

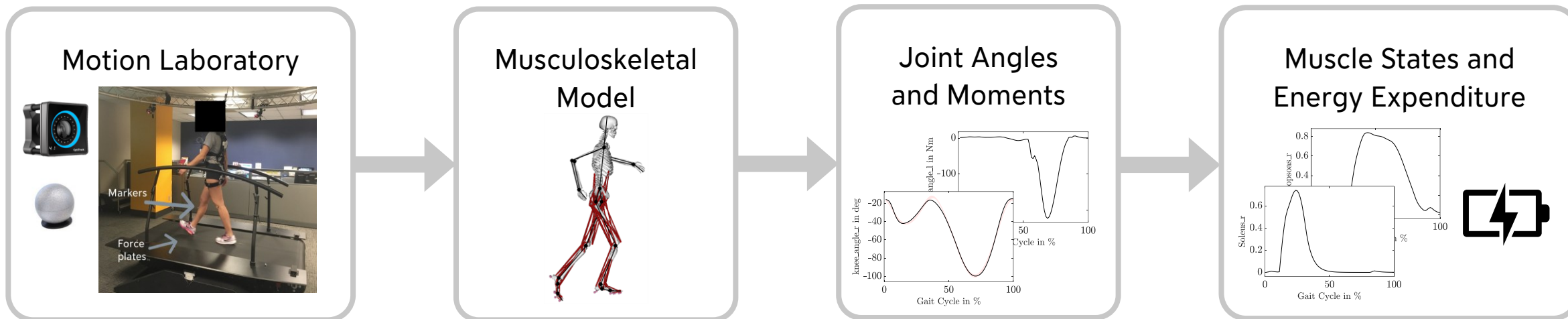
“In the wild” movement analysis using dynamic simulations

Anne Koelewijn and Ton van den Bogert

With help from: Biomechanical Motion Analysis and Creation (BioMAC) group
Friedrich-Alexander-Universität Erlangen-Nürnberg (FAU), Erlangen, Germany
Cleveland State University, Cleveland, USA

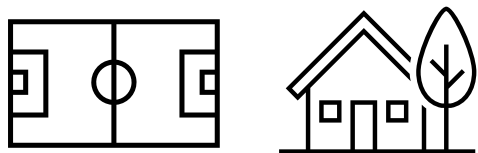
Movement Analysis

Standard Approach: Optical Motion Capture and inverse methods



Challenges

- Restricted environment

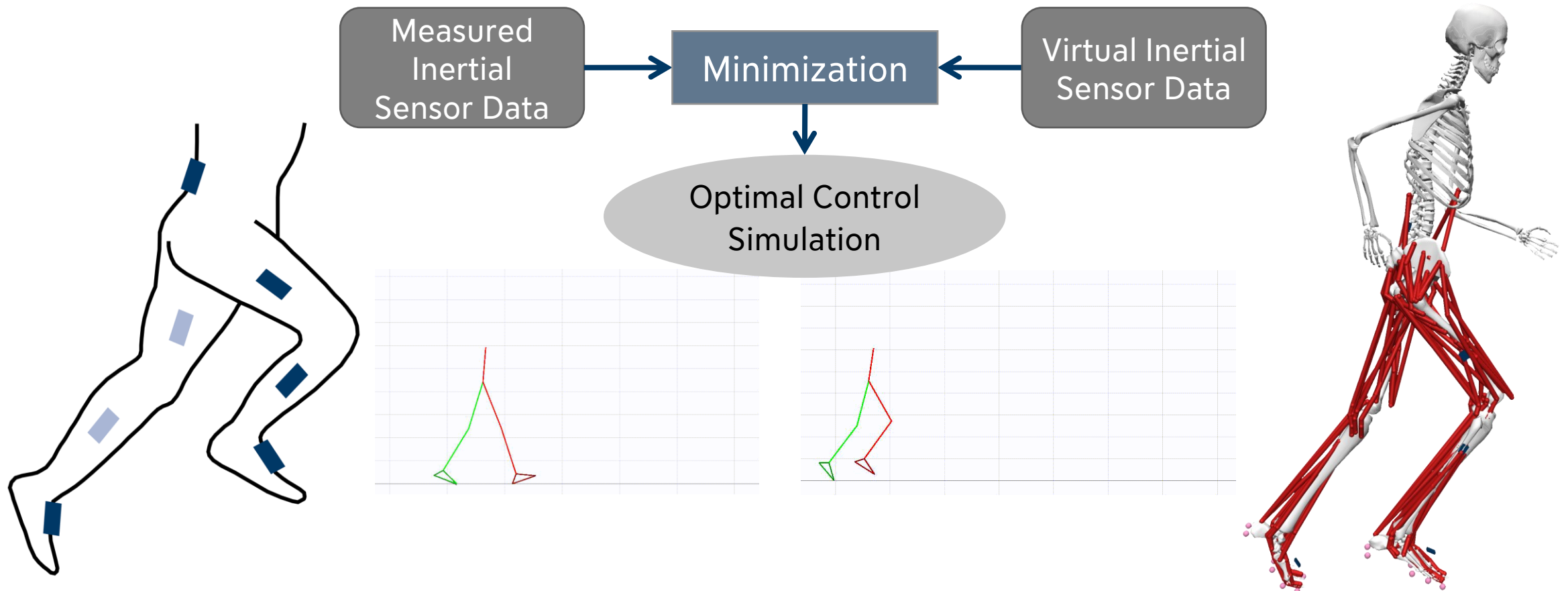


- Time consuming



Optimal Control Simulations

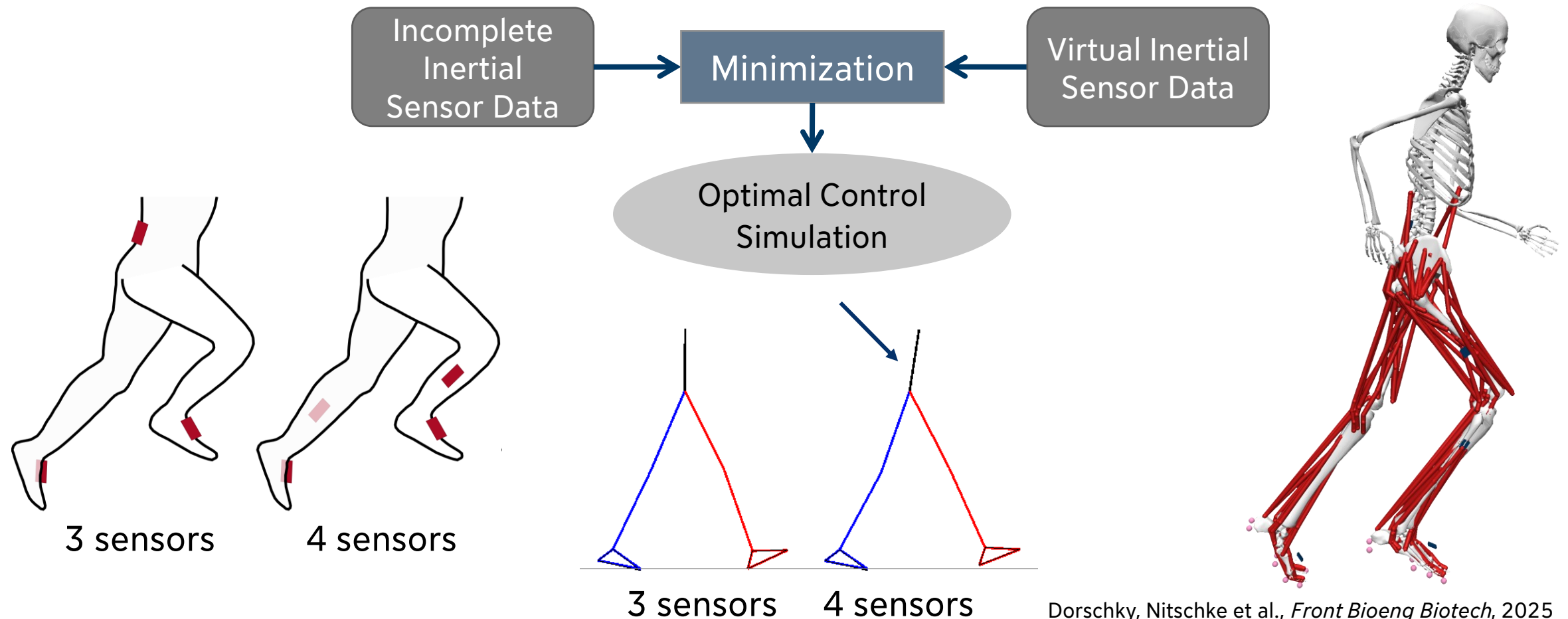
Movement Reconstruction Concept



Dorschky et al., *J Biomech*, 2019

Optimal Control Simulations

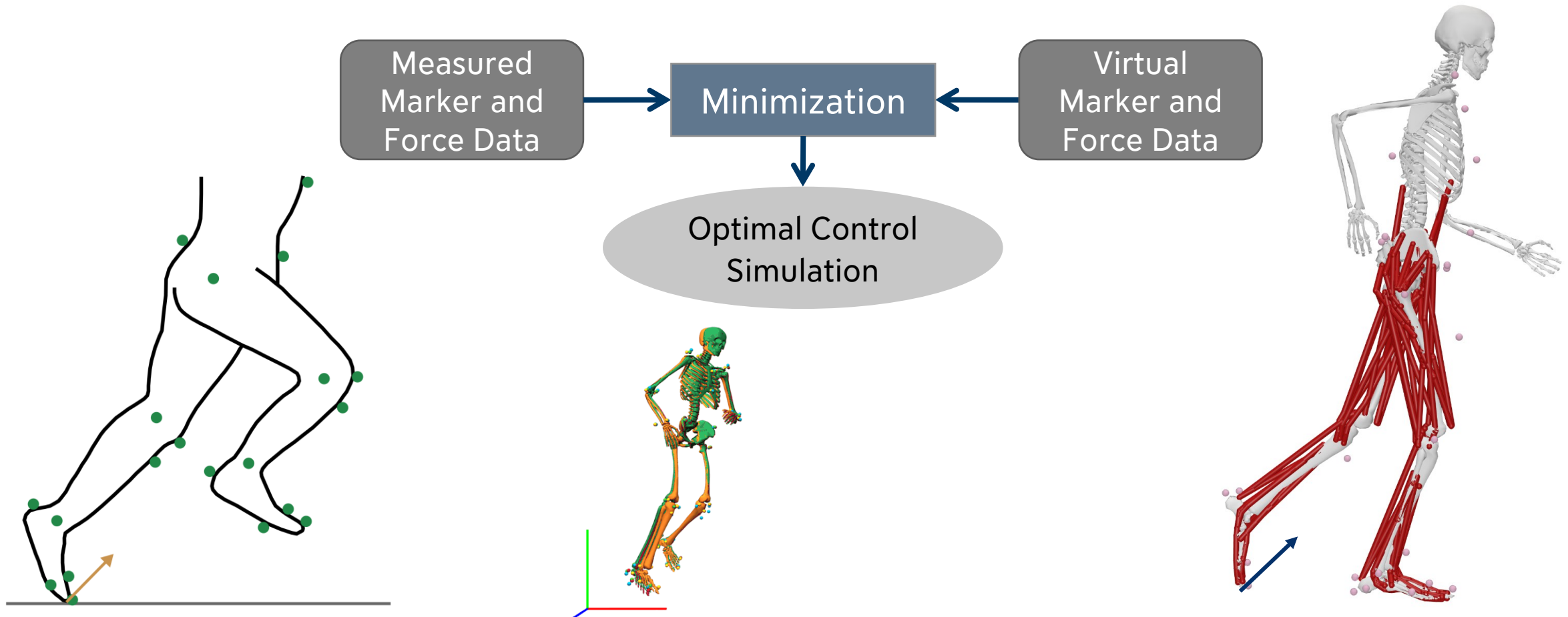
Incomplete Data



Dorschky, Nitschke et al., *Front Bioeng Biotech*, 2025

Optimal Control Simulations

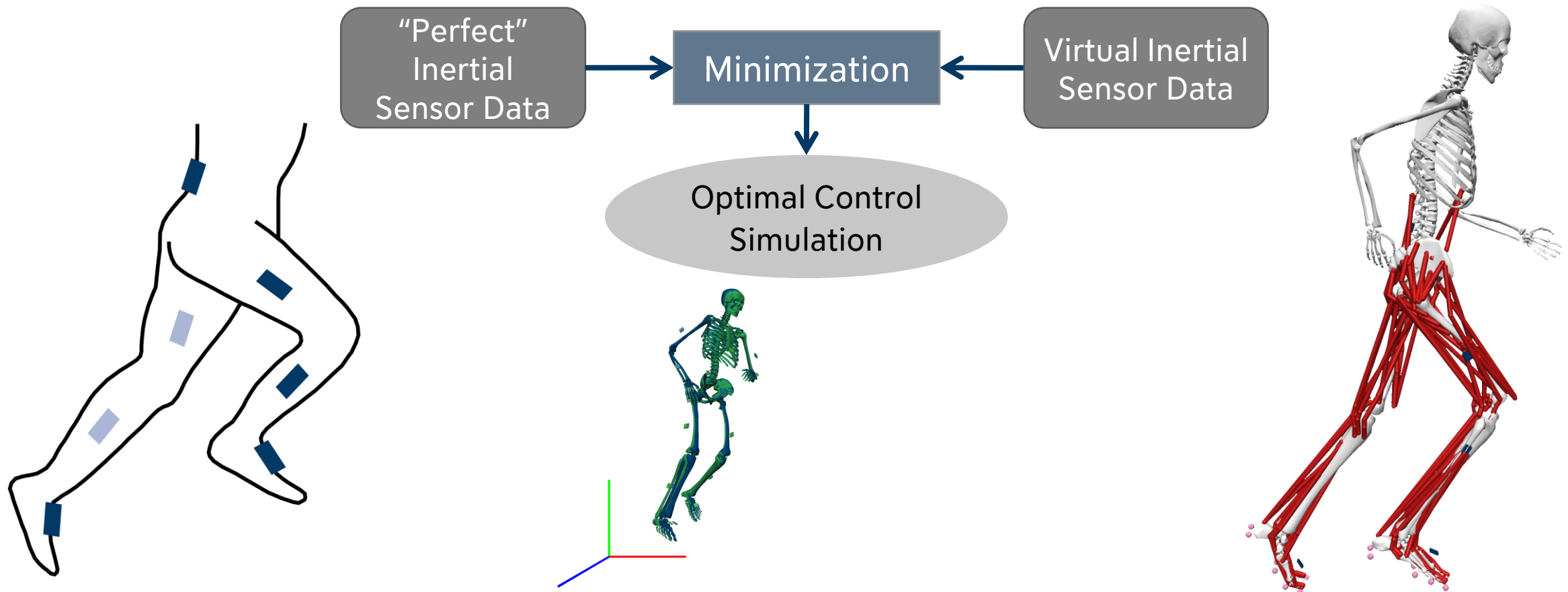
3D Reconstruction from Marker and Force Data



Nitschke, ..., Koelewijn, *PeerJ*, 2023

Optimal Control Simulations

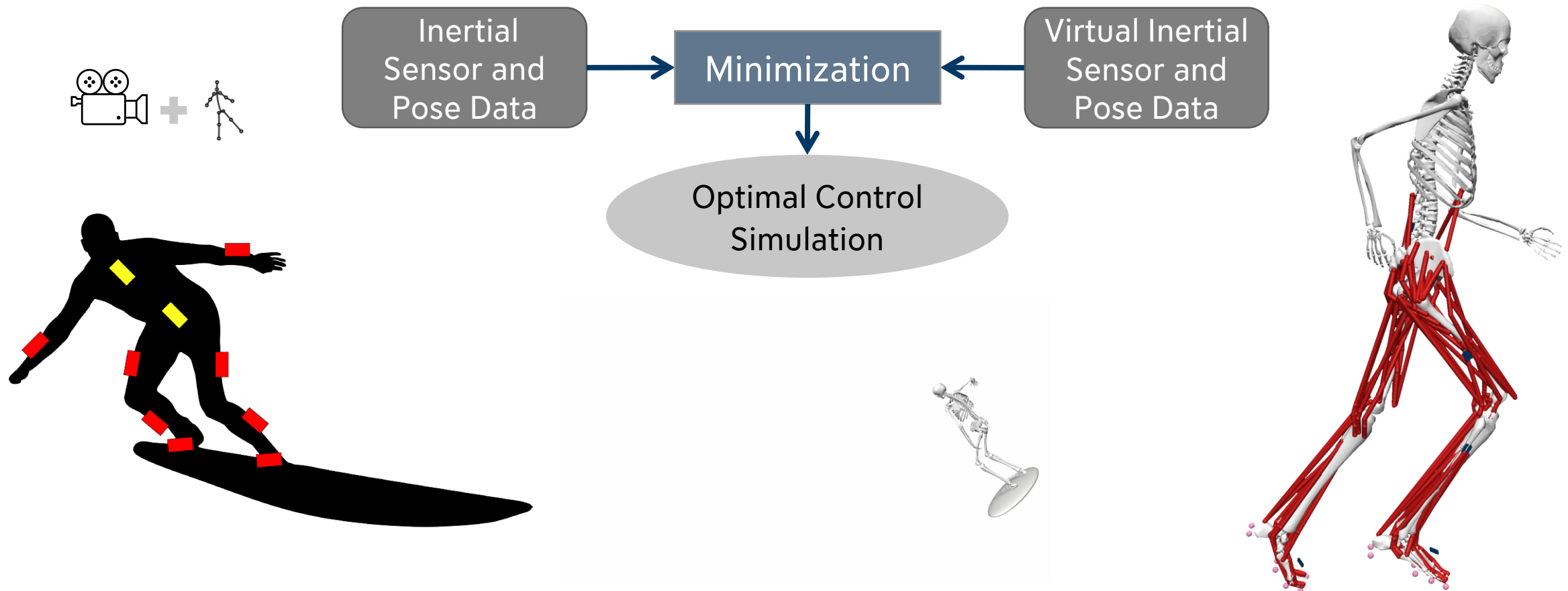
3D Reconstruction from Inertial Sensor Data (Proof of Concept)



Nitschke et al., *Front Bioeng Biotech*, 2024

Biomechanical Analysis of Surfing

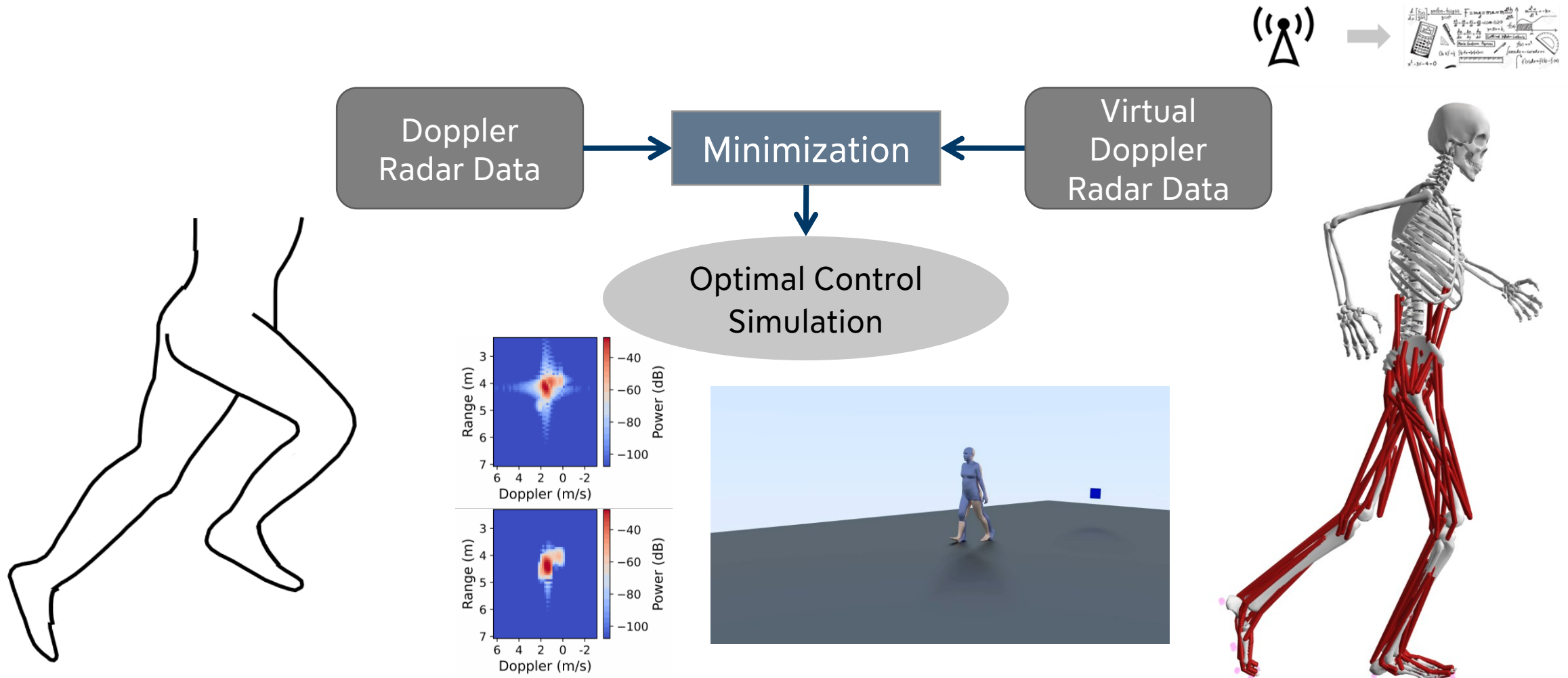
3D Reconstruction from Inertial Sensor and Video Data



Weiss et al., *Mult Sys Dyn*, 2025

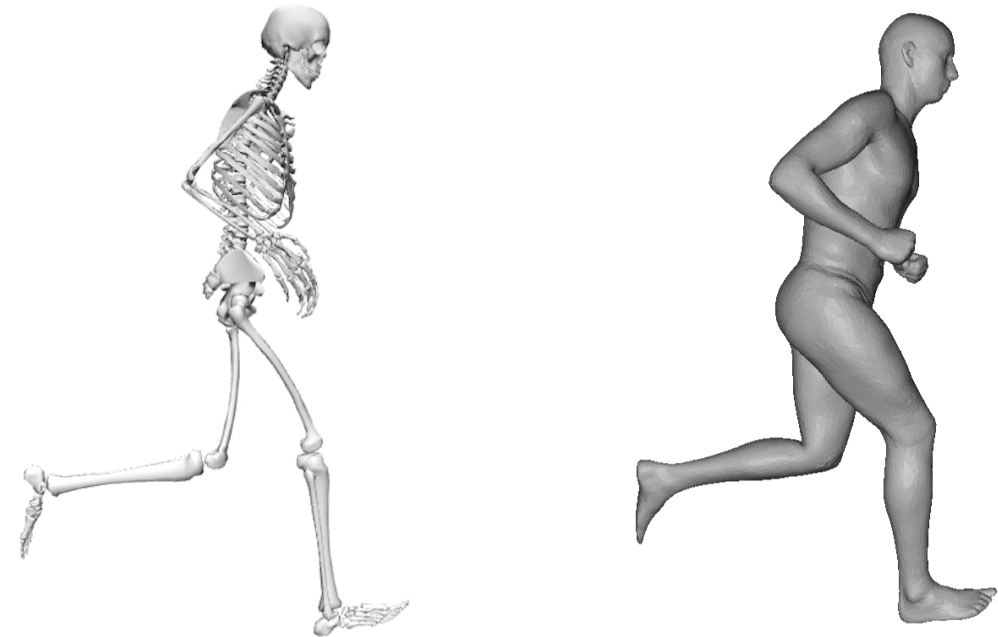
Optimal Control Simulations

Movement Reconstructions from Radar Sensors



Gambietz et al., *ASILOMAR*, 2024; Schüßler et al., *IEEE J Microw*, 2021

- 1 Optimal Control Simulations
 - Forward Dynamics Simulation
 - Trajectory Optimization/Optimal Control
 - Direct Collocation
- 2 Inertial Sensor Model
- 3 Hands-On Tutorial
 - Toolbox and Tutorial Introduction
 - Familiarizing with the Output and Objects
 - Comparing 2D Simulations from IMU Data
 - Writing New Code
- 4 Conclusion



Forward Dynamics Simulation

Dynamics: description of an object's motion

- Accelerations are related to the applied forces

The motion of the body is defined by the skeleton

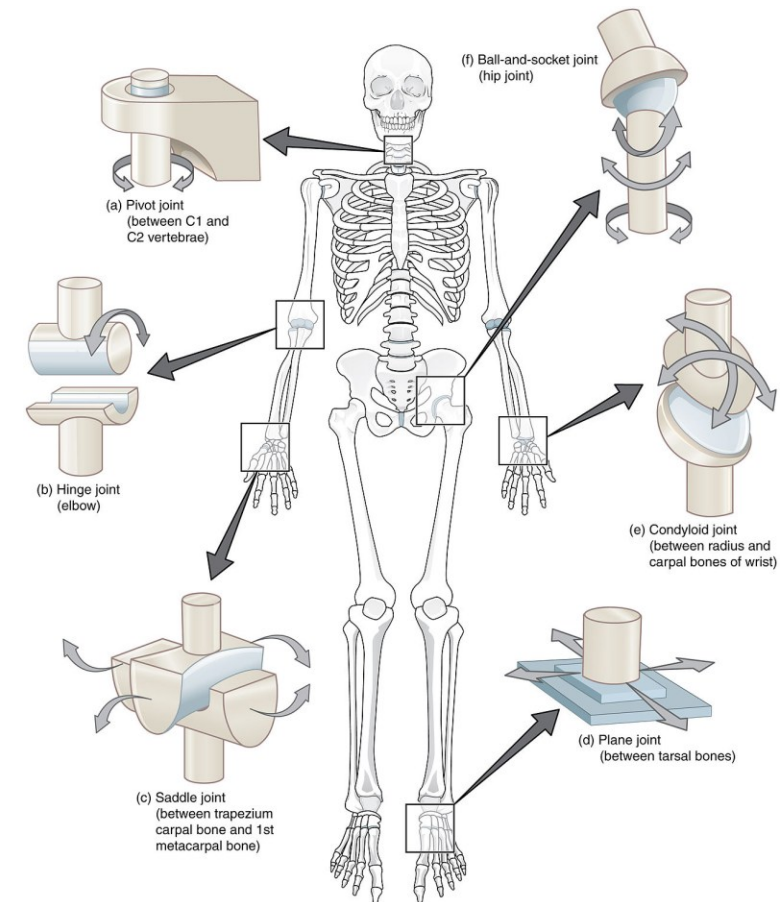
- Rigid bodies connected by joints
- Joint type defines degrees of freedom

Multibody dynamics

- Define the degrees of freedom
 - Global position and orientation of one reference segment (trunk)
 - Angles between segments

Propulsion: joint torques or muscle stimulations

- Muscle stimulation require muscle dynamics in addition



$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) = \tau + J^T(q)F_{ext}$$

q : degrees of freedom

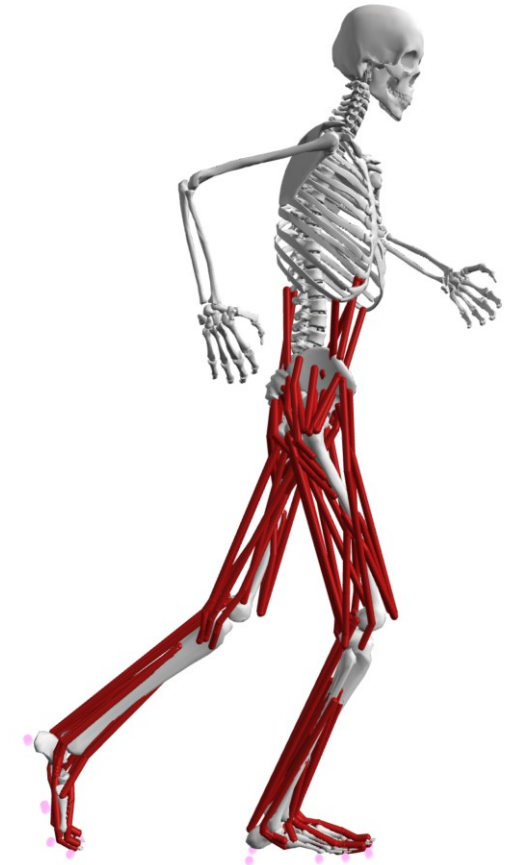
M : mass/inertia matrix, dependent on the joint angles

C : Centrifugal/coriolis matrix, dependent on joint angles and velocities

G : Gravity matrix, dependent on the joint angles

$J^T(q)F_{ext}$: External forces (ground reaction forces) using Jacobian

τ : internal moments / generalized forces / joint moments



$$M(q(t))\ddot{q}(t) + C(q(t), \dot{q}(t))\dot{q}(t) + G(q(t)) = \tau(t) + J^T(q(t))F_{ext}(t)$$

q : degrees of freedom

M : mass/inertia matrix, dependent on the joint angles

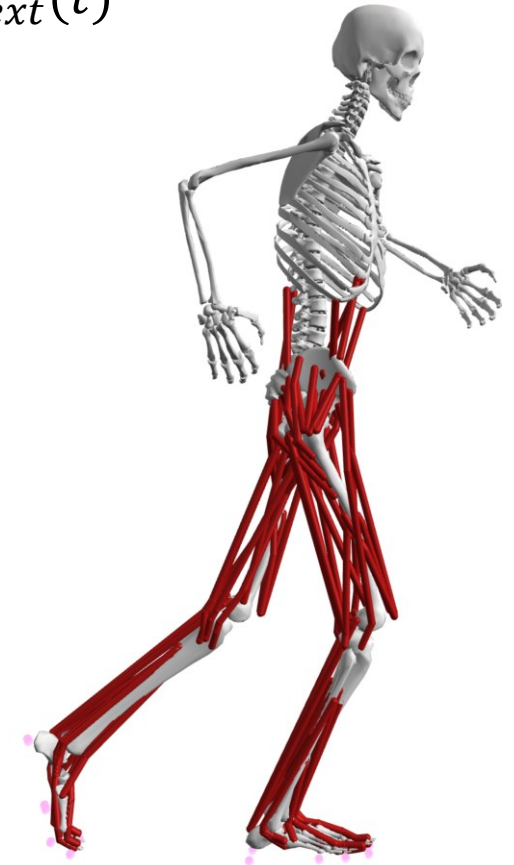
C : Centrifugal/coriolis matrix, dependent on joint angles and velocities

G : Gravity matrix, dependent on the joint angles

$J^T(q)F_{ext}$: External forces (ground reaction forces) using Jacobian

τ : internal moments / generalized forces / joint moments

Goal of a simulation: find $q(t)$ and $\tau(t)$



$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) = \tau + J^T(q)F_{ext}$$

Dynamics equation includes the second derivative of the joint angle, while numerical integration methods are first order.

- Use state $x = \begin{bmatrix} q \\ \dot{q} \end{bmatrix}$ with joint angles and velocities (and global orientation and position and derivative)

$$\dot{x} = \begin{bmatrix} \dot{q} \\ \ddot{q} \end{bmatrix} = \begin{bmatrix} \dot{q} \\ M^{-1}(q)(\tau + J^T(q)F_{ext} - C(q, \dot{q})\dot{q} - G(q)) \end{bmatrix} = \begin{bmatrix} \dot{q}(t) \\ f(q(t), \dot{q}(t)) \end{bmatrix}$$

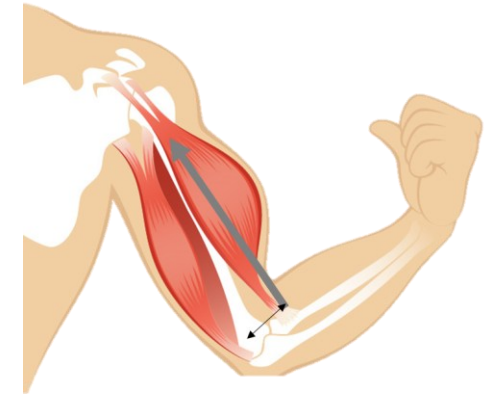
And the state at the next time point:

$$x(t + \Delta t) = \begin{bmatrix} q(t + \Delta t) \\ \dot{q}(t + \Delta t) \end{bmatrix} = \begin{bmatrix} q(t) \\ \dot{q}(t) \end{bmatrix} + \Delta t \begin{bmatrix} \dot{q}(t) \\ f(q(t), \dot{q}(t)) \end{bmatrix}$$

$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) = \tau + J^T(q)F_{ext}$$

Inputs are τ : joint torques

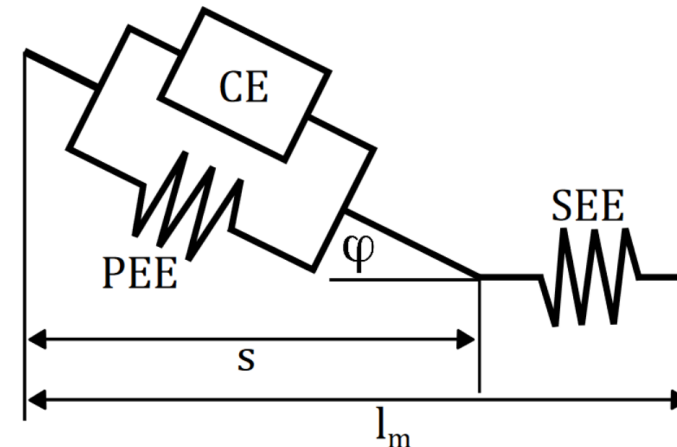
- Joint torques can be input directly
- Determine joint torques from muscle forces $\tau = DF_{SEE}$
 - D : matrix of moment arms



Muscle dynamics

- $F_{SEE} = (F_{ce} + F_{PEE}) \cos(\phi)$
- Two differential equations
 - $F_{CE} = af(l_{CE})g(v_{CE})F_{iso}$
 - $\frac{da}{dt} = \left(\frac{u(t)}{T_{act}} + \frac{1-u(t)}{T_{deact}} \right) (u(t) - a(t))$

→ Input is neural stimulation $u(t)$



$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) = \tau + J^T(q)F_{ext}$$

Creating a simulation (for a human musculoskeletal system):

$$x(t + \Delta t) = \begin{bmatrix} q(t + \Delta t) \\ \dot{q}(t + \Delta t) \\ a(t + \Delta t) \\ l_{CE}(t + \Delta t) \end{bmatrix} = \begin{bmatrix} q(t) \\ \dot{q}(t) \\ a(t) \\ l_{CE}(t) \end{bmatrix} + \Delta t \begin{bmatrix} \dot{q}(t) \\ f(q, \dot{q}, a, l_{CE}) \\ \dot{a}(t, u) \\ v_{CE}(t) \end{bmatrix}$$
$$f(q, \dot{q}, a, l_{CE}) = M^{-1}(q)(\tau + J^T(q)F_{ext} - C(q, \dot{q})\dot{q} - G(q))$$

- τ comes from the muscle forces
- The equation for \dot{a} and v_{CE} are the Hill model

→ What is u ?

- The muscle inputs for the model to perform the desired task

Questions?

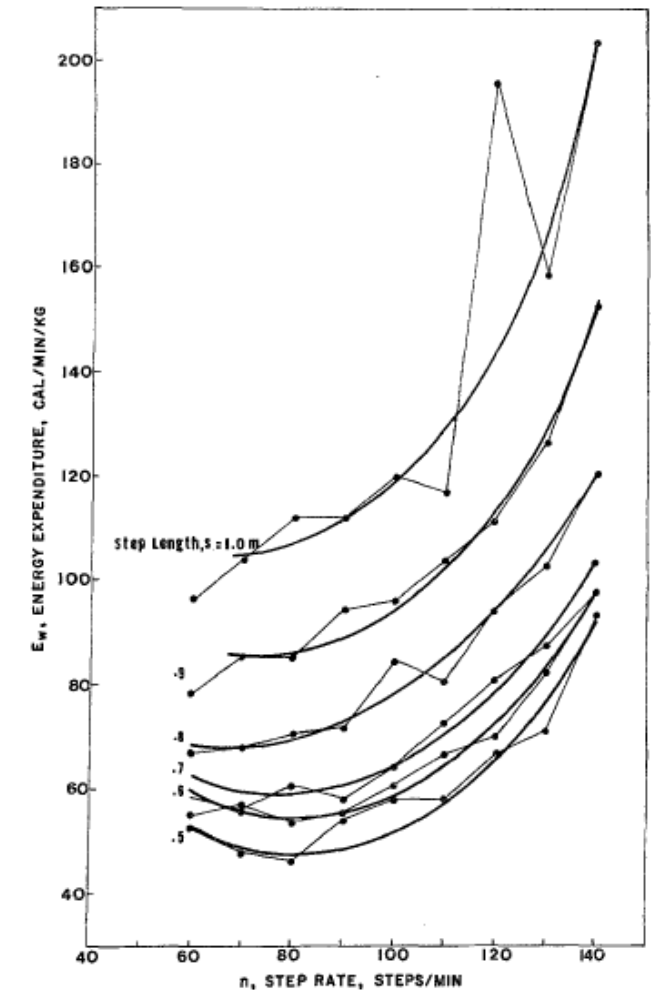
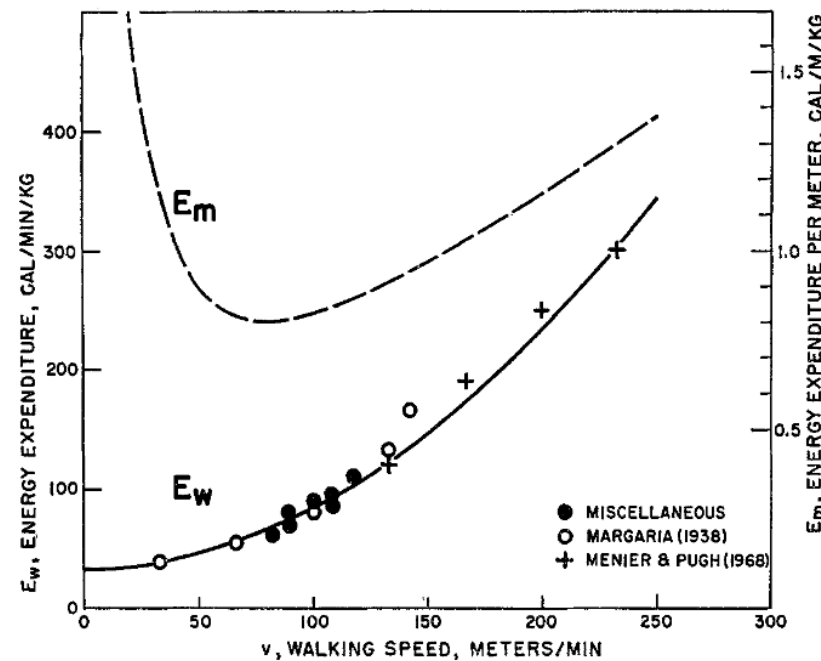


Optimal Control/Trajectory Optimization

Why an Optimization?

People minimize energy expenditure when planning movements

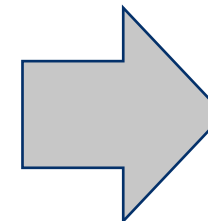
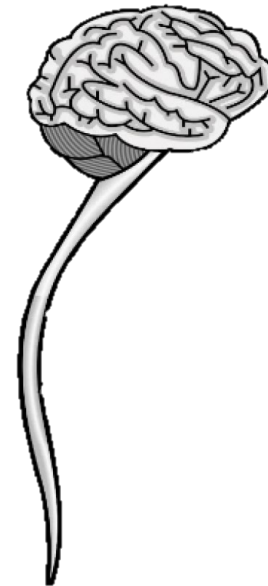
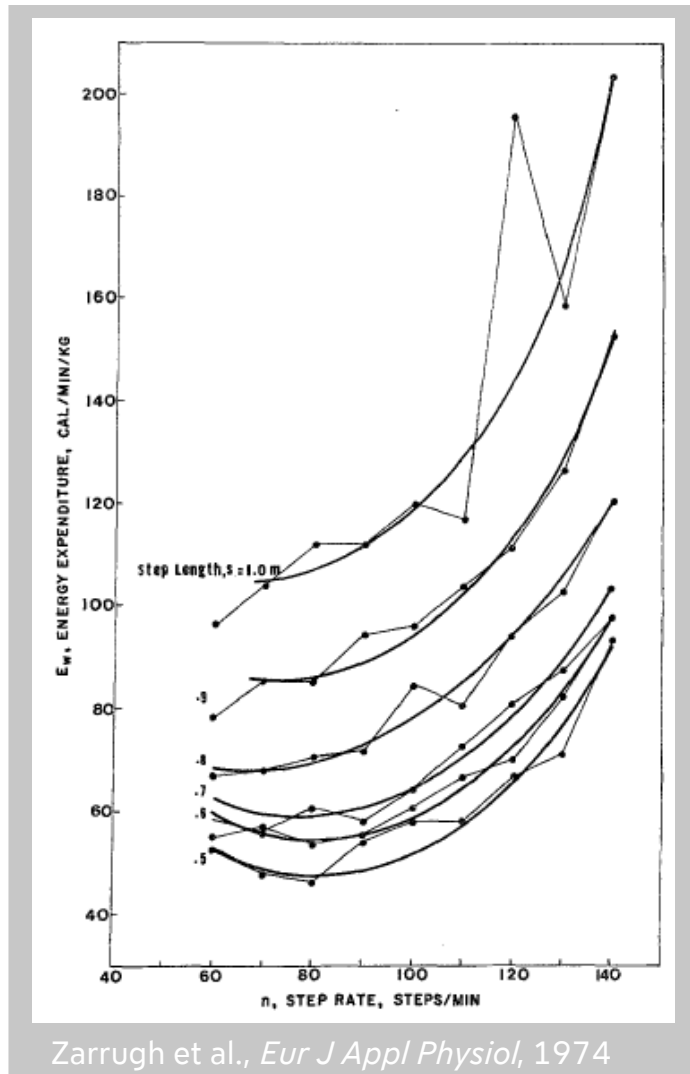
- This is an optimization
- It can be converted to a computer optimization



Zarrugh et al., *Europ. J. Appl. Physiol.*, 1974

Creating Movement Simulations

Solve the same optimization on a computer as in the nervous system

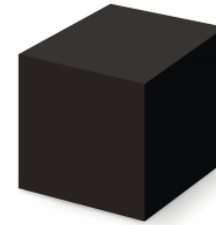


Two types of simulations

How is muscle stimulation created?

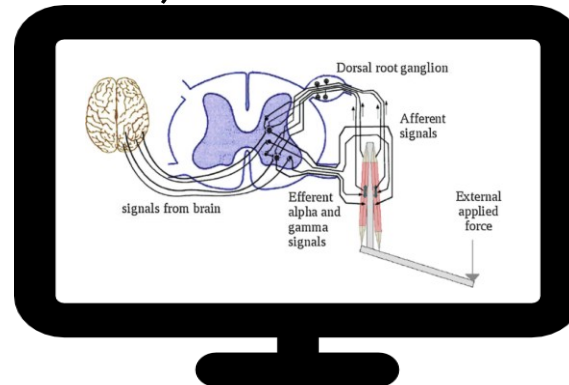
- Trajectory focused

Be energy efficient
(optimize objective)



Muscle stimulations for
gait cycle

- Outcome: time-series of muscle stimulations and movement
- Neural control (control focused)



- Outcome: reflex or other control model parameters

Term	Definition
Constraints	Requirements on variables that are required to be satisfied
Optimization variables	The variables that are changed in order to solve the optimization
Objective	The function that is minimized (or maximized)

Optimization variables:

Find inputs $u(t)$, $0 \leq t \leq T$

Dynamics:

For system $\dot{x}(t) = f(x(t), u(t))$

That minimize:

Objective:

$$J(x, u, t) = \frac{1}{T} \int_{t=0}^T c(x(t), u(t)) dt$$

Subject to:

Task constraints:

$$g(x(t_h)) = 0$$



Term	Definition
Constraints	Requirements on variables that are required to be satisfied
Optimization variables	The variables that are changed in order to solve the optimization
Objective	<div>How do we solve this problem?</div>
Optimization	
Dynamic	
Objective	

Task constraints: $g(x(t_h)) = 0$

Compare to shooting a cannon

- Initial conditions $x(0)$ are known

Try control input $u(t)$ and simulate

- Numerical integration

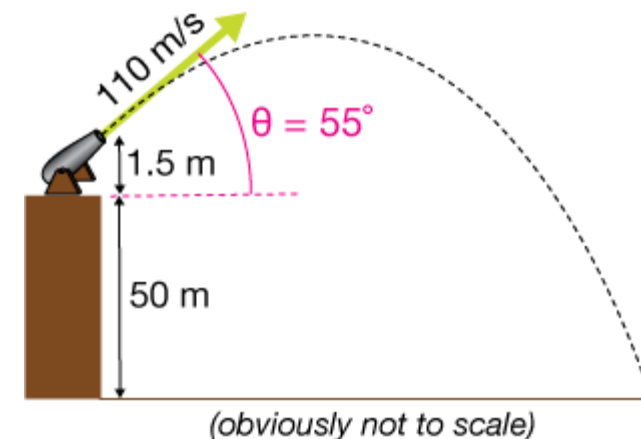
$$x(\Delta t) = x(0) + \Delta t f(x(0), u(0))$$

$$x(2\Delta t) = x(\Delta t) + \Delta t f(x(\Delta t), u(\Delta t))$$

\vdots

$$x(t + \Delta t) = x(t) + \Delta t f(x(t), u(t))$$

Iterate until objective is minimized



<http://xaktly.com/ProjectileMotion.html>

Try states at several key times, $x(0)$, $x(t_1)$, $x(t_2)$ and control input $u(t)$

Iterate until

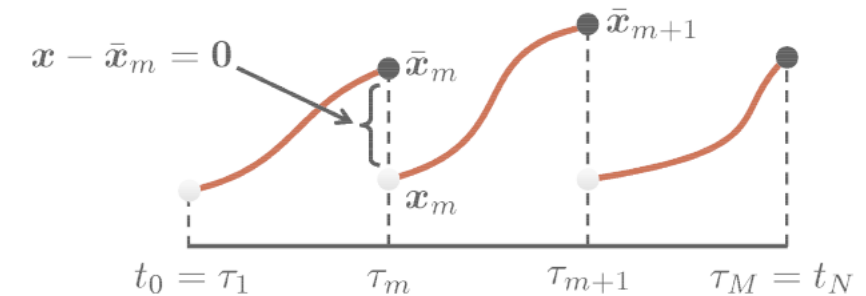
- Objective is minimized
- Constraints ensure system goes from $x(0)$ to $x(t_1)$ to $x(t_2)$

Optimization variables:

$$v_{opt} = \begin{bmatrix} u(0) \\ \vdots \\ u(T) \\ x(t_1) \\ x(t_2) \\ \vdots \\ x(t_f) \end{bmatrix}$$

Example in gait:

- Separate dynamics for swing, stance and double stance
- Allows for fixed base dynamics



No forward simulation: dynamics added to the constraints

- Forward simulation: $x(t + 1) = x(t) + \Delta t f(x(t), u(t))$
- Can be converted to a constraint $g(x(t_h)) = 0$

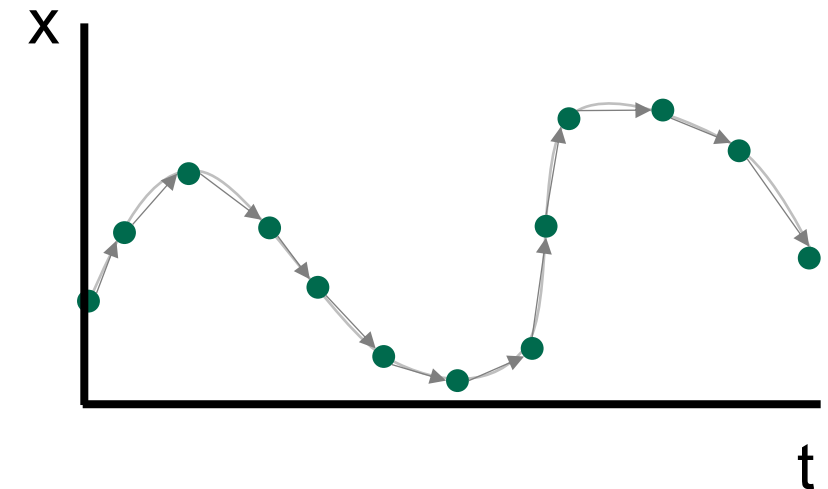
Try a set of states $x(t)$, and inputs

$$u(t), 0 \leq t \leq T$$

Iterate until

- Objective is minimized
- States and inputs follow dynamics

$$v_{opt} = \begin{bmatrix} u(0) \\ \vdots \\ u(T) \\ x(0) \\ x(t_1) \\ \vdots \\ x(T) \end{bmatrix}$$



Optimization problem with many optimization variables and constraints

Questions?



Direct Collocation

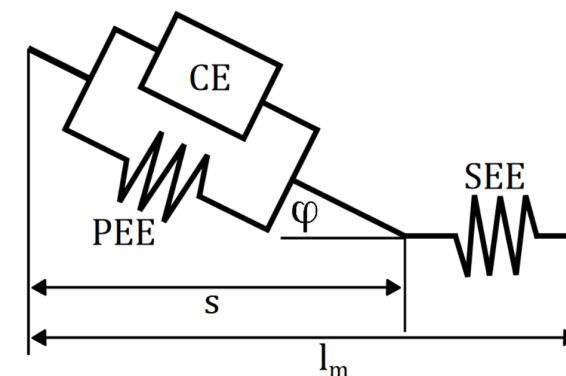
NO forward simulation → Adds dynamics to the constraints

Forward Simulation:

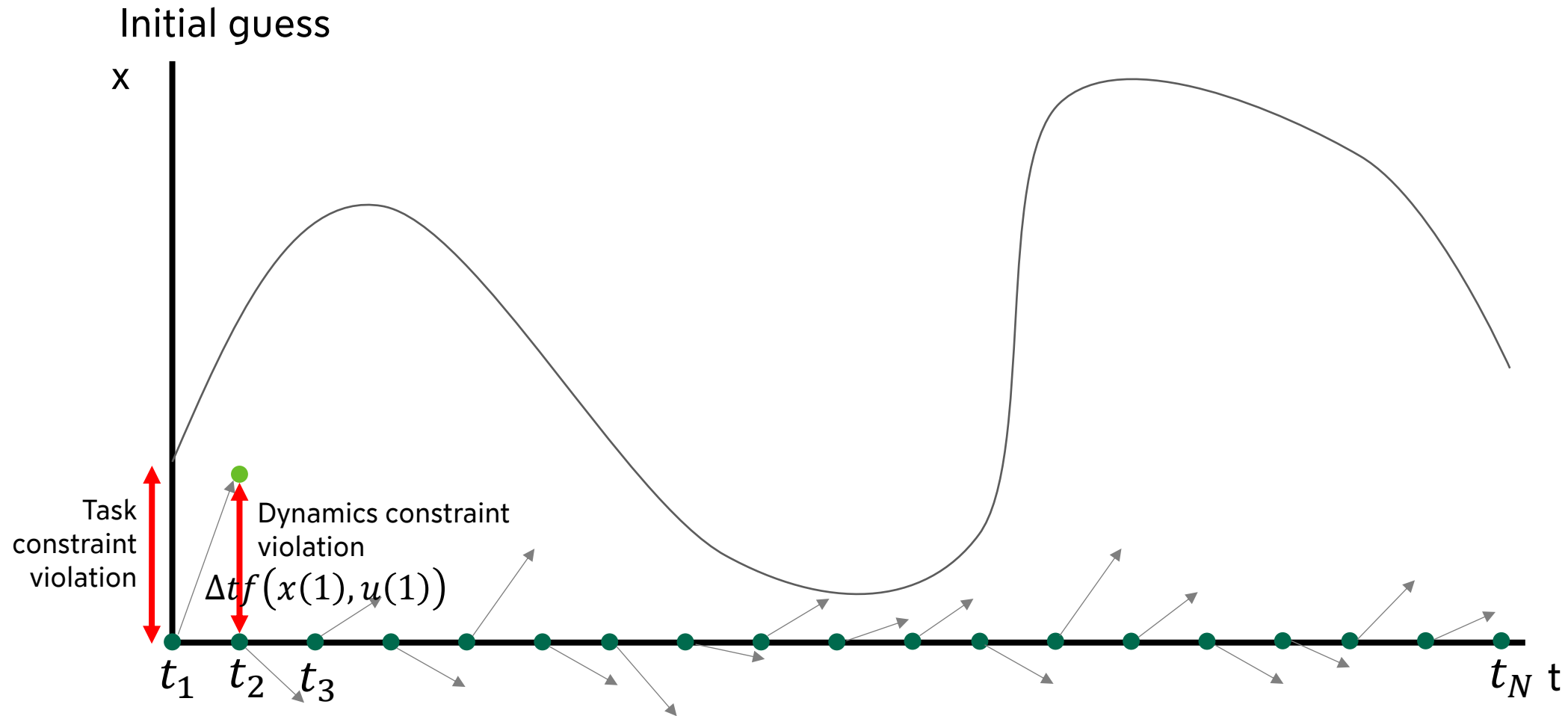
- Forward Euler iteration: $x(t + \Delta t) = x(t) + \Delta t \dot{x}(t)$, where $\dot{x} = f(x, u)$
- This can be a constraint: $g(x(t_k)) = 0$
 - Evaluated at each time (collocation) point
 - States are added to optimization variables

Dynamics in constraints:

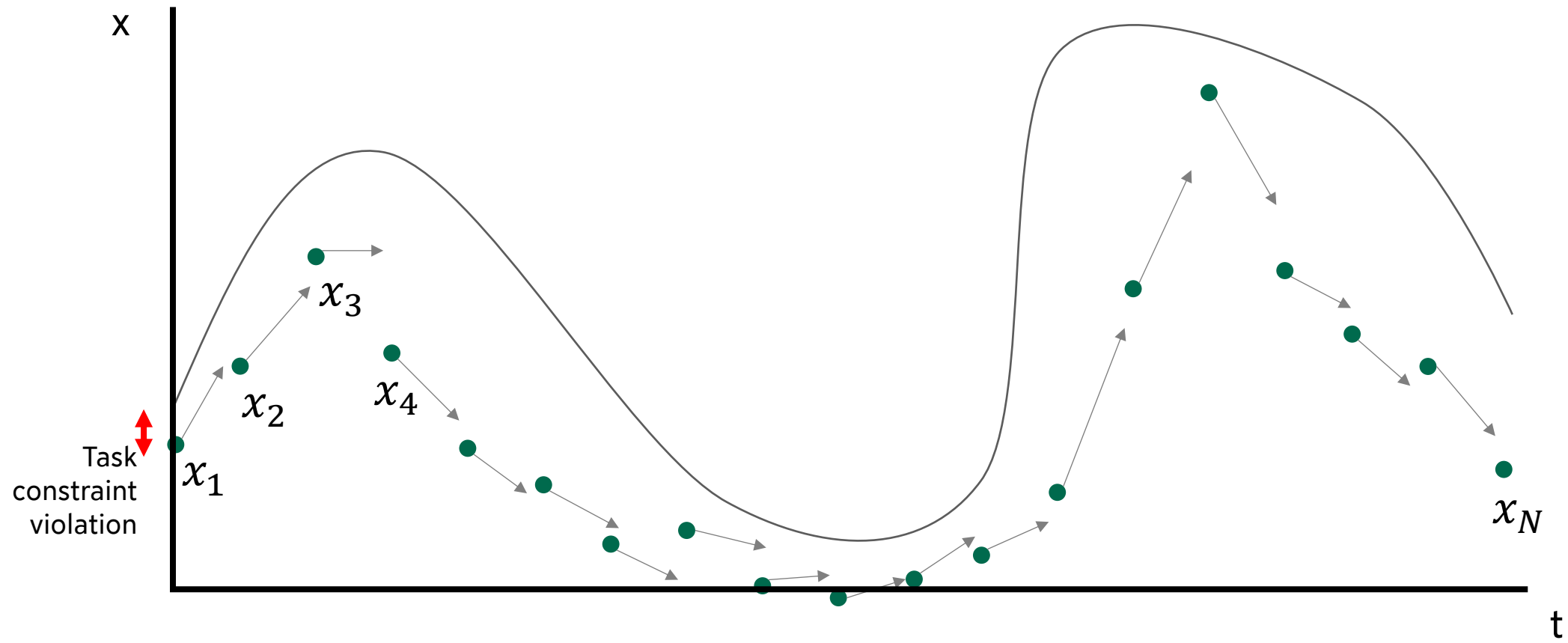
- Implicit dynamics can be used $f(x(t), \dot{x}(t), u) = 0$
 - Suitable for muscle dynamics: no division by activation required
- Possible integration schemes
 - We normally use backward Euler: $f(x(t + \Delta t), \dot{x}(t), u(t + \Delta t)) = 0$
 - Higher order: e.g., Radau collocation schemes



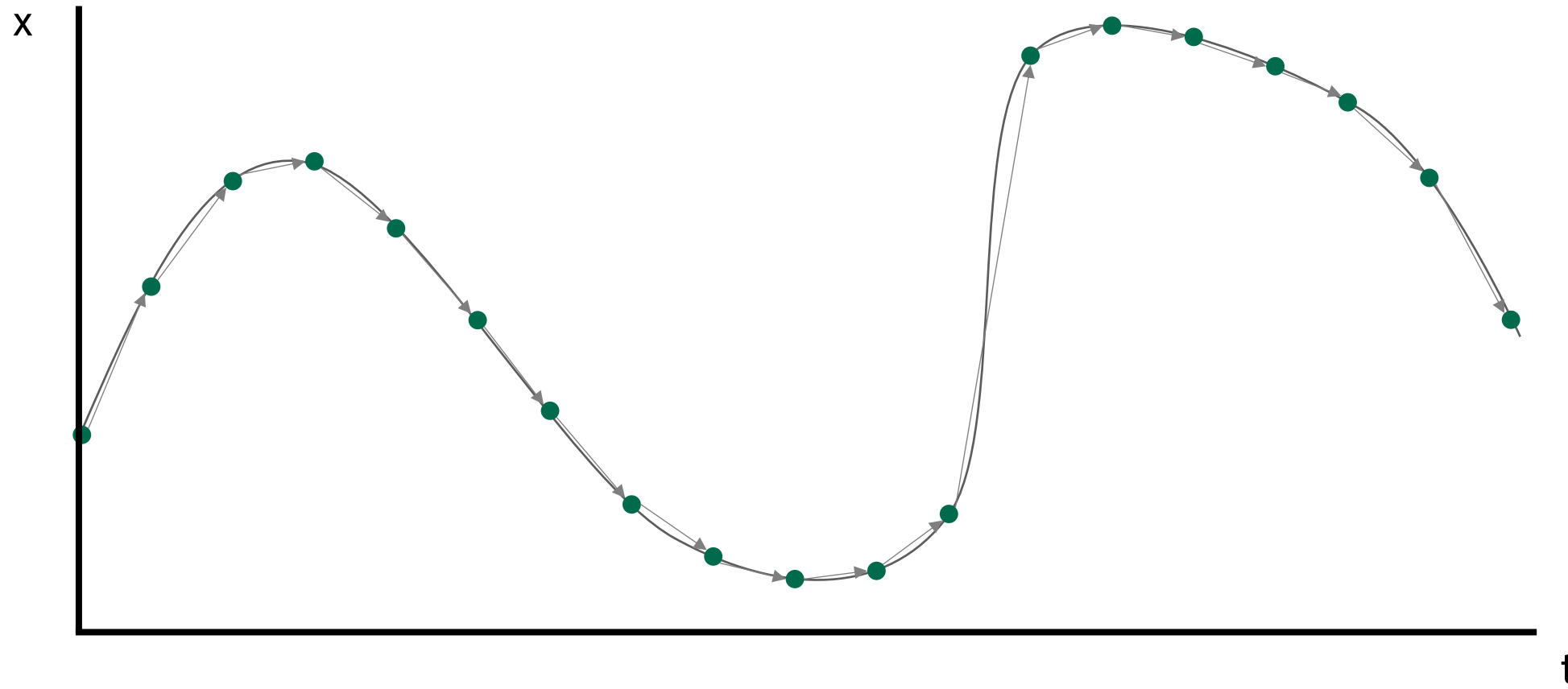
$$F_{CE} = af(l_{CE})g(v_{CE})F_{iso}$$



Some iterations later



Many more iterations later



Origin: Spacetime Constraints (1988)



Character animation

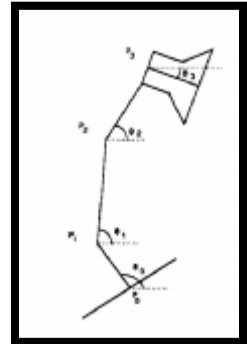
Describe:

- What the character should do
- How it should do it (objective)
- Available resources (control input)
- Newton's laws
- Solution: physically valid motion

Spacetime Constraints

Andrew Witkin
Michael Kass

Schlumberger Palo Alto Research
3340 Hillview Avenue, Palo Alto, CA 94304

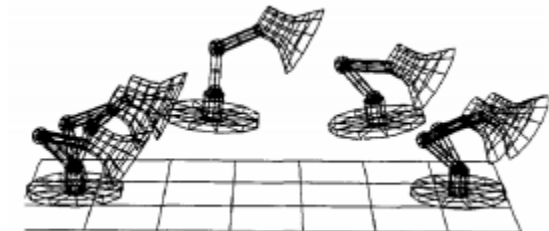
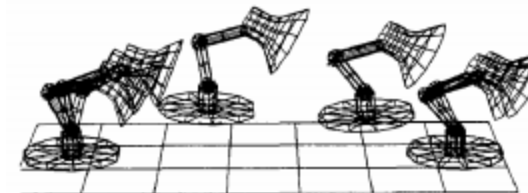
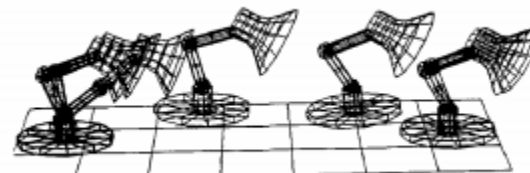
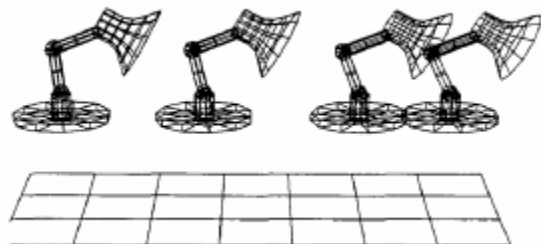


Abstract

Spacetime constraints are a new method for creating character animation. The animator specifies *what* the character has to do, for instance, "jump from here to there, clearing a hurdle in between" *how* the motion should be performed

Siggraph '87 [9]. Although *Luxo, Jr.* showed us that the team of animator, keyframe system, and renderer can be a powerful one, the responsibility for defining the motion remains almost entirely with the animator.

Some aspects of animation—personality and appeal, for example—will surely be left to the animator's artistry and



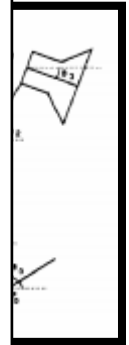
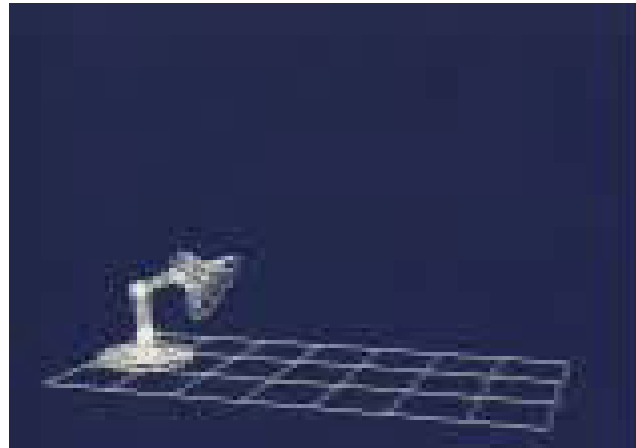
Inspiration: Spacetime Constraints (1988)



Character animation

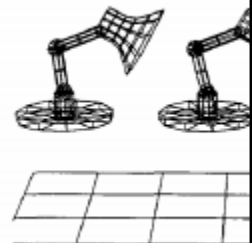
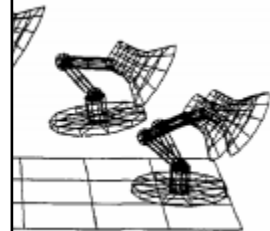
Describe:

- What the
- How it s
- Availab
- Newton
- Solution



showed us that the
renderer can be
using the motion

and appeal, for
the artists and



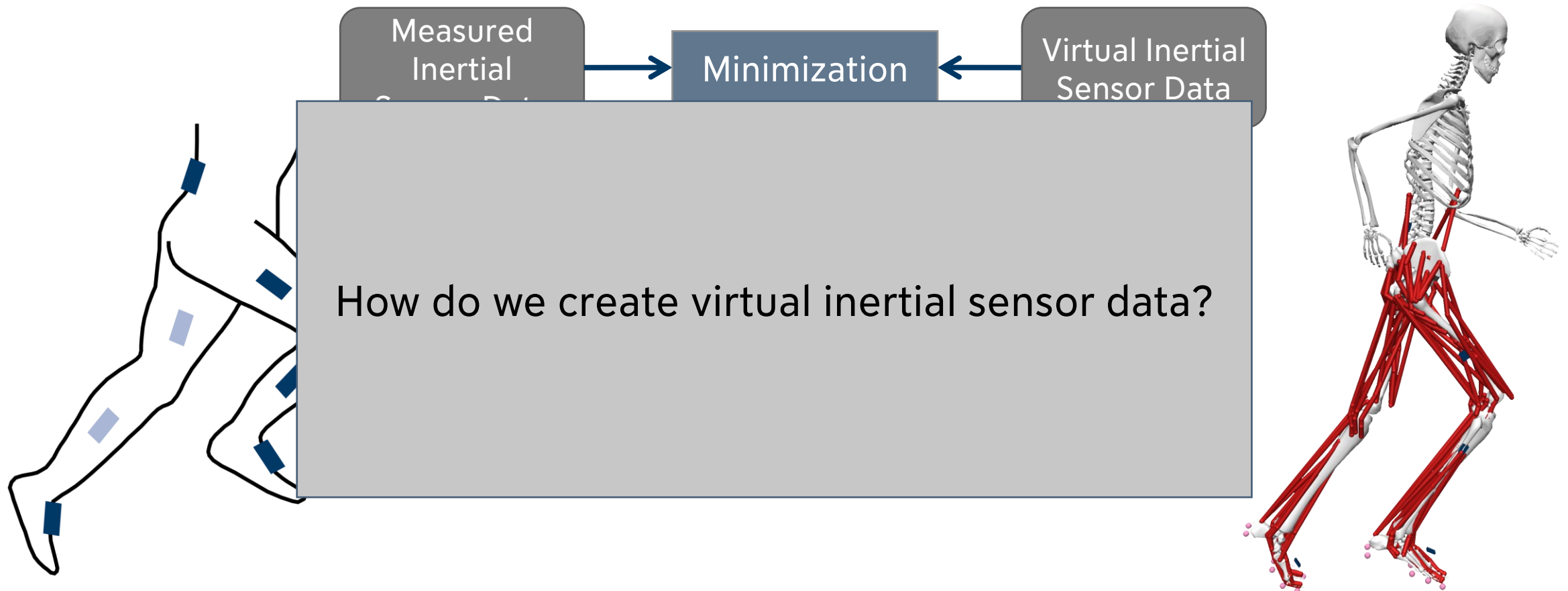
Questions?



Inertial Sensor Monitoring

Recap: Virtual Sensor Data

Movement Reconstruction Concept



Dorschky et al., *J Biomech*, 2019

Contain accelerometers and gyroscopes

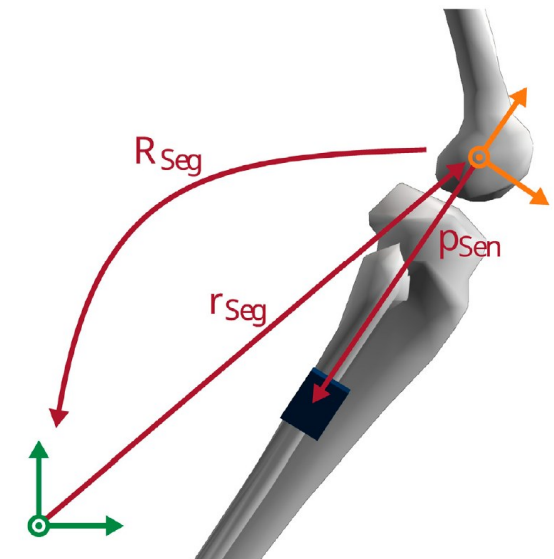
- Accelerometer: linear acceleration \mathbf{a}_s

$$\mathbf{a}_s = \mathbf{R}_{Seg}^T (\ddot{\mathbf{r}}_{Seg} + \ddot{\mathbf{R}}_{Seg} \mathbf{p}_{Sen} - \mathbf{g})$$

- Gyroscope: angular velocity $\boldsymbol{\omega}_s = [\omega_x \ \omega_y \ \omega_z]^T$

$$\boldsymbol{\Omega} = \mathbf{R}_{Seg}^T \dot{\mathbf{R}}_{Seg} = \begin{bmatrix} 0 & -\omega_z & \omega_y \\ \omega_z & 0 & -\omega_x \\ -\omega_y & \omega_x & 0 \end{bmatrix}$$

Variable	Meaning
\mathbf{R}_{Seg}	Segment orientation matrix
\mathbf{r}_{Seg}	Location of segment origin
\mathbf{p}_{Sen}	Local sensor position location
\mathbf{g}	Gravity



Van den Bogert, Read, Nigg, *J Biomech*, 1996; Nitschke et al., *Front Bioeng Biotech*, 2024

Questions?

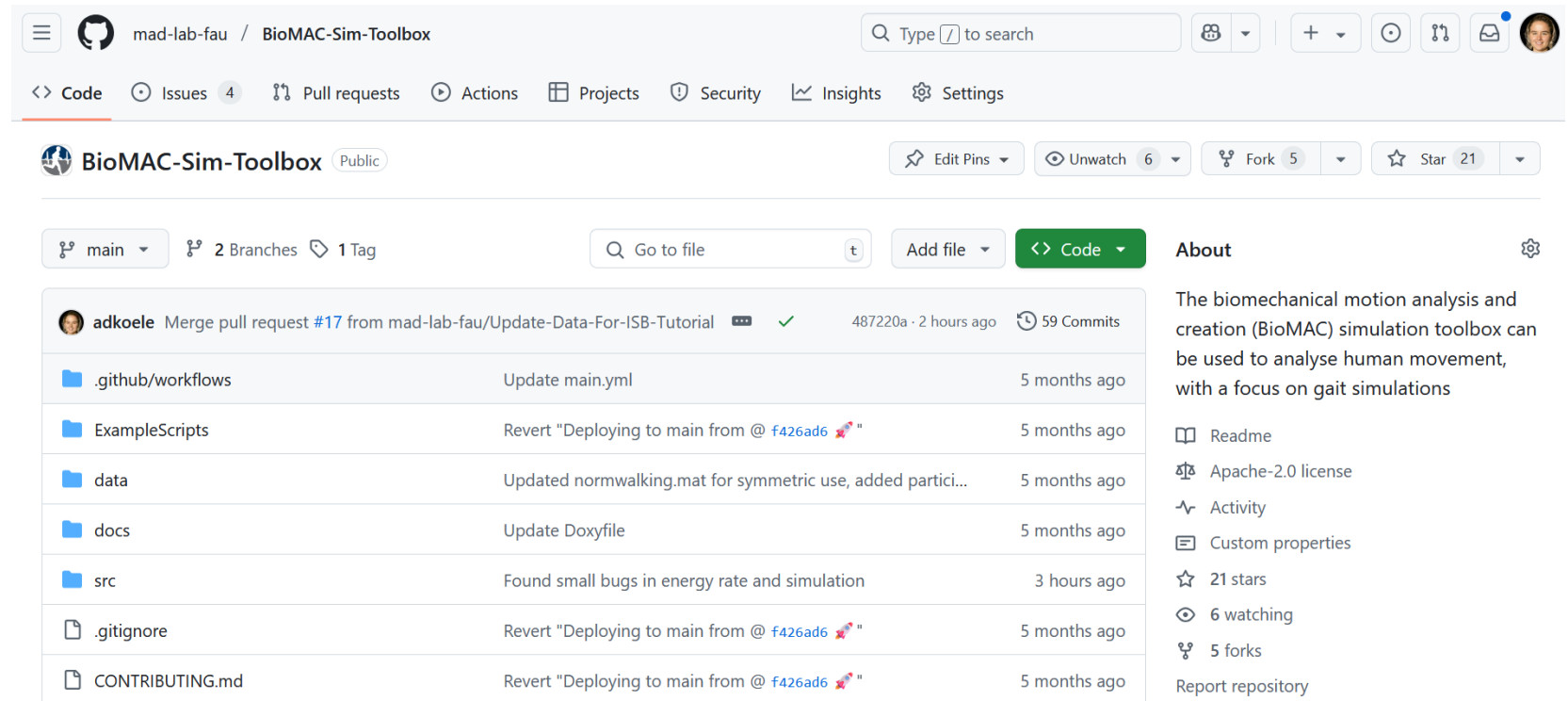


Tutorial Today

Toolbox available at: <https://github.com/mad-lab-fau/BioMAC-Sim-Toolbox>

Object oriented

- Object: entity with state, behaviour, and identity
- Fields: variables providing information
 - Visible in MATLAB's Workspace
- Methods: actions associated with objects
 - Located in associated folder in **src**



The screenshot shows the GitHub repository page for BioMAC-Sim-Toolbox. The repository is owned by mad-lab-fau and is public. It has 4 issues, 0 pull requests, 0 actions, 0 projects, 0 security alerts, 0 insights, and 0 settings. The repository has 6 forks, 21 stars, and 6 watchers. The repository is described as "The biomechanical motion analysis and creation (BioMAC) simulation toolbox can be used to analyse human movement, with a focus on gait simulations". The repository contains the following files and folders:

File/Folder	Description	Time
.github/workflows	Update main.yml	5 months ago
ExampleScripts	Revert "Deploying to main from @ f426ad6"	5 months ago
data	Updated normwalking.mat for symmetric use, added partici...	5 months ago
docs	Update Doxyfile	5 months ago
src	Found small bugs in energy rate and simulation	3 hours ago
.gitignore	Revert "Deploying to main from @ f426ad6"	5 months ago
CONTRIBUTING.md	Revert "Deploying to main from @ f426ad6"	5 months ago

The repository also includes a README, Apache-2.0 license, Activity, Custom properties, 21 stars, 6 watching, 5 forks, and a Report repository link.

Goals

- Get familiar with the code
 - Where can I find which information?
 - How do I create my own optimization?
- Understand impact of several choices
 - What is an appropriate number of nodes?
 - What happens when I change the objective weights?
 - What should my initial guess look like?

Tasks

- Analyse result object → contains all the relevant objects (problem, model, solver)
- Run several simulations and analyse results
- (Optional) Create a constraint function → creating new simulation scripts/functions

Use the PDF

All result files provided in folder Results

All finished code with "_final.m"

Three sections

1. Getting familiar with result object (15 minutes)
2. Running and comparing simulations (30 minutes)
3. Create your own constraint function (optional)

Two options

- TODO: MATLAB coding/actions
- Questions: Analyse what you see

>> TODO 1. Add path to the location of the BioMAC-Sim-Toolbox in line 24

>> TODO 2: (re)run the code up to line 73 until you get a solution standing on flat feet

Getting Familiar with Result Object

Time: 15 minutes



TODOs

>> TODO 3. Load Section1Example.mat, an example result object.

Questions

Q1. What does it mean when converged is equal to 1? Hint: use the toolbox documentation

Q2. What was the final objective value?

Q3. How long did the optimization take?

Q4. What variables are part of the optimization variables in this problem?

Q5. What was the full objective that was solved for this problem?

Q6. Did we assume left-right symmetry in the problem? Hint: you can find this in the problem itself and in the constraintTerms.

Q7. What are the different states in the model state?

Q8. How many degrees of freedom does the skeletal model have?

Running and Comparing Simulations

Time: 30 minutes



TODOs

- Objective weighting: lines 101-140
- >> **TODO 4: copy the results that you do not want to run to your result folder. See line 30 in scriptTutorial to find the result folder.**
- >> **TODO 5-8: set up the simulations in lines 105, 107, 112, and 123**
- Initial guess: lines 142-178
- >> **TODO 9-10: set up the simulations in lines 147 and 159**
- Number of nodes: lines 180-224
- >> **TODO 11: set up the simulations in line 194**
- >> **TODO 12: create a convergence plot showing the metabolic cost as a function of the number of nodes in line 223**

Questions (qualitative comparisons only):

- Objective weighting

Q9. Would you discard a solution as unrealistic when looking at the ground reaction forces and activations?

Q10. How much difference do you see in the joint angles and joint moments of the acceptable solutions?

- Initial guess

Q11: Do you see any differences between the three simulations?

- Number of nodes

Q12. What does a convergence plot showing metabolic cost versus the number of nodes tell you about a suitable number of nodes?

Q13: Based on the joint angles and joint moments, from which number of nodes do you not see a clear difference between the different simulations anymore?

Create your own constraint function

Optional



TODOs

- >> **TODO optional 1:** give the function `move2D_IMU` a new name in line 27 and save it accordingly with the new name.
- >> **TODO optional 2:** comment line 83 and uncomment line 82 in the new function to remove the strict bounds on the optimization variable
- >> **TODO optional 3-4:** add the output and Jacobian according to the comments in line 30 and 33 of `speedConstraint_IMU`.
- >> **TODO optional 5:** move this function from the tutorial folder into the `@Collocation` folder
- >> **TODO optional 6:** ensure that the file is added to the path
- >> **TODO optional 7:** add the code in line 96 of the new `move2D_IMU` to ensure that `speedConstraint_IMU` is used.
- >> **TODO optional 8:** create a problem with a small number of nodes, e.g., 4, to do the derivative test in line 233 of `scriptTutorial`.
- >> **TODO optional 9.** Add code to run the derivative test function in line 234
- >> **TODO optional 10.** Run the new optimization by adding code in line 246

Questions

Q14: Do you think that the constraint function is correct?

Q15: Do you get a different result than when the speed is set using the bounds?

Questions?



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“In the wild” movement analysis using dynamic simulations

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