

4.

$$X_t = \begin{cases} 0 & \text{if 정상} \\ 1 & \text{if 고장} \end{cases}$$

$$P_{00} = \{X_{t+1}=0 \mid X_t=0\} = 0.9$$

$$P_{01} = \{X_{t+1}=1 \mid X_t=0\} = 0.1$$

$$P_{10} = \{X_{t+1}=0 \mid X_t=1\} = 1$$

$$P_{11} = \{X_{t+1}=1 \mid X_t=1\} = 0$$

$$\therefore P = \begin{matrix} & \text{state} & 0 & 1 \\ \begin{matrix} 0 \\ 1 \end{matrix} & \begin{bmatrix} 0.9 & 0.1 \\ 1 & 0 \end{bmatrix} \end{matrix}$$

$$\mu_{00} = 1 + P_{01} \cdot \mu_{10} = 1 + 0.1 \cdot \mu_{10} \dots \textcircled{1}$$

$$\mu_{01} = 1 + P_{00} \cdot \mu_{01} = 1 + 0.9 \cdot \mu_{01} \dots \textcircled{2}$$

$$\mu_{10} = 1 + P_{11} \cdot \mu_{10} = 1 + 0 \cdot \mu_{10} \dots \textcircled{3}$$

$$\mu_{11} = 1 + P_{10} \cdot \mu_{01} = 1 + 1 \cdot \mu_{01} \dots \textcircled{4}$$

$$\textcircled{2} \rightarrow \mu_{01} = 1 + 0.9 \cdot \mu_{01} \Rightarrow \mu_{01} = 10$$

$\therefore 10 \text{ 일}$