

Mastering Bitcoin Ch2-Ch4

Agenda

- How Bitcoin Works?
- Bitcoin Core: The Reference Implement (Installation guide)
- Keys, Address

How Bitcoin Works?

Buying a Cup of Coffee

- Alice has 0.1 BTC (10,000,000 Satoshi)
- Buying a cup of coffee costs 0.015 BTC
- Flow:
 - Alice send a transaction to Bob.
 - After Bob verifying the transaction, Alice got a cup of coffee.

Transaction Input: Payment Request

- Bip-21 Format:
 - A URI scheme for making Bitcoin payment
 - easily make payments by simply clicking links on webpages or scanning QR Codes.



```
bitcoin:1GdK9UzpHBzqzX2A9JFP3Di4weBwqgmoQA?  
amount=0.015&  
label=Bob%27s%20Cafe&  
message=Purchase%20at%20Bob%27s%20Cafe
```

Components of the URL

A bitcoin address: "1GdK9UzpHBzqzX2A9JFP3Di4weBwqgmoQA"

The payment amount: "0.015"

A label for the recipient address: "Bob's Cafe"

A description for the payment: "Purchase at Bob's Cafe"

Transaction

- Alice's transaction
- Input: Alice's address
- Two outputs:
 - Pay to Bob.
 - Pay to herself for change. (pay to change address)
- Transaction fee:
 - $\text{Fee} = \text{Total Input} - \text{Total Output}$

Bob's View

- Should Bob wait for bitcoin network to confirm the transaction?
 - A merchant may accept a valid small-value transaction with no confirmations, with no more risk than a credit card payment made without an ID or a signature, as merchants routinely accept today.

Discussion of Transaction

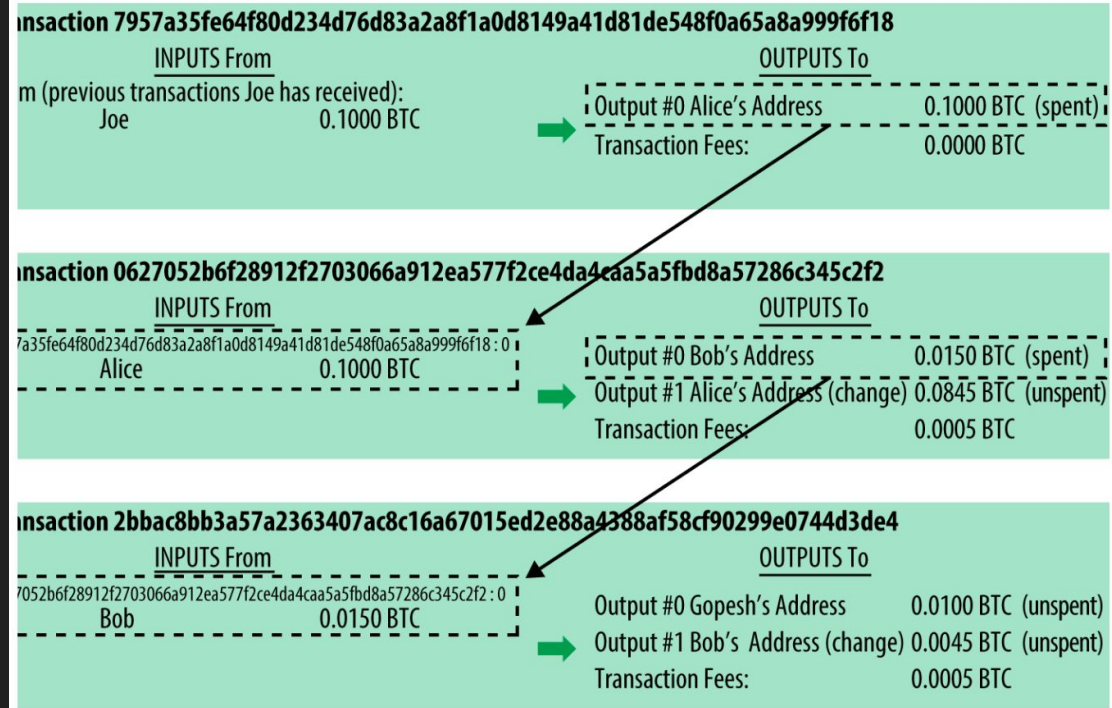
- What is wallet software
 - Lightweight client: Keep track of all the available outputs belonging to addresses in the wallet
 - No copy: Ask a full-node using an application programming interface (API) call
 - Aggregate many small inputs, or use one that is equal to or larger than the desired payment.

```
$ curl https://blockchain.info/unspent?active=1Cdid9KFAaatwczBwBttQcwXYCpvK8h7FK
```

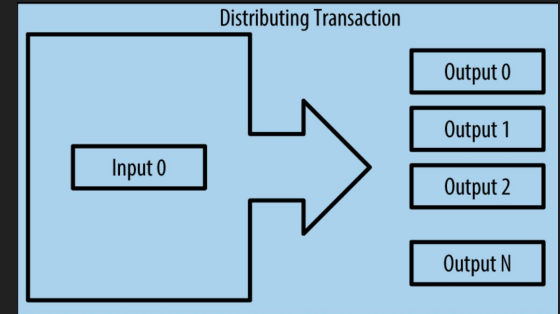
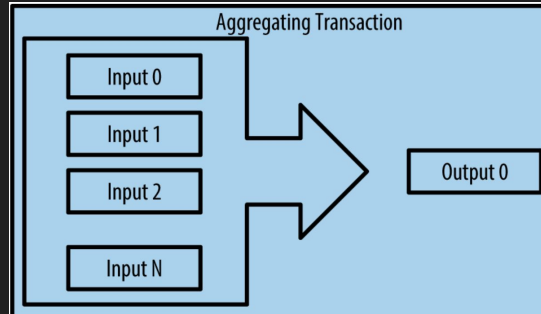
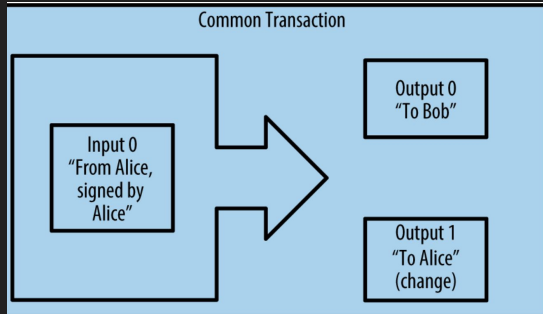
```
{
  "unspent_outputs": [
    {
      "tx_hash": "186f9f998a5...2836dd734d2804fe65fa35779",
      "tx_index": 104810202,
      "tx_output_n": 0,
      "script": "76a9147f9b1a7fb68d60c536c2fd8aeaa53a8f3cc025a888ac",
      "value": 10000000,
      "value_hex": "00989680",
      "confirmations": 0
    }
  ]
}
```


More and More Transaction: Transaction Chains

- Alice gets bitcoin from Joe.
- Alice buys a cup of coffee.
- The inputs from the latest transaction correspond to outputs from previous transactions.



Bitcoin Transaction Types



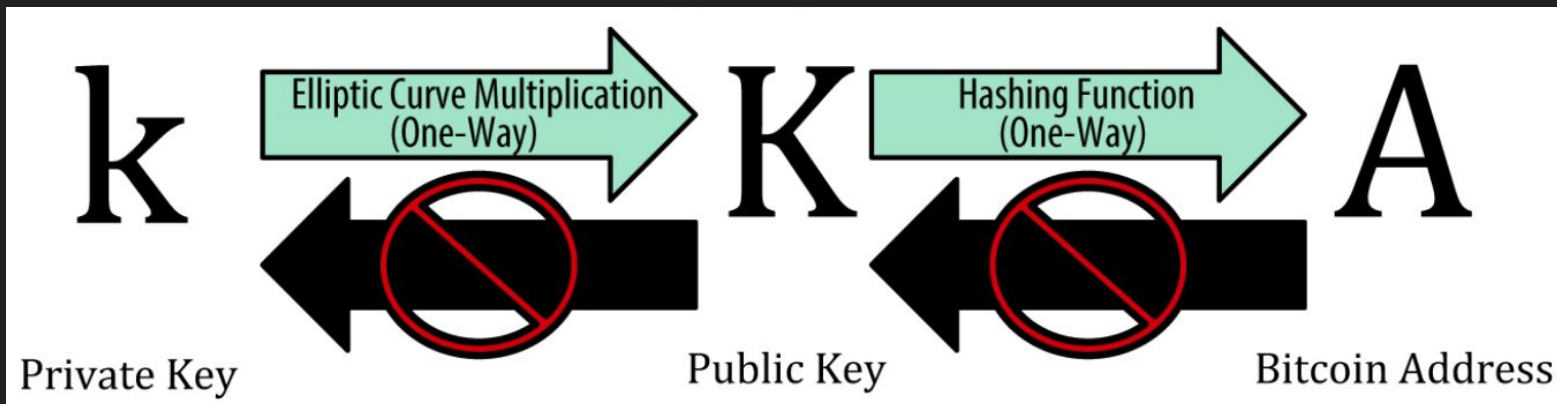
Keys, Address

What are Key Pairs Doing in Blockchain Tech

- Provide:
 - Decentralized trust
 - Control
 - Ownership attestation
- Cryptography is not an important part of bitcoin.

How to Generate Key Pairs

- Pick a *random* number as a private key
- Use elliptic curve multiplication to generate public key from private key
- Use hashing function to get address



How to Generate Private Key

- The private key is a number between 1 and $2^{256} - 1$ (*256 bits)
- Generate it by using:
 - Toss a coin 256 times (manually)
 - Feed a larger string of random bits into the SHA256 hash algorithm.
 - Do not use *simple* random algorithm.

* 256 nits is defined as the order of the elliptic curve

Encrypted Private Key(Bip-38)

- Motivation: safely store in the wallet.
- User needs Password to activate the wallet.

Public Key

- Elliptic curve multiplication:

$$K = k * G$$

K: public key; k: private key; G: generate point

- k can be reversed by brute-force searching

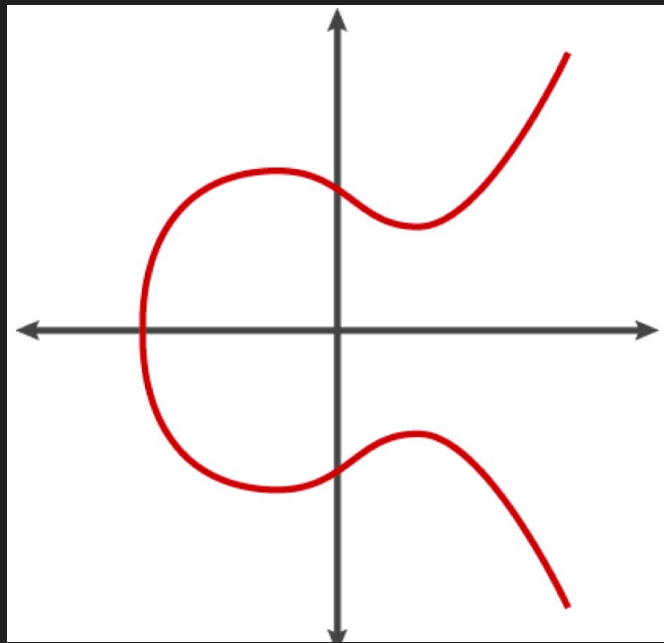
Elliptic Curve Cryptography

- The **secp256k1** Elliptic Curve:

$$y^2 = (x^3 + 7) \bmod p$$

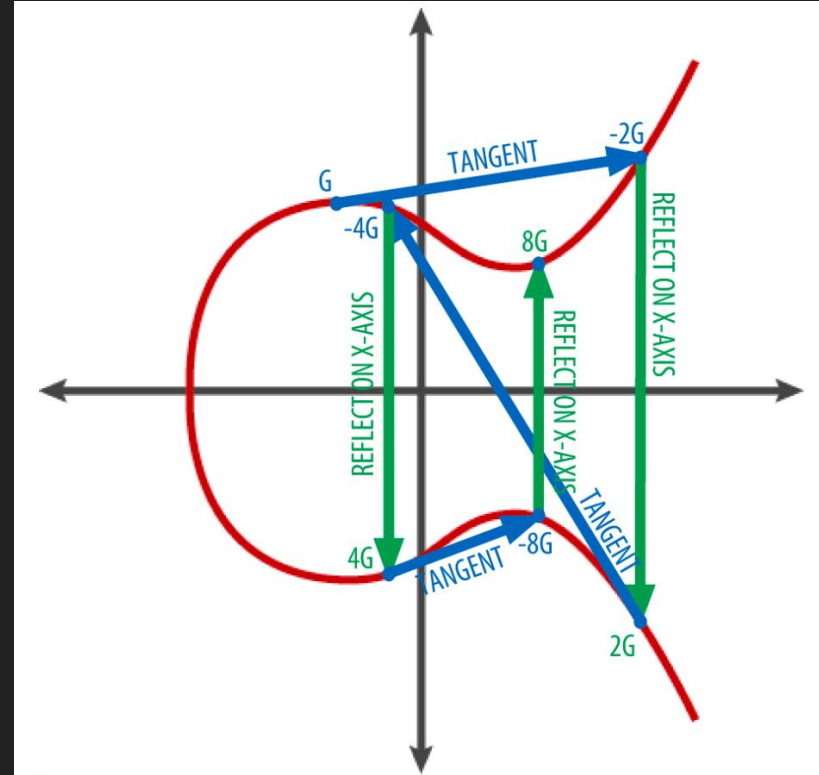
$$p = 2^{256} - 2^{32} - 2^9 - 2^8 - 2^7 - 2^6 - 2^4 - 1$$

- Addition operator $+$ in F_p
 - $P_3 = P_1 + P_2$ is defined as:
 - Draw a line L between P_1 and P_2
 - P_3' is the only one point that L intersect the elliptic curve
 - P_3 is the reflect of P_3'



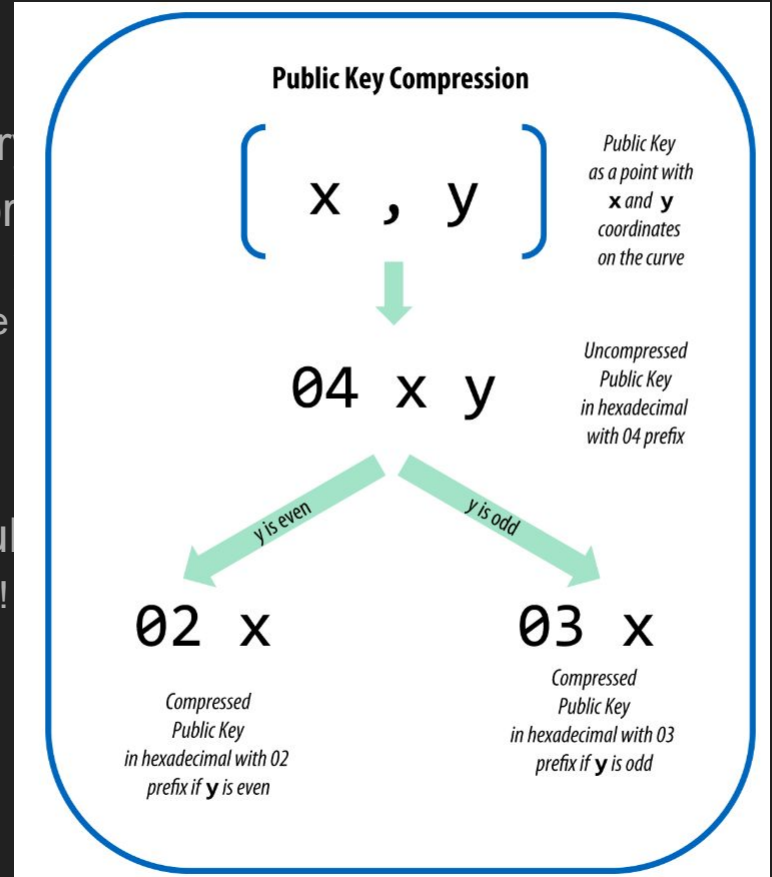
Example

- $K = k * G$
 - $K = G + G + G + \dots$
 - If P1 and P2 are the same point, L is extend to be the tangent on the curve.
- The steps of generating public key:
 - Draw a tangent line L on the point
 - Find where L intersects the curve to derive P'
 - Reflect P' on the x-axis to get next P
 - Finish until k times
 - The public key is: **(04 x y)**
 - Where 04 is prefix, (x,y) is the coordinate of K



Compressed Public Keys

- Motivation: reduce the storage size in every transaction
- Compressed public key: prefix + the x coordinate
 - The y Coordinate can be derived by $(y^2 \bmod p)$
 - The problem is y can be positive or negative (use prefix)
 - We use prefix to store the sign of y
 - 02: even number
 - 03: odd number
- How to deal with one private key to two public keys
 - The bitcoin regards two public keys are different!



Compressed Private Keys???

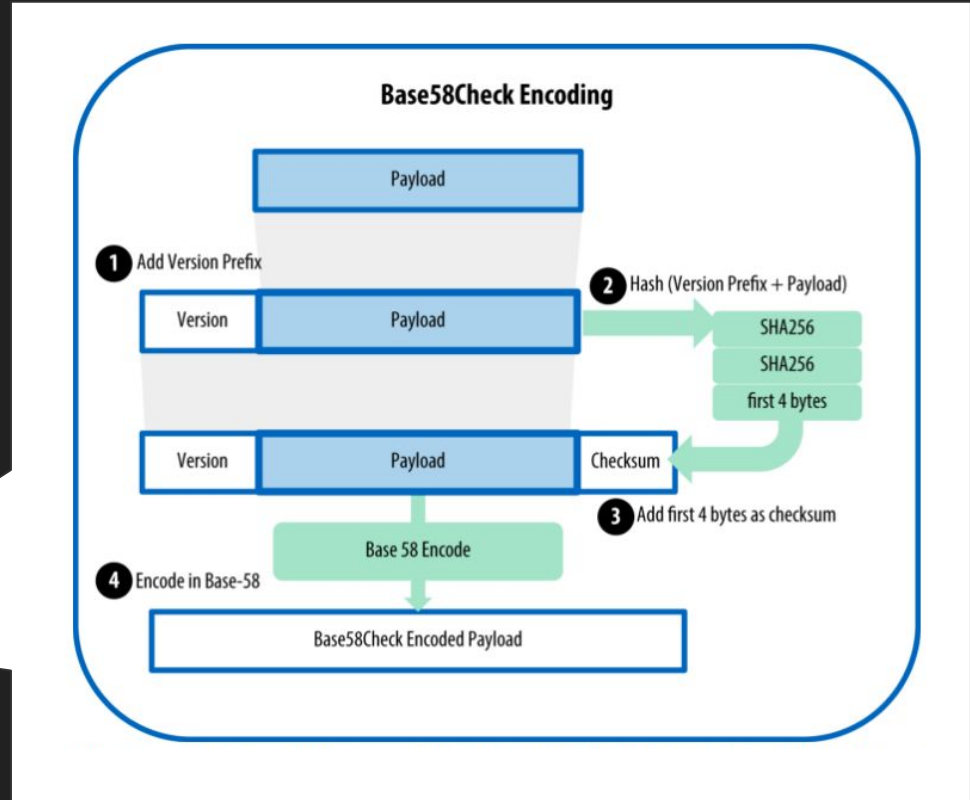
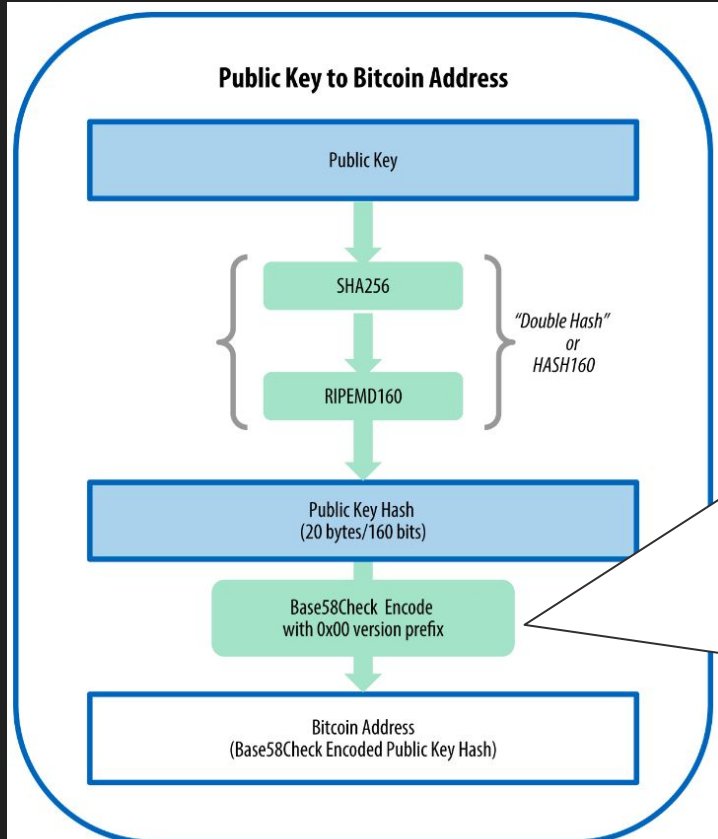
- No real "COMPRESSED" Private keys.
- The compressed private key is the private key with a suffix to signify that the compressed private key should only be used to produce compressed public key.

Format	Private key
Hex	1E99423A4ED27608A15A2616A2B0E9E52CED330AC530EDCC32C8FFC6A526AEDD
WIF	5J3mBbAH58CpQ3Y5RNJpUKPE62SQ5tfcvU2JpbnkeyhfsYB1Jcn
Hex-compressed	1E99423A4ED27608A15A2616A2B0E9E52CED330AC530EDCC32C8FFC6A526AEDD01
WIF-compressed	KxFC1jmwwCoACiCAWZ3eXa96mBM6tb3TYzGmf6YwgdGWZgawvrtJ

Bitcoin Address

- Bitcoin address is not the same as a public key, but it is derived from a public key using one-way function which is called pay-to-public-key-hash (P2PKH).
- Bitcoin addresses are always encoded as Base58Check.
 - Base58 = Base64 - {"0", "O", "l", "I", "+", "/"}
 - Base64: 26 lower and capital letters, 10 numbers, "+", "/"
 - Base58Check = Base58 + error-checking code
 - Error-checking code is derived from the hash of the encoded data and can be used to detect and prevent transcription and typing error.

Bitcoin Address Flowchart



Further Reading

- Pay-to-script-hash(P2SH)
- Vanity addresses (special pattern addresses)