


2. A sky-diver of mass, m , opens her parachute and finds that the air resistance, F_a , is given by the formula $F_a = bv$, where b is a constant and v is the velocity.

- Set up, but do not solve a differential equation for her velocity as a function of time.
- Set up, but do not solve a differential equation for distance as a function of time.
- Find the terminal velocity in terms of m , b , and g .
- If in a different situation the formula for air resistance were $F_a = bv + cv^2$, where c is another constant find the terminal velocity in terms of the above plus c .
- If you are in Calc 2**, solve the differential equations from parts b and c.

a.

$$F_a = -bv \quad F_{\text{net}} = ma$$


$$-bv - mg = m \frac{dv}{dt}$$

d.

$$F_a = bv + cv^2$$

$$cv^2 + bv - mg = 0$$

$$v = \frac{-b \pm \sqrt{b^2 - 4ac}}{2c}$$

$$v = \frac{-b \pm \sqrt{b^2 - 4cm}}{2c}$$

b.

$$-b \frac{dx}{dt} - mg = m \frac{dx^2}{dt^2}$$

c.

$$F_a = bv$$

$$v = \frac{F}{b}$$

$$v = \frac{mg}{b}$$