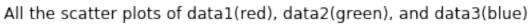
Final Project_2015-17231_박우정

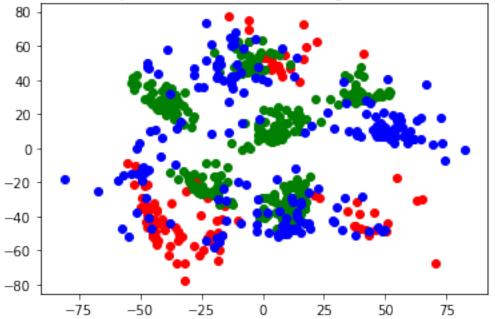
November 28, 2019

```
[9]: #1. k-means clustering
                   ## initialization. k\Omega = \max_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{j=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{j
                  k=int(input("number of cluster?"))
                  max_iter=int(input("number of max_iteration?"))
                  ##import library
                  import numpy as np
                  import matplotlib.pyplot as plt
                   ##read data.csv
                  data1=np.loadtxt('data1.csv',delimiter=',')
                  data2=np.loadtxt('data2.csv',delimiter=',')
                  data3=np.loadtxt('data3.csv',delimiter=',') #\Price 120 * 2 matrix
                  x1=data1[:,0]
                  y1=data1[:,1]
                  x2=data2[:,0]
                  y2=data2[:,1]
                  x3=data3[:,0]
                  y3=data3[:,1] #coordinates 별로 저장
                  plt.scatter(x1,y1,color='red')
                  plt.scatter(x2,y2,color='green')
                  plt.scatter(x3,y3,color='blue')
                  plt.title("All the scatter plots of data1(red), data2(green), and data3(blue)")
                  plt.show()
                  print("\n\n\n")
                  ##declare functions
                  def dist(a,b): #Euclidean norm
                                 return np.linalg.norm(b-a)
                  def init_centroids(data, k): #k를 받고, initial points로부터 k개의 중심 c1, c2, u
                      → c3, ..., ck를 리턴하는 함수
                                 centroids = data.copy()
                                 np.random.shuffle(centroids)
```

```
return centroids[:k]
def closest_centroid(data, centroids): #Euclidean norm을 거리로 하는 distance를 주
고, 그것이 최소가 되게 하는 중심좌표 index 반환.
   distances = np.sqrt(((data - centroids[:, np.newaxis])**2).sum(axis=2))
    #np.newaxis를 통해 각 data안의 성분들에 고정된 centroids가 모두 빼지도록 한다.
    #np.newaxis는 차원을 확장하는 함수. 가령, [1,2,3,4] -> [[1,2,3,4]] ->u
→[[1][2][3][4]] 이런 방식으로 확장.
   return np.argmin(distances, axis=0)
#closest_centroid(data3,centroids) #출력된 값은 c_0, c_1, ..., c_(k-1)의 index 0μ
→1 2 ... k-1 중 하나이다. 가까운 index 반환
def new_centroids(data, closest, centroids): #위에서 구한 index들끼리 모아서 새로운
 →centroid를 구하다.
   return np.array([data[closest==k].mean(axis=0) for k in range(centroids.
 \rightarrowshape [0])])
##data 1
plt.scatter(data1[:, 0], data1[:, 1])
centroids = init_centroids(data1, k)
for i in range(0, max_iter):
   closest = closest_centroid(data1, centroids)
   ncentroids = new_centroids(data1, closest, centroids)
   if(dist(ncentroids, centroids)<10^(-3) or dist(ncentroids, centroids)==0):
       print("The iteration number of data 1 is: ", i)
       break:
   centroids=new_centroids(data1, closest, centroids)
plt.scatter(centroids[:, 0], centroids[:, 1], c='r', s=100)
plt.title("data 1 k-means clustering result with error=10^-3")
plt.show()
print("The coordinates of centroids of data1 is:\n", centroids)
print("The clusters of data1 is:\n", closest)
print("\n\n\n")
```

number of cluster?4
number of max_iteration?1000





The iteration number of data 1 is: 3



```
[2]: #1. k-means clustering

## initialization. k$\Omega$ max_iteration I, r_nk
k=int(input("number of cluster?"))

max_iter=int(input("number of max_iteration?"))

##import library
import numpy as np
import matplotlib.pyplot as plt
```

```
##read data.csv
data1=np.loadtxt('data1.csv',delimiter=',')
data2=np.loadtxt('data2.csv',delimiter=',')
data3=np.loadtxt('data3.csv',delimiter=',') #모두 120 * 2 matrix
x1=data1[:,0]
y1=data1[:,1]
x2=data2[:,0]
y2=data2[:,1]
x3=data3[:,0]
y3=data3[:,1] #coordinates 별로 저장
plt.scatter(x1,y1,color='red')
plt.scatter(x2,y2,color='green')
plt.scatter(x3,y3,color='blue')
plt.title("All the scatter plots of data1(red), data2(green), and data3(blue)")
plt.show()
print("\n\n\n")
##declare functions
def dist(a,b): #Euclidean norm
         return np.linalg.norm(b-a)
def init_centroids(data, k): #k를 받고, initial points로부터 k개의 중심 c1, c2, provided the control of t
  → c3, ..., ck를 리턴하는 함수
         centroids = data.copy()
         np.random.shuffle(centroids)
         return centroids[:k]
def closest_centroid(data, centroids): #Euclidean norm을 거리로 하는 distance를 주
고, 그것이 최소가 되게 하는 중심좌표 index 반환.
         distances = np.sqrt(((data - centroids[:, np.newaxis])**2).sum(axis=2))
         #np.newaxis를 통해 각 data안의 성분들에 고정된 centroids가 모두 빼지도록 한다.
         #np.newaxis는 차원을 확장하는 함수. 가령, [1,2,3,4] -> [[1,2,3,4]] ->__
  →[[1][2][3][4]] 이런 방식으로 확장.
         return np.argmin(distances, axis=0)
#closest_centroid(data3,centroids) #출력된 값은 c_0, c_1, ..., c_(k-1)의 index 0u
  →1 2 ... k-1 중 하나이다. 가까운 index 반환
def new_centroids(data, closest, centroids): #위에서 구한 index들끼리 모아서 새로운
  →centroid를 구한다.
         return np.array([data[closest==k].mean(axis=0) for k in range(centroids.
  →shape[0])])
##data 2
plt.scatter(data2[:, 0], data2[:, 1])
```

```
centroids = init_centroids(data2, k)

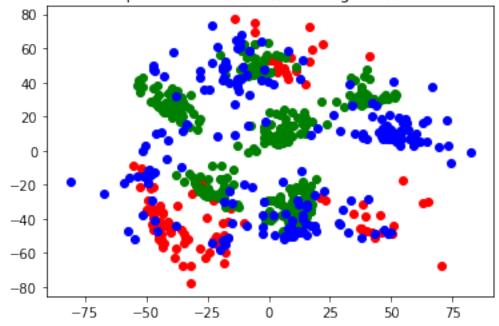
for i in range(0, max_iter):
    closest = closest_centroid(data2, centroids)
    ncentroids = new_centroids(data2, closest, centroids)
    if(dist(ncentroids, centroids)<10^(-3) or dist(ncentroids, centroids)==0):
        print("The iteration number of data 2 is: ", i)
        break;
    centroids=new_centroids(data2, closest, centroids)

plt.scatter(centroids[:, 0], centroids[:, 1], c='r', s=100)
plt.title("data 2 k-means clustering result with error=10^-3")
plt.show()

print("The coordinates of centroids of data2 is:\n", centroids)
print("The clusters of data1 is:\n", closest)
print("\n\n\n")</pre>
```

number of cluster?6
number of max_iteration?1000

All the scatter plots of data1(red), data2(green), and data3(blue)



The iteration number of data 2 is: 1



```
The coordinates of centroids of data2 is:
[[-40.69362868 26.77287789]
[ 40.29056533 31.42481471]
[ 5.23192998 10.58650307]
[ -5.35294772 50.73166275]
[ 12.12524292 -32.66803269]
[-23.14794187 -22.33230429]]
```

```
[7]: #1. k-means clustering

## initialization. k$\mathbb{L}$ max_iteration I, r_nk
k=int(input("number of cluster?"))

max_iter=int(input("number of max_iteration?"))

##import library
import numpy as np
import matplotlib.pyplot as plt
```

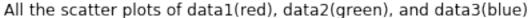
```
##read data.csv
data1=np.loadtxt('data1.csv',delimiter=',')
data2=np.loadtxt('data2.csv',delimiter=',')
data3=np.loadtxt('data3.csv',delimiter=',') #모두 120 * 2 matrix
x1=data1[:,0]
y1=data1[:,1]
x2=data2[:,0]
y2=data2[:,1]
x3=data3[:,0]
y3=data3[:,1] #coordinates 별로 저장
plt.scatter(x1,y1,color='red')
plt.scatter(x2,y2,color='green')
plt.scatter(x3,y3,color='blue')
plt.title("All the scatter plots of data1(red), data2(green), and data3(blue)")
plt.show()
print("\n\n\n")
##declare functions
def dist(a,b): #Euclidean norm
   return np.linalg.norm(b-a)
def init_centroids(data, k): #k를 받고, initial points로부터 k개의 중심 c1, c2, u
→ c3, ..., ck를 리턴하는 함수
   centroids = data.copy()
   np.random.shuffle(centroids)
   return centroids[:k]
def closest_centroid(data, centroids): #Euclidean norm을 거리로 하는 distance를 주
고, 그것이 최소가 되게 하는 중심좌표 index 반환.
   distances = np.sqrt(((data - centroids[:, np.newaxis])**2).sum(axis=2))
    #np.newaxis를 통해 각 data안의 성분들에 고정된 centroids가 모두 빼지도록 한다.
    #np.newaxis는 차원을 확장하는 함수. 가령, [1,2,3,4] -> [[1,2,3,4]] ->u
→[[1][2][3][4]] 이런 방식으로 확장.
   return np.argmin(distances, axis=0)
#closest_centroid(data3,centroids) #출력된 값은 c_0, c_1, ..., c_k1)의 index 0_{\sqcup}
→1 2 ... k-1 중 하나이다. 가까운 index 반환
def new_centroids(data, closest, centroids): #위에서 구한 index들끼리 모아서 새로운」
 →centroid를 구한다.
   return np.array([data[closest==k].mean(axis=0) for k in range(centroids.
 \rightarrowshape [0])])
##data 3
plt.scatter(data3[:, 0], data3[:, 1])
centroids = init_centroids(data3, k)
```

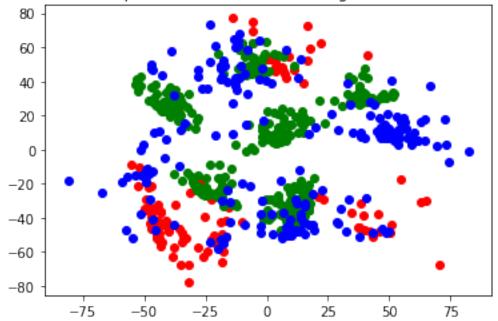
```
for i in range(0, max_iter):
    closest = closest_centroid(data3, centroids)
    ncentroids = new_centroids(data3, closest, centroids)
    if(dist(ncentroids, centroids)<10^(-3) or dist(ncentroids, centroids)==0):
        print("The iteration number of data3 is: ", i)
        break;
    centroids=new_centroids(data3, closest, centroids)

plt.scatter(centroids[:, 0], centroids[:, 1], c='r', s=100)
plt.title("data 3 k-means clustering result with error=10^-3")
plt.show()

print("The coordinates of centroids of data3 is:\n", centroids)
print("The clusters of data1 is:\n", closest)</pre>
```

number of cluster?6
number of max_iteration?1000





The iteration number of data3 is: 6



```
[ 21.82375815 -40.63277086]
[ -6.32328949 -40.99479766]]

[11]: #2. LBG clustering

## initialization. k2 max_iteration I, r_nk
epsilon=float(input("error?(10^-3 recommended)"))
max_iter=int(input("number of max_iteration?"))

##import library
import numpy as np
import matplotlib.pyplot as plt

##read data.csv
data1=np.loadtxt('data1.csv',delimiter=',')
data2=np.loadtxt('data2.csv',delimiter=',')
data3=np.loadtxt('data3.csv',delimiter=',') #£ 120 * 2 matrix
x1=data1[:,0]
```

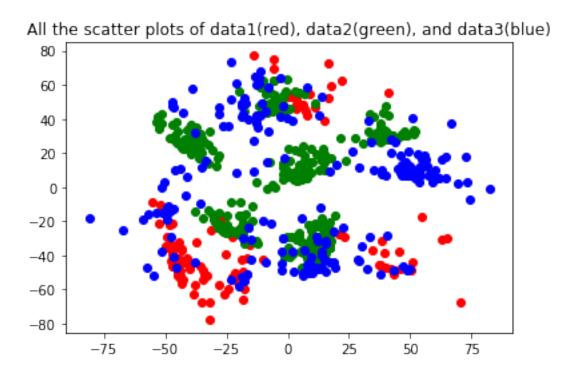
The coordinates of centroids of data3 is:

[[-50.95008522 -20.46132768] [-11.50396023 49.98153678] [51.14102688 11.88825836] [-31.02680348 25.77939495]

```
y1=data1[:,1]
x2=data2[:,0]
y2=data2[:,1]
x3=data3[:,0]
y3=data3[:,1] #coordinates 별로 저장
plt.scatter(x1,y1,color='red')
plt.scatter(x2,y2,color='green')
plt.scatter(x3,y3,color='blue')
plt.title("All the scatter plots of data1(red), data2(green), and data3(blue)")
plt.show()
print("\n\n\n")
##declare functions
def dist(a,b): #Euclidean norm
   return np.linalg.norm(b-a)
def init_centroids(data, k): #k를 받고, initial points로부터 k개의 중심 c1, c2, u
→ c3, ..., ck를 리턴하는 함수
   centroids = data.copy()
   np.random.shuffle(centroids)
   return centroids[:k]
def closest_centroid(data, centroids): #Euclidean norm을 거리로 하는 distance를 주
고, 그것이 최소가 되게 하는 중심좌표 index 반환.
   distances = np.sqrt(((data - centroids[:, np.newaxis])**2).sum(axis=2))
    #np.newaxis를 통해 각 data안의 성분들에 고정된 centroids가 모두 빼지도록 한다.
    #np.newaxis는 차원을 확장하는 함수. 가령, [1,2,3k4] -> [[1,2,3,4]] ->u
→[[1][2][3][4]] 이런 방식으로 확장.
   return np.argmin(distances, axis=0)
#closest_centroid(data3,centroids) #출력된 값은 c_0, c_1, ..., c_(k-1)의 index 0_{f \sqcup}
→1 2 ... k-1 중 하나이다. 가까운 index 반환
def new_centroids(data, closest, centroids): #위에서 구한 index들끼리 모아서 새로운」
 →centroid를 구한다.
   return np.array([data[closest==k].mean(axis=0) for k in range(centroids.
 \rightarrowshape[0])])
##data 1
plt.scatter(data1[:, 0], data1[:, 1])
### start at k_1=1
k_1=1
centroids = np.array([[data1[:,0].mean(), data1[:,1].mean()]]) #초기 중심은 무게중
심.
```

```
distance = ((data1 - centroids[:, np.newaxis])**2).sum(axis=2) #120개 거리만을 적
은 벡터. 가장 가까운 것을 찾자.
add_centroids=np.array([data1[distance.argmin(),]]) #가장 가까운 것.
for j in range(0, max_iter):
   centroids=np.array(np.append(centroids, add_centroids, axis=0)) #둘을 결합하
여 중심 2개 집합 생성
   D_old = ((data1 - centroids[:, np.newaxis])**2).sum()
   for i in range(0, max_iter):
       closest = closest_centroid(data1, centroids)
       ncentroids = new_centroids(data1, closest, centroids)
       if(dist(ncentroids, centroids)<10^(-3) or dist(ncentroids,
 #print("The iteration number of data 1 is: ", i)
           break
       else:
           centroids=new_centroids(data1, closest, centroids)
   D_new = ((data1 - centroids[:, np.newaxis])**2).sum()
   error=abs(D_new-D_old)/D_new
   if((D_new-D_old)/D_new<epsilon or D_new==0 or k_1>=120):
       break
   else:
       k_1=k_1*2
       add_centroids=init_centroids(data1, k_1)
       continue
plt.scatter(centroids[:, 0], centroids[:, 1], c='r', s=100)
plt.title("data 1 k-means clustering result with error=10^-3")
plt.show()
print("The optimized number of clusters is: n", k_1*2)
print("The coordinates of centroids of data1 is:\n", centroids)
print("The clusters of data1 is:\n", closest)
print("\n\n\n")
```

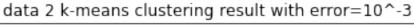
error?(10^-3 recommended)0.001 number of max_iteration?100

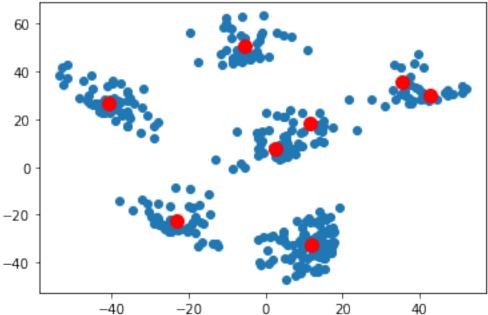




```
[41]: ##data 2
     plt.scatter(data2[:, 0], data2[:, 1])
     ### start at k_2=1
     k_2=1
     centroids = np.array([[data2[:,0].mean(), data2[:,1].mean()]]) #초기 중심은 무게중
     심.
     distance = ((data2 - centroids[:, np.newaxis])**2).sum(axis=2) #120개 거리만을 적
     은 벡터. 가장 가까운 것을 찾자.
     add_centroids=np.array([data2[distance.argmin(),]]) #가장 가까운 것.
     for j in range(0, max_iter):
         centroids=np.array(np.append(centroids, add_centroids, axis=0)) #둘을 결합하
     여 중심 2개 집합 생성
         D_old = ((data2 - centroids[:, np.newaxis])**2).sum()
         for i in range(0, max_iter):
             closest = closest_centroid(data2, centroids)
             ncentroids = new_centroids(data2, closest, centroids)
             if(dist(ncentroids, centroids)<10^(-3) or dist(ncentroids, __
      →centroids)==0):
                 #print("The iteration number of data 1 is: ", i)
                 break
```

```
else:
            centroids=new_centroids(data2, closest, centroids)
    D_new = ((data2 - centroids[:, np.newaxis])**2).sum()
    error=abs(D_new-D_old)/D_new
    if((D_new-D_old)/D_new<epsilon or D_new==0 or k_2>=120):
        break
    else:
       k_2=2*k_2
        add_centroids=init_centroids(data2, k_2)
        continue
plt.scatter(centroids[:, 0], centroids[:, 1], c='r', s=100)
plt.title("data 2 k-means clustering result with error=10^-3")
plt.show()
print("The optimized number of clusters is: n", k_2*2)
print("The coordinates of centroids of data2 is:\n", centroids)
print("The clusters of data2 is:\n", closest)
print("\n\n\n")
```





```
The optimized number of clusters is: 8

The coordinates of centroids of data2 is: [[ 11.57463154    18.02447884] [ -5.35294772    50.73166275]
```

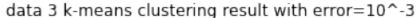
```
[-40.69362868 26.77287789]
 [ 12.12524292 -32.66803269]
 [-23.14794187 -22.33230429]
 [ 2.62094678
                    7.49833923]
 [ 42.91385454 29.73755941]
 [ 35.75965734 35.33087055]]
The clusters of data2 is:
 [1 3 0 6 5 7 4 2 3 1 3 4 2 3 2 0 3 3 1 1 7 6 5 6 3 4 0 3 1 6 2 6 3 2 7 3 6
 3\ 3\ 5\ 2\ 3\ 5\ 3\ 1\ 2\ 0\ 1\ 3\ 3\ 6\ 1\ 3\ 3\ 3\ 5\ 3\ 1\ 3\ 2\ 4\ 4\ 3\ 3\ 5\ 3\ 0\ 3\ 2\ 3\ 3\ 5
 1\; 3\; 3\; 6\; 6\; 5\; 7\; 4\; 7\; 5\; 3\; 3\; 2\; 2\; 1\; 2\; 0\; 7\; 5\; 4\; 3\; 6\; 1\; 2\; 3\; 5\; 2\; 1\; 6\; 2\; 5\; 2\; 4\; 6\; 3\; 0\; 3
 5\; 4\; 3\; 3\; 4\; 3\; 3\; 5\; 4\; 1\; 3\; 6\; 1\; 5\; 6\; 5\; 3\; 2\; 3\; 4\; 1\; 6\; 3\; 5\; 6\; 2\; 4\; 3\; 2\; 3\; 0\; 2\; 3\; 4\; 0\; 7\; 2
 5\; 3\; 2\; 3\; 2\; 3\; 1\; 6\; 4\; 4\; 5\; 6\; 3\; 3\; 4\; 2\; 4\; 2\; 2\; 1\; 3\; 3\; 0\; 2\; 0\; 4\; 7\; 5\; 3\; 1\; 2\; 1\; 1\; 5\; 3\; 5\; 2
 4 3 7 5 3 0 6 3 4 5 6 2 3 3 4 3 4 3 6 2 2 4 2 3 5 4 1 2 3 5 3 3 3 6 3 5 3
 3 2 1 4 5 5 2 3 3 3 5 3 3 1 5 4 2 5 5 5 6 0 0 4 2 3 2 1 0 3 1 5 2 4 5 5 3
 3\ 6\ 7\ 5\ 3\ 6\ 0\ 1\ 5\ 6\ 3\ 7\ 1\ 5\ 2\ 4\ 0\ 3\ 3\ 0\ 2\ 3\ 5\ 6\ 4\ 4\ 5\ 3\ 2\ 2\ 3\ 7\ 2\ 4\ 4\ 3\ 6
 4 3 3 3 1 4 5 6 1 5 1 3 2 1 2 2 4 2 1 1 2 4 2 3 4 3 3 1 4 2 2 4 0 4 6 5 2
 3\ 4\ 4\ 2\ 2\ 0\ 1\ 3\ 4\ 1\ 3\ 1\ 2\ 3\ 7\ 1\ 2\ 4\ 3\ 2\ 3\ 3\ 7\ 3\ 6\ 6\ 1\ 2\ 3\ 3\ 5\ 0\ 3\ 4\ 6\ 5\ 4
 5 2 3 4 3 5 2 0 2 5 2 7 0 3 0 1 2 4 2 3 3 3 3 3 5 5 2 1 3 1]
```

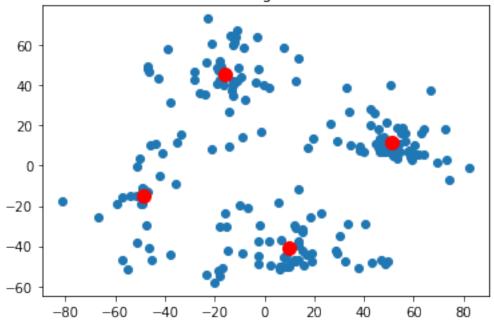
```
[43]: ##data 3
     plt.scatter(data3[:, 0], data3[:, 1])
     ### start at k_3=1
     k_3=1
     centroids = np.array([[data3[:,0].mean(), data3[:,1].mean()]]) #초기 중심은 무게중
     심.
     distance = ((data3 - centroids[:, np.newaxis])**2).sum(axis=2) #120개 거리만을 적
     은 벡터. 가장 가까운 것을 찾자.
     add_centroids=np.array([data3[distance.argmin(),]]) #가장 가까운 것.
     for j in range(0, max_iter):
         centroids=np.array(np.append(centroids, add_centroids, axis=0)) #둘을 결합하
     여 중심 2개 집합 생성
         D_old = ((data3 - centroids[:, np.newaxis])**2).sum()
         for i in range(0, max_iter):
             closest = closest_centroid(data3, centroids)
             ncentroids = new_centroids(data3, closest, centroids)
             if(dist(ncentroids, centroids)<10^(-3) or dist(ncentroids,
      #print("The iteration number of data 1 is: ", i)
                 break
             else:
```

```
centroids=new_centroids(data3, closest, centroids)
D_new = ((data3 - centroids[:, np.newaxis])**2).sum()
error=abs(D_new-D_old)/D_new
if((D_new-D_old)/D_new<epsilon or D_new==0 or k_3>=120):
    break
else:
    k_3=2*k_3
    add_centroids=init_centroids(data3, k_3)
    continue

plt.scatter(centroids[:, 0], centroids[:, 1], c='r', s=100)
plt.title("data 3 k-means clustering result with error=10^-3")
plt.show()

print("The optimized number of clusters is: \n", k_3*2)
print("The coordinates of centroids of data3 is:\n", centroids)
print("The clusters of data3 is:\n", closest)
print("\n\n\n")
```





```
The optimized number of clusters is:
4
The coordinates of centroids of data3 is:
[[-48.4467347 -15.01285632]
[ 51.14102688 11.88825836]
[ 10.17670395 -40.78257506]
```

```
[-15.8484895     45.67220216]]
The clusters of data3 is:

[2 1 0 2 2 0 1 1 1 1 1 0 3 2 2 0 2 1 3 1 0 3 1 3 3 3 1 1 2 2 3 3 3 3 3 2 0 0
0 0 2 3 1 3 1 2 1 1 0 2 3 2 2 1 1 1 1 2 1 0 2 2 0 3 1 2 2 1 1 0 1 2 2 2 2
2 1 2 2 1 3 1 0 0 0 2 0 1 1 3 1 2 0 0 0 1 1 1 3 3 1 0 3 2 1 3 2 1 3 2 1 1
0 1 3 2 3 2 1 1 2 3 1 0 1 1 3 2 2 2 2 2 1 3 2 0 1 2 2 2 2 2 1 3 2 0 1 3 0 2 2
2 1 3 1 3 3 1 3 3 3 1 1 1 0 0 0 0 2 2 3 2 3 1 0 0 3 3 2 2 0 2 2 3 2 1 3 3
1 1 3 2 0 3 2 2 3 3 1 1 1 1 1]
```

```
[14]: #3. SVM
      from sklearn.model_selection import GridSearchCV
      from sklearn.svm import SVC
      from sklearn.decomposition import PCA
      from sklearn.metrics import accuracy_score
      #keras libary에서 MNIST dataset을 다운받는다.
      from tensorflow.keras.datasets import mnist
      (x_train, y_train), (x_test, y_test) = mnist.load_data()
      #60000 by 28 by 28을 데이터처리를 위해 60000 by 28로 reshape한다.
      x_{train} = x_{train.reshape}(60000, 784)
      x_{test} = x_{test.reshape}(10000, 784)
      # normalize를 위해 나눗셈이 필요하고, 이를 위해서는 int형 대신 float 형을 사용.
      x_train = x_train.astype('float32')
      x_test = x_test.astype('float32')
      # Scale the data to lie between -1 to 1(SVM ppt 참조)
      x_{train} = x_{train} / 255.0*100 - 50
      x_{test} = x_{test} / 255.0*100 - 50
      print(x_train.shape[0], 'train samples')
      print(x_test.shape[0], 'test samples')
      #I one hot encoding step.
      y_train =y_train % 2
      y_test = y_test % 2
      # PCA
      pca = PCA(n_components=50)
      x_train = pca.fit_transform(x_train)
      x_test = pca.transform(x_test)
      #매개변수 gamma와 C의 최적값을 찾기 위해 Gridsearchcv 이용
```

```
svm = SVC()
parameters = [{'kernel': ['rbf'], 'gamma': [1e-3, 1e-4], 'C': [1, 10, 100, 100]
 →1000]}]
print("Grid search")
grid = GridSearchCV(svm, parameters, verbose=3)
print("Grid.fit")
grid.fit(x_train[0:7000], y_train[0:7000]) #qrid search learning the best,
 \rightarrowparameters
print("Grid done")
print (grid.best_params_)
#훈련 학습
print("training svm")
best_svm = grid.best_estimator_
best_svm.fit(x_train , y_train)
print("svm done")
print("Testing")
print("score: ", best_svm.score(x_test, y_test,))
60000 train samples
10000 test samples
Grid search
Grid.fit
Fitting 3 folds for each of 8 candidates, totalling 24 fits
[CV] C=1, gamma=0.001, kernel=rbf ...
C:\Users\dnrlf\Anaconda3\lib\site-
packages\sklearn\model_selection\_split.py:1978: FutureWarning: The default
value of cv will change from 3 to 5 in version 0.22. Specify it explicitly to
silence this warning.
  warnings.warn(CV_WARNING, FutureWarning)
[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
[CV] ... C=1, gamma=0.001, kernel=rbf, score=0.509, total=
[CV] C=1, gamma=0.001, kernel=rbf ...
[Parallel(n_jobs=1)]: Done 1 out of
                                       1 | elapsed:
                                                         5.9s remaining:
                                                                            0.0s
[CV] ... C=1, gamma=0.001, kernel=rbf, score=0.508, total=
                                                              5.5s
[CV] C=1, gamma=0.001, kernel=rbf ...
[Parallel(n_jobs=1)]: Done
                             2 out of
                                        2 | elapsed:
                                                       11.4s remaining:
                                                                            0.0s
[CV] ... C=1, gamma=0.001, kernel=rbf, score=0.508, total=
                                                              5.8s
[CV] C=1, gamma=0.0001, kernel=rbf ...
[CV] ... C=1, gamma=0.0001, kernel=rbf, score=0.592, total=
```

```
[CV] C=1, gamma=0.0001, kernel=rbf ...
[CV] ... C=1, gamma=0.0001, kernel=rbf, score=0.596, total=
                                                               5.2s
[CV] C=1, gamma=0.0001, kernel=rbf ...
[CV] ... C=1, gamma=0.0001, kernel=rbf, score=0.594, total=
                                                               4.7s
[CV] C=10, gamma=0.001, kernel=rbf ...
[CV] ... C=10, gamma=0.001, kernel=rbf, score=0.509, total=
                                                               4.9s
[CV] C=10, gamma=0.001, kernel=rbf ...
[CV] ... C=10, gamma=0.001, kernel=rbf, score=0.508, total=
                                                               4.9s
[CV] C=10, gamma=0.001, kernel=rbf ...
[CV] ... C=10, gamma=0.001, kernel=rbf, score=0.508, total=
                                                               4.9s
[CV] C=10, gamma=0.0001, kernel=rbf ...
[CV] ... C=10, gamma=0.0001, kernel=rbf, score=0.597, total=
                                                                4.9s
[CV] C=10, gamma=0.0001, kernel=rbf ...
[CV] ... C=10, gamma=0.0001, kernel=rbf, score=0.604, total=
                                                                5.2s
[CV] C=10, gamma=0.0001, kernel=rbf ...
[CV] ... C=10, gamma=0.0001, kernel=rbf, score=0.600, total=
                                                                5.0s
[CV] C=100, gamma=0.001, kernel=rbf ...
[CV] ... C=100, gamma=0.001, kernel=rbf, score=0.509, total=
                                                                5.1s
[CV] C=100, gamma=0.001, kernel=rbf ...
[CV] ... C=100, gamma=0.001, kernel=rbf, score=0.508, total=
                                                                5.2s
[CV] C=100, gamma=0.001, kernel=rbf ...
[CV] ... C=100, gamma=0.001, kernel=rbf, score=0.508, total=
                                                                5.1s
[CV] C=100, gamma=0.0001, kernel=rbf ...
[CV] ... C=100, gamma=0.0001, kernel=rbf, score=0.597, total=
                                                                 4.9s
[CV] C=100, gamma=0.0001, kernel=rbf ...
[CV] ... C=100, gamma=0.0001, kernel=rbf, score=0.604, total=
                                                                 4.9s
[CV] C=100, gamma=0.0001, kernel=rbf ...
[CV] ... C=100, gamma=0.0001, kernel=rbf, score=0.600, total=
                                                                 4.8s
[CV] C=1000, gamma=0.001, kernel=rbf ...
[CV] ... C=1000, gamma=0.001, kernel=rbf, score=0.509, total=
                                                                 4.9s
[CV] C=1000, gamma=0.001, kernel=rbf ...
[CV] ... C=1000, gamma=0.001, kernel=rbf, score=0.508, total=
                                                                 5.1s
[CV] C=1000, gamma=0.001, kernel=rbf ...
[CV] ... C=1000, gamma=0.001, kernel=rbf, score=0.508, total=
                                                                 5.5s
[CV] C=1000, gamma=0.0001, kernel=rbf ...
[CV] ... C=1000, gamma=0.0001, kernel=rbf, score=0.597, total=
                                                                  5.0s
[CV] C=1000, gamma=0.0001, kernel=rbf ...
[CV] ... C=1000, gamma=0.0001, kernel=rbf, score=0.604, total=
                                                                  4.9s
[CV] C=1000, gamma=0.0001, kernel=rbf ...
[CV] ... C=1000, gamma=0.0001, kernel=rbf, score=0.600, total=
                                                                  4.7s
[Parallel(n_jobs=1)]: Done 24 out of 24 | elapsed: 2.0min finished
Grid done
{'C': 10, 'gamma': 0.0001, 'kernel': 'rbf'}
training svm
svm done
Testing
score: 0.6283
```

```
[13]: #4 MLP
     import tensorflow as tf
     from tensorflow.python.framework import ops
     ops.reset_default_graph()
     import tensorflow.keras
     from tensorflow.keras.datasets import mnist
     from tensorflow.keras.models import Sequential
     from tensorflow.keras.layers import Dense, Dropout
     from tensorflow.keras.optimizers import RMSprop
     batch_size = 128 #batch : 나누어진 dataset이고 batch_size는 한 번의 batch마다 주는
     데이터 샘폴의 size를 의미한다.
     num_classes = 10 #MNIST는 0부터 9까지 10개의 카테고리를 가지므로 10으로 둔다.
     epochs = 20 #1 epoch : 신경망에서 전체 dataset 학습을 한 번 완료. 즉 각 퍼셉트론 간 w
     를 계산하는 것이 한 세션 완료.
     (x_train, y_train), (x_test, y_test) = mnist.load_data() #데이터 download 하고 각
     각 항목에 저장.
     #x_train, x_test에는 각각 60000 by 28 * 28 , 10000 by 28 * 28
     #y_train, y_test에는 각각 60000, 100000 개의 label 저장.
     #위에서 다운받은 MNIST data는 60000 by 28 by 28 이다. 처리를 위해 60000 by 784 by 1
     로 만들기 위해 다음을 이용한다.
     x_train = x_train.reshape((x_train.shape[0], -1)) #-1은 차원을 줄이는 역할.
     x_test = x_test.reshape((x_test.shape[0], -1))
     #normalizing process
     x_train = x_train.astype('float32') #int type이면 나누는데 오류가 발생하므로 floatu
      →tupe으로 바꾸어준다.
     x_test = x_test.astype('float32')
     x_train /= 255 #MNIST matrix는 0~255사이의 값을 element로 가지므로 255로 나누어,
      →normalize한다.
     x_test /= 255
     print(x_train.shape[0], 'train samples')
     print(x_test.shape[0], 'test samples')
     # 신경망을 구현하기 위해 one-hot encoding하는 과정.
     ##one-hot encoding : data, label에 해당되는 index만 1로, 나머지는 0으로 단순화하는 자
     연어 처리과정.
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     #이제 keras 내장함수를 이용해 relu activation function을 활용해 MLP를 구현.
     #hidden layer=27#
     model = Sequential()
```

```
model.add(Dense(512, activation='relu', input_shape=(784,))) #784개 입력해서 512
개 출력
model.add(Dropout(0.2)) #For fast modelling and prevent overfitting.dropout 0.2
는 randomly하게 연결된 뉴런들을 0.2만큼 drop out한다는 뜻이다.
model.add(Dense(512, activation='relu')) #512개 출력
model.add(Dropout(0.2))
model.add(Dense(num_classes, activation='softmax')) #10개 출력
model.summary()
model.compile(loss='categorical_crossentropy', optimizer=RMSprop(), __
 →metrics=['accuracy'])
model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1,__
 →validation_data=(x_test, y_test))
score = model.evaluate(x_test, y_test, verbose=0) #verbose=0 로깅 없음
print('Test loss:', score[0])
print('Test accuracy:', score[1])
60000 train samples
10000 test samples
Model: "sequential"
Layer (type)
                Output Shape
______
dense (Dense)
                     (None, 512)
                                        401920
_____
                    (None, 512)
dropout (Dropout)
_____
dense_1 (Dense)
                    (None, 512)
                                        262656
______
                (None, 512)
dropout_1 (Dropout)
_____
                               5130
dense_2 (Dense) (None, 10)
_____
Total params: 669,706
Trainable params: 669,706
Non-trainable params: 0
Train on 60000 samples, validate on 10000 samples
Epoch 1/20
60000/60000 [============ ] - 18s 302us/sample - loss: 0.2447 -
accuracy: 0.9237 - val_loss: 0.1264 - val_accuracy: 0.9603
Epoch 2/20
60000/60000 [============== ] - 16s 265us/sample - loss: 0.1030 -
accuracy: 0.9685 - val_loss: 0.0853 - val_accuracy: 0.9751
```

```
Epoch 3/20
60000/60000 [============== ] - 17s 288us/sample - loss: 0.0758 -
accuracy: 0.9778 - val_loss: 0.0833 - val_accuracy: 0.9776
60000/60000 [============ ] - 17s 287us/sample - loss: 0.0609 -
accuracy: 0.9815 - val_loss: 0.0783 - val_accuracy: 0.9786
accuracy: 0.9841 - val_loss: 0.0727 - val_accuracy: 0.9810
Epoch 6/20
60000/60000 [============= ] - 17s 280us/sample - loss: 0.0450 -
accuracy: 0.9867 - val_loss: 0.0773 - val_accuracy: 0.9801
Epoch 7/20
60000/60000 [============= ] - 17s 280us/sample - loss: 0.0400 -
accuracy: 0.9880 - val_loss: 0.0803 - val_accuracy: 0.9812
Epoch 8/20
60000/60000 [============= ] - 17s 276us/sample - loss: 0.0353 -
accuracy: 0.9898 - val_loss: 0.0817 - val_accuracy: 0.9830
Epoch 9/20
60000/60000 [============] - 17s 285us/sample - loss: 0.0311 -
accuracy: 0.9909 - val_loss: 0.0857 - val_accuracy: 0.9822
Epoch 10/20
60000/60000 [============= ] - 17s 287us/sample - loss: 0.0279 -
accuracy: 0.9917 - val_loss: 0.0949 - val_accuracy: 0.9837
Epoch 11/20
60000/60000 [============] - 17s 284us/sample - loss: 0.0279 -
accuracy: 0.9919 - val_loss: 0.1037 - val_accuracy: 0.9822
Epoch 12/20
60000/60000 [============ ] - 17s 278us/sample - loss: 0.0239 -
accuracy: 0.9933 - val_loss: 0.0983 - val_accuracy: 0.9829
Epoch 13/20
accuracy: 0.9931 - val_loss: 0.1016 - val_accuracy: 0.9832
Epoch 14/20
60000/60000 [============= ] - 16s 271us/sample - loss: 0.0202 -
accuracy: 0.9939 - val_loss: 0.1044 - val_accuracy: 0.9830
Epoch 15/20
60000/60000 [============ ] - 17s 282us/sample - loss: 0.0226 -
accuracy: 0.9939 - val_loss: 0.1041 - val_accuracy: 0.9838
Epoch 16/20
60000/60000 [============ ] - 18s 301us/sample - loss: 0.0207 -
accuracy: 0.9944 - val_loss: 0.1126 - val_accuracy: 0.9822
60000/60000 [============ ] - 17s 276us/sample - loss: 0.0183 -
accuracy: 0.9950 - val_loss: 0.1079 - val_accuracy: 0.9830
Epoch 18/20
60000/60000 [============ ] - 17s 277us/sample - loss: 0.0193 -
accuracy: 0.9947 - val_loss: 0.1296 - val_accuracy: 0.9828
```

```
Epoch 19/20
60000/60000 [=============] - 16s 266us/sample - loss: 0.0187 - accuracy: 0.9949 - val_loss: 0.1311 - val_accuracy: 0.9835
Epoch 20/20
60000/60000 [==============] - 13s 218us/sample - loss: 0.0206 - accuracy: 0.9947 - val_loss: 0.1226 - val_accuracy: 0.9832
Test loss: 0.12259161651833374
Test accuracy: 0.9832
```