

Code Library for ACM-ICPC 2016 World Finals

ACM-ICPC 2016 世界总决赛 参考模板

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二维几何

二维几何基本操作

```

1 struct Point {
2     Point rotate(const double ang) { // 逆时针旋转 ang 弧度
3         return Point(cos(ang) * x - sin(ang) * y, cos(ang) * y + sin(ang) * x);
4     }
5     Point turn90() { // 逆时针旋转 90 度
6         return Point(-y, x);
7     }
8 };
9 Point isLL(const Line &l1, const Line &l2) {
10     double s1 = det(l2.b - l2.a, l1.a - l2.a),
11         s2 = -det(l2.b - l2.a, l1.b - l2.a);
12     return (l1.a * s2 + l1.b * s1) / (s1 + s2);
13 }
14 bool onSeg(const Line &l, const Point &p) { // 点在线段上
15     return sign(det(p - l.a, l.b - l.a)) == 0 && sign(dot(p - l.a, p - l.b)) <= 0;
16 }
17 Point projection(const Line &l, const Point &p) { // 点到直线投影
18     return l.a + (l.b - l.a) * (dot(p - l.a, l.b - l.a) / (l.b - l.a).len2());
19 }
20 double disToLine(const Line &l, const Point &p) {
21     return abs(det(p - l.a, l.b - l.a) / (l.b - l.a).len());
22 }
23 double disToSeg(const Line &l, const Point &p) { // 点到线段距离
24     return sign(dot(p - l.a, l.b - l.a)) * sign(dot(p - l.b, l.a - l.b)) != 1 ?
25         disToLine(l, p) : min((p - l.a).len(), (p - l.b).len());
26 }
27 Point symmetryPoint(const Point a, const Point b) { // 点 b 关于点 a 的中心对称点
28     return a + a - b;
29 }
30 Point reflection(const Line &l, const Point &p) { // 点关于直线的对称点
31     return symmetryPoint(projection(l, p), p);
32 }
33 // 求圆与直线的交点
34 bool isCL(Circle a, Line l, Point &p1, Point &p2) {
35     double x = dot(l.a - a.o, l.b - l.a),
36         y = (l.b - l.a).len2(),
37         d = x * x - y * ((l.a - a.o).len2() - a.r * a.r);
38     if (sign(d) < 0) return false;
39     d = max(d, 0.0);
40     Point p = l.a - ((l.b - l.a) * (x / y)), delta = (l.b - l.a) * (sqrt(d) / y);
41     p1 = p + delta, p2 = p - delta;
42     return true;
43 }
44 // 求圆与圆的交面积
45 double areaCC(const Circle &c1, const Circle &c2) {
46     double d = (c1.o - c2.o).len();
47     if (sign(d - (c1.r + c2.r)) >= 0) {

```

```

48         return 0;
49     }
50     if (sign(d - abs(c1.r - c2.r)) <= 0) {
51         double r = min(c1.r, c2.r);
52         return r * r * PI;
53     }
54     double x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),
55         t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);
56     return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
57 }
58 // 求圆与圆的交点, 注意调用前要先判定重圆
59 bool isCC(Circle a, Circle b, Point &p1, Point &p2) {
60     double s1 = (a.o - b.o).len();
61     if (sign(s1 - a.r - b.r) > 0 || sign(s1 - abs(a.r - b.r)) < 0) return false;
62     double s2 = (a.r * a.r - b.r * b.r) / s1;
63     double aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
64     Point o = (b.o - a.o) * (aa / (aa + bb)) + a.o;
65     Point delta = (b.o - a.o).unit().turn90() * newSqrt(a.r * a.r - aa * aa);
66     p1 = o + delta, p2 = o - delta;
67     return true;
68 }
69 // 求点到圆的切点, 按关于点的顺时针方向返回两个点
70 bool tanCP(const Circle &c, const Point &p0, Point &p1, Point &p2) {
71     double x = (p0 - c.o).len2(), d = x - c.r * c.r;
72     if (d < EPS) return false; // 点在圆上认为没有切点
73     Point p = (p0 - c.o) * (c.r * c.r / x);
74     Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
75     p1 = c.o + p + delta;
76     p2 = c.o + p - delta;
77     return true;
78 }
79 // 求圆到圆的外公切线, 按关于 c1.o 的顺时针方向返回两条线
80 vector<Line> extanCC(const Circle &c1, const Circle &c2) {
81     vector<Line> ret;
82     if (sign(c1.r - c2.r) == 0) {
83         Point dir = c2.o - c1.o;
84         dir = (dir * (c1.r / dir.len())).turn90();
85         ret.push_back(Line(c1.o + dir, c2.o + dir));
86         ret.push_back(Line(c1.o - dir, c2.o - dir));
87     } else {
88         Point p = (c1.o * -c2.r + c2.o * c1.r) / (c1.r - c2.r);
89         Point p1, p2, q1, q2;
90         if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
91             if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
92             ret.push_back(Line(p1, q1));
93             ret.push_back(Line(p2, q2));
94         }
95     }
96     return ret;
97 }

```

```

98 // 求圆到圆的内共切线, 按关于 c1.o 的顺时针方向返回两条线
99 vector<Line> intanCC(const Circle &c1, const Circle &c2) {
100     vector<Line> ret;
101     Point p = (c1.o * c2.r + c2.o * c1.r) / (c1.r + c2.r);
102     Point p1, p2, q1, q2;
103     if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) { // 两圆相切认为没有切线
104         ret.push_back(Line(p1, q1));
105         ret.push_back(Line(p2, q2));
106     }
107     return ret;
108 }
109 bool contain(vector<Point> polygon, Point p) { // 判断点 p
    ↪ 是否被多边形包含, 包括落在边界上
110     int ret = 0, n = polygon.size();
111     for(int i = 0; i < n; ++i) {
112         Point u = polygon[i], v = polygon[(i + 1) % n];
113         if (onSeg(Line(u, v), p)) return true;
114         if (sign(u.y - v.y) <= 0) swap(u, v);
115         if (sign(p.y - u.y) > 0 || sign(p.y - v.y) <= 0) continue;
116         ret += sign(det(p, v, u)) > 0;
117     }
118     return ret & 1;
119 }
120 vector<Point> convexCut(const vector<Point>&ps, Line l) { // 用半平面 (q1,q2)
    ↪ 的逆时针方向去切凸多边形
121     vector<Point> qs;
122     int n = ps.size();
123     for (int i = 0; i < n; ++i) {
124         Point p1 = ps[i], p2 = ps[(i + 1) % n];
125         int d1 = sign(det(l.a, l.b, p1)), d2 = sign(det(l.a, l.b, p2));
126         if (d1 >= 0) qs.push_back(p1);
127         if (d1 * d2 < 0) qs.push_back(isLL(Line(p1, p2), l));
128     }
129     return qs;
130 }
131 vector<Point> convexHull(vector<Point> ps) { // 求点集 ps 组成的凸包
132     int n = ps.size(); if (n <= 1) return ps;
133     sort(ps.begin(), ps.end());
134     vector<Point> qs;
135     for (int i = 0; i < n; qs.push_back(ps[i++]))
136         while (qs.size() > 1 && sign(det(qs[qs.size()-2], qs.back(), ps[i])) <= 0)
            ↪ qs.pop_back();
137     for (int i = n - 2, t = qs.size(); i >= 0; qs.push_back(ps[i--]))
138         while ((int)qs.size() > t && sign(det(qs[(int)qs.size()-2], qs.back(), ps[i])) <= 0)
            ↪ qs.pop_back();
139     qs.pop_back(); return qs;
140 }

```

 $n \log n$ 半平面交

```

1 struct Point {
2     int quad() const { return sign(y) == 1 || (sign(y) == 0 && sign(x) >= 0); }
3 };
4 struct Line {
5     bool include(const Point &p) const { return sign(det(b - a, p - a)) > 0; }
6     Line push() const { // 将半平面向外推 eps
7         const double eps = 1e-6;
8         Point delta = (b - a).turn90().norm() * eps;
9         return Line(a - delta, b - delta);
10    }
11 };
12 bool sameDir(const Line &l0, const Line &l1) { return parallel(l0, l1) && sign(dot(l0.b
    ↪ - l0.a, l1.b - l1.a)) == 1; }
13 bool operator < (const Point &a, const Point &b) {
14     if (a.quad() != b.quad()) {
15         return a.quad() < b.quad();
16     } else {
17         return sign(det(a, b)) > 0;
18     }
19 }
20 bool operator < (const Line &l0, const Line &l1) {
21     if (sameDir(l0, l1)) {
22         return l1.include(l0.a);
23     } else {
24         return (l0.b - l0.a) < (l1.b - l1.a);
25     }
26 }
27 bool check(const Line &u, const Line &v, const Line &w) { return w.include(intersect(u,
    ↪ v)); }
28 vector<Point> intersection(vector<Line> &l) {
29     sort(l.begin(), l.end());
30     deque<Line> q;
31     for (int i = 0; i < (int)l.size(); ++i) {
32         if (i && sameDir(l[i], l[i - 1])) {
33             continue;
34         }
35         while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], l[i])) q.pop_back();
36         while (q.size() > 1 && !check(q[1], q[0], l[i])) q.pop_front();
37         q.push_back(l[i]);
38     }
39     while (q.size() > 2 && !check(q[q.size() - 2], q[q.size() - 1], q[0])) q.pop_back();
40     while (q.size() > 2 && !check(q[1], q[0], q[q.size() - 1])) q.pop_front();
41     vector<Point> ret;
42     for (int i = 0; i < (int)q.size(); ++i) ret.push_back(intersect(q[i], q[(i + 1) %
    ↪ q.size()]));
43     return ret;
44 }

```

三角形的心

```

1 Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心
2     double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(),
3         s = fabs(det(B - A, C - A)),
4         r = s / p;
5     return (A * a + B * b + C * c) / (a + b + c);
6 }
7 Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
8     Point bb = b - a, cc = c - a;
9     double db = bb.len2(), dc = cc.len2(), d = 2 * det(bb, cc);
10    return a - Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
11 }
12 Point othroCenter(const Point &a, const Point &b, const Point &c) { // 垂心
13     Point ba = b - a, ca = c - a, bc = b - c;
14     double Y = ba.y * ca.y * bc.y,
15         A = ca.x * ba.y - ba.x * ca.y,
16         x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
17         y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
18     return Point(x0, y0);
19 }

```

圆与多边形面积交

```

1 double areaCT(Point pa, Point pb, double r) {
2     if (pa.len() < pb.len()) swap(pa, pb);
3     if (sign(pb.len()) == 0) return 0;
4     double a = pb.len(), b = pa.len(), c = (pb - pa).len();
5     double sinB = fabs(det(pb, pb - pa) / a / c),
6         cosB = dot(pb, pb - pa) / a / c,
7         sinC = fabs(det(pa, pb) / a / b),
8         cosC = dot(pa, pb) / a / b;
9     double B = atan2(sinB, cosB), C = atan2(sinC, cosC);
10    if (a > r) {
11        S = C / 2 * r * r;
12        h = a * b * sinC / c;
13        if (h < r && B < PI / 2) {
14            S -= (acos(h / r) * r * r - h * sqrt(r * r - h * h));
15        }
16    } else if (b > r) {
17        double theta = PI - B - asin(sinB / r * a);
18        S = a * r * sin(theta) / 2 + (C - theta) / 2 * r * r;
19    } else {
20        S = sinC * a * b / 2;
21    }
22    return S;
23 }

```

圆的面积模板 ($n^2 \log n$)

```

1 struct Event {
2     Point p;
3     double ang;
4     int delta;
5     Event (Point p = Point(0, 0), double ang = 0, double delta = 0) : p(p), ang(ang),
6         ↪ delta(delta) {}
7 };
8 bool operator < (const Event &a, const Event &b) {
9     return a.ang < b.ang;
10 }
11 void addEvent(const Circle &a, const Circle &b, vector<Event> &evt, int &cnt) {
12     double d2 = (a.o - b.o).len2(),
13         dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2,
14         pRatio = sqrt(-(d2 - sqr(a.r - b.r)) * (d2 - sqr(a.r + b.r)) / (d2 * d2 * 4));
15     Point d = b.o - a.o, p = d.rotate(PI / 2),
16         q0 = a.o + d * dRatio + p * pRatio,
17         q1 = a.o + d * dRatio - p * pRatio;
18     double ang0 = (q0 - a.o).ang(),
19         ang1 = (q1 - a.o).ang();
20     evt.push_back(Event(q1, ang1, 1));
21     evt.push_back(Event(q0, ang0, -1));
22     cnt += ang1 > ang0;
23 }
24 bool issame(const Circle &a, const Circle &b) { return sign((a.o - b.o).len()) == 0 &&
25     ↪ sign(a.r - b.r) == 0; }
26 bool overlap(const Circle &a, const Circle &b) { return sign(a.r - b.r - (a.o -
27     ↪ b.o).len()) >= 0; }
28 bool intersect(const Circle &a, const Circle &b) { return sign((a.o - b.o).len() - a.r -
29     ↪ b.r) < 0; }
30 int C;
31 Circle c[N];
32 double area[N];
33 void solve() {
34     memset(area, 0, sizeof(double) * (C + 1));
35     for (int i = 0; i < C; ++i) {
36         int cnt = 1;
37         vector<Event> evt;
38         for (int j = 0; j < i; ++j) if (issame(c[i], c[j])) ++cnt;
39         for (int j = 0; j < C; ++j) {
40             if (j != i && !issame(c[i], c[j]) && overlap(c[j], c[i])) {
41                 ++cnt;
42             }
43         }
44         for (int j = 0; j < C; ++j) {
45             if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i],
46                 ↪ c[j])) {
47                 addEvent(c[i], c[j], evt, cnt);
48             }
49         }
50     }
51 }

```

```

45     if (evt.size() == 0) {
46         area[cnt] += PI * c[i].r * c[i].r;
47     } else {
48         sort(evt.begin(), evt.end());
49         evt.push_back(evt.front());
50         for (int j = 0; j + 1 < (int)evt.size(); ++j) {
51             cnt += evt[j].delta;
52             area[cnt] += det(evt[j].p, evt[j + 1].p) / 2;
53             double ang = evt[j + 1].ang - evt[j].ang;
54             if (ang < 0) {
55                 ang += PI * 2;
56             }
57             area[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r / 2;
58         }
59     }
60 }
61 }

```

凸包快速询问

```

1  /*
2   给定凸包,  $\log n$  内完成各种询问, 具体操作有 :
3   1. 判定一个点是否在凸包内
4   2. 询问凸包外的点到凸包的两个切点
5   3. 询问一个向量关于凸包的切点
6   4. 询问一条直线和凸包的交点
7   INF 为坐标范围, 需要定义点类大于号
8   改成实数只需修改 sign 函数, 以及把 long long 改为 double 即可
9   构造函数时传入凸包要求无重点, 面积非空, 以及 pair(x,y) 的最小点放在第一个
10 */
11 const int INF = 1000000000;
12 struct Convex
13 {
14     int n;
15     vector<Point> a, upper, lower;
16     Convex(vector<Point> _a) : a(_a) {
17         n = a.size();
18         int ptr = 0;
19         for(int i = 1; i < n; ++ i) if (a[ptr] < a[i]) ptr = i;
20         for(int i = 0; i <= ptr; ++ i) lower.push_back(a[i]);
21         for(int i = ptr; i < n; ++ i) upper.push_back(a[i]);
22         upper.push_back(a[0]);
23     }
24     int sign(long long x) { return x < 0 ? -1 : x > 0; }
25     pair<long long, int> get_tangent(vector<Point> &convex, Point vec) {
26         int l = 0, r = (int)convex.size() - 2;
27         for( ; l + 1 < r; ) {
28             int mid = (l + r) / 2;
29             if (sign((convex[mid + 1] - convex[mid]).det(vec)) > 0) r = mid;
30             else l = mid;

```

```

31     }
32     return max(make_pair(vec.det(convex[r]), r), make_pair(vec.det(convex[0]), 0));
33 }
34 void update_tangent(const Point &p, int id, int &i0, int &i1) {
35     if ((a[i0] - p).det(a[id] - p) > 0) i0 = id;
36     if ((a[i1] - p).det(a[id] - p) < 0) i1 = id;
37 }
38 void binary_search(int l, int r, Point p, int &i0, int &i1) {
39     if (l == r) return;
40     update_tangent(p, l % n, i0, i1);
41     int sl = sign((a[l % n] - p).det(a[(l + 1) % n] - p));
42     for( ; l + 1 < r; ) {
43         int mid = (l + r) / 2;
44         int smid = sign((a[mid % n] - p).det(a[(mid + 1) % n] - p));
45         if (smid == sl) l = mid;
46         else r = mid;
47     }
48     update_tangent(p, r % n, i0, i1);
49 }
50 int binary_search(Point u, Point v, int l, int r) {
51     int sl = sign((v - u).det(a[l % n] - u));
52     for( ; l + 1 < r; ) {
53         int mid = (l + r) / 2;
54         int smid = sign((v - u).det(a[mid % n] - u));
55         if (smid == sl) l = mid;
56         else r = mid;
57     }
58     return l % n;
59 }
60 // 判定点是否在凸包内, 在边界返回 true
61 bool contain(Point p) {
62     if (p.x < lower[0].x || p.x > lower.back().x) return false;
63     int id = lower_bound(lower.begin(), lower.end(), Point(p.x, -INF)) - lower.begin();
64     if (lower[id].x == p.x) {
65         if (lower[id].y > p.y) return false;
66     } else if ((lower[id - 1] - p).det(lower[id] - p) < 0) return false;
67     id = lower_bound(upper.begin(), upper.end(), Point(p.x, INF), greater<Point>()) -
    ↪ upper.begin();
68     if (upper[id].x == p.x) {
69         if (upper[id].y < p.y) return false;
70     } else if ((upper[id - 1] - p).det(upper[id] - p) < 0) return false;
71     return true;
72 }
73 // 求点 p
74 ↪ 关于凸包的两个切点, 如果在凸包外则有序返回编号, 共线的多个切点返回任意一个, 否则返回
75 ↪ false
76 bool get_tangent(Point p, int &i0, int &i1) {
77     if (contain(p)) return false;
78     i0 = i1 = 0;
79     int id = lower_bound(lower.begin(), lower.end(), p) - lower.begin();

```

```

78     binary_search(0, id, p, i0, i1);
79     binary_search(id, (int)lower.size(), p, i0, i1);
80     id = lower_bound(upper.begin(), upper.end(), p, greater<Point>()) - upper.begin();
81     binary_search((int)lower.size() - 1, (int)lower.size() - 1 + id, p, i0, i1);
82     binary_search((int)lower.size() - 1 + id, (int)lower.size() - 1 + (int)upper.size(),
    ↪ p, i0, i1);
83     return true;
84 }
85 // 求凸包上和向量 vec 叉积最大的点, 返回编号, 共线的多个切点返回任意一个
86 int get_tangent(Point vec) {
87     pair<long long, int> ret = get_tangent(upper, vec);
88     ret.second = (ret.second + (int)lower.size() - 1) % n;
89     ret = max(ret, get_tangent(lower, vec));
90     return ret.second;
91 }
92 // 求凸包和直线 u,v 的交点, 如果无严格相交返回 false. 如果有则是和 (i,next(i)) 的交点,
    ↪ 两个点无序, 交在点上不确定返回前后两条线段其中之一
93 bool get_intersection(Point u, Point v, int &i0, int &i1) {
94     int p0 = get_tangent(u - v), p1 = get_tangent(v - u);
95     if (sign((v - u).det(a[p0] - u)) * sign((v - u).det(a[p1] - u)) < 0) {
96         if (p0 > p1) swap(p0, p1);
97         i0 = binary_search(u, v, p0, p1);
98         i1 = binary_search(u, v, p1, p0 + n);
99         return true;
100     } else {
101         return false;
102     }
103 }
104 };

```

Delaunay 三角剖分

```

1  /*
2  Delaunay Triangulation 随机增量算法 :
3  节点数至少为点数的 6 倍, 空间消耗较大注意计算内存使用
4  建图的过程在 build 中, 注意初始化内存池和初始三角形的坐标范围 (Triangulation::LOTS)
5  Triangulation::find 返回包含某点的三角形
6  Triangulation::add_point 将某点加入三角剖分
7  某个 Triangle 在三角剖分中当且仅当它的 has_children 为 0
8  如果要找到三角形 u 的邻域, 则枚举它的所有 u.edge[i].tri, 该条边的两个点为 u.p[(i+1)%3],
    ↪ u.p[(i+2)%3]
9  */
10 const int N = 100000 + 5, MAX_TRIS = N * 6;
11 const double EPSILON = 1e-6, PI = acos(-1.0);
12 struct Point {
13     double x,y; Point():x(0),y(0){} Point(double x, double y):x(x),y(y){}
14     bool operator==(Point const& that)const {return x==that.x&&y==that.y;}
15 };
16 inline double sqr(double x) { return x*x; }
17 double dist_sqr(Point const& a, Point const& b){return sqr(a.x-b.x)+sqr(a.y-b.y);}

```

```

18 bool in_circumcircle(Point const& p1, Point const& p2, Point const& p3, Point const& p4)
    ↪ {
19     double u11 = p1.x - p4.x, u21 = p2.x - p4.x, u31 = p3.x - p4.x;
20     double u12 = p1.y - p4.y, u22 = p2.y - p4.y, u32 = p3.y - p4.y;
21     double u13 = sqr(p1.x) - sqr(p4.x) + sqr(p1.y) - sqr(p4.y);
22     double u23 = sqr(p2.x) - sqr(p4.x) + sqr(p2.y) - sqr(p4.y);
23     double u33 = sqr(p3.x) - sqr(p4.x) + sqr(p3.y) - sqr(p4.y);
24     double det = -u13*u22*u31 + u12*u23*u31 + u13*u21*u32 - u11*u23*u32 - u12*u21*u33 +
    ↪ u11*u22*u33;
25     return det > EPSILON;
26 }
27 double side(Point const& a, Point const& b, Point const& p) { return (b.x-a.x)*(p.y-a.y)
    ↪ - (b.y-a.y)*(p.x-a.x);}
28 typedef int SideRef; struct Triangle; typedef Triangle* TriangleRef;
29 struct Edge {
30     TriangleRef tri; SideRef side; Edge() : tri(0), side(0) {}
31     Edge(TriangleRef tri, SideRef side) : tri(tri), side(side) {}
32 };
33 struct Triangle {
34     Point p[3]; Edge edge[3]; TriangleRef children[3]; Triangle() {}
35     Triangle(Point const& p0, Point const& p1, Point const& p2) {
36         p[0]=p0;p[1]=p1;p[2]=p2;children[0]=children[1]=children[2]=0;
37     }
38     bool has_children() const { return children[0] != 0; }
39     int num_children() const {
40         return children[0] == 0 ? 0
41             : children[1] == 0 ? 1
42             : children[2] == 0 ? 2 : 3;
43     }
44     bool contains(Point const& q) const {
45         double a=side(p[0],p[1],q), b=side(p[1],p[2],q), c=side(p[2],p[0],q);
46         return a >= -EPSILON && b >= -EPSILON && c >= -EPSILON;
47     }
48 } triange_pool[MAX_TRIS], *tot_triangles;
49 void set_edge(Edge a, Edge b) {
50     if (a.tri) a.tri->edge[a.side] = b;
51     if (b.tri) b.tri->edge[b.side] = a;
52 }
53 class Triangulation {
54 public:
55     Triangulation() {
56         const double LOTS = 1e6;
57         the_root = new(tot_triangles++)
    ↪ Triangle(Point(-LOTS,-LOTS),Point(+LOTS,-LOTS),Point(0,+LOTS));
58     }
59     TriangleRef find(Point p) const { return find(the_root,p); }
60     void add_point(Point const& p) { add_point(find(the_root,p),p); }
61 private:
62     TriangleRef the_root;
63     static TriangleRef find(TriangleRef root, Point const& p) {

```



```

64     for( ; ; ) {
65         if (!root->has_children()) return root;
66         else for (int i = 0; i < 3 && root->children[i] ; ++i)
67             if (root->children[i]->contains(p))
68                 {root = root->children[i]; break;}
69     }
70 }
71 void add_point(TriangleRef root, Point const& p) {
72     TriangleRef tab,tbc,tca;
73     tab = new(tot_triangles++) Triangle(root->p[0], root->p[1], p);
74     tbc = new(tot_triangles++) Triangle(root->p[1], root->p[2], p);
75     tca = new(tot_triangles++) Triangle(root->p[2], root->p[0], p);
76     set_edge(Edge(tab,0),Edge(tbc,1));set_edge(Edge(tbc,0),Edge(tca,1));
77     set_edge(Edge(tca,0),Edge(tab,1));set_edge(Edge(tab,2),root->edge[2]);
78     set_edge(Edge(tbc,2),root->edge[0]);set_edge(Edge(tca,2),root->edge[1]);
79     root->children[0]=tab;root->children[1]=tbc;root->children[2]=tca;
80     flip(tab,2); flip(tbc,2); flip(tca,2);
81 }
82 void flip(TriangleRef tri, SideRef pi) {
83     TriangleRef trj = tri->edge[pi].tri; int pj = tri->edge[pi].side;
84     if (!trj||!in_circumcircle(tri->p[0],tri->p[1],tri->p[2],trj->p[pj])) return;
85     TriangleRef trk = new(tot_triangles++) Triangle(tri->p[(pi+1)%3], trj->p[pj],
86     ↪ tri->p[pi]);
87     TriangleRef trl = new(tot_triangles++) Triangle(trj->p[(pj+1)%3], tri->p[pi],
88     ↪ trj->p[pj]);
89     set_edge(Edge(trk,0), Edge(trl,0));
90     set_edge(Edge(trk,1), tri->edge[(pi+2)%3]); set_edge(Edge(trk,2),
91     ↪ trj->edge[(pj+1)%3]);
92     set_edge(Edge(trl,1), trj->edge[(pj+2)%3]); set_edge(Edge(trl,2),
93     ↪ tri->edge[(pi+1)%3]);
94     tri->children[0]=trk;tri->children[1]=trl;tri->children[2]=0;
95     trj->children[0]=trk;trj->children[1]=trl;trj->children[2]=0;
96     flip(trk,1); flip(trk,2); flip(trl,1); flip(trl,2);
97 }
98 };
99 int n; Point ps[N];
100 void build(){
101     tot_triangles = triange_pool; cin >> n;
102     for(int i = 0; i < n; ++ i) scanf("%lf%lf",&ps[i].x,&ps[i].y);
103     random_shuffle(ps, ps + n); Triangulation tri;
104     for(int i = 0; i < n; ++ i) tri.add_point(ps[i]);
105 }

```

三维几何

三维几何基本操作

```

1 struct Point3D {
2     double x, y, z;
3 };
4 Point3D det(const Point3D &a, const Point3D &b) {

```

```

5     return Point3D(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x);
6 }
7 // 平面法向量 : 平面上两个向量叉积
8 // 点共平面 : 平面上一点与之的向量点积法向量为 0
9 // 点在线段 ( 直线 ) 上 : 共线且两边点积非正
10 // 点在三角形内 ( 不包含边界, 需再判断是与某条边共线 )
11 bool pointInTri(const Point3D &a, const Point3D &b, const Point3D &c, const Point3D &p)
12     ↪ {
13     return sign(det(a - b, a - c).len() - det(p - a, p - b).len() - det(p - b, p -
14     ↪ c).len() - det(p - c, p - a).len()) == 0;
15 }
16 // 共平面的两点是否在这平面上一条直线的同侧
17 bool sameSide(const Point3D &a, const Point3D &b, const Point3D &p0, const Point3D &p1)
18     ↪ {
19     return sign(dot(det(a - b, p0 - b), det(a - b, p1 - b))) > 0;
20 }
21 // 两点在平面同侧 : 点积法向量符号相同
22 // 两直线平行 / 垂直 : 同二维
23 // 平面平行 / 垂直 : 判断法向量
24 // 线面垂直 : 法向量和直线平行
25 // 判断空间线段是否相交 : 四点共面两线段不平行相互在异侧
26 // 线段和三角形是否相交 : 线段在三角形平面不同侧
27     ↪ 三角形任意两点在线段和第三点组成的平面的不同侧
28 // 求空间直线交点
29 Point3D intersection(const Point3D &a0, const Point3D &b0, const Point3D &a1, const
30     ↪ Point3D &b1) {
31     double t = ((a0.x - a1.x) * (a1.y - b1.y) - (a0.y - a1.y) * (a1.x - b1.x)) / ((a0.x -
32     ↪ b0.x) * (a1.y - b1.y) - (a0.y - b0.y) * (a1.x - b1.x));
33     return a0 + (b0 - a0) * t;
34 }
35 // 求平面和直线的交点
36 Point3D intersection(const Point3D &a, const Point3D &b, const Point3D &c, const Point3D
37     ↪ &l0, const Point3D &l1) {
38     Point3D p = pVec(a, b, c); // 平面法向量
39     double t = (p.x * (a.x - l0.x) + p.y * (a.y - l0.y) + p.z * (a.z - l0.z)) / (p.x *
40     ↪ (l1.x - l0.x) + p.y * (l1.y - l0.y) + p.z * (l1.z - l0.z));
41     return l0 + (l1 - l0) * t;
42 }
43 // 求平面交线 : 取不平行的一条直线的一个交点, 以及法向量叉积得到直线方向
44 // 点到直线距离 : 叉积得到三角形的面积除以底边
45 // 点到平面距离 : 点积法向量
46 // 直线间距离 : 平行时随便取一点求距离, 否则叉积方向向量得到方向点积计算长度
47 // 直线夹角 : 点积 平面夹角 : 法向量点积
48 // 三维向量旋转操作(绕向量 s 旋转 ang 角度), 对于右手系 s 指向观察者时逆时针
49 // 矩阵版
50 void rotate(const Point3D &s, double ang) {
51     double l = s.len(), x = s.x / l, y = s.y / l, z = s.z / l, sinA = sin(ang), cosA =
52     ↪ cos(ang);
53     double p[4][4] = {CosA + (1 - CosA) * x * x, (1 - CosA) * x * y - SinA * z, (1 - CosA)
54     ↪ * x * z + SinA * y, 0,

```



```

45 (1 - CosA) * y * x + SinA * z, CosA + (1 - CosA) * y * y, (1 - CosA) * y * z - SinA
    ↪ * x, 0,
46 (1 - CosA) * z * x - SinA * y, (1 - CosA) * z * y + SinA * x, CosA + (1 - CosA) * z
    ↪ * z, 0,
47 0, 0, 0, 1 };
48 }
49 // 计算版 : 把需要旋转的向量按照 s 分解, 做二维旋转, 再回到三维

```

三维凸包求重心

```

1 #define SIZE(X) (int(X.size()))
2 #define PI 3.14159265358979323846264338327950288
3 struct Point {
4     Point cross(const Point &p) const {
5         return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x);
6     }
7 } info[1005];
8 int mark[1005][1005], n, cnt;;
9 double mix(const Point &a, const Point &b, const Point &c) {
10     return a.dot(b.cross(c));
11 }
12 double area(int a, int b, int c) {
13     return ((info[b] - info[a]).cross(info[c] - info[a])).length();
14 }
15 double volume(int a, int b, int c, int d) {
16     return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]);
17 }
18 struct Face {
19     int a, b, c; Face() {}
20     Face(int a, int b, int c): a(a), b(b), c(c) {}
21     int &operator [](int k) {
22         if (k == 0) return a; if (k == 1) return b; return c;
23     }
24 };
25 vector <Face> face;
26 inline void insert(int a, int b, int c) {
27     face.push_back(Face(a, b, c));
28 }
29 void add(int v) {
30     vector <Face> tmp; int a, b, c; cnt++;
31     for (int i = 0; i < SIZE(face); i++) {
32         a = face[i][0]; b = face[i][1]; c = face[i][2];
33         if (Sign(volume(v, a, b, c)) < 0)
34             mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] = mark[a][c] = cnt;
35         else tmp.push_back(face[i]);
36     } face = tmp;
37     for (int i = 0; i < SIZE(tmp); i++) {
38         a = face[i][0]; b = face[i][1]; c = face[i][2];
39         if (mark[a][b] == cnt) insert(b, a, v);
40         if (mark[b][c] == cnt) insert(c, b, v);

```

```

41     if (mark[c][a] == cnt) insert(a, c, v);
42 }
43 }
44 int Find() {
45     for (int i = 2; i < n; i++) {
46         Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
47         if (ndir == Point()) continue; swap(info[i], info[2]);
48         for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j)) != 0) {
49             swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1); return 1;
50         }
51     }
52     return 0;
53 }
54 int main() {
55     for (; scanf("%d", &n) == 1; ) {
56         for (int i = 0; i < n; i++) info[i].Input();
57         sort(info, info + n); n = unique(info, info + n) - info;
58         face.clear(); random_shuffle(info, info + n);
59         if (Find()) {
60             memset(mark, 0, sizeof(mark)); cnt = 0;
61             for (int i = 3; i < n; i++) add(i); vector<Point> Ndir;
62             for (int i = 0; i < SIZE(face); ++i) {
63                 Point p = (info[face[i][0]] - info[face[i][1]]).cross(info[face[i][2]] -
    ↪ info[face[i][1]]);
64                 p = p / p.length(); Ndir.push_back(p);
65             }
66             sort(Ndir.begin(), Ndir.end());
67             int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
68             printf("%d\n", ans);
69         } else printf("1\n");
70     }
71 }
72 // 求重心
73 double calcDist(const Point &p, int a, int b, int c) {
74     return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area(a, b, c));
75 }
76 //compute the minimal distance of center of any faces
77 double findDist() { //compute center of mass
78     double totalWeight = 0;
79     Point center(.0, .0, .0);
80     Point first = info[face[0][0]];
81     for (int i = 0; i < SIZE(face); ++i) {
82         Point p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+first)*.25;
83         double weight = mix(info[face[i][0]] - first, info[face[i][1]] - first,
    ↪ info[face[i][2]] - first);
84         totalWeight += weight; center = center + p * weight;
85     }
86     center = center / totalWeight;
87     double res = 1e100; //compute distance
88     for (int i = 0; i < SIZE(face); ++i)

```

```

89     res = min(res, calcDist(center, face[i][0], face[i][1], face[i][2]));
90     return res;
91 }

```

求四点外界球

```

1 // 注意, 无法处理小于四点的退化情况
2 int nouter; Tpoint outer[4], res; double radius;
3 void ball() {
4     Tpoint q[3]; double m[3][3], sol[3], L[3], det;
5     int i, j; res.x = res.y = res.z = radius = 0;
6     for (i=0; i<3; ++i) q[i]=outer[i+1]-outer[0], sol[i]=dot(q[i], q[i]);
7     for (i=0; i<3; ++i) for (j=0; j<3; ++j) m[i][j]=dot(q[i], q[j])*2;
8     det= m[0][0]*m[1][1]*m[2][2]
9     + m[0][1]*m[1][2]*m[2][0]
10    + m[0][2]*m[2][1]*m[1][0]
11    - m[0][2]*m[1][1]*m[2][0]
12    - m[0][1]*m[1][0]*m[2][2]
13    - m[0][0]*m[1][2]*m[2][1];
14    if ( fabs(det)<eps ) return;
15    for (j=0; j<3; ++j) {
16        for (i=0; i<3; ++i) m[i][j]=sol[i];
17        L[j]=( m[0][0]*m[1][1]*m[2][2]
18        + m[0][1]*m[1][2]*m[2][0]
19        + m[0][2]*m[2][1]*m[1][0]
20        - m[0][2]*m[1][1]*m[2][0]
21        - m[0][1]*m[1][0]*m[2][2]
22        - m[0][0]*m[1][2]*m[2][1]
23        ) / det;
24        for (i=0; i<3; ++i) m[i][j]=dot(q[i], q[j])*2;
25    } res=outer[0];
26    for (i=0; i<3; ++i ) res = res + q[i] * L[i];
27    radius=dist2(res, outer[0]);
28 }

```

图论

Hungarian

```

1 // 最小匹配, 自带初始化 n <= m 方案存在 p[] 中
2 const int N = 105;
3 const int INF = 1000000000; // 严格大于最大边权
4 int n, m, a[N][N];
5 int u[N], v[N], p[N], fa[N], minv[N];
6 bool used[N];
7 int km() {
8     memset(u, 0, sizeof(int) * n);
9     for (int i = 0; i <= m; ++i) v[i] = 0, p[i] = n;
10    for (int i = 0; i < n; ++i) {
11        p[m] = i;

```

```

12    int j0 = m;
13    for (int j = 0; j <= m; ++j) minv[j] = INF, used[j] = false;
14    do {
15        used[j0] = true;
16        int i0 = p[j0], delta = INF, j1;
17        for (int j = 0; j < m; ++j) {
18            if (!used[j]) {
19                int cur = a[i0][j] - u[i0] - v[j];
20                if (cur < minv[j]) minv[j] = cur, fa[j] = j0;
21                if (minv[j] < delta) delta = minv[j], j1 = j;
22            }
23        }
24        for (int j = 0; j <= m; ++j) {
25            if (used[j]) {
26                u[p[j]] += delta, v[j] -= delta;
27            } else {
28                minv[j] -= delta;
29            }
30        }
31        j0 = j1;
32    } while (p[j0] != n);
33    do {
34        int j1 = fa[j0];
35        p[j0] = p[j1];
36        j0 = j1;
37    } while (j0 != m);
38    }
39    return -v[m];
40 }

```

Hopcroft

```

1 // 左侧 N 个点, 右侧 K 个点, 1-based, 初始化将 matx[], maty[] 都置为 0
2 int N, K;
3 int que[N], dx[N], dy[N], matx[N], maty[N];
4 int BFS()
5 {
6     int flag = 0, qt = 0, qh = 0;
7     for(int i = 1; i <= K; ++ i) dy[i] = 0;
8     for(int i = 1; i <= N; ++ i) {
9         dx[i] = 0;
10        if (! matx[i]) que[qt++] = i;
11    }
12    while (qh < qt) {
13        int u = que[qh++];
14        for(Edge *e = E[u]; e; e = e->n)
15            if (! dy[e->t]) {
16                dy[e->t] = dx[u] + 1;
17                if (! maty[e->t]) flag = true;

```

```

18     else {
19         dx[maty[e->t]] = dx[u] + 2;
20         que[qt++] = maty[e->t];
21     }
22 }
23 }
24 return flag;
25 }
26 int DFS(int u)
27 {
28     for(Edge *e = E[u]; e; e = e->n)
29         if (dy[e->t] == dx[u] + 1) {
30             dy[e->t] = 0;
31             if (! maty[e->t] || DFS(maty[e->t])) {
32                 matx[u] = e->t; maty[e->t] = u;
33                 return true;
34             }
35         }
36     return false;
37 }
38 void Hopcroft()
39 {
40     while (BFS()) for(int i = 1; i <= N; ++ i) if (! matx[i]) DFS(i);
41 }

```

最大团

```

1 // Super Fast Maximum Clique
2 // To Build Graph: Maxclique(Edges, Number of Nodes)
3 // To Get Answer: mcqdyn(AnswerNodes Index Array, AnswerLength)
4 typedef bool BB[N];
5 struct Maxclique {
6     const BB* e; int pk, level; const float Tlimit;
7     struct Vertex{ int i, d; Vertex(int i):i(i),d(0){} };
8     typedef vector<Vertex> Vertices; typedef vector<int> ColorClass;
9     Vertices V; vector<ColorClass> C; ColorClass QMAX, Q;
10     static bool desc_degree(const Vertex &vi, const Vertex &vj){
11         return vi.d > vj.d;
12     }
13     void init_colors(Vertices &v){
14         const int max_degree = v[0].d;
15         for(int i = 0; i < (int)v.size(); i++) v[i].d = min(i, max_degree) + 1;
16     }
17     void set_degrees(Vertices &v){
18         for(int i = 0, j; i < (int)v.size(); i++)
19             for(v[i].d = j = 0; j < (int)v.size(); j++)
20                 v[i].d += e[v[i].i][v[j].i];
21     }
22     struct StepCount{ int i1, i2; StepCount():i1(0),i2(0){} };
23     vector<StepCount> S;

```

```

24 bool cut1(const int pi, const ColorClass &A){
25     for(int i = 0; i < (int)A.size(); i++) if (e[pi][A[i]]) return true;
26     return false;
27 }
28 void cut2(const Vertices &A, Vertices &B){
29     for(int i = 0; i < (int)A.size() - 1; i++)
30         if(e[A.back().i][A[i].i])
31             B.push_back(A[i].i);
32 }
33 void color_sort(Vertices &R){
34     int j = 0, maxno = 1, min_k = max((int)QMAX.size() - (int)Q.size() + 1, 1);
35     C[1].clear(), C[2].clear();
36     for(int i = 0; i < (int)R.size(); i++) {
37         int pi = R[i].i, k = 1;
38         while(cut1(pi, C[k])) k++;
39         if(k > maxno) maxno = k, C[maxno + 1].clear();
40         C[k].push_back(pi);
41         if(k < min_k) R[j++] .i = pi;
42     }
43     if(j > 0) R[j - 1].d = 0;
44     for(int k = min_k; k <= maxno; k++)
45         for(int i = 0; i < (int)C[k].size(); i++)
46             R[j].i = C[k][i], R[j++].d = k;
47 }
48 void expand_dyn(Vertices &R){// diff -> diff with no dyn
49     S[level].i1 = S[level].i1 + S[level - 1].i1 - S[level].i2;//diff
50     S[level].i2 = S[level - 1].i1;//diff
51     while((int)R.size() > 0) {
52         if((int)Q.size() + R.back().d > (int)QMAX.size()){
53             Q.push_back(R.back().i); Vertices Rp; cut2(R, Rp);
54             if((int)Rp.size() > 0){
55                 if((float)S[level].i1 / ++pk < Tlimit) degree_sort(Rp);//diff
56                 color_sort(Rp);
57                 S[level].i1++, level++;//diff
58                 expand_dyn(Rp);
59                 level--;//diff
60             }
61             else if((int)Q.size() > (int)QMAX.size()) QMAX = Q;
62             Q.pop_back();
63         }
64         else return;
65         R.pop_back();
66     }
67 }
68 void mcqdyn(int* maxclique, int &sz){
69     set_degrees(V); sort(V.begin(),V.end(), desc_degree); init_colors(V);
70     for(int i = 0; i < (int)V.size() + 1; i++) S[i].i1 = S[i].i2 = 0;
71     expand_dyn(V); sz = (int)QMAX.size();
72     for(int i = 0; i < (int)QMAX.size(); i++) maxclique[i] = QMAX[i];
73 }

```

```

74 void degree_sort(Vertexes &R){
75     set_degrees(R); sort(R.begin(), R.end(), desc_degree);
76 }
77 Maxclique(const BB* conn, const int sz, const float tt = 0.025) \
78 : pk(0), level(1), Tlimit(tt){
79     for(int i = 0; i < sz; i++) V.push_back(Vertex(i));
80     e = conn, C.resize(sz + 1), S.resize(sz + 1);
81 }
82 };

```

最小树形图

```

1  const int MAXN,INF;// INF >= sum( W_ij )
2  int from[MAXN + 10][MAXN * 2 + 10],n,m,edge[MAXN + 10][MAXN * 2 + 10];
3  int sel[MAXN * 2 + 10],fa[MAXN * 2 + 10],vis[MAXN * 2 + 10];
4  int getfa(int x){if(x == fa[x]) return x; return fa[x] = getfa(fa[x]);}
5  void liuzhu(){ // 1-base: root is 1, answer = (sel[i], i) for i in [2..n]
6      fa[1] = 1;
7      for(int i = 2; i <= n; ++i){
8          sel[i] = 1; fa[i] = i;
9          for(int j = 1; j <= n; ++j) if(fa[j] != i)
10             if(from[j][i] = i, edge[sel[i]][i] > edge[j][i]) sel[i] = j;
11     }
12     int limit = n;
13     while(1){
14         int prelimit = limit; memset(vis, 0, sizeof(vis)); vis[1] = 1;
15         for(int i = 2; i <= prelimit; ++i) if(fa[i] == i && !vis[i]){
16             int j = i; while(!vis[j]) vis[j] = i, j = getfa(sel[j]);
17             if(j == 1 || vis[j] != i) continue; vector<int> C; int k = j;
18             do C.push_back(k), k = getfa(sel[k]); while(k != j);
19             ++limit;
20             for(int i = 1; i <= n; ++i){
21                 edge[i][limit] = INF, from[i][limit] = limit;
22             }
23             fa[limit] = vis[limit] = limit;
24             for(int i = 0; i < int(C.size()); ++i){
25                 int x = C[i], fa[x] = limit;
26                 for(int j = 1; j <= n; ++j)
27                     if(edge[j][x] != INF && edge[j][limit] > edge[j][x] - edge[sel[x]][x]){
28                         edge[j][limit] = edge[j][x] - edge[sel[x]][x];
29                         from[j][limit] = x;
30                     }
31             }
32             for(int j=1;j<=n;++j) if(getfa(j)==limit) edge[j][limit] = INF;
33             sel[limit] = 1;
34             for(int j = 1; j <= n; ++j)
35                 if(edge[sel[limit]][limit] > edge[j][limit]) sel[limit] = j;
36         }
37         if(prelimit == limit) break;
38     }

```

```

39     for(int i = limit; i > 1; --i) sel[from[sel[i]][i]] = sel[i];
40 }

```

带花树

```

1  vector<int> link[maxn];
2  int n,match[maxn],Queue[maxn],head,tail;
3  int pred[maxn],base[maxn],start,finish,newbase;
4  bool InQueue[maxn],InBlossom[maxn];
5  void push(int u){ Queue[tail++]=u;InQueue[u]=true; }
6  int pop(){ return Queue[head++]; }
7  int FindCommonAncestor(int u,int v){
8      bool InPath[maxn];
9      for(int i=0;i<n;i++) InPath[i]=0;
10     while(true){ u=base[u];InPath[u]=true;if(u==start) break;u=pred[match[u]]; }
11     while(true){ v=base[v];if(InPath[v]) break;v=pred[match[v]]; }
12     return v;
13 }
14 void ResetTrace(int u){
15     int v;
16     while(base[u]!=newbase){
17         v=match[u];
18         InBlossom[base[u]]=InBlossom[base[v]]=true;
19         u=pred[v];
20         if(base[u]!=newbase) pred[u]=v;
21     }
22 }
23 void BlossomContract(int u,int v){
24     newbase=FindCommonAncestor(u,v);
25     for (int i=0;i<n;i++)
26         InBlossom[i]=0;
27     ResetTrace(u);ResetTrace(v);
28     if(base[u]!=newbase) pred[u]=v;
29     if(base[v]!=newbase) pred[v]=u;
30     for(int i=0;i<n;i++)
31         if(InBlossom[base[i]]){
32             base[i]=newbase;
33             if(!InQueue[i]) push(i);
34         }
35 }
36 bool FindAugmentingPath(int u){
37     bool found=false;
38     for(int i=0;i<n;i++) pred[i]=-1,base[i]=i;
39     for (int i=0;i<n;i++) InQueue[i]=0;
40     start=u;finish=-1; head=tail=0; push(start);
41     while(head<tail){
42         int u=pop();
43         for(int i=link[u].size()-1;i>=0;i--){
44             int v=link[u][i];

```

```

45     if(base[u] != base[v] && match[u] != v)
46         if(v == start || (match[v] >= 0 && pred[match[v]] >= 0))
47             BlossomContract(u, v);
48         else if(pred[v] == -1) {
49             pred[v] = u;
50             if(match[v] >= 0) push(match[v]);
51             else{ finish = v; return true; }
52         }
53     }
54 }
55 return found;
56 }
57 void AugmentPath(){
58     int u = finish, v = w;
59     while(u >= 0){ v = pred[u]; w = match[v]; match[v] = u; match[u] = v; u = w; }
60 }
61 void FindMaxMatching(){
62     for(int i = 0; i < n; ++i) match[i] = -1;
63     for(int i = 0; i < n; ++i) if(match[i] == -1) if(FindAugmentingPath(i)) AugmentPath();
64 }

```

Dominator Tree

```

1 vector<int> prec[N], succ[N];
2 vector<int> ord;
3 int stamp, vis[N];
4 int num[N];
5 int fa[N];
6 void dfs(int u) {
7     vis[u] = stamp;
8     num[u] = ord.size();
9     ord.push_back(u);
10    for (int i = 0; i < (int)succ[u].size(); ++i) {
11        int v = succ[u][i];
12        if (vis[v] != stamp) {
13            fa[v] = u;
14            dfs(v);
15        }
16    }
17 }
18 int fs[N], mins[N], dom[N], sem[N];
19 int find(int u) {
20     if (u != fs[u]) {
21         int v = fs[u];
22         fs[u] = find(fs[u]);
23         if (mins[v] != -1 && num[sem[mins[v]]] < num[sem[mins[u]]]) {
24             mins[u] = mins[v];
25         }
26     }
27     return fs[u];

```

```

28 }
29 void merge(int u, int v) { fs[u] = v; }
30 vector<int> buf[N];
31 int buf2[N];
32 void mark(int source) {
33     ord.clear();
34     ++stamp;
35     dfs(source);
36     for (int i = 0; i < (int)ord.size(); ++i) {
37         int u = ord[i];
38         fs[u] = u, mins[u] = -1, buf2[u] = -1;
39     }
40     for (int i = (int)ord.size() - 1; i > 0; --i) {
41         int u = ord[i], p = fa[u];
42         sem[u] = p;
43         for (int j = 0; j < (int)prec[u].size(); ++j) {
44             int v = prec[u][j];
45             if (use[v] != stamp) continue;
46             if (num[v] > num[u]) {
47                 find(v); v = sem[mins[v]];
48             }
49             if (num[v] < num[sem[u]]) {
50                 sem[u] = v;
51             }
52         }
53         buf[sem[u]].push_back(u);
54         mins[u] = u;
55         merge(u, p);
56         while (buf[p].size()) {
57             int v = buf[p].back();
58             buf[p].pop_back();
59             find(v);
60             if (sem[v] == sem[mins[v]]) {
61                 dom[v] = sem[v];
62             } else {
63                 buf2[v] = mins[v];
64             }
65         }
66     }
67     dom[ord[0]] = ord[0];
68     for (int i = 0; i < (int)ord.size(); ++i) {
69         int u = ord[i];
70         if (~buf2[u]) {
71             dom[u] = dom[buf2[u]];
72         }
73     }
74 }

```

主流

```

1 // Q is a priority_queue<PII, vector<PII>, greater<PII> >
2 // for an edge(s, t): u is the capacity, v is the cost, nxt is the next edge,
3 // op is the opposite edge
4 // this code can not deal with negative cycles
5 typedef pair<int,int> PII;
6 struct edge{ int t,u,v; edge *nxt,*op; }E[MAXE],*V[MAXV];
7 int D[MAXN], dist[MAXN], maxflow, mincost; bool in[MAXN];
8 bool modlabel(){
9     while(!Q.empty()) Q.pop();
10    for(int i=S;i<=T;++i) if(in[i]) D[i]=0,Q.push(PII(0,i)); else D[i]=inf;
11    while(!Q.empty()){
12        int x=Q.top().first,y=Q.top().second; Q.pop();
13        if(y==T) break; if(D[y]<x) continue;
14        for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->u)
15            if(x+(ii->v+dist[ii->t]-dist[y])<D[ii->t]){
16                D[ii->t]=x+(ii->v+dist[ii->t]-dist[y]);
17                Q.push(PII(D[ii->t],ii->t));
18            }
19    }
20    if(D[T]==inf) return false;
21    for(int i=S;i<=T;++i) if(D[i]>D[T]) dist[i]+=D[T]-D[i];
22    return true;
23 }
24 int aug(int p,int limit){
25     if(p==T) return maxflow+=limit,mincost+=limit*dist[S],limit;
26     in[p]=1; int kk,ll=limit;
27     for(edge *ii=V[p];ii;ii=ii->nxt) if(ii->u){
28         if(!in[ii->t]&&dist[ii->t]+ii->v==dist[p]){
29             kk=aug(ii->t,min(ii->u,ll)); ll-=kk,ii->op->u+=kk;
30             if(!ll) return in[p]=0,limit;
31         }
32     }
33     return limit-ll;
34 }
35 PII mincostFlow(){
36     for(int i=S;i<=T;++i) dist[i]=i==T?inf:0;
37     while(!Q.empty()) Q.pop(); Q.push(PII(0,T));
38     while(!Q.empty()){
39         int x=Q.top().first,y=Q.top().second; Q.pop(); if(dist[y]<x) continue;
40         for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->op->u&&ii->v+x<dist[ii->t])
41             dist[ii->t]=ii->v+x,Q.push(PII(dist[ii->t],ii->t));
42     }
43     maxflow=mincost=0;
44     do{
45         do{
46             memset(in,0,sizeof(in));
47         }while(aug(S,maxflow));
48     }while(modlabel());
49     return PII(maxflow,mincost);

```

50 }

无向图最小割

```

1 int cost[maxn][maxn],seq[maxn],len[maxn],n,m,pop,ans;
2 bool used[maxn];
3 void Init(){
4     int i,j,a,b,c;
5     for(i=0;i<n;i++) for(j=0;j<n;j++) cost[i][j]=0;
6     for(i=0;i<m;i++){
7         scanf("%d %d %d",&a,&b,&c); cost[a][b]+=c; cost[b][a]+=c;
8     }
9     pop=n; for(i=0;i<n;i++) seq[i]=i;
10 }
11 void Work(){
12     ans=inf; int i,j,k,l,mm,sum,pk;
13     while(pop > 1){
14         for(i=1;i<pop;i++) used[seq[i]]=0; used[seq[0]]=1;
15         for(i=1;i<pop;i++) len[seq[i]]=cost[seq[0]][seq[i]];
16         pk=0; mm=-inf; k=-1;
17         for(i=1;i<pop;i++) if(len[seq[i]] > mm){ mm=len[seq[i]]; k=i; }
18         for(i=1;i<pop;i++){
19             used[seq[l=k]]=1;
20             if(i==pop-2) pk=k;
21             if(i==pop-1) break;
22             mm=-inf;
23             for(j=1;j<pop;j++) if(!used[seq[j]])
24                 if((len[seq[j]]+cost[seq[l]][seq[j]]) > mm)
25                     mm=len[seq[j]], k=j;
26         }
27         sum=0;
28         for(i=0;i<pop;i++) if(i != k) sum+=cost[seq[k]][seq[i]];
29         ans=min(ans,sum);
30         for(i=0;i<pop;i++)
31             cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+cost[seq[pk]][seq[i]];
32         seq[pk]=seq[--pop];
33     }
34     printf("%d\n",ans);
35 }

```

数论

素数判定

```

1 int strong_pseudo_primetest(long long n,int base) {
2     long long n2=n-1,res;
3     int s=0;
4     while(n%2==0) n2>>=1,s++;
5     res=powmod(base,n2,n);

```

```

6     if((res==1)|| (res==n-1)) return 1;
7     s--;
8     while(s>=0) {
9         res=mulmod(res,res,n);
10        if(res==n-1) return 1;
11        s--;
12    }
13    return 0; // n is not a strong pseudo prime
14 }
15 int isprime(long long n) {
16     static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
17     static LL lim[]={4,0,1373653LL,25326001LL,250000000000LL,2152302898747LL,
18         ↪ 3474749660383LL,341550071728321LL,0,0,0,0};
19     if(n<2||n==3215031751LL) return 0;
20     for(int i=0;i<12;++i){
21         if(n<lim[i]) return 1;
22         if(strong_pseudoprime_test(n,testNum[i])==0) return 0;
23     }
24     return 1;
25 }

```

启发式分解

```

1 int ansn; LL ans[1000];
2 LL func(LL x,LL n){ return(mod_mul(x,x,n)+1)%n; }
3 LL Pollard(LL n){
4     LL i,x,y,p;
5     if(Rabin_Miller(n)) return n;
6     if(!(n&1)) return 2;
7     for(i=1;i<20;i++){
8         x=i; y=func(x,n); p=gcd(y-x,n);
9         while(p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)%n,n);}
10        if(p==0||p==n) continue;
11        return p;
12    }
13 }
14 void factor(LL n){
15     LL x;
16     x=Pollard(n);
17     if(x==n){ ans[ansn++]=x; return; }
18     factor(x); factor(n/x);
19 }

```

直线下整点个数

```

1 //  $\sum_{i=0}^{n-1} \lfloor \frac{a+bi}{m} \rfloor$ ,  $n, m, a, b > 0$ 
2 LL solve(LL n,LL a,LL b,LL m){
3     if(b==0) return n*(a/m);
4     if(a>=m) return n*(a/m)+solve(n,a%m,b,m);

```

```

5     if(b>=m) return (n-1)*n/2*(b/m)+solve(n,a,b%m,m);
6     return solve((a+b*n)/m,(a+b*n)%m,m,b);
7 }

```

二次剩余

```

1 void calcH(int &t, int &h, const int p) {
2     int tmp = p - 1; for (t = 0; (tmp & 1) == 0; tmp /= 2) t++; h = tmp;
3 }
4 // solve equation  $x^2 \bmod p = a$ 
5 bool solve(int a, int p, int &x, int &y) {
6     srand(19920225);
7     if (p == 2) { x = y = 1; return true; }
8     int p2 = p / 2, tmp = power(a, p2, p);
9     if (tmp == p - 1) return false;
10    if ((p + 1) % 4 == 0) {
11        x = power(a, (p + 1) / 4, p); y = p - x; return true;
12    } else {
13        int t, h, b, pb; calcH(t, h, p);
14        if (t >= 2) {
15            do {b = rand() % (p - 2) + 2;
16            } while (power(b, p / 2, p) != p - 1);
17            pb = power(b, h, p);
18        } int s = power(a, h / 2, p);
19        for (int step = 2; step <= t; step++) {
20            int ss = (((long long)(s * s) % p) * a) % p;
21            for (int i = 0; i < t - step; i++) ss = ((long long)ss * ss) % p;
22            if (ss + 1 == p) s = (s * pb) % p; pb = ((long long)pb * pb) % p;
23        } x = ((long long)s * a) % p; y = p - x;
24    } return true;
25 }

```

Pell 方程

```

1 ULL A,B,p[maxn],q[maxn],a[maxn],g[maxn],h[maxn];
2 int main() {
3     for (int test=1; n;scanf("%d",&n) && n;++test) {
4         printf("Case %d: ",test);
5         if (fabs(sqrt(n)-floor(sqrt(n)+1e-7))<=1e-7) {
6             int a=(int)(floor(sqrt(n)+1e-7)); printf("%d %d\n",a,1);
7         } else {
8             // 求  $x^2 - ny^2 = 1$  的最小正整数根, n 不是完全平方数
9             p[1]=q[0]=h[1]=1;p[0]=q[1]=g[1]=0;
10            a[2]=(int)(floor(sqrt(n)+1e-7));
11            for (int i=2;i;++i) {
12                g[i]=-g[i-1]+a[i]*h[i-1]; h[i]=(n-sqr(g[i]))/h[i-1];
13                a[i+1]=(g[i]+a[2])/h[i]; p[i]=a[i]*p[i-1]+p[i-2];
14                q[i]=a[i]*q[i-1]+q[i-2];

```



```

15     if (sqr((ULL)(p[i]))-n*sqr((ULL)(q[i]))==1){
16         A=p[i];B=q[i];break;
17     }
18 }
19 cout << A << ' ' << B << endl;
20 }
21 }
22 }

```

代数 FFT

```

1 // double 精度对 $10^9 + 7$  取模最多可以做到 $2^{20}$ 
2 const int MOD = 1000003;
3 const double PI = acos(-1);
4 typedef complex<double> Complex;
5 const int N = 65536, L = 15, MASK = (1 << L) - 1;
6 Complex w[N];
7 void FFTInit() {
8     for (int i = 0; i < N; ++i) {
9         w[i] = Complex(cos(2 * i * PI / N), sin(2 * i * PI / N));
10    }
11 }
12 void FFT(Complex p[], int n) {
13     for (int i = 1, j = 0; i < n - 1; ++i) {
14         for (int s = n; j ^= s >= 1, ~j & s;);
15         if (i < j) {
16             swap(p[i], p[j]);
17         }
18     }
19     for (int d = 0; (1 << d) < n; ++d) {
20         int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
21         for (int i = 0; i < n; i += m2) {
22             for (int j = 0; j < m; ++j) {
23                 Complex &p1 = p[i + j + m], &p2 = p[i + j];
24                 Complex t = w[rm * j] * p1;
25                 p1 = p2 - t;
26                 p2 = p2 + t;
27             }
28         }
29     }
30 }
31 Complex A[N], B[N], C[N], D[N];
32 void mul(int a[N], int b[N]) {
33     for (int i = 0; i < N; ++i) {
34         A[i] = Complex(a[i] >> L, a[i] & MASK);
35         B[i] = Complex(b[i] >> L, b[i] & MASK);
36     }
37     FFT(A, N), FFT(B, N);
38     for (int i = 0; i < N; ++i) {

```

```

39     int j = (N - i) % N;
40     Complex da = (A[i] - conj(A[j])) * Complex(0, -0.5),
41             db = (A[i] + conj(A[j])) * Complex(0.5, 0),
42             dc = (B[i] - conj(B[j])) * Complex(0, -0.5),
43             dd = (B[i] + conj(B[j])) * Complex(0.5, 0);
44     C[j] = da * dd + da * dc * Complex(0, 1);
45     D[j] = db * dd + db * dc * Complex(0, 1);
46 }
47 FFT(C, N), FFT(D, N);
48 for (int i = 0; i < N; ++i) {
49     long long da = (long long)(C[i].imag() / N + 0.5) % MOD,
50             db = (long long)(C[i].real() / N + 0.5) % MOD,
51             dc = (long long)(D[i].imag() / N + 0.5) % MOD,
52             dd = (long long)(D[i].real() / N + 0.5) % MOD;
53     a[i] = ((dd << (L * 2)) + ((db + dc) << L) + da) % MOD;
54 }
55 }

```

线性规划

```

1 // 求 $\max\{cx \mid Ax \leq b, x \geq 0\}$ 的解
2 typedef vector<double> VD;
3 VD simplex(vector<VD> A, VD b, VD c) {
4     int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
5     vector<VD> D(n + 2, VD(m + 1, 0)); vector<int> ix(n + m);
6     for (int i = 0; i < n + m; ++i) ix[i] = i;
7     for (int i = 0; i < n; ++i) {
8         for (int j = 0; j < m - 1; ++j) D[i][j] = -A[i][j];
9         D[i][m - 1] = 1; D[i][m] = b[i];
10        if (D[r][m] > D[i][m]) r = i;
11    }
12    for (int j = 0; j < m - 1; ++j) D[n][j] = c[j];
13    D[n + 1][m - 1] = -1;
14    for (double d; ; ) {
15        if (r < n) {
16            int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
17            D[r][s] = 1.0 / D[r][s]; vector<int> speedUp;
18            for (int j = 0; j <= m; ++j) if (j != s) {
19                D[r][j] *= -D[r][s];
20                if (D[r][j]) speedUp.push_back(j);
21            }
22            for (int i = 0; i <= n + 1; ++i) if (i != r) {
23                for (int j = 0; j < speedUp.size(); ++j)
24                    D[i][speedUp[j]] += D[r][speedUp[j]] * D[i][s];
25                D[i][s] *= D[r][s];
26            } r = -1; s = -1;
27            for (int j = 0; j < m; ++j) if (s < 0 || ix[s] > ix[j])
28                if (D[n + 1][j] > EPS || (D[n + 1][j] > -EPS && D[n][j] > EPS)) s = j;
29            if (s < 0) break;

```

```

30     for (int i = 0; i < n; ++ i) if (D[i][s] < -EPS)
31         if (r < 0 || (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS
32             || (d < EPS && ix[r + m] > ix[i + m])) r = i;
33     if (r < 0) return VD(); // 无边界
34 }
35 if (D[n + 1][m] < -EPS) return VD(); // 无解
36 VD x(m - 1);
37 for (int i = m; i < n + m; ++ i) if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
38 return x; // 最优值在 D[n][m]
39 }

```

Schreier-Sims

```

1 struct Permutation{
2     vector<int> P; Permutation(){} Permutation(int n){ P.resize(n); }
3     Permutation inv()const{
4         Permutation ret(P.size());
5         for(int i = 0; i < int(P.size()); ++i) ret.P[P[i]] = i;
6         return ret;
7     }
8     int &operator [](const int &dn){ return P[dn]; }
9     void resize(const size_t &sz){ P.resize(sz); }
10    size_t size()const{ return P.size(); }
11    const int &operator [](const int &dn)const{ return P[dn]; }
12 };
13 Permutation operator *(const Permutation &a, const Permutation &b){
14     Permutation ret(a.size());
15     for(int i = 0; i < (int)a.size(); ++i) ret[i] = b[a[i]];
16     return ret;
17 }
18 typedef vector<Permutation> Bucket;
19 typedef vector<int> Table; typedef pair<int,int> pii;
20 int n, m;
21 vector<Bucket> buckets, bucketsInv; vector<Table> lookupTable;
22 int fastFilter(const Permutation &g, bool addToGroup = true){
23     int n = buckets.size();
24     Permutation p;
25     for(int i = 0; i < n; ++i){
26         int res = lookupTable[i][p[i]];
27         if(res == -1){
28             if(addToGroup){
29                 buckets[i].push_back(p); bucketsInv[i].push_back(p.inv());
30                 lookupTable[i][p[i]] = (int)buckets[i].size() - 1;
31             }
32             return i;
33         }
34         p = p * bucketsInv[i][res]; swap(i1,i2);
35     }
36     return -1;
37 }

```

```

38 long long calcTotalSize(){
39     long long ret = 1;
40     for(int i = 0; i < n; ++i) ret *= buckets[i].size();
41     return ret;
42 }
43 bool inGroup(const Permutation &g){ return fastFilter(g, false) == -1; }
44 void solve(const Bucket &gen,int _n){ // m perm[0..n - 1]s
45     n = _n, m = gen.size();
46     //clear all
47     vector<Bucket> _buckets(n); swap(buckets, _buckets);
48     vector<Bucket> _bucketsInv(n); swap(bucketsInv, _bucketsInv);
49     vector<Table> _lookupTable(n); swap(lookupTable, _lookupTable);
50 }
51 for(int i = 0; i < n; ++i){
52     lookupTable[i].resize(n);
53     fill(lookupTable[i].begin(), lookupTable[i].end(), -1);
54 }
55 Permutation id(n);
56 for(int i = 0; i < n; ++i) id[i] = i;
57 for(int i = 0; i < n; ++i){
58     buckets[i].push_back(id); bucketsInv[i].push_back(id);
59     lookupTable[i][i] = 0;
60 }
61 for(int i = 0; i < m; ++i) fastFilter(gen[i]);
62 queue<pair<point,point> > toUpdate;
63 for(int i = 0; i < n; ++i)
64     for(int j = i; j < n; ++j)
65         for(int k = 0; k < (int)buckets[i].size(); ++k)
66             for(int l = 0; l < (int)buckets[j].size(); ++l)
67                 toUpdate.push(make_pair(pii(i,k), pii(j,l)));
68 while(!toUpdate.empty()){
69     pii a = toUpdate.front().first, b = toUpdate.front().second;
70     toUpdate.pop();
71     int res=fastFilter(buckets[a.first][a.second]*buckets[b.first][b.second]);
72     if(res==-1) continue;
73     pii newPair(res, (int)buckets[res].size() - 1);
74     for(int i = 0; i < n; ++i)
75         for(int j = 0; j < (int)buckets[i].size(); ++j){
76             if(i <= res) toUpdate.push(make_pair(pii(i, j), newPair));
77             if(res <= i) toUpdate.push(make_pair(newPair, pii(i, j)));
78         }
79 }
80 }

```

字符串

后缀数组 (倍增)

```

1 int rank[MAX_N],height[MAX_N];
2 int cmp(int *x,int a,int b,int d){

```

```

3   return x[a]==x[b]&&x[a+d]==x[b+d];
4 }
5 void doubling(int *a,int N,int M){
6     static int sRank[MAX_N],tmpA[MAX_N],tmpB[MAX_N];
7     int *x=tmpA,*y=tmpB;
8     for(int i=0;i<M;++i) sRank[i]=0;
9     for(int i=0;i<N;++i) ++sRank[x[i]=a[i]];
10    for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];
11    for(int i=N-1;i>=0;--i) sa[--sRank[x[i]]]=i;
12    for(int d=1,p=0;p<N;M=p,d<=1){
13        p=0; for(int i=N-d;i<N;++i) y[p++]=i;
14        for(int i=0;i<N;++i) if(sa[i]>=d) y[p++] = sa[i]-d;
15        for(int i=0;i<M;++i) sRank[i]=0;
16        for(int i=0;i<N;++i) ++sRank[x[i]];
17        for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];
18        for(int i=N-1;i>=0;--i) sa[--sRank[x[y[i]]]]=y[i];
19        swap(x,y); x[sa[0]]=0; p=1;
20        for(int i=1;i<N;++i) x[sa[i]]=cmp(y,sa[i],sa[i-1],d)?p-1:p++;
21    }
22 }
23 void calcHeight(){
24     for(int i=0;i<N;++i) rank[sa[i]]=i;
25     int cur=0; for(int i=0;i<N;++i)
26     if(rank[i]){
27         if(cur) cur--;
28         for(;a[i+cur]==a[sa[rank[i]-1]+cur];++cur);
29         height[rank[i]]=cur;
30     }
31 }

```

后缀自动机

```

1 struct State {
2     int length;
3     State *parent,*go[C];
4     State(int length = 0):length(length),parent(NULL){
5         memset(go,0,sizeof(go));
6     }
7     State* extend(State*, int token);
8 } node_pool[V], *tot_node;
9 State* State::extend(State *start,int token){
10    State *p=this;
11    State *np=new(tot_node++) State(this->length+1);
12    while(p!=NULL&&p->go[token]==NULL)
13        p->go[token]=np, p=p->parent;
14    if(p==NULL) np->parent=start;
15    else{
16        State *q=p->go[token];
17        if(p->length+1==q->length) np->parent=q;
18        else{

```

```

19        State *nq=new(tot_node++) State(p->length+1);
20        memcpy(nq->go,q->go,sizeof(q->go));
21        nq->parent=q->parent;
22        np->parent=q->parent=nq;
23        while(p!=NULL&&p->go[token]==q)
24            p->go[token]=nq, p=p->parent;
25    }
26 }
27 return np;
28 }

```

Manacher/ 扩展 KMP

```

1 void Manacher(char text[], int n, int palindrome[]) {
2     palindrome[0] = 1;
3     for (int i = 1, j = 0, i < (n << 1) - 1; ++ i) {
4         int p = i >> 1;
5         int q = i - p;
6         int r = (j + 1 >> 1) + palindrome[j] - 1;
7         palindrome[i] = r < q ? 0 : min(r - q + 1, palindrome[(j << 1) - i]);
8         while (0 <= p - palindrome[i] && q + palindrome[i] < n && text[p - palindrome[i]] ==
9             text[q + palindrome[i]]) {
10             palindrome[i] ++;
11         }
12         if (q + palindrome[i] - 1 > r) {
13             j = i;
14         }
15     }
16 }
17 void ExtendedKMP(char *s, int next[]) {
18     int l = strlen(s), i = 0, j = 0, k = 1;
19     while (1 + j < l && s[j] == s[1 + j]) {
20         ++j;
21     }
22     next[1] = j;
23     for (int i = 2; i < l; ++i) {
24         int len = k + next[k], ll = next[i - k];
25         if (ll < len - i) {
26             next[i] = ll;
27         } else {
28             j = max(0, len - i);
29             while (i + j < l && s[j] == s[i + j]) {
30                 ++j;
31             }
32             next[i] = j;
33             k = i;
34         }

```

```

35     }
36 }

```

字符串最小表示

```

1 std::string find(std::string s) {
2     int i,j,k,l,N=s.length(); s+=s;
3     for(i=0,j=1;j<N;){
4         for(k=0;k<N&&s[i+k]==s[j+k];k++);
5         if(k>=N) break;
6         if(s[i+k]<s[j+k]) j+=k+1;
7         else l=i+k,i=j,j=max(l,j)+1;
8     }
9     return s.substr(i,N);
10 }

```

后缀树 (With Pop Front)

```

1 int pos, text[N];
2 struct Node {
3     int l, r;
4     Node *suf, *ch[C];
5     int dgr;
6     Node *fa;
7     Node (int l = -1, int r = INF) : l(l), r(r) {
8         suf = fa = NULL;
9         memset(ch, 0, sizeof(ch));
10        dgr = 0;
11    }
12    Node* addEdge(Node *t) {
13        int c = text[t->l];
14        dgr += !ch[c];
15        ch[c] = t;
16        t->fa = this;
17        return t;
18    }
19    int len() {
20        return min(r, pos + 1) - l;
21    }
22 };
23
24 int top;
25 Node pool[N << 1], *root, *nxtSuf, *cur;
26 int remCnt, curP, curLen;
27 long long size;
28 queue<Node*> leaves;
29 void init() {
30     top = 0, pos = -1;
31     remCnt = 0, curP = 0, curLen = 0;

```

```

32     nxtSuf = NULL;
33     root = cur = new(pool + (top++)) Node(-1, -1);
34     size = 0;
35     while (leaves.size()) leaves.pop();
36 }
37 void link(Node *u) {
38     if (nxtSuf) nxtSuf->suf = u;
39     nxtSuf = u;
40 }
41 bool walk(Node *u) {
42     int len = u->len();
43     if (curLen >= len) {
44         curP += len, curLen -= len, cur = u;
45         return true;
46     }
47     return false;
48 }
49 void extend(int c) {
50     text[++pos] = c;
51     nxtSuf = NULL;
52     ++remCnt;
53     while (remCnt) {
54         curP = curLen ? curP : pos;
55         int curE = text[curP];
56         if (!cur->ch[curE]) {
57             leaves.push(cur->addEdge(new(pool + (top++)) Node(pos)));
58             link(cur);
59         } else {
60             Node *nxt = cur->ch[curE];
61             if (walk(nxt)) continue;
62             if (text[nxt->l + curLen] == c) {
63                 ++curLen;
64                 link(cur);
65                 break;
66             }
67             Node *split = new(pool + (top++)) Node(nxt->l, nxt->l + curLen);
68             cur->addEdge(split);
69             leaves.push(split->addEdge(new(pool + (top++)) Node(pos)));
70             nxt->l += curLen;
71             split->addEdge(nxt);
72             link(split);
73         }
74         --remCnt;
75         if (cur == root && curLen > 0) {
76             curP = pos - (--curLen);
77         } else {
78             cur = cur->suf ? cur->suf : root;
79         }
80     }
81     size += leaves.size();

```

```

82 }
83 void finish() {
84     nxtSuf = NULL;
85     for (int i = 0; i < top; ++i) if (pool[i].r == INF) link(pool + i);
86     while (remCnt > 0) {
87         if (curLen) {
88             int curE = text[curP];
89             Node *nxt = cur->ch[curE];
90             if (walk(nxt)) continue;
91             Node *split = new(pool + (top++)) Node(nxt->l, nxt->l + curLen);
92             leaves.push(cur->addEdge(split));
93             nxt->l += curLen;
94             split->addEdge(nxt);
95             link(split);
96         } else {
97             leaves.push(cur);
98             link(cur);
99         }
100         --remCnt;
101         if (cur == root && curLen > 0) {
102             --curLen;
103             curP = pos - remCnt + 1;
104         } else {
105             cur = cur->suf ? cur->suf : root;
106         }
107     }
108     if (nxtSuf != root) link(root);
109 }
110 void eraseUp(Node *u) {
111     size -= u->len();
112     int ch = text[u->l];
113     u = u->fa;
114     u->ch[ch] = NULL;
115     --(u->dgr);
116 }
117 void erase() {
118     Node *u = leaves.front();
119     leaves.pop();
120     while (u->dgr == 0 && u != cur) eraseUp(u);
121     if (u == cur) {
122         if (cur->dgr == 0 && curLen == 0) {
123             int len = u->len();
124             curLen = len;
125             curP = pos - len + 1;
126             cur = cur->fa;
127             eraseUp(u);
128         }
129         if (curLen) {
130             int curE = text[curP];
131             if (!cur->ch[curE]) {

```

```

132         Node *leaf = new(pool + (top++)) Node(pos - curLen + 1);
133         leaves.push(cur->addEdge(leaf));
134         size += leaf->len();
135         --remCnt;
136         if (cur == root && curLen > 0) {
137             curP = pos - (--curLen) + 1;
138         } else {
139             cur = cur->suf ? cur->suf : root;
140         }
141         while (curLen && walk(cur->ch[text[curP]])) continue;
142     }
143 }
144 }
145 }
146 int n;
147 char s[N], buf[N];
148 int ord[N], stop, sord[N << 1];
149 void dfs(Node *u) {
150     sord[u - pool] = stop++;
151     for (int i = 0; i < C; ++i) {
152         if (u->ch[i]) {
153             dfs(u->ch[i]);
154         }
155     }
156 }
157 void getOrd() {
158     init();
159     for (int i = 0; i < n; ++i) extend(s[i] - 'a');
160     finish();
161     stop = 0;
162     dfs(root);
163     int i = 0;
164     while (leaves.size()) {
165         ord[i++] = sord[leaves.front() - pool];
166         leaves.pop();
167     }
168 }

```

数据结构

Splay Tree

```

1 // 注意初始化内存池和 null 节点
2 struct Node{
3     int rev,size; Node *ch[2],*p;
4     void set(Node*,int); int dir(); void update(); void relax(); void appRev();
5 } nodePool[MAX_NODE],*curNode,*null;
6 Node *newNode(){
7     Node *t=curNode++; t->rev=0, t->size=1;
8     t->ch[0]=t->ch[1]=t->p=null; return t;
9 }

```

```

10 struct Splay{
11     Node *root;
12     Splay(){ root=newNode(); root->set(newNode(),0); root->update(); }
13     void rot(Node *t){
14         Node *p=t->p; int d=t->dir();
15         p->relax(); t->relax();
16         if(p==root) root=t;
17         p->set(t->ch[!d],d); p->p->set(t,p->dir()); t->set(p,!d);
18         p->update();
19     }
20     void splay(Node *t,Node *f=null){
21         for(t->relax();t->p!=f;){
22             if(t->p->p==f) rot(t);
23             else t->dir()==t->p->dir()?rot(t->p),rot(t):(rot(t),rot(t));
24             t->update();
25         }
26     };
27     void initNull(){ curNode=nodePool;null=curNode++;null->size=0; }
28     void Node::set(Node *t,int _d){ ch[_d]=t; t->p=this; }
29     int Node::dir(){ return this==p->ch[1]; }
30     void Node::update(){ size=ch[0]->size+ch[1]->size+1;}
31     void Node::relax(){ if(rev) ch[0]->appRev(), ch[1]->appRev(), rev=false; }
32     void Node::appRev(){ if(this==null) return; rev^=true; swap(ch[0],ch[1]); }

```

Link Cut Tree

```

1 // 注意初始化 null 节点, 单点的 is_root 初始为 true
2 struct Node{
3     Node *ch[2], *p;
4     int is_root, rev;
5     bool dir();
6     void set(Node*, bool);
7     void update();
8     void relax();
9     void app_rev();
10 } *null;
11 void rot(Node *t){
12     Node *p=t->p; bool d=t->dir();
13     p->relax(); t->relax(); p->set(t->ch[!d],d);
14     if(p->is_root) t->p=p->p,swap(p->is_root,t->is_root);
15     else p->p->set(t,p->dir());
16     t->set(p,!d); p->update();
17 }
18 void splay(Node *t){
19     for(t->relax();!t->is_root;){
20         if(t->p->is_root) rot(t);
21         else t->dir()==t->p->dir() ?(rot(t->p),rot(t)) :(rot(t),rot(t));
22         t->update();
23     }
24     void access(Node *t){

```

```

25     for(Node *s=null; t!=null; s=t,t=t->p){
26         splay(t);
27         if (t->p == null) { /*TODO*/ }
28         t->ch[1]->is_root=true; s->is_root=false;
29         t->ch[1]=s; t->update();
30     }
31 }
32 bool Node::dir(){ return this==p->ch[1]; }
33 void Node::set(Node *t,bool _d){ ch[_d]=t; t->p=this; }
34 void Node::update(){ }
35 void Node::app_rev(){ if (this == null) return; rev ^= true; swap(ch[0], ch[1]); }
36 void Node::relax() { if(this==null) return; if (rev) { ch[0]->app_rev();
37     ↪ ch[1]->app_rev(); rev = false; } }
38 void make_root(Node *u) { access(u); splay(u); u->app_rev(); }

```

轻重链剖分

```

1 struct Tree(){*root[N];
2 int father[N],size[N],depth[N];
3 int bfsOrd[N],pathId[N],ordInPath[N],sqn[N];
4 void doBfs(int s){
5     int qh=0,qt=0,*que=bfsOrd; father[s]=-1; depth[s]=0;
6     for(que[qt++]=s;qh<qt;){
7         int u=que[qh++];
8         foreach(iter,adj[u]){
9             int v=*iter; if(v==father[u]) continue;
10            father[v]=u; depth[v]=depth[u]+1; que[qt++]=v;
11        }
12    }
13 }
14 void doSplit(){
15     for(int i=N-1;i>=0;--i){
16         int u=bfsOrd[i]; size[u]=1;
17         foreach(iter,adj[u]){
18             int v=*iter; if(v==father[u]) continue; size[u]+=size[v];
19         }
20     }
21     memset(pathId,-1,sizeof pathId);
22     for(int i=0;i<N;++i){
23         int top=bfsOrd[i],cnt=0;
24         if(pathId[top]!=-1) continue;
25         for(int next,u=top;u!=-1;u=next){
26             sqn[cnt]=val[u]; ordInPath[u]=cnt; pathId[u]=top; ++cnt;
27             next=-1;
28             foreach(iter,adj[u]){
29                 int v=*iter; if(v==father[u]) continue;
30                 if(next<0||size[next]<size[v]) next=v;
31             }
32         }

```

```

33     root[top]=new Tree(0,cnt,sqn);
34 }
35 }
36 void prepare(){ doBfs(0); doSplit(); }

```

综合

DancingLinks

```

1 struct node{
2     node *left,*right,*up,*down,*col; int row,cnt;
3 }*head,*col[MAXC],Node[MAXNODE],*ans[MAXNODE];
4 int totNode;
5 void insert(const std::vector<int> &V,int rownum){
6     std::vector<node*> N;
7     for(int i=0;i<int(V.size());++i){
8         node* now=Node+(totNode++); now->row=rownum;
9         now->col=now->up=col[V[i]], now->down=col[V[i]]->down;
10        now->up->down=now, now->down->up=now;
11        now->col->cnt++; N.push_back(now);
12    }
13    for(int i=0;i<int(V.size());++i)
14        N[i]->right=N[(i+1)%V.size()], N[i]->left=N[(i-1+V.size())%V.size()];
15 }
16 void Remove(node *x){
17     x->left->right=x->right, x->right->left=x->left;
18     for(node *i=x->down;i!=x;i=i->down)
19         for(node *j=i->right;j!=i;j=j->right)
20             j->up->down=j->down, j->down->up=j->up, --(j->col->cnt);
21 }
22 void Resume(node *x){
23     for(node *i=x->up;i!=x;i=i->up)
24         for(node *j=i->left;j!=i;j=j->left)
25             j->up->down=j->down->up=j, ++(j->col->cnt);
26     x->left->right=x, x->right->left=x;
27 }
28 bool search(int tot){
29     if(head->right==head) return true;
30     node *choose=NULL;
31     for(node *i=head->right;i!=head;i=i->right){
32         if(choose==NULL||choose->cnt>i->cnt) choose=i;
33         if(choose->cnt<2) break;
34     }
35     Remove(choose);
36     for(node *i=choose->down;i!=choose;i=i->down){
37         for(node *j=i->right;j!=i;j=j->right) Remove(j->col);
38         ans[tot]=i;
39         if(search(tot+1)) return true;
40         ans[tot]=NULL;
41         for(node *j=i->left;j!=i;j=j->left) Resume(j->col);
42     }

```

```

43     Resume(choose);
44     return false;
45 }
46 void prepare(int totC){
47     head=Node+totC;
48     for(int i=0;i<totC;++i) col[i]=Node+i;
49     totNode=totC+1;
50     for(int i=0;i<=totC;++i){
51         (Node+i)->right=Node+(i+1)%totC;
52         (Node+i)->left=Node+(i+totC)%totC;
53         (Node+i)->up=(Node+i)->down=Node+i;
54     }
55 }

```

日期公式

```

1 int zeller(int y,int m,int d) {
2     if (m<=2) y--,m+=12; int c=y/100; y%=100;
3     int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
4     if (w<0) w+=7; return(w);
5 }
6 int getId(int y, int m, int d) {
7     if (m < 3) {y --; m += 12};
8     return 365 * y + y / 4 - y / 100 + y / 400 + (153 * m + 2) / 5 + d;
9 }

```

环状最长公共子序列

```

1 int n, a[N << 1], b[N << 1];
2 bool has(int i, int j) { return a[(i - 1) % n] == b[(j - 1) % n];}
3 const int DELTA[3][2] = {{0, -1}, {-1, -1}, {-1, 0}};
4 int from[N][N];
5 int solve() {
6     memset(from, 0, sizeof(from));
7     int ret = 0;
8     for (int i = 1; i <= 2 * n; ++ i) {
9         from[i][0] = 2;
10        int left = 0, up = 0;
11        for (int j = 1; j <= n; ++ j) {
12            int upleft = up + 1 + !!from[i - 1][j];
13            if (!has(i, j)) upleft = INT_MIN;
14            int max = std::max(left, std::max(upleft, up));
15            if (left == max) {
16                from[i][j] = 0;
17            } else if (upleft == max) {
18                from[i][j] = 1;
19            } else {
20                from[i][j] = 2;

```



```

21     }
22     left = max;
23 }
24 if (i >= n) {
25     int count = 0;
26     for (int x = i, y = n; y;) {
27         int t = from[x][y];
28         count += t == 1;
29         x += DELTA[t][0];
30         y += DELTA[t][1];
31     }
32     ret = std::max(ret, count);
33     int x = i - n + 1, y = 0;
34     from[x][0] = 0;
35     while (y <= n && from[x][y] == 0) y++;
36     for (; x <= i; ++x) {
37         from[x][y] = 0;
38         if (x == i) break;
39         for (; y <= n; ++y) {
40             if (from[x + 1][y] == 2) break;
41             if (y + 1 <= n && from[x + 1][y + 1] == 1) {
42                 y++; break;
43             }
44         }
45     }
46 }
47 }
48 return ret;
49 }

```

经纬度球面距离

```

1 double sphereDis(double lon1, double lat1, double lon2, double lat2, double R) {
2     return R * acos(cos(lat1) * cos(lat2) * cos(lon1 - lon2) + sin(lat1) * sin(lat2));
3 }

```

长方体表面两点最短距离

```

1 int r;
2 void turn(int i, int j, int x, int y, int z, int x0, int y0, int L, int W, int H) {
3     if (z==0) { int R = x*x+y*y; if (R<r) r=R;
4     } else {
5         if(i>=0 && i< 2) turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
6         if(j>=0 && j< 2) turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
7         if(i<=0 && i>-2) turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
8         if(j<=0 && j>-2) turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
9     }
10 }
11 int main(){

```

```

12 int L, H, W, x1, y1, z1, x2, y2, z2;
13 cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
14 if (z1!=0 && z1!=H) if (y1==0 || y1==W)
15     swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
16 else swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
17 if (z1==H) z1=0, z2=H-z2;
18 r=0x3fffffff;
19 turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
20 cout<<r<<endl;
21 }

```

其他

简易积分表

$$\begin{aligned}
 \int \frac{1}{1+x^2} dx &= \tan^{-1} x & \int \frac{1}{a^2+x^2} dx &= \frac{1}{a} \tan^{-1} \frac{x}{a} \\
 \int \frac{x}{a^2+x^2} dx &= \frac{1}{2} \ln |a^2+x^2| & \int \frac{x^2}{a^2+x^2} dx &= x - a \tan^{-1} \frac{x}{a} \\
 \int \sqrt{x^2 \pm a^2} dx &= \frac{1}{2} x \sqrt{x^2 \pm a^2} \pm \frac{1}{2} a^2 \ln \left| x + \sqrt{x^2 \pm a^2} \right| \\
 \int \sqrt{a^2 - x^2} dx &= \frac{1}{2} x \sqrt{a^2 - x^2} + \frac{1}{2} a^2 \tan^{-1} \frac{x}{\sqrt{a^2 - x^2}} \\
 \int \frac{x^2}{\sqrt{x^2 \pm a^2}} dx &= \frac{1}{2} x \sqrt{x^2 \pm a^2} \mp \frac{1}{2} a^2 \ln \left| x + \sqrt{x^2 \pm a^2} \right| \\
 \int \frac{1}{\sqrt{x^2 \pm a^2}} dx &= \ln \left| x + \sqrt{x^2 \pm a^2} \right| \\
 \int \frac{1}{\sqrt{a^2 - x^2}} dx &= \sin^{-1} \frac{x}{a} & \int \frac{x}{\sqrt{x^2 \pm a^2}} dx &= \sqrt{x^2 \pm a^2} & \int \frac{x}{\sqrt{a^2 - x^2}} dx &= -\sqrt{a^2 - x^2} \\
 \int \sqrt{ax^2 + bx + c} dx &= \frac{b+2ax}{4a} \sqrt{ax^2 + bx + c} + \frac{4ac-b^2}{8a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| \\
 \int x^n e^{ax} dx &= \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} dx \\
 \int \sin^2 ax dx &= \frac{x}{2} - \frac{1}{4a} \sin 2ax & \int \sin^3 ax dx &= -\frac{3 \cos ax}{4a} + \frac{\cos 3ax}{12a} \\
 \int \cos^2 ax dx &= \frac{x}{2} + \frac{\sin 2ax}{4a} & \int \cos^3 ax dx &= \frac{3 \sin ax}{4a} + \frac{\sin 3ax}{12a} \\
 \int \tan ax dx &= -\frac{1}{a} \ln \cos ax & \int \tan^2 ax dx &= -x + \frac{1}{a} \tan ax \\
 \int x \cos ax dx &= \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax & \int x^2 \cos ax dx &= \frac{2x \cos ax}{a^2} + \frac{a^2 x^2 - 2}{a^3} \sin ax \\
 \int x \sin ax dx &= -\frac{x \cos ax}{a} + \frac{\sin ax}{a^2} & \int x^2 \sin ax dx &= \frac{2-a^2 x^2}{a^3} \cos ax + \frac{2x \sin ax}{a^2}
 \end{aligned}$$

常用结论

弦图

设 $next(v)$ 表示 $N(v)$ 中最前的点。令 w^* 表示所有满足 $A \in B$ 的 w 中最后的一个点，判断 $v \cup N(v)$ 是否为极大团，只需判断是否存在一个 $w \in w^*$ ，满足 $Next(w) = v$ 且 $|N(v)| + 1 \leq |N(w)|$ 即可。

五边形数

$$\prod_{n=1}^{\infty} (1 - x^n) = \sum_{n=0}^{\infty} (-1)^n (1 - x^{2n+1}) x^{n(3n+1)/2}$$

重心

半径为 r , 圆心角为 θ 的扇形重心与圆心的距离为 $\frac{4r \sin(\theta/2)}{3\theta}$
半径为 r , 圆心角为 θ 的圆弧重心与圆心的距离为 $\frac{4r \sin^3(\theta/2)}{3(\theta - \sin(\theta))}$

第二类 Bernoulli number

$$B_m = 1 - \sum_{k=0}^{m-1} \binom{m}{k} \frac{B_k}{m-k+1}$$
$$S_m(n) = \sum_{k=1}^n k^m = \frac{1}{m+1} \sum_{k=0}^m \binom{m+1}{k} B_k n^{m+1-k}$$

Stirling 数

第一类 :n 个元素的项目分作 k 个环排列的方法数目

$$s(n, k) = (-1)^{n+k} |s(n, k)|$$
$$|s(n, 0)| = 0$$
$$|s(1, 1)| = 1$$
$$|s(n, k)| = |s(n-1, k-1)| + (n-1) * |s(n-1, k)|$$

第二类 :n 个元素的集定义 k 个等价类的方法数

$$S(n, 1) = S(n, n) = 1$$
$$S(n, k) = S(n-1, k-1) + k * S(n-1, k)$$

三角公式

$$\sin(a \pm b) = \sin a \cos b \pm \cos a \sin b \quad \cos(a \pm b) = \cos a \cos b \mp \sin a \sin b$$
$$\tan(a \pm b) = \frac{\tan(a) \pm \tan(b)}{1 \mp \tan(a) \tan(b)} \quad \tan(a) \pm \tan(b) = \frac{\sin(a \pm b)}{\cos(a) \cos(b)}$$
$$\sin(a) + \sin(b) = 2 \sin(\frac{a+b}{2}) \cos(\frac{a-b}{2}) \quad \sin(a) - \sin(b) = 2 \cos(\frac{a+b}{2}) \sin(\frac{a-b}{2})$$
$$\cos(a) + \cos(b) = 2 \cos(\frac{a+b}{2}) \cos(\frac{a-b}{2}) \quad \cos(a) - \cos(b) = -2 \sin(\frac{a+b}{2}) \sin(\frac{a-b}{2})$$
$$\sin(na) = n \cos^{n-1} a \sin a - \binom{n}{3} \cos^{n-3} a \sin^3 a + \binom{n}{5} \cos^{n-5} a \sin^5 a - \dots$$
$$\cos(na) = \cos^n a - \binom{n}{2} \cos^{n-2} a \sin^2 a + \binom{n}{4} \cos^{n-4} a \sin^4 a - \dots$$

Java 读入优化

```
1 import java.io.*;
2 import java.util.*;
3 import java.math.*;
4 public class Main{
```

```
5   BufferedReader reader = new BufferedReader(new InputStreamReader(System.in));
6   PrintWriter writer = new PrintWriter(System.out);
7   StringTokenizer tokenizer = null;
8   void solve() throws Exception {
9   }
10  void run()throws Exception{
11      try{
12          while (true) {
13              solve();
14          }
15      }
16      catch(Exception e){
17      }
18      finally{
19          reader.close();
20          writer.close();
21      }
22  }
23  String next()throws Exception{
24      for(;tokenizer == null || !tokenizer.hasMoreTokens();){
25          tokenizer = new StringTokenizer(reader.readLine());
26      }
27      return tokenizer.nextToken();
28  }
29  int nextInt()throws Exception{
30      return Integer.parseInt(next());
31  }
32  double nextDouble()throws Exception{
33      return Double.parseDouble(next());
34  }
35  BigInteger nextBigInteger()throws Exception{
36      return new BigInteger(next());
37  }
38  public static void main(String args[])throws Exception{
39      (new Main()).run();
40  }
41 }
```

Vimrc

```
1 set nu si mouse=a sw=4 ts=4 sts=4
2 set mp=g++\ -O2\ -Wall\ --std=c++11\ -Wno-unused-result\ %:r.cpp\ -o\ %:r
3 nmap <F2> :vs %:r.in <CR>
4 nmap <F8> :!time ./%:r < %:r.in <CR>
5 nmap <F9> :w <CR> :make<CR>
```

n	log10 n	n!	n C(n/2)	LCM(1...n)	Pn	Bn
2	0.30	2	2	2	2	2
3	0.48	6	3	6	3	5
4	0.60	24	6	12	5	15
5	0.70	120	10	60	7	52
6	0.78	720	20	60	11	203
7	0.85	5040	35	420	15	877
8	0.90	40320	70	840	22	4140
9	0.95	362880	126	2520	30	21147
10	1	3628800	252	2520	42	115975
11		39916800	462	27720	56	678570
12		479001600	924	27720	77	4213597
15			6435	360360	176	1382958545
20			184756	232792560	627	
25			5200300		1958	
30			155117520		5604	
40					37338	
50					204226	
70					4087968	
100					190569292	