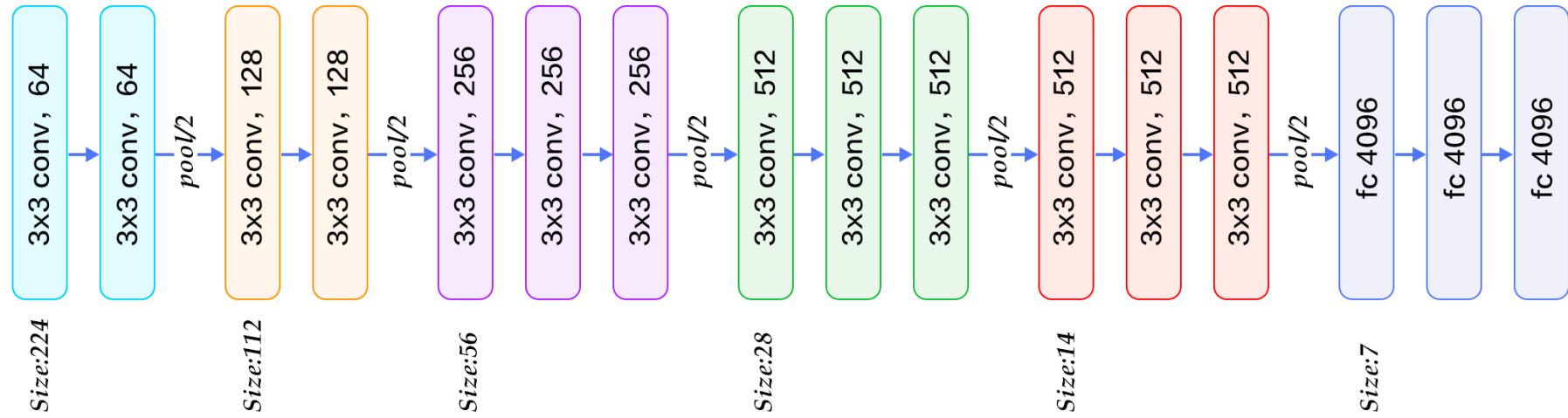
5.7 유명한 모델들과 원리

Code

VGGNet

<https://arxiv.org/pdf/1409.1556.pdf>

*2014 ILSVRC 2nd place



즉, Pooling 연산 후에만 이미지 사이즈가 반으로 줄어듦

5.7 유명한 모델들과 원리

Code

VGGNet

<https://arxiv.org/pdf/1409.1556.pdf>

*2014 ILSVRC 2nd place

컨볼루션 연산이 2번 연속하는 경우

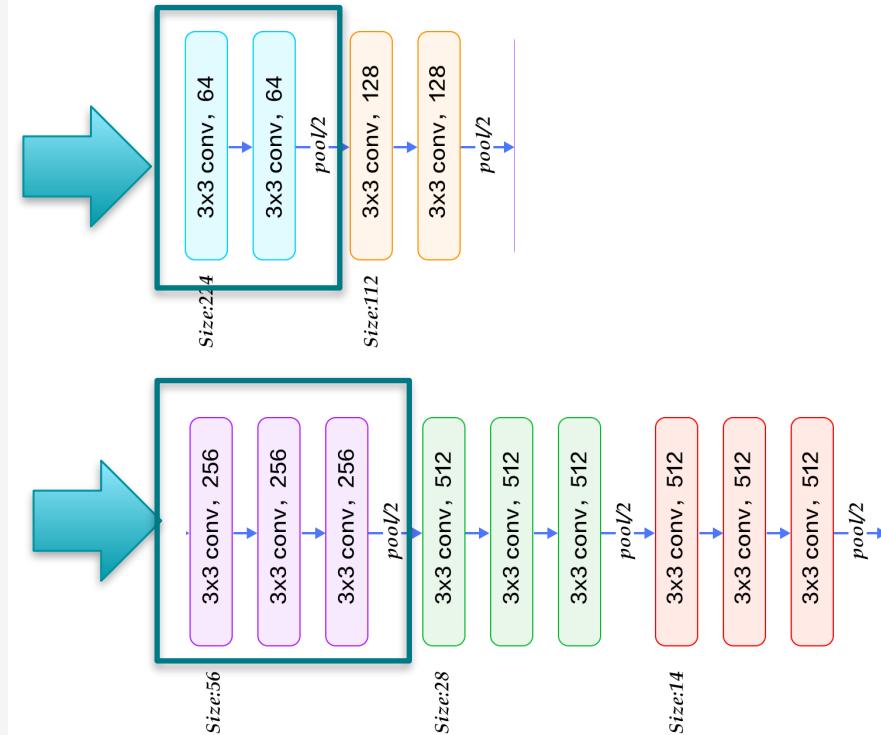
컨볼루션-활성화함수-컨볼루션-활성화함수-풀링

```
def conv_2_block(in_dim,out_dim):
    model = nn.Sequential(
        nn.Conv2d(in_dim,out_dim,kernel_size=3,padding=1),
        nn.ReLU(),
        nn.Conv2d(out_dim,out_dim,kernel_size=3,padding=1),
        nn.ReLU(),
        nn.MaxPool2d(2,2)
    )
    return model
```

컨볼루션 연산이 3번 연속하는 경우

컨볼루션-활성화함수-컨볼루션-활성화함수-컨볼루션-활성화함수-풀링

```
def conv_3_block(in_dim,out_dim):
    model = nn.Sequential(
        nn.Conv2d(in_dim,out_dim,kernel_size=3,padding=1),
        nn.ReLU(),
        nn.Conv2d(out_dim,out_dim,kernel_size=3,padding=1),
        nn.ReLU(),
        nn.Conv2d(out_dim,out_dim,kernel_size=3,padding=1),
        nn.ReLU(),
        nn.MaxPool2d(2,2)
    )
    return model
```



5.7 유명한 모델들과 원리

[Code](#)

VGGNet

<https://arxiv.org/pdf/1409.1556.pdf>

```
class VGG(nn.Module):
    def __init__(self, base_dim, num_classes=2):
        super(VGG, self).__init__()
        self.feature = nn.Sequential(
            conv_2_block(3,base_dim),
            conv_2_block(base_dim,2*base_dim),
            conv_3_block(2*base_dim,4*base_dim),
            conv_3_block(4*base_dim,8*base_dim),
            conv_3_block(8*base_dim,8*base_dim),
        )
        self.fc_layer = nn.Sequential(
            nn.Linear(8*base_dim * 7 * 7, 100),
            nn.ReLU(True),
            #nn.Dropout(),
            nn.Linear(100, 20),
            nn.ReLU(True),
            #nn.Dropout(),
            nn.Linear(20, num_classes),
        )
    def forward(self, x):
        x = self.feature(x)
        x = x.view(x.size(0), -1)
        x = self.fc_layer(x)
        return x
```

입력 이미지 RGB 채널 = 3

Conv 채널 = 64

Conv 채널 = 512

최종 이미지 사이즈 = 7 x 7

FC Hidden Layer 1 노드 수 = 100

FC Hidden Layer 2 노드 수 = 20

Output Layer 노드 수 = 2 (dog or cat)

*2014 ILSVRC 2nd place

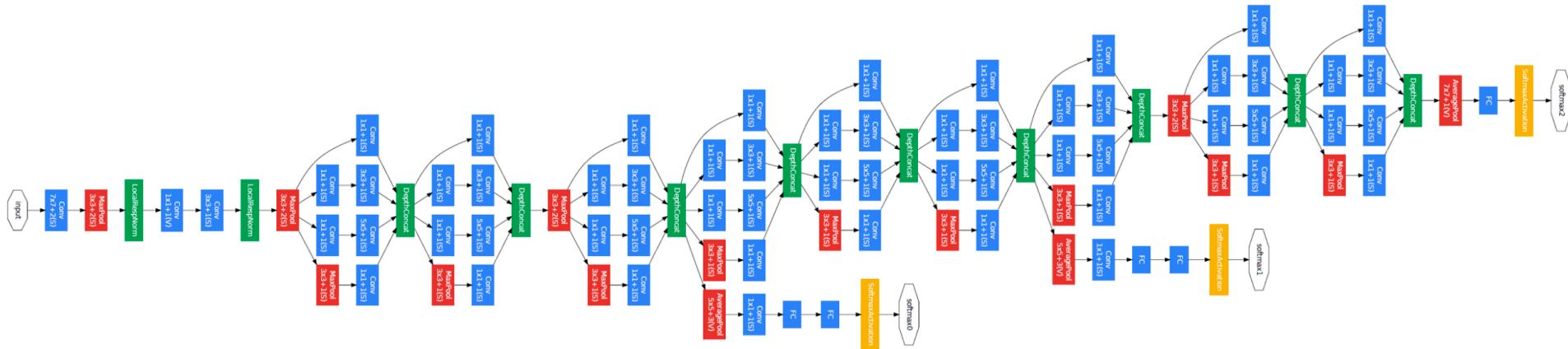
5.7 유명한 모델들과 원리

Code

GoogLeNet

<https://arxiv.org/pdf/1409.4842.pdf>

*2014 ILSVRC 1st place



A.k.a 인셉션 네트워크

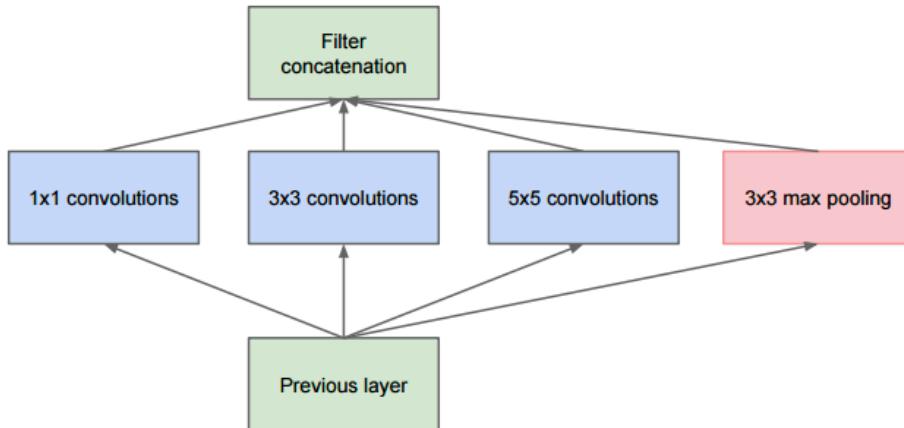
5.7 유명한 모델들과 원리

[Code](#)

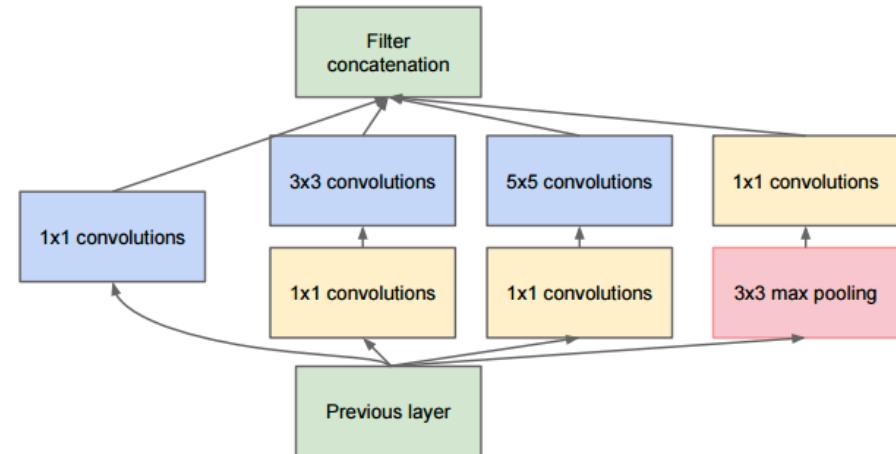
GoogLeNet

<https://arxiv.org/pdf/1409.4842.pdf>

*2014 ILSVRC 1st place



(a) Inception module, naïve version



(b) Inception module with dimension reductions

1x1 Conv를 추가하면 메모리 효율성이 높아짐

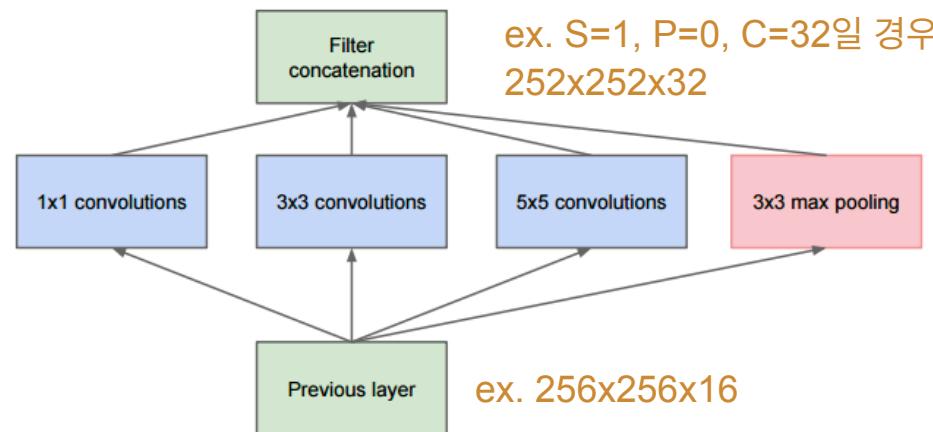
5.7 유명한 모델들과 원리

[Code](#)

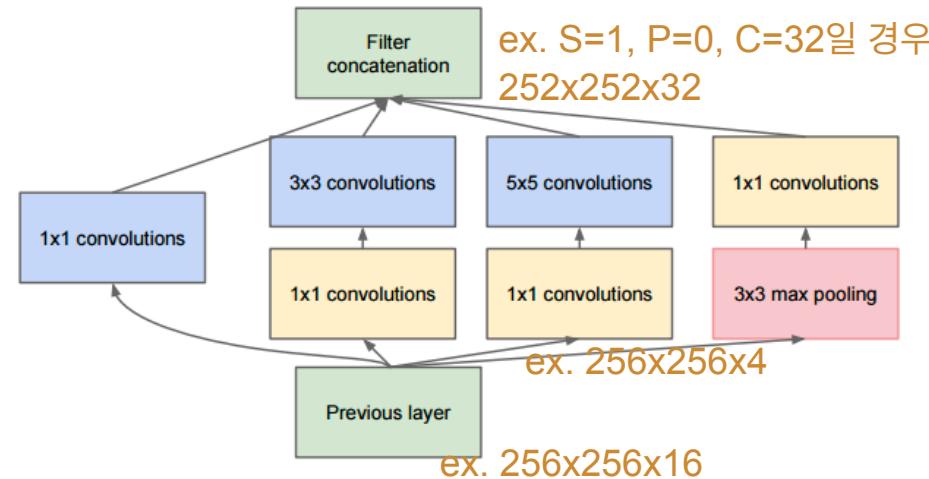
GoogLeNet

<https://arxiv.org/pdf/1409.4842.pdf>

*2014 ILSVRC 1st place



(a) Inception module, naïve version



(b) Inception module with dimension reductions

직전 텐서의 가로, 세로 사이즈는 유지하면서 채널 수를 줄일 수 있음

5.7 유명한 모델들과 원리

Code

GoogLeNet

<https://arxiv.org/pdf/1409.4842.pdf>

*2014 ILSVRC 1st place

5.7 유명한 모델들과 원리

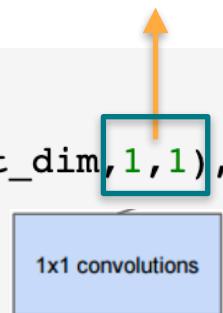
[Code](#)

GoogLeNet

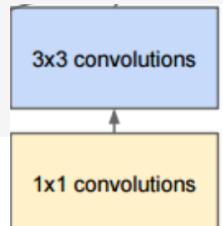
<https://arxiv.org/pdf/1409.4842.pdf>

```
def conv_1(in_dim,out_dim):  
    model = nn.Sequential(  
        nn.Conv2d(in_dim,out_dim,1,1),  
        nn.ReLU(),  
    )  
    return model
```

커널(필터)=1, 스트라이드=1, (패딩=0)

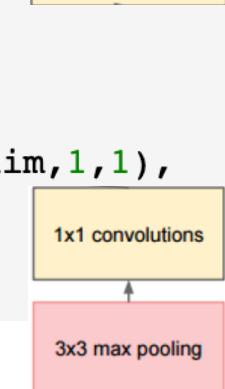
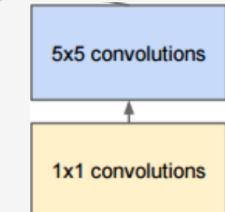


```
def conv_1_3(in_dim,mid_dim,out_dim):  
    model = nn.Sequential(  
        nn.Conv2d(in_dim,mid_dim,1,1),  
        nn.ReLU(),  
        nn.Conv2d(mid_dim,out_dim,3,1,1),  
        nn.ReLU()  
    )  
    return model
```



```
def conv_1_5(in_dim,mid_dim,out_dim):  
    model = nn.Sequential(  
        nn.Conv2d(in_dim,mid_dim,1,1),  
        nn.ReLU(),  
        nn.Conv2d(mid_dim,out_dim,5,1,2),  
        nn.ReLU()  
    )  
    return model
```

```
def max_3_1(in_dim,out_dim):  
    model = nn.Sequential(  
        nn.MaxPool2d(3,1,1),  
        nn.Conv2d(in_dim,out_dim,1,1),  
        nn.ReLU()  
    )  
    return model
```



*2014 ILSVRC 1st place

5.7 유명한 모델들과 원리

[Code](#)

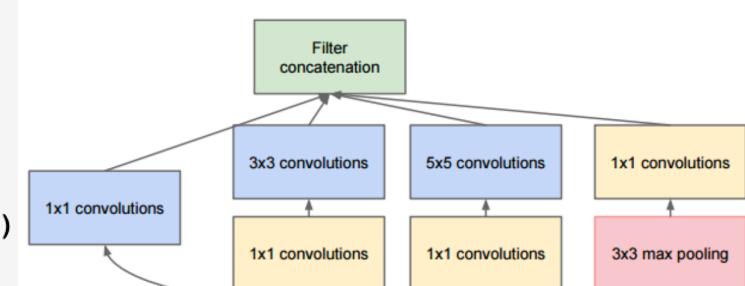
GoogLeNet

<https://arxiv.org/pdf/1409.4842.pdf>

*2014 ILSVRC 1st place

```
class inception_module(nn.Module):
    def __init__(self,in_dim,out_dim_1,mid_dim_3,out_dim_3,mid_dim_5,out_dim_5,pool):
        super(inception_module,self).__init__()
        self.conv_1 = conv_1(in_dim,out_dim_1)
        self.conv_1_3 = conv_1_3(in_dim,mid_dim_3,out_dim_3)
        self.conv_1_5 = conv_1_5(in_dim,mid_dim_5,out_dim_5)
        self.max_3_1 = max_3_1(in_dim,pool)

    def forward(self,x):
        out_1 = self.conv_1(x)
        out_2 = self.conv_1_3(x)
        out_3 = self.conv_1_5(x)
        out_4 = self.max_3_1(x)
        output = torch.cat([out_1,out_2,out_3,out_4],1)
        return output
```



5.7 유명한 모델들과 원리

Code

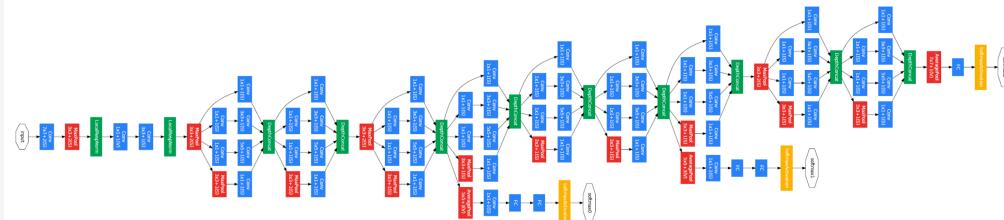
GoogLeNet

<https://arxiv.org/pdf/1409.4842.pdf>

```
class GoogLeNet(nn.Module):
    def __init__(self, base_dim, num_classes=2):
        super(GoogLeNet, self).__init__()
        self.num_classes = num_classes
        self.layer_1 = nn.Sequential(
            nn.Conv2d(3, base_dim, 7, 2, 3),
            nn.MaxPool2d(3, 2, 1),
            nn.Conv2d(base_dim, base_dim * 3, 3, 1, 1),
            nn.MaxPool2d(3, 2, 1),
        )
        self.layer_2 = nn.Sequential(
            inception_module(base_dim * 3, 64, 96, 128, 16, 32, 32),
            inception_module(base_dim * 4, 128, 128, 192, 32, 96, 64),
            nn.MaxPool2d(3, 2, 1),
        )
        self.layer_3 = nn.Sequential(
            inception_module(480, 192, 96, 208, 16, 48, 64),
            inception_module(512, 160, 112, 224, 24, 64, 64),
            inception_module(512, 128, 128, 256, 24, 64, 64),
            inception_module(512, 112, 144, 288, 32, 64, 64),
            inception_module(528, 256, 160, 320, 32, 128, 128),
            nn.MaxPool2d(3, 2, 1),
        )
        self.layer_4 = nn.Sequential(
            inception_module(832, 256, 160, 320, 32, 128, 128),
            inception_module(832, 384, 192, 384, 48, 128, 128),
            nn.AvgPool2d(7, 1),
        )
        self.layer_5 = nn.Dropout2d(0.4)
        self.fc_layer = nn.Linear(1024, self.num_classes)
```

*2014 ILSVRC 1st place

```
def forward(self, x):
    out = self.layer_1(x)
    out = self.layer_2(out)
    out = self.layer_3(out)
    out = self.layer_4(out)
    out = self.layer_5(out)
    out = out.view(batch_size, -1)
    out = self.fc_layer(out)
    return out
```



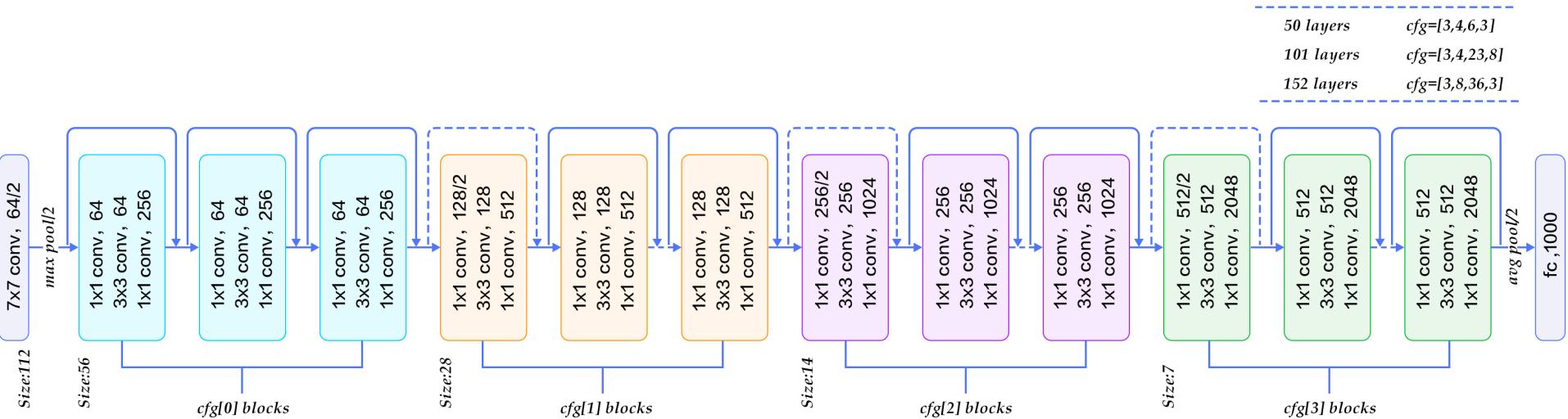
5.7 유명한 모델들과 원리

Code

ResNet

<https://arxiv.org/pdf/1512.03385.pdf>

*2015 ILSVRC 1st place



잔차 학습을 통한 매우 깊은 네트워크 제시

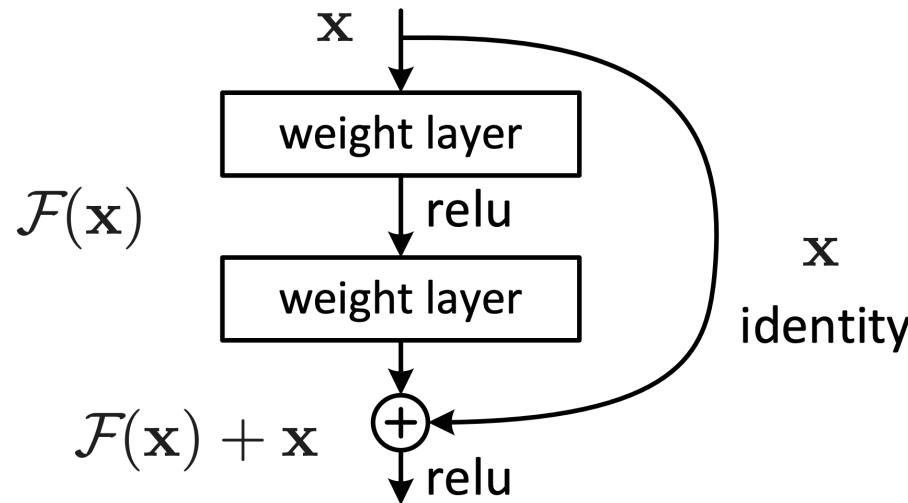
5.7 유명한 모델들과 원리

[Code](#)

ResNet

<https://arxiv.org/pdf/1512.03385.pdf>

*2015 ILSVRC 1st place



Skip Connection

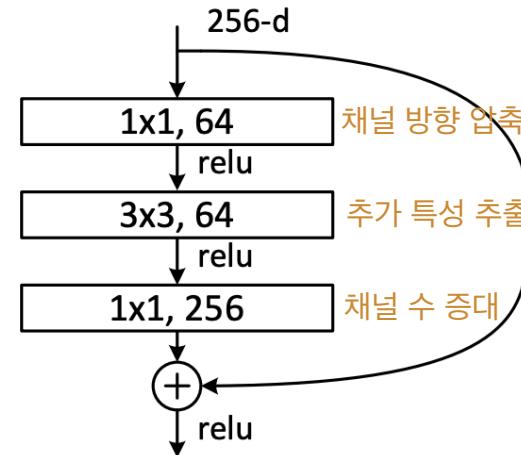
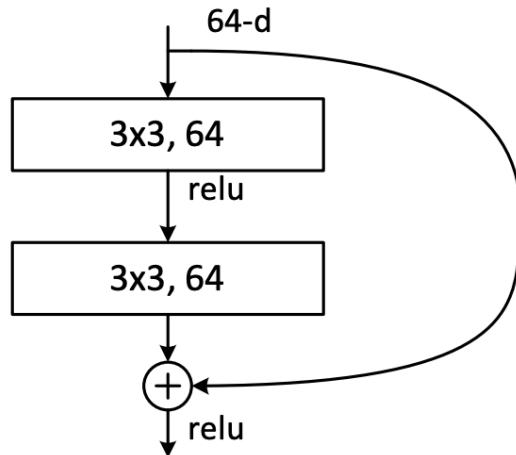
5.7 유명한 모델들과 원리

[Code](#)

ResNet

<https://arxiv.org/pdf/1512.03385.pdf>

*2015 ILSVRC 1st place



Bottleneck Block

5.7 유명한 모델들과 원리

[Code](#)

ResNet

<https://arxiv.org/pdf/1512.03385.pdf>

*2015 ILSVRC 1st place

```
def conv_block_1(in_dim,out_dim,act_fn,stride=1):
    model = nn.Sequential(
        nn.Conv2d(in_dim,out_dim, kernel_size=1, stride=stride),
        act_fn,
    )
    return model

def conv_block_3(in_dim,out_dim,act_fn):
    model = nn.Sequential(
        nn.Conv2d(in_dim,out_dim, kernel_size=3, stride=1, padding=1),
        act_fn,
    )
    return model
```

5.7 유명한 모델들과 원리

[Code](#)

ResNet

<https://arxiv.org/pdf/1512.03385.pdf>

*2015 ILSVRC 1st place

```
class Bottleneck(nn.Module):
    def __init__(self,in_dim,mid_dim,out_dim,act_fn,down=False):
        super(Bottleneck,self).__init__()
        self.down=down
        # 특성지도의 크기가 감소하는 경우
        if self.down:
            self.layer = nn.Sequential(
                conv_block_1(in_dim,mid_dim,act_fn,2),
                conv_block_3(mid_dim,mid_dim,act_fn),
                conv_block_1(mid_dim,out_dim,act_fn),
            )
            self.downsample = nn.Conv2d(in_dim,out_dim,1,2)
        # 특성지도의 크기가 그대로인 경우
        else:
            self.layer = nn.Sequential(
                conv_block_1(in_dim,mid_dim,act_fn),
                conv_block_3(mid_dim,mid_dim,act_fn),
                conv_block_1(mid_dim,out_dim,act_fn),
            )
        # 더하기를 위해 차원을 맞춰주는 부분
        self.dim_equalizer = nn.Conv2d(in_dim,out_dim,kernel_size=1)
```

스트라이드 = 2



```
def forward(self,x):
    if self.down:
        downsample = self.downsample(x)
        out = self.layer(x)
        out = out + downsample
    else:
        out = self.layer(x)
        if x.size() is not out.size():
            x = self.dim_equalizer(x)
        out = out + x
    return out
```

5.7 유명한 모델들과 원리

Code

ResNet

<https://arxiv.org/pdf/1512.03385.pdf>

```
class ResNet(nn.Module):
    def __init__(self, base_dim, num_classes=2):
        super(ResNet, self).__init__()
        self.act_fn = nn.ReLU()
        self.layer_1 = nn.Sequential(
            nn.Conv2d(3,base_dim,7,2,3),
            nn.ReLU(),
            nn.MaxPool2d(3,2,1),
        )
        self.layer_2 = nn.Sequential(
            BottleNeck(base_dim,base_dim,base_dim*4,self.act_fn),
            BottleNeck(base_dim*4,base_dim,base_dim*4,self.act_fn),
            BottleNeck(base_dim*4,base_dim,base_dim*4,self.act_fn,down=True),
        )
        self.layer_3 = nn.Sequential(
            BottleNeck(base_dim*4,base_dim*2,base_dim*8,self.act_fn),
            BottleNeck(base_dim*8,base_dim*2,base_dim*8,self.act_fn),
            BottleNeck(base_dim*8,base_dim*2,base_dim*8,self.act_fn),
            BottleNeck(base_dim*8,base_dim*2,base_dim*8,self.act_fn,down=True),
        )
        self.layer_4 = nn.Sequential(
            BottleNeck(base_dim*8,base_dim*4,base_dim*16,self.act_fn),
            BottleNeck(base_dim*16,base_dim*4,base_dim*16,self.act_fn),
            BottleNeck(base_dim*16,base_dim*4,base_dim*16,self.act_fn),
            BottleNeck(base_dim*16,base_dim*4,base_dim*16,self.act_fn),
            BottleNeck(base_dim*16,base_dim*4,base_dim*16,self.act_fn),
            BottleNeck(base_dim*16,base_dim*4,base_dim*16,self.act_fn,down=True),
        )
        self.layer_5 = nn.Sequential(
            BottleNeck(base_dim*16,base_dim*8,base_dim*32,self.act_fn),
            BottleNeck(base_dim*32,base_dim*8,base_dim*32,self.act_fn),
            BottleNeck(base_dim*32,base_dim*8,base_dim*32,self.act_fn),
        )
        self.avgpool = nn.AvgPool2d(7,1)
        self.fc_layer = nn.Linear(base_dim*32,num_classes)
```

*2015 ILSVRC 1st place

```
def forward(self, x):
    out = self.layer_1(x)
    out = self.layer_2(out)
    out = self.layer_3(out)
    out = self.layer_4(out)
    out = self.layer_5(out)
    out = self.avgpool(out)
    out = out.view(batch_size,-1)
    out = self.fc_layer(out)

    return out
```

Q&A

감사합니다.