

Classification Metrics

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 **Confusion Matrix**

 **ROC&PR**

 **AUC**

Confusion Matrix

	Actual Positive	Actual Negative
Predicted Positive	TP	FP
Predicted Negative	FN	TN

$$Recall = \frac{TP}{TP + FN}$$

$$Precision = \frac{TP}{TP + FP}$$


$$Accuracy = \frac{TP + TN}{TP + FP + FN + TN}$$

$$\frac{1}{F_1} = \frac{1}{2} \left(\frac{1}{Recall} + \frac{1}{Precision} \right)$$

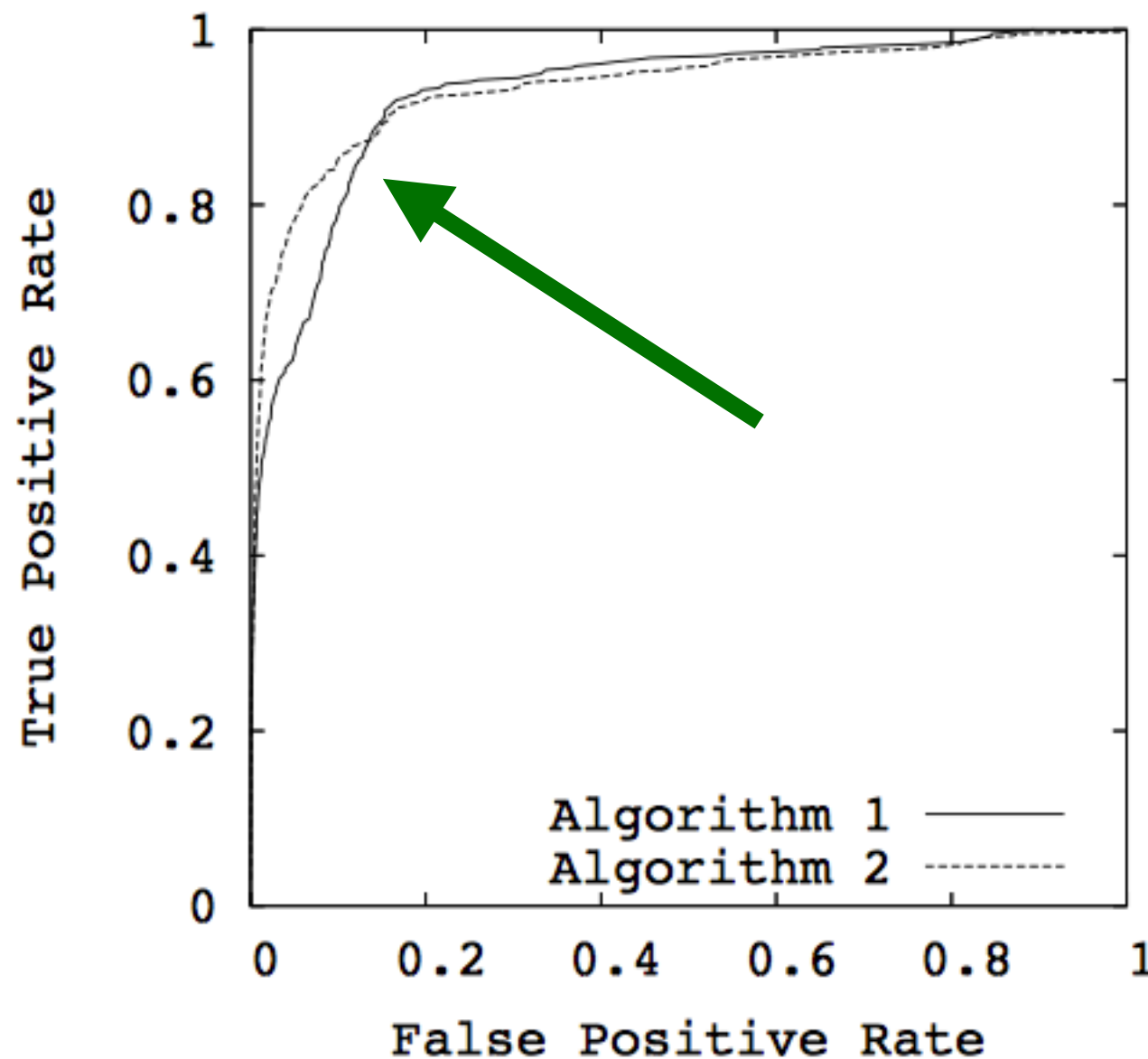
Metrics Analysis

$$\frac{a+b}{2} \geq \sqrt{ab} (a > 0, b > 0, =) \longrightarrow \frac{a+b}{2} \geq \frac{2ab}{a+b}$$

$$F_{\beta} = \frac{Precision * Recall}{\frac{\beta^2}{1+\beta^2} * Precision + \frac{1}{1+\beta^2} * Recall}$$

$$G = \sqrt{Precision * Recall} \quad Precision = Recall + g$$
$$\lim_{g \rightarrow \infty} \frac{2}{\frac{1}{Precision} + \frac{1}{Recall}} = 2 * Recall$$


ROC(Receiver Operator Characteristic Curve)



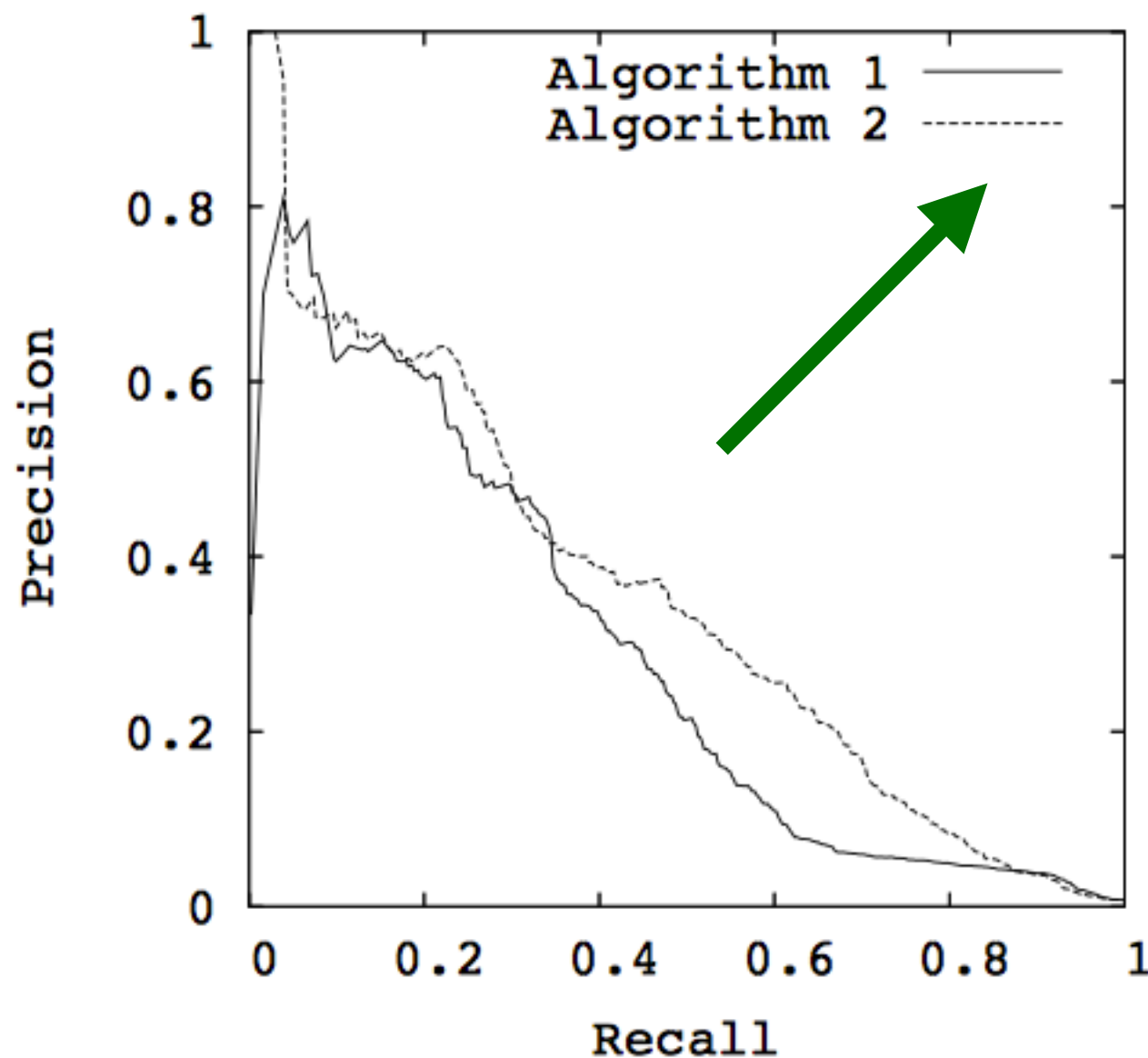
	Actual Positive	Actual Negative
Predicted Positive	TP	FP
Predicted Negative	FN	TN

$$Recall = \frac{TP}{TP + FN}$$

$$True\ Positive\ Rate = \frac{TP}{TP + FN}$$

$$False\ Positive\ Rate = \frac{FP}{FP + TN}$$

PR(Precision Recall)



	Actual Positive	Actual Negative
Predicted Positive	TP	FP
Predicted Negative	FN	TN

$$Recall = \frac{TP}{TP + FN}$$

$$Precision = \frac{TP}{TP + FP}$$

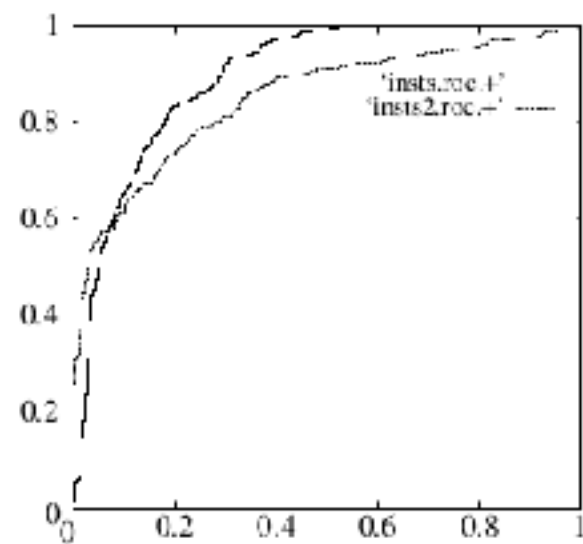
How to get PR/ROC curve?

Sample_No	Label	Threshold_0	Threshold_1	Threshold_2
0	P	Y	...	Y
1	P	Y	...	Y
2	P	Y	...	N
3	P	Y	...	N
4	P	Y	...	N
5	P	N	...	N
6	N	N	...	N
7	N	N	...	Y
8	N	N	...	N
9	N	N	...	Y

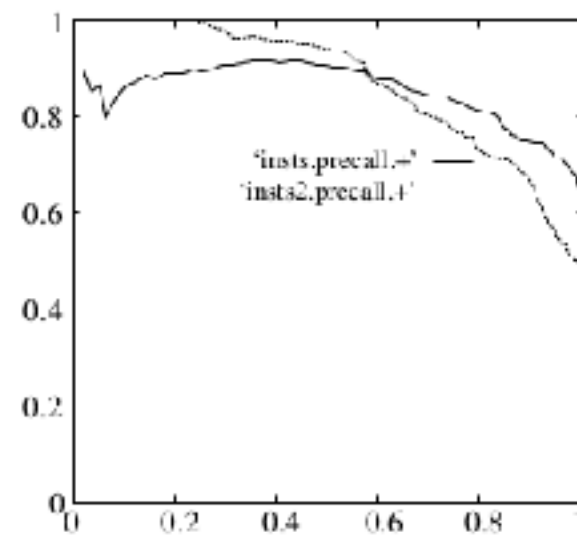
Relationships_(ROC&PR)

- ROC $\xleftrightarrow{\text{Recall} \neq 0}$ PR
- Curve dominates in ROC
 \updownarrow
Curve dominates in PR

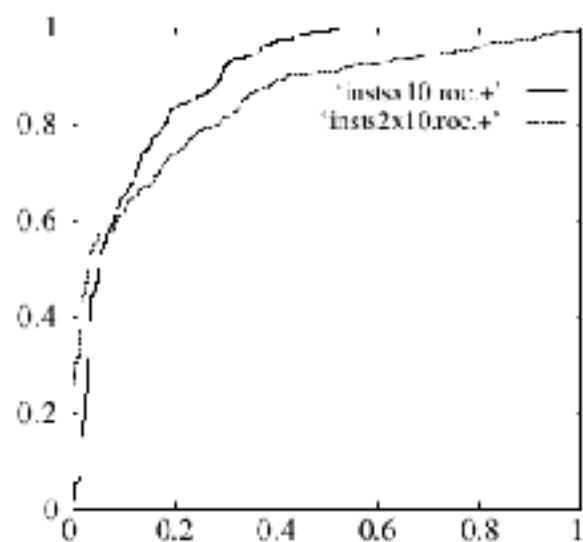
Imbalanced & AUC (Area Under Curve)



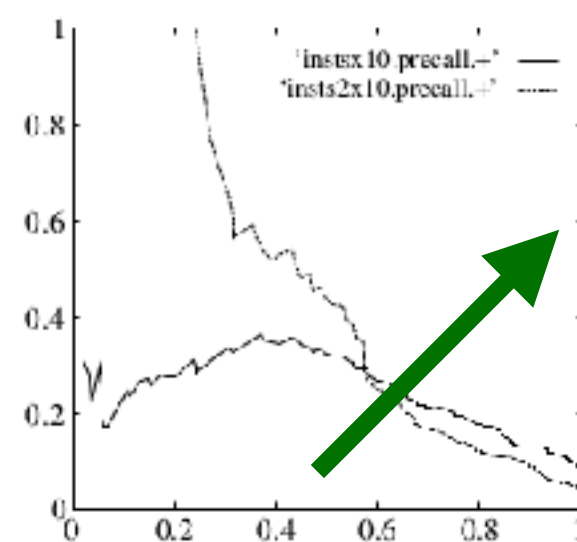
(a)



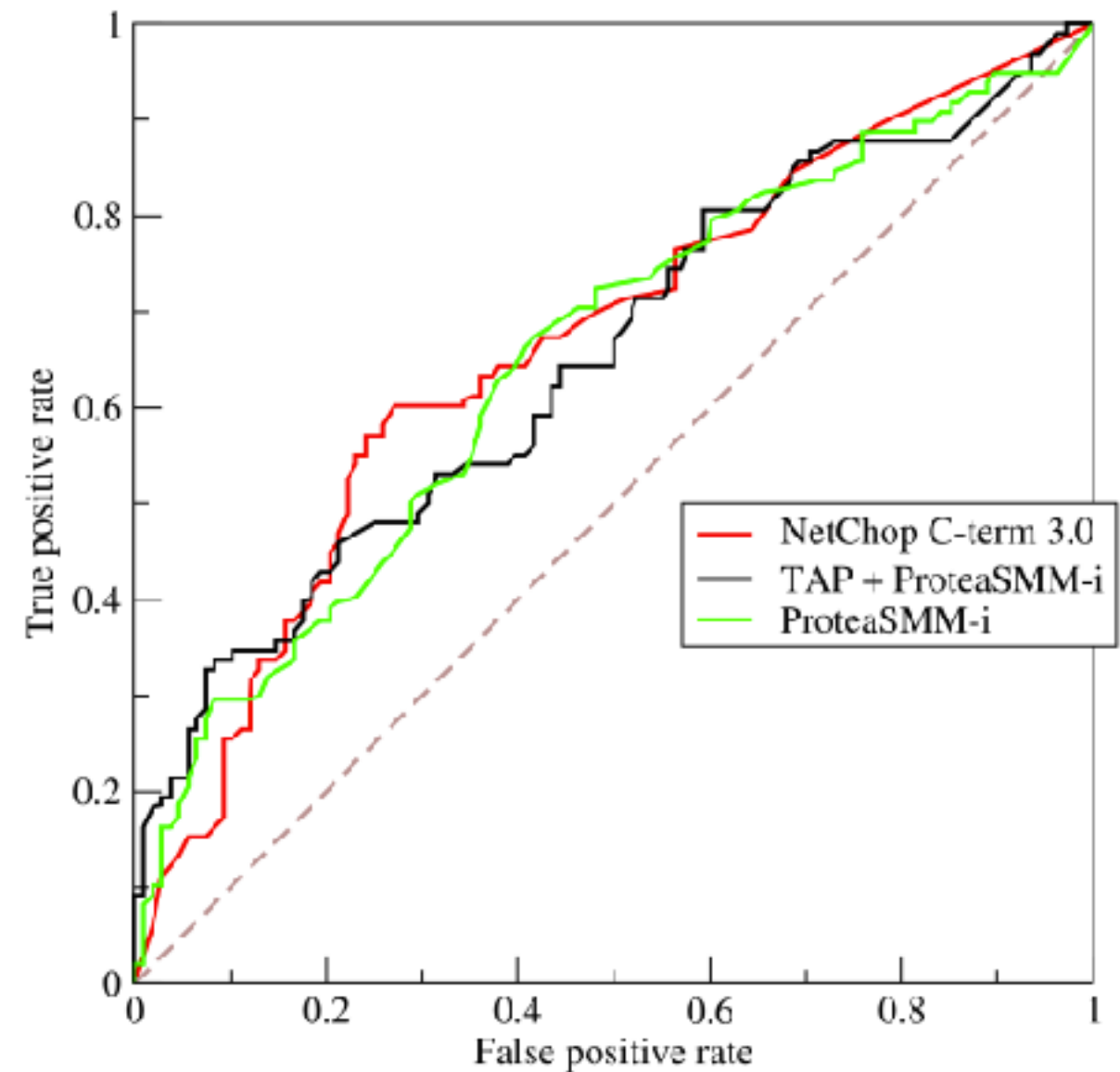
(b)



(c)



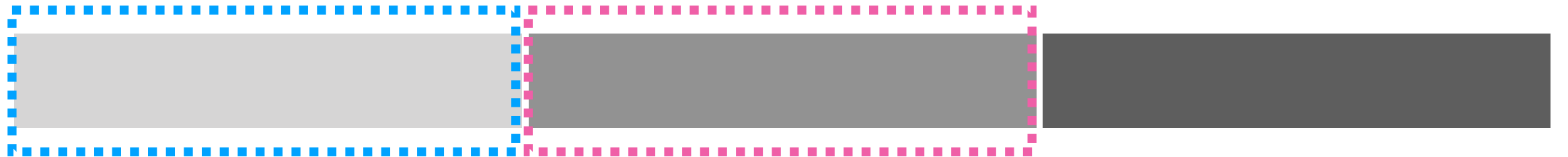
(d)



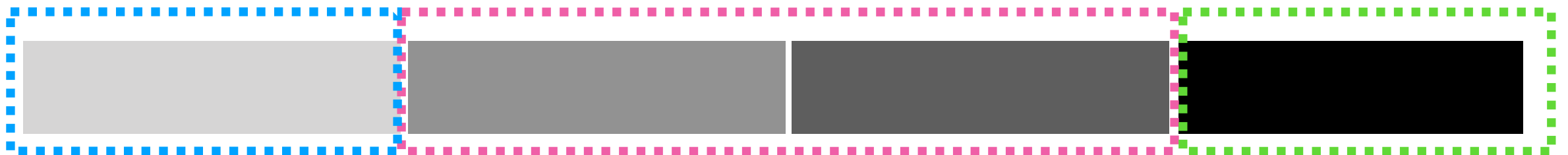
Binary2Multi Classification



(A)



(B)



(C)

参考文献

1. 如何理解与应用调和平均数? <https://www.zhihu.com/question/23096098>
2. 精确率, 召回率, F1值, ROC, AUC各自的优缺点是什么? <https://www.zhihu.com/question/30643044/answer/48955833>
3. Receiver Operating Characteristic: https://en.wikipedia.org/wiki/Receiver_operating_characteristic
4. 《The Relationship Between Precision-Recall and ROC Curves》
5. 《An introduction to ROC analysis》
6. 《支持向量机在多类分类问题中的推广》

TKS

有啥问题需要探讨的吗？