Template

yuanyuan

December 13, 2018

目录

1 !

1.1 .vimrc

```
set nu ai ci si mouse=a ts=2 sts=2 sw=2
nmap<F2> : vs %<.in <CR>
nmap<F3> : !gedit % <CR>
nmap<F8> : !time ./%< < %<.in <CR>
nmap<F9> : :w <CR> :!g++ % -o %< -O2 -g -std=c++11 -Wall <CR>

nmap<F5> : !./%< <CR>
nmap<F10> : :w <CR> :make %< <CR>
```

1.2 Head

```
#include<bits/stdc++.h>
using namespace std;
#define fi first
#define se second
#define mp make_pair
#define pb push_back
#define rep(i, a, b) for(int i=(a); i<(b); i++)
#define per(i, a, b) for(int i=(b)-1; i>=(a); i--)
#define sz(a) (int)a.size()
#define de(a) cout << #a << " = " << a << endl
#define dd(a) cout << #a << " = " << a << " "
#define all(a) a.begin(), a.end()
#define pw(x) (1ll<<(x))
#define endl "\n"
typedef long long ll;
typedef pair<int, int> pii;
typedef vector<int> vi;

int main() {
   std::ios::sync_with_stdio(false);
   std::cin.tie(0);
   cout << setiosflags(ios::fixed);
   cout << setprecision(3);
   return 0;
}
```

2 DataStructure

2.1 1. Splay

```
struct Splay {
   #define ls son[u][0]
   #define rs son[u][1]
   static const int N = ::N;
   int rt, L, w[N], fa[N], son[N][2], cnt[N], siz[N];
   bool rev[N];
   void init() {
      fill_n(w, L+1, 0);
      fill_n(fa, L+1, 0);
      fill_n(son[0], L+1, 0);
      fill_n(son[1], L+1, 0);
      fill_n(cnt, L+1, 0);
      fill_n(siz, L+1, 0);
      fill_n(rev, L+1, 0);
      L=rt=0;
   }
   void up(int u) {
      if(!u) return ;
      siz[u] = cnt[u];
      if(ls) siz[u] += siz[ls];
      if(rs) siz[u] += siz[rs];
   }
   int build(int l, int r, int pre) {
      if(l > r) return 0;
      int mid = l + r >> 1, u = ++L;
      w[u] = ::w[mid];
      fa[u] = pre;
      cnt[u] = 1;
      ls = build(l, mid - 1, u);
      rs = build(mid + 1, r, u);
      up(u);
      return u;
   }
   void gao(int u) {
      if(!u) return ;
      rev[u] ^= 1;
      swap(ls, rs);
   }
   void down(int u) {
      if(!rev[u]) return ;
      gao(ls), gao(rs);
      rev[u] = 0;
   }
   int id(int u) {
      return son[fa[u]][1]==u;
   }
   void rot(int x) {
      int y=fa[x], z=fa[y];
      int l=id(x), r=(l^1);
      fa[x]=z;
      if(z) son[z][id(y)]=x;
      son[y][l]=son[x][r];
      if(son[y][l]) fa[son[y][l]]=y;
      son[x][r]=y;
      fa[y]=x;
      up(y); up(x);
   }
   void splay(int x, int g = 0) {
      while(fa[x]!=g) {
         int y=fa[x], z=fa[y];
         if(z!=g) (id(x)^id(y))?rot(x):rot(y);
         rot(x);
```

```
    }
    if(!g) rt=x;
}
void ins(int c) {
    if(!rt) {
        w[++L]=c;
        cnt[L]=siz[L]=1;
        rt=L;
        return ;
    }
    int u=rt, f=0;
    while(1) {
        if(c==w[u]) {
            ++cnt[u];
            up(u); up(f);
            splay(u);
            return ;
        }
        f=u;
        u=son[u][w[u]<c];
        if(!u) {
            w[++L]=c;
            fa[L]=f;
            if(f) son[f][w[f]<c]=L;
            cnt[L]=siz[L]=1;
            up(f);
            splay(L);
            return ;
        }
    }
}
// c in splay
// splay(u)
int rank(int c) {
    int u=rt, ans=0;
    while(1) {
        if(c<w[u]) {
            u=ls;
        } else if(c==w[u]) {
            if(ls) ans+=siz[ls];
            splay(u);
            return ans+1;
        } else {
            ans+=cnt[u];
            if(ls) ans+=siz[ls];
            u=rs;
        }
    }
}
// return w[u]
int mink(int k) {
    int u=rt;
    while(1) {
        if(siz[ls]>=k) {
            u=ls;
        } else {
            k-=siz[ls];
            if(cnt[u]>=k) {
                splay(u);
                return w[u];
            } else {
                k-=cnt[u];
                u=rs;
            }
        }
    }
}
// Next of rt
// 0 pre 1 next
// return u
int Next(int t) {
    int u=son[rt][t];
    while(son[u][t^1]) u=son[u][t^1];
    return u;
}
void del(int c) {
    rank(c);
    int u=rt;
    if(cnt[rt]>1) {
        --cnt[rt];
        up(rt);
        return ;
    }
    if(ls&&rs) {
        int pre=Next(0);
        int ne=Next(1);
        splay(pre);
        splay(ne, pre);
        son[ne][0]=0;
        up(ne);
        up(pre);
    } else if(ls) {
        rt=ls;
        fa[ls]=0;
    } else if(rs) {
        rt=rs;
        fa[rs]=0;
    } else {
        rt=0;
    }
}
};
```

2.2 2. Treap

```
// init!!
struct Treap {
    #define ls son[u][0]
    #define rs son[u][1]
    static const int N=101010;
```

```
static const int inf=1e9+7;
int rt, L, son[N][2], w[N], cnt[N], siz[N];
ll r[N];
void init() {
    fill_n(son[0], L+1, 0);
    fill_n(son[1], L+1, 0);
    fill_n(w, L+1, 0);
    fill_n(r, L+1, 0);
    fill_n(cnt, L+1, 0);
    fill_n(siz, L+1, 0);
    rt=L=0;
    srand(time(0));
}
void up(int u) {
    if(!u) return ;
    siz[u]=cnt[u];
    if(ls) siz[u]+=siz[ls];
    if(rs) siz[u]+=siz[rs];
}
// 1 left 0 right
void rot(int &u, int t) {
    int v=son[u][t];
    son[u][t]=son[v][t^1];
    son[v][t^1]=u;
    up(u); up(v);
    u=v;
}
// return u w[u]=c
int ins(int &u, int c) {
    int po;
    if(!u) {
        u=++L;
        w[u]=c;
        r[u]=((1ll*rand()<<30)^(rand()));
        cnt[u]=siz[u]=1;
        po=u;
    } else if(w[u]==c) {
        ++cnt[u];
        po=u;
    } else {
        int &s=son[u][w[u]<c];
        po=ins(s, c);
        if(r[s]<r[u]) rot(u, w[u]<c);
    }
    up(u);
    return po;
}
void del(int &u, int c) {
    if(w[u]==c) {
        if(cnt[u]>1) {
            --cnt[u];
        } else {
            if(ls&&rs) {
                int t=r[ls]>r[rs];
                rot(u, t);
                del(son[u][t^1], c);
            } else {
                u=ls+rs;
            }
        }
    } else {
        del(son[u][w[u]<c], c);
    }
    up(u);
}
// c in treap
int rank(int c) {
    int u=rt, ans=0;
    while(1) {
        if(c<w[u]) {
            u=ls;
        } else if(c==w[u]) {
            if(ls) ans+=siz[ls];
            return ans+1;
        } else {
            if(ls) ans+=siz[ls];
            ans+=cnt[u];
            u=rs;
        }
    }
}
// return w[u]
int mink(int k) {
    int u=rt;
    while(1) {
        if(siz[ls]>=k) {
            u=ls;
        } else {
            k-=siz[ls];
            if(cnt[u]>=k) {
                return w[u];
            } else {
                k-=cnt[u];
                u=rs;
            }
        }
    }
}
int Pre(int u, int c) {
    if(!u) return -inf;
    if(w[u]>=c) return Pre(ls, c);
    return max(w[u], Pre(rs, c));
}
int Next(int u, int c) {
    if(!u) return inf;
    if(w[u]<=c) return Next(rs, c);
    return min(w[u], Next(ls, c));
}
}T;
```

2.3 3. fhqTreap

```
// init!!
// rt=merge()
struct fhqTreap {
    #define ls son[u][0]
    #define rs son[u][1]
    static const int N=101010;
    int rt, L;
    int w[N], son[N][2], siz[N];
    ll r[N];
    void init() {
        fill_n(w, L+1, 0);
        fill_n(r, L+1, 0);
        fill_n(siz, L+1, 0);
        fill_n(son[0], L+1, 0);
        fill_n(son[1], L+1, 0);
        rt=L=0;
        srand(time(0));
    }
    void up(int u) {
        if(!u) return ;
        siz[u]=1;
        if(ls) siz[u]+=siz[ls];
        if(rs) siz[u]+=siz[rs];
    }
    int newnode(int c) {
        w[++L]=c;
        siz[L]=1;
        r[L]=((1ll*rand()<<30)^rand());
        return L;
    }
    // c
    void split(int u, int c, int &x, int &y) {
        if(!u) {
            x=y=0;
        } else {
            if(w[u]<=c) {
                x=u;
                split(rs, c, rs, y);
            } else {
                y=u;
                split(ls, c, x, ls);
            }
            up(u);
        }
    }
    // k
   void split(int u, int k, int &x, int &y) {
      if(!u) {
         x = y = 0;
      } else {
         if(siz[ls] < k) {
            x = u;
            split(rs, k - siz[ls] - 1, rs, y);
         } else {
            y = u;
            split(ls, k, x, ls);
         }
         up(u);
      }
   }
   int merge(int x,int y) {
       if(x&&y) {
           if(r[x]<r[y]) {
               son[x][1]=merge(son[x][1], y);
               up(x);
               return x;
           } else {
               son[y][0]=merge(x, son[y][0]);
               up(y);
               return y;
           }
       } else {
           return x+y;
       }
   }
   void ins(int c) {
       int x, y;
       split(rt, c, x, y);
       rt=merge(x, merge(newnode(c), y));
   }
   void del(int c) {
       int x, y, z;
       split(rt, c-1, x, y);
       split(y, c, y, z);
       y=merge(son[y][0], son[y][1]);
       rt=merge(x, merge(y, z));
   }
   int rank(int c) {
       int x, y;
       split(rt, c-1, x, y);
       int res=siz[x]+1;
       rt=merge(x, y);
       return res;
   }
   int mink(int k) {
       int u=rt;
       while(1) {
           if(k<=siz[ls]) {
               u=ls;
           } else {
               k-=siz[ls];
               if(k==1) {
                   return w[u];
               } else {
                   --k;
                   u=rs;
               }
           }
```

```
        }
    }
    int Pre(int c) {
        int x, y;
        split(rt, c-1, x, y);
        int u=x;
        while(rs) u=rs;
        rt=merge(x, y);
        return w[u];
    }
    int Next(int c) {
        int x, y;
        split(rt, c, x, y);
        int u=y;
        while(ls) u=ls;
        rt=merge(x, y);
        return w[u];
    }
}T;
```

2.4 4. PerTreap

```
// init!!
struct PerTreap {
    #define ls son[u][0]
    #define rs son[u][1]
    static const int N=500005;
    int L, tim;
    int rt[N], w[N*50], siz[N*50], son[N*50][2], r[N*50];
    void init() {
        fill_n(rt, tim+1, 0);
        fill_n(w, L+1, 0);
        fill_n(r, L+1, 0);
        fill_n(siz, L+1, 0);
        fill_n(son[0], L+1, 0);
        fill_n(son[1], L+1, 0);
        L=tim=0;
        srand(time(0));
    }
    void up(int u) {
        if(!u) return ;
        siz[u]=1;
        if(ls) siz[u]+=siz[ls];
        if(rs) siz[u]+=siz[rs];
    }
    int newnode(int c) {
        w[++L]=c;
        siz[L]=1;
        r[L]=rand();
        return L;
    }
    void copy(int &x, int u) {
        x=++L;
        w[x]=w[u];
        r[x]=r[u];
        siz[x]=siz[u];
        son[x][0]=son[u][0];
        son[x][1]=son[u][1];
    }
    void split(int u, int c, int &x, int &y) {
        if(!u) {
            x=y=0;
        } else {
            if(w[u]<=c) {
                copy(x, u);
                split(rs, c, son[x][1], y);
                up(x);
            } else {
                copy(y, u);
                split(ls, c, x, son[y][0]);
                up(y);
            }
        }
    }
    int merge(int x,int y) {
        if(x&&y) {
            int u;
            if(r[x]<r[y]) {
                copy(u, x);
                son[u][1]=merge(son[x][1], y);
            } else {
                copy(u, y);
                son[u][0]=merge(x, son[y][0]);
            }
            up(u);
            return u;
        } else {
            return x+y;
        }
    }
    void ins(int pre, int &now, int c) {
        int x, y;
        split(pre, c, x, y);
        now=merge(x, merge(newnode(c), y));
    }
    void del(int pre, int &now, int c) {
        int x, y, z;
        split(pre, c-1, x, y);
        split(y, c, y, z);
        if(!y) {
            now=pre;
            return ;
        }
        y=merge(son[y][0], son[y][1]);
        now=merge(x, merge(y, z));
    }
    int rank(int now, int c) {
        int x, y;
        split(now, c-1, x, y);
        int res=siz[x]+1;
```

```
        now=merge(x, y);
        return res;
    }
    int mink(int now, int k) {
        int u=now;
        while(1) {
            if(k<=siz[ls]) {
                u=ls;
            } else {
                k-=siz[ls];
                if(k==1) {
                    return w[u];
                } else {
                    --k;
                    u=rs;
                }
            }
        }
    }
    int Pre(int now, int c) {
        int x, y;
        split(now, c-1, x, y);
        if(!x) return -2147483647;
        int u=x;
        while(rs) u=rs;
        now=merge(x, y);
        return w[u];
    }
    int Next(int now, int c) {
        int x, y;
        split(now, c, x, y);
        if(!y) return 2147483647;
        int u=y;
        while(ls) u=ls;
        now=merge(x, y);
        return w[u];
    }
}T;
```

2.5 5. SegIntervalMax

```
// O(nlogn)
// 区间取 max, 区间求和
struct Seg {
#define ls rt << 1
#define rs ls | 1
   static const int N = ::N << 2;
   ll sum[N];
   int mi[N][2], cnt[N];
   void up(int rt) {
      sum[rt] = sum[ls] + sum[rs];
      rep(i, 0, 2) mi[rt][i] = min(mi[ls][i], mi[rs][i]);
      cnt[rt] = 0;
      rep(i, 0, 2) {
         if(mi[rt][0] == mi[ls | i][0]) cnt[rt] += cnt[ls | i];
         else mi[rt][1] = min(mi[rt][1], mi[ls | i][0]);
      }
   }
   void build(int l, int r, int rt) {
      if(l == r) {
         sum[rt] = mi[rt][0] = l; //modify
         mi[rt][1] = inf;
         cnt[rt] = 1;
         return ;
      }
      int mid = l + r >> 1;
      build(l, mid, ls);
      build(mid + 1, r, rs);
      up(rt);
   }
   void gao(int rt, int c) {
      if(c <= mi[rt][0]) return ;
      sum[rt] += 1ll * cnt[rt] * (c - mi[rt][0]);
      mi[rt][0] = c;
   }
   void down(int rt) {
      gao(ls, mi[rt][0]);
      gao(rs, mi[rt][0]);
   }
   void upd(int L, int R, int c, int l, int r, int rt) {
      if(L > R) return ;
      if(L <= l && r <= R && c < mi[rt][1]) {
         gao(rt, c);
         return ;
      }
      int mid = l + r >> 1;
      down(rt);
      if(L <= mid) upd(L, R, c, l, mid, ls);
      if(R > mid) upd(L, R, c, mid + 1, r, rs);
      up(rt);
   }
}seg;
```

2.6 6. 2DSegTree

```
// 区域覆盖、标记永久化、标记单调
const int N=1010;
int n,m,q;
struct seg {
    int ma[N<<2], la[N<<2];
    void upd(int L,int R,int c,int l=0,int r=m,int rt=1) {
        ma[rt]=max(ma[rt], c);
        if(L<=l&&r<=R) {
            la[rt]=max(la[rt], c);
            return ;
        }
        int mid=l+r>>1;
        if(L<=mid) upd(L, R, c, l, mid, rt<<1);
        if(R>=mid+1) upd(L, R, c, mid+1, r, rt<<1|1);
    }
```

```
    int qry(int L,int R,int l=0,int r=m,int rt=1) {
        int ans=0;
        ans=max(ans, la[rt]);
        if(L<=l&&r<=R) {
            ans=max(ans, ma[rt]);
            return ans;
        }
        int mid=l+r>>1;
        if(L<=mid) ans=max(ans, qry(L, R, l, mid, rt<<1));
        if(R>=mid+1) ans=max(ans, qry(L, R, mid+1, r, rt<<1|1));
        return ans;
    }
};
struct Seg {
    seg ma[N<<2], la[N<<2];
    void upd(int x1,int x2,int y1,int y2,int c,int l=0,int r=n,int rt=1) {
        ma[rt].upd(y1, y2, c);
        if(x1<=l&&r<=x2) {
            la[rt].upd(y1, y2, c);
            return ;
        }
        int mid=l+r>>1;
        if(x1<=mid) upd(x1, x2, y1, y2, c, l, mid, rt<<1);
        if(x2>=mid+1) upd(x1, x2, y1, y2, c, mid+1, r, rt<<1|1);
    }
    int qry(int x1,int x2,int y1,int y2,int l=0,int r=n,int rt=1) {
        int ans=0;
        ans=max(ans, la[rt].qry(y1, y2));
        if(x1<=l&&r<=x2) {
            ans=max(ans, ma[rt].qry(y1, y2));
            return ans;
        }
        int mid=l+r>>1;
        if(x1<=mid) ans=max(ans, qry(x1, x2, y1, y2, l, mid, rt<<1));
        if(x2>=mid+1) ans=max(ans, qry(x1, x2, y1, y2, mid+1, r, rt<<1|1));
        return ans;
    }
}T;
int main() {
    scanf("%d%d%d",&n,&m,&q);
    while(q--) {
        int d,s,h,x,y;scanf("%d%d%d%d%d",&d,&s,&h,&x,&y);
        int t=T.qry(x, x+d-1, y, y+s-1);
        T.upd(x, x+d-1, y, y+s-1, h+t);
    }
    printf("%d\n",T.qry(0, n, 0, m));
    return 0;
}
```

2.7 7. Fenwick

```
// [1,n] , init!!
template<class T>
struct Fenwick{
#define lb(x) ((x)&-(x))
    static const int N = 100001;
    int n;T a[N];
    void ini(int _n){ fill_n(a+1,n=_n,0);}
    void Pre(){ for(int i=1,j=i+lb(i);i<=n;++i,j=i+lb(i)) if(j<=n) a[j]+=a[i];}
    void add(int x,T d){ for(;x<=n;x+=lb(x)) a[x]+=d;}
    T sum(int x){ T r=0;for(;x>=1;x^=lb(x)) r+=a[x];return r;}
};
```

2.8 Rope

```
#include <ext/rope>
using namespace __gnu_cxx;

//index : [0..sz(rp))
rope<char> rp;
rp.push_back(ch);              // 在末尾添加 ch
rp.erase(cur, len);            // 删除 cur 开始的 len 个字符
rp.insert(cur, 字符数组 );     // 在 cur 处插入字符数组
rp.copy(cur, len, 字符数组 ); // 复制 cur 处开始的 len 个字符到字符数组
rp.replace(cur, 字符数组 );   // 删除 cur 处的字符，换成字符数组
rp.substr(cur, len);           // 提取从 cur 处开始的 len 个字符
rp.at(cur);                    // 取第 cur 个字符
rp[cur];                       // 同上
rp[i] = rp[i - 1];             // 可持久化, O(1), 直接拷贝根节点

/*

* 一）翻转操作
*  1. 维护一正一反两个 rope
*  2. 翻转等价于交换两个子串

* 二）区间循环位移
*  1. 拆成多个子串连在一起

* 三）区间 a>b, b>c, c>d ... z>a
*  1. 维护 26 个 rope

*/
```

2.9 ST

```
// [0,n)
// 实现不同功能请谨慎复用
// 求下标最好用 pair 存
struct ST{
   static const int N = 101010;
   int a[20][N], lg[N];
   void build(int *v, int n){
      rep(i, 2, n + 1) lg[i] = lg[i >> 1] + 1;
      rep(i, 0, n) a[0][i] = v[i];
      rep(i, 1, lg[n] + 1) rep(j, 0, n - (1 << i) + 1) {
         a[i][j] = max(a[i - 1][j], a[i - 1][j + (1 << i >> 1)]);
      }
   }
```

```
   int qry(int l, int r){
      if(l > r) swap(l, r);
      int i = lg[r - l + 1];
      return max(a[i][l] , a[i][r + 1 - (1 << i)]);
   }
};
```

2.10 lcSegTree

```
// need init
// 1. use id
// 2. init mi/nd as max/min val
struct Node {
    ll k, b;
    Node() : k(0), b(0) {}
    Node(ll k, ll b) : k(k), b(b) {}
    ll getf(int x) const {
        return k * x + b;
    }
};
struct Seg {
#define ls rt << 1
#define rs ls | 1
    static const int N = ::N << 2;
    Node nd[N], mi[N];
    void _upd(Node k, int l, int r, int rt) {
        int mid = l + r >> 1;
        if(k.getf(v[mid]) > nd[rt].getf(v[mid])) swap(k, nd[rt]);
        if(l == r) return ;
        if(min(nd[rt].getf(v[l]), nd[rt].getf(v[r])) >= max(k.getf(v[l]), k.getf(v[r])))
         return ;
        if(nd[rt].k > k.k) _upd(k, l, mid, ls);
        else _upd(k, mid + 1, r, rs);
    }
    void _min(Node k, int l, int r, int rt) {
        int mid = l + r >> 1;
        if(k.getf(v[mid]) < mi[rt].getf(v[mid])) swap(k, mi[rt]);
        if(l == r) return ;
        if(max(mi[rt].getf(v[l]), mi[rt].getf(v[r])) <= min(k.getf(v[l]), k.getf(v[r])))
         return ;
        if(mi[rt].k <= k.k) _min(k, l, mid, ls);
        else _min(k, mid + 1, r, rs);
    }
    void upd(int L, int R, Node c, int l, int r, int rt) {
        if(L > R) return ;
        if(L <= l && r <= R) {
            _upd(c, l, r, rt);
            _min(c, l, r, rt);
            return ;
        }
        int mid = l + r >> 1;
        if(L <= mid) upd(L, R, c, l, mid, ls);
        if(R > mid) upd(L, R, c, mid + 1, r, rs);
    }
    ll qry(int p, int l, int r, int rt) {
        ll ans = max(abs(nd[rt].getf(v[p])), abs(mi[rt].getf(v[p])));
        if(l == r) return ans;
        int mid = l + r >> 1;
        if(p <= mid) ans = max(ans, qry(p, l, mid, ls));
        else ans = max(ans, qry(p, mid + 1, r, rs));
        return ans;
    }
}seg;
```

2.11 动态 k 大

```
// zoj 2112 动态区间 k 大
const int N = 50505, M = 10101;
int n, m, a[N], rt[N<<1];
vi V, add, sub;
inline int rk(int x) {
   return lower_bound(all(V), x) - V.begin();
}
struct Q {
   bool op;
   int a, b, k;
}q[M];
struct Seg {
   static const int N = 2500005;//(::N + 32 * ::M) * 16;
   int cntn, cnt[N], ls[N], rs[N];
   void init() {
      fill_n(rt+1, n, cntn = 0);
   }
   void upd(int pre, int &now, int p, int c, int l, int r) {
      now = ++cntn;
      cnt[now] = cnt[pre] + c;
      ls[now] = ls[pre];
      rs[now] = rs[pre];
      if(l == r) return ;
      int mid = l+r>>1;
      if(p<=mid) upd(ls[pre], ls[now], p, c, l, mid);
      else upd(rs[pre], rs[now], p, c, mid+1, r);
   }
   int qry(int L, int R, int k, int l, int r) {
      if(l == r) return l;
      int mid = l+r>>1;
      int lc = 0;
      for(auto i : add) lc += cnt[ls[i]];
      for(auto i : sub) lc -= cnt[ls[i]];
      if(lc>=k) {
         rep(i, 0, sz(add)) add[i] = ls[add[i]];
         rep(i, 0, sz(sub)) sub[i] = ls[sub[i]];
         return qry(L, R, k, l, mid);
      } else {
         rep(i, 0, sz(add)) add[i] = rs[add[i]];
         rep(i, 0, sz(sub)) sub[i] = rs[sub[i]];
         return qry(L, R, k-lc, mid+1, r);
      }
   }
}seg;
```

```
struct Fenwick {
#define lb(x) ((x)&(-x))
   void init() {
      fill_n(rt+1+n, n, 0);
   }
   void upd(int x, int p, int c) {
      for(; x<=n; x+=lb(x)) seg.upd(rt[x+n], rt[x+n], p, c, 0, sz(V)-1);
   }
   int qry(int l, int r, int k) {
      add.clear();sub.clear();
      add.pb(rt[r]);sub.pb(rt[l-1]);
      int x = r;
      for(; x; x^=lb(x)) add.pb(rt[n+x]);
      x = l-1;
      for(; x; x^=lb(x)) sub.pb(rt[n+x]);
      return seg.qry(l, r, k, 0, sz(V)-1);
   }
}fw;
int main() {
   std::ios::sync_with_stdio(false);
   std::cin.tie(0);
   int T;
   cin >> T;
   while(T--) {
      ///
      cin >> n >> m;
      ///init
      V.clear();
      seg.init();
      fw.init();
      ///read
      rep(i, 1, n+1) cin >> a[i], V.pb(a[i]);
      rep(i, 1, m+1) {
         string s;
         cin >> s >> q[i].a >> q[i].b;
         q[i].op = (s[0]=='Q');
         if(s[0]=='Q') {
            cin >> q[i].k;
         } else {
            V.pb(q[i].b);
         }
      }
      ///solve
      sort(all(V));
      V.erase(unique(all(V)), V.end());
      rep(i, 1, n+1) seg.upd(rt[i-1], rt[i], rk(a[i]), 1, 0, sz(V)-1);
      rep(i, 1, m+1) {
         if(q[i].op) {
            cout << V[fw.qry(q[i].a, q[i].b, q[i].k)] << endl;
         } else {
            int p = q[i].a, c = q[i].b;
            fw.upd(p, rk(a[p]), -1);
            fw.upd(p, rk(a[p] = c), 1);
         }
      }
   }
   return 0;
}
```

2.12 覆盖大于 k 次的矩形面积

```
/*
 * 这里是覆盖次数大于 1 次的
 */
struct Seg {
#define ls rt << 1
#define rs ls | 1
   static const int N = ::N << 2;
   int la[N], len[2][N];
   void up(int rt, int l, int r) {
      if(la[rt] >= 2) {
         len[0][rt] = r - l + 1;
         len[1][rt] = r - l + 1;
      } else if(la[rt] >= 1) {
         len[0][rt] = r - l + 1;
         len[1][rt] = (l == r) ? 0 : len[0][ls] + len[0][rs];
      } else {
         len[0][rt] = (l == r) ? 0 : len[0][ls] + len[0][rs];
         len[1][rt] = (l == r) ? 0 : len[1][ls] + len[1][rs];
      }
   }
   void upd(int L, int R, int c, int l, int r, int rt) {
      if(L <= l && r <= R) {
         la[rt] += c;
         up(rt, l, r);
         return ;
      }
      int mid = l + r >> 1;
      if(L <= mid) upd(L, R, c, l, mid, ls);
      if(R > mid) upd(L, R, c, mid + 1, r, rs);
      up(rt, l, r);
   }
}seg;
```

3 Game

3.1 Game

```
// 威佐夫博弈
//      * 两堆物品，个数 (n, m)(n <= m) ，两人轮流从某一堆拿任意数量的物品或同时从两堆中取同样多的物品，每次至少一个，不能操作的人败。
//      * 必败态： (m - n) * (1 + sqrt5) / 2 == n
// 威佐夫博弈扩展
//      * 两堆物品，个数 (n, m)(n <= m) ，两人轮流从某一堆拿任意数量的物品或同时从两堆中取绝对值 <=k 的物品，每次至少一个，不能操作的人败。
//      * 必败态：
//          * d = k + 1, t^2 + (d - 2) * t - d = 0 -> 解出 t
//          * 必败： (m - n) / d * t == n
// 博弈fib
```

```
//      * 一堆石子，两人轮流取。先手不能在第一次取光，之后可以取的石子数介于 1 到对手刚取的石子数的两倍之间（左闭右闭），不能操作的人败。
//      * 必败态：石子个数是 fib 数
```

4 Geo

4.1 1. 2D

```
/*
 * 欧拉定理：平面图满足  V+F-E=2
 * 直线的一般式：  Ax+By+C=0
 * 点到直线的距离：  |Ax0+By0+C|/sqrt(A*A+B*B)
*/
// 向量 ab 与 x 轴的夹角，弧度，取值范围 (-pi, pi]
db ang(P a, P b) {
    return atan2(y(b)-y(a),x(b)-x(a));
}
// 向量 oa 与 ob 的夹角，弧度，取值范围 [0, pi]
db ang(P a, P o, P b) {
    return acos(dot(a - o, b - o) / abs(a - o) / abs(b - o));
}
// 向量逆时针旋转 rad （弧度）
P rot(P a, db rad) {
    return P(x(a) * cos(rad) - y(a) * sin(rad), x(a) * sin(rad) + y(a) * cos(rad));
}
P rot(P a, P o, db rad) {
    return rot(a - o, rad) + o;
}
// 逆时针旋转 90 度
P rot90(P p) {
    return P(-y(p), x(p));
}
// 向量 p 在向量 v 方向上的投影（点）
P proj(P p, P v) {
    return v * dot(p, v) / norm(v);
}
// 向量 ap 在向量 ab 方向上的投影（点）
P proj(P p, P a, P b) {
    return proj(p - a, b - a) + a;
}
// p 点关于 ab 的对称点
P reflect(P p, P a, P b) {
    P o = proj(p, a, b);
    return o * 2 - p;
}
// 直线 pv 和 qw 的交点
P insLL(P p, P v, P q, P w) {
    P u = p - q;
    v = v - p;
    w = w - q;
    db t = cross(w, u) / cross(v, w);
    return p + v * t;
}
// 判断点是否在线段上（不包括端点）
bool onS0(P p, P a, P b) {
    return sign(cross(p - a, b - a)) == 0 && sign(dot(p - a, p - b)) < 0;
}
// 判断点是否在线段上（包括端点）
bool onS1(P p, P a, P b) {
    return sign(cross(p - a, b - a)) == 0 && sign(dot(p - a, p - b)) <= 0;
}
// 判断两直线是否相交
bool isLL(P a1, P a2, P b1, P b2) {
   return sign(cross(a2 - a1, b2 - b1)) != 0;
}
// 判断线段是否规范相交（交点不在任一个端点上）
bool isSS0(P a1, P a2, P b1, P b2) {
    db c1 = cross(a2 - a1, b1 - a1), c2 = cross(a2 - a1, b2 - a1),
       c3 = cross(b2 - b1, a1 - b1), c4 = cross(b2 - b1, a2 - b1);
    return sign(c1) * sign(c2) < 0 && sign(c3) * sign(c4) < 0;
}
// 判断线段是否不规范相交
bool isSS1(P a1, P a2, P b1, P b2) {
    db c1 = cross(a2 - a1, b1 - a1), c2 = cross(a2 - a1, b2 - a1),
       c3 = cross(b2 - b1, a1 - b1), c4 = cross(b2 - b1, a2 - b1);
   return sign(max(x(a1), x(a2)) - min(x(b1), x(b2))) >= 0 &&
         sign(max(x(b1), x(b2)) - min(x(a1), x(a2))) >= 0 &&
         sign(max(y(a1), y(a2)) - min(y(b1), y(b2))) >= 0 &&
         sign(max(y(b1), y(b2)) - min(y(a1), y(a2))) >= 0 &&
         sign(c1) * sign(c2) <= 0 && sign(c3) * sign(c4) <= 0;
}
// 判断直线线段是否相交（端点也算）
bool isLS(P a1, P a2, P b1, P b2) {
    db c1 = cross(a2 - a1, b1 - a1), c2 = cross(a2 - a1, b2 - a1);
    return sign(c1) * sign(c2) <= 0;
}
// 点到直线距离
db distoL(P p, P a, P b) {
    return fabs(cross(b - a, p - a)) / abs(b - a);
}
// 点到线段距离
db distoS(P p, P a, P b) {
    if(sign(dot(b - a, p - a)) < 0) return abs(p - a);
    if(sign(dot(a - b, p - b)) < 0) return abs(p - b);
    return distoL(p, a, b);
}
// 直线两点式转一般式
// 直线的一般式：  Ax+By+C=0
void getLABC(P a, P b, db &A, db &B, db &C) {
    A = y(a) - y(b);
   B = x(b) - x(a);
   C = x(a) * y(b) - y(a) * x(b);
}
// 多边形面积
db areaP(P *p, int n) {
   db ans = 0;p[n] = p[0];
   rep(i, 0, n) ans += cross(p[i], p[i+1]);
   return fabs(ans) / 2;
}
```

```
// 判断点和多边形关系边上 -1 外 0 内 1
int Pinploy(P o, P *p, int n) {
   int res = 0;
   rep(i, 0, n) {
      P u = p[i], v = p[(i + 1) % n];
      if(onS1(o, u, v)) return -1;
      int k = sign(cross(v - u, o - u));
      int d1 = sign(y(u) - y(o));
      int d2 = sign(y(v) - y(o));
      if(k > 0 && d1 <= 0 && d2 > 0) ++res;
      if(k < 0 && d2 <= 0 && d1 > 0) --res;
   }
   return res != 0;
}
// 求凸包：把给定点包围在内部的，面积最小的凸多边形
// 复杂度： O(n) 加上排序： O(nlogn)
// 输入的点要先去重
// 如果不希望在凸包的边上有输入点，把两个 <= 改成 <
int convexhull(P *p, int n, P *ch) {
   sort(p, p + n);
   int m = 0;
   rep(i, 0, n) {
      while(m > 1 && sign(cross(ch[m - 1] - ch[m - 2], p[i] - ch[m - 2])) <= 0) --m;
      ch[m++] = p[i];
   }
   int k = m;
   for(int i = n - 2; i >= 0; --i) {
      while(m > k && sign(cross(ch[m - 1] - ch[m - 2], p[i] - ch[m - 2])) <= 0) --m;
      ch[m++] = p[i];
   }
   if(n > 1) --m;
   return m;
}

struct C {
   // 通过圆心角（弧度）求圆上坐标
   P point(db rad) {
      return P(o.x + cos(rad) * r, o.y + sin(rad) * r);
   }
};
// 判断、求线圆交点
bool isLC(C c, P a, P b, P &p1, P &p2) {
   db x = dot(a - c.o, b - a), y = norm(b - a),
      d = x * x - y * (norm(a - c.o) - c.r * c.r);
   if(sign(d) < 0) return 0; if(d < 0) d = 0;
   P q1 = a - (b - a) * (x / y),
     q2 = (b - a) * (sqrt(d) / y);
   p1 = q1 - q2;
   p2 = q1 + q2;
   return 1;
}
// 判断两圆关系
// 相等 0 相离 1 外切 2 相交 3 内切 4 内含 5
int relCC(C c1, C c2) {
   P p1 = c1.o, p2 = c2.o;
   db r1 = c1.r, r2 = c2.r;
   db d = dis(p1, p2);
   if(sign(d) == 0 && sign(r1 - r2) == 0) return 0;
   int x = sign(d - r1 - r2), y = sign(d - fabs(r1 - r2));
   if(x == 0) return 2;
   if(y == 0) return 4;
   if(x > 0) return 1;
   if(y < 0) return 5;
   if(y > 0 && x < 0) return 3;
   return -1;
}
// 返回值表示是否有交点
// 求圆圆交点
bool isCC(C c1, C c2, P &p1, P &p2) {
   db x = norm(c1.o - c2.o),
      y = ((c1.r * c1.r - c2.r * c2.r) / x + 1) / 2,
      d = c1.r * c1.r / x - y * y;
   if(sign(d) < 0) return 0; if(d < 0) d = 0;
   P q1 = (c2.o - c1.o) * y + c1.o,
     q2 = rot90((c2.o - c1.o) * sqrt(d));
   p1 = q1 - q2;
   p2 = q1 + q2;
   return 1;
}
// 求点圆切点
vector<P> tanCP(P p, C c, P &p1, P &p2) {
   db x = norm(p - c.o), d = x - c.r * c.r;
   vector<P> ans;
   if(sign(d) < 0) return ans; if(d < 0) d = 0;
   P q1 = (p - c.o) * (c.r * c.r / x),
     q2 = rot90((p - c.o) * (-c.r * sqrt(d) / x));
   p1 = c.o + q1 - q2;
   p2 = c.o + q1 + q2;
   ans.pb(p1);ans.pb(p2);
   return ans;
}
// 求圆圆切线
vector<pair<P, P> > tanCC(C c1, C c2) {
   vector<pair<P, P> > ans;
   if(!sign(c1.r - c2.r)) {
      P dir = c2.o - c1.o;
      dir = rot90(dir * (c1.r / abs(dir)));
      ans.pb(mp(c1.o + dir, c2.o + dir));
      ans.pb(mp(c1.o - dir, c2.o - dir));
   } else {
      P p = (c1.o * (-c2.r) + c2.o * c1.r) / (c1.r - c2.r);
      P t1,t2;
      vector<P> ps = tanCP(p, c1, t1, t2);
      vector<P> qs = tanCP(p, c2, t1, t2);
      for (int i = 0; i < sz(ps) && i < sz(qs); ++i) {
         if(!i || !(ps[i] == ps[i-1] && qs[i] == qs[i-1]))
            ans.pb(mp(ps[i],qs[i]));
      }
   }
   P p = (c1.o * c2.r + c2.o * c1.r) / (c1.r + c2.r);
```

```
   P t1,t2;
   vector<P> ps = tanCP(p, c1, t1, t2);
   vector<P> qs = tanCP(p, c2, t1, t2);
   for (int i = 0; i < sz(ps) && i < sz(qs); ++i) {
      if(!i || !(ps[i] == ps[i-1] && qs[i] == qs[i-1]))
         ans.pb(mp(ps[i],qs[i]));
   }
   return ans;
}
// 圆面积交
db areaCC(C c1, C c2) {
   db d = abs(c1.o - c2.o);
   if(sign(c1.r + c2.r - d) <= 0) return 0;
   if(sign(d - fabs(c1.r - c2.r)) <= 0) {
      db r = min(c1.r, c2.r);
      return r*r*pi;
   }
   db x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d);
   db t1 = acos(x / c1.r);
   db t2 = acos((d - x) / c2.r);
   return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
}
// 圆三角形面积交
// 圆：半径： r 圆心：原点
// 三角形：圆心、 p1 、 p2
db areaCT(db r, P p1, P p2) {
   P q1, q2, o = P(0, 0);
   C c = C(o, r);
   int f = isLC(c, p1, p2, q1, q2);
   if(!f) return r * r * ang(p1, o, p2) / 2;
   bool b1 = sign(abs(p1) - r) > 0;
   bool b2 = sign(abs(p2) - r) > 0;
   if(b1 && b2) {
      if(sign(dot(p1 - q1, p2 - q1)) <= 0 && sign(dot(p1 - q2, p2 - q2)) <= 0) {
         return (r * r * (ang(p1, o, p2) - ang(q1, o, q2))) + fabs(cross(q1, q2)) / 2;
      } else {
         return r * r * ang(p1, o, p2) / 2;
      }
   } else if(b1) {
      return (r * r * ang(p1, o, q1) ) + fabs(cross(q1, p2)) / 2;
   } else if(b2) {
      return (r * r * ang(q2, o, p2) ) + fabs(cross(p1, q2)) / 2;
   } else {
      return fabs(cross(p1, p2)) / 2;
   }
}
// 三角形内心
P inC(P A, P B, P C) {
   db a = abs(B - C);
   db b = abs(A - C);
   db c = abs(A - B);
   return (A * a + B * b + C * c) / (a + b + c);
}
// 三角形外心
P outC(P A, P B, P C) {
   P b = B - A, c = C - A;
   db db = norm(b), dc = norm(c), d = 2 * cross(b, c);
   return A - P(y(b) * dc - y(c) * db, x(c) * db - x(b) * dc) / d;
}
// 三角形垂心
P othroC(P A, P B, P C) {
   P ba = B - A, ca = C - A, bc = B - C;
   db Y = y(ba) * y(ca) * y(bc);
   db a = cross(ca, ba);
   db xx = (Y + x(ca) * y(ba) * x(B) - x(ba) * y(ca) * x(C)) / a;
   db yy = -x(ba) * (xx - x(C)) / y(ba) + y(ca);
   return P(xx, yy);
}
// 最小圆覆盖 O(n)
void Mincir(P *p, int n){
   random_shuffle(p, p+n);
   P cir = p[0]; db r= 0;
   for(int i = 1; i < n; i++){
      if(sign(dis(cir, p[i]) - r) <= 0) continue;
      cir = p[i], r = 0;
      for(int j = 0; j < i; j++){
         if(sign(dis(cir, p[j]) - r) <= 0) continue;
         cir = P ((x(p[i]) + x(p[j])) / 2, (y(p[i]) + y(p[j])) / 2);
         r = dis(cir, p[j]);
         for(int k = 0; k < j; k++){
            if(sign(dis(cir, p[k]) - r) <= 0) continue;
            cir = outC(p[i], p[j], p[k]);
            r = dis(cir, p[k]);
         }
      }
   }
   printf("%.2f %.2f %.2f\n", x(cir), y(cir), r);
}
// 半平面交未测试
const int N=450005;
struct Seg{
   P s, e;
   double r;
   void getr(){r = atan2(y(e)-y(s), x(e)-x(s));}
   bool operator < (const Seg& c)const {
      int d = sign(r - c.r);
      if (!d) return sign(cross(c.s - s, c.e -s)) > 0;
      return d < 0;
   }
}seg[N], Q[N];
int sz;
P insLL(Seg a, Seg b){return insLL(a.s,a.e,b.s,b.e);}
void add_seg(db xa, db ya, db xb, db yb){
   seg[sz].s=P(xa,ya);seg[sz].e=P(xb,yb);
   seg[sz].getr();sz++;
}
int hpi(P *p){
   sort(seg, seg+sz);
   int tmp=1;
   for(int i=1; i<sz; i++)
```

```
      if(sign(seg[i].r-seg[tmp-1].r))
         seg[tmp++]=seg[i];
   sz=tmp; Q[0]=seg[0];Q[1]=seg[1];
   int h=0,r=1;
   for(int i=2; i<sz; i++){
      while(h<r&&sign(cross(seg[i].e-seg[i].s,insLL(Q[r],Q[r-1])-seg[i].s))<=0) r--;
      while(h<r&&sign(cross(seg[i].e-seg[i].s,insLL(Q[h],Q[h+1])-seg[i].s))<=0) h++;
      Q[++r]=seg[i];
   }
   while(h<r&&sign(cross(Q[h].e-Q[h].s,insLL(Q[r],Q[r-1])-Q[h].s))<=0)r--;
   while(h<r&&sign(cross(Q[r].e-Q[r].s,insLL(Q[h],Q[h+1])-Q[r].s))<=0)h++;
   if(h+1>=r) return 0;
   int m=0;
   for(int i=h;i<r;i++)p[m++]=insLL(Q[i], Q[i+1]);
   if(r>h+1)p[m++]=insLL(Q[h], Q[r]);
   return m;
}
// 圆面积交 k
struct Event{
   P p;
   db ang;
   int delta;
   Event() {}
   Event (P p = P(0, 0), db ang = 0, int delta = 0):p(p), ang(ang), delta(delta){}
   bool operator <(const Event& c) const {return ang < c.ang;}
};
db sqr(db x) {return x*x;}
void addEvent(C a, C b, vector<Event> &evt, int&cnt){
   db d2=norm(a.o - b.o),
   dRatio=((a.r - b.r) * (a.r + b.r)/d2+1)/2,
   pRatio=sqrt(-(d2-sqr(a.r-b.r))*(d2-sqr(a.r+b.r))/(d2*d2*4));
   P d=b.o-a.o, p=rot(d, pi/2),
     q0=a.o+d*dRatio+p*pRatio,
     q1=a.o+d*dRatio-p*pRatio;
   db ang0 = ang(a.o, q0), ang1=ang(a.o, q1);
   evt.pb(Event(q1, ang1, 1));evt.pb(Event(q0, ang0, -1));
   cnt += ang1>ang0;
}
bool issame(C a, C b){return !sign(abs(a.o - b.o))&&!sign(a.r-b.r);}
bool overlap(C a, C b){return sign(a.r-b.r-abs(a.o-b.o))>=0;}
bool intersect(C a, C b){return sign(abs(a.o-b.o) - a.r - b.r) < 0;}
void solve(C *c, int n, db *ans){
   memset(ans, 0, sizeof(db) * (n+2));
   for(int i=0; i<n; i++){
      int cnt=1;
      vector<Event> evt;
      for(int j=0; j<i; j++) if(issame(c[i], c[j])) ++cnt;
      for(int j=0; j<n; j++)
         if(j != i && !issame(c[i], c[j]) && overlap(c[j], c[i]))
            cnt++;
      for(int j=0; j<n; j++)
         if(j!=i&&!overlap(c[j], c[i])&& !overlap(c[i], c[j])&&intersect(c[i], c[j]))
         addEvent(c[i], c[j], evt, cnt);
      if(!sz(evt))ans[cnt]+=pi*c[i].r*c[i].r;
      else{
         sort(evt.begin(), evt.end());
         evt.pb(evt.front());
         for(int j=0; j+1<sz(evt); j++){
            cnt+=evt[j].delta;
            ans[cnt]+=cross(evt[j].p, evt[j+1].p)/2;
            db ang=evt[j+1].ang-evt[j].ang;
            if(ang<0)ang+=pi*2;
            ans[cnt]+=ang*c[i].r*c[i].r/2-sin(ang)*c[i].r*c[i].r/2;
         }
      }
   }
}
```

4.2 2. zp_Geo2D

```
/*
 * 平面图欧拉定理：V + F - E = 2
 */
typedef db T;
const db eps = 1e-9 , pi = acosl(-1.);
int sgn(T x){return (x>eps)-(x<-eps);}
struct P{
   T x,y; P(){} P(T x,T y):x(x),y(y){}
   P operator - (const P&b) const {return P(x-b.x,y-b.y);}
   P operator + (const P&b) const {return P(x+b.x,y+b.y);}
   T operator * (const P&b) const {return x*b.x+y*b.y;}
   T operator / (const P&b) const {return x*b.y-y*b.x;}
   P operator * (const T&k) const {return P(x*k,y*k);}
   P operator / (const T&k) const {return P(x/k,y/k);}
   bool operator < (const P&b) const {return sgn(x-b.x)?x<b.x:y<b.y;}
   bool operator == (const P&b) const{return !sgn(x-b.x)&&!sgn(y-b.y);}
   bool operator != (const P&b) const{return !(*this == b);}
   P rot90(){return P(-y,x);}
   // 向量与 x 轴的夹角，取值范围（ -，pi pi]
   db arg() const {return atan2(y,x);}
};
T norm(P a){return a*a;}
T abs(P a) {return sqrtl(norm(a));}
// For given three points a,b,p, find the projection point x of p onto ab.
P proj(P p,P a,P b){return (b-a)*((p-a)*(b-a)/norm(b-a))+a;}
// For given three points a,b,p, find the reflection point x of p onto ab.
P reflect(P p,P a,P b){return proj(p,a,b)*2-p;}
T cross(P o,P a,P b){return (a-o)/(b-o);}
int crossOp(P o,P a,P b){return sgn(cross(o,a,b));}
// 向量夹角
db rad(P p1,P p2){return atan2l(p1/p2,p1*p2);}
bool onPS(P p,P s,P t){return sgn((t-s)/(p-s))==0&&sgn((p-s)*(p-t))<=0;}
bool order(const P&a,const P&b){ return a.arg() < b.arg();}
// 向量逆时针旋转 rad （弧度，精度可能不太够）
P rot(P a, T rad) {
    return P(a.x * cos(rad) - a.y * sin(rad), a.x * sin(rad) + a.y * cos(rad));
}
P rot(P a, P o, T rad) {
    return rot(a - o, rad) + o;
}
```

```
struct L{ P s,t;L(){} L(P s,P t):s(s),t(t){}};
P insLL(L a,L b){ // line x line
   P s = a.s - b.s , v = a.t - a.s , w = b.t - b.s;
   db k1 = s / w , k2 = w / v;
   if(sgn(k2) == 0) return abs(b.s - a.s) < abs(b.t - a.s) ? b.s : b.t;
   return a.s + v * (k1 / k2);
}
// 判断点是否在线段上（不包括端点）
bool onS0(P p, P a, P b) {
    return sgn((p - a) / (b - a)) == 0 && sgn((p - a) * (p - b)) < 0;
}
// 判断点是否在线段上（包括端点）
bool onS1(P p, P a, P b) {
    return sgn((p - a) / (b - a)) == 0 && sgn((p - a) * (p - b)) <= 0;
}
bool isSSr(const L&a,const L&b){ // seg x seg restrict
   T c1=(a.t-a.s)/(b.s-a.s) , c2=(a.t-a.s)/(b.t-a.s),
     c3=(b.t-b.s)/(a.s-b.s) , c4=(b.t-b.s)/(a.t-b.s);
   return sgn(c1) * sgn(c2) < 0 && sgn(c3) * sgn(c4) < 0;
}
bool isSS(L a,L b){ // seg x seg , replace x->y to accelerate
   T c1=(a.t-a.s)/(b.s-a.s),c2=(a.t-a.s)/(b.t-a.s);
   T c3=(b.t-b.s)/(a.s-b.s),c4=(b.t-b.s)/(a.t-b.s);
   return sgn(c1) * sgn(c2) <= 0 && sgn(c3) * sgn(c4) <= 0 &&
      sgn(max(a.s.x,a.t.x) - min(b.s.x,b.t.x)) >= 0 &&
      sgn(max(b.s.x,b.t.x) - min(a.s.x,a.t.x)) >= 0 &&
      sgn(max(a.s.y,a.t.y) - min(b.s.y,b.t.y)) >= 0 &&
      sgn(max(b.s.y,b.t.y) - min(a.s.y,a.t.y)) >= 0;
}
// 判断直线线段是否相交（端点也算）
bool isLS(P a1, P a2, P b1, P b2) {
    T c1 = (a2 - a1) / (b1 - a1), c2 = (a2 - a1) / (b2 - a1);
    return sgn(c1) * sgn(c2) <= 0;
}
bool inRegion(T a,T p,T b) {return sgn(a-p)==0||sgn(b-p)==0||(a<p!=b<p);}
bool inRec(P p,L a){ // p in Rectangle
   return inRegion(a.s.x,p.x,a.t.x) && inRegion(a.s.y,p.y,a.t.y);
}
db disPL(P p,L a){return fabs((a.t-a.s)/(p-a.s)) / abs(a.t-a.s);}
db disPS(P p,L a){ // p x seg dis
   if(sgn((a.t-a.s)*(p-a.s)) == -1) return abs(p-a.s);
   if(sgn((a.s-a.t)*(p-a.t)) == -1) return abs(p-a.t);
   return disPL(p,a);
}
db disSS(L a,L b){ // seg x seg dis
   if(isSS(a,b)) return 0;
   return min(min(disPS(a.s,b),disPS(a.t,b)),min(disPS(b.s,a),disPS(b.t,a)));
}
// 直线两点式转一般式
// 直线的一般式： Ax+By+C=0
void getLABC(P a, P b, T &A, T &B, T &C) {
    A = a.y - b.y;
   B = b.x - a.x;
   C = a / b;
}
```

```
typedef vector<P> polygon;
polygon convex(polygon A){ // counter-clockwise , < : <=180 , <= : <180
   int n=sz(A),m=0;
   polygon B;B.resize(n<<1);
   sort(all(A));
   rep(i,0,n){
      while(m > 1 && sgn((B[m-1]-B[m-2])/(A[i]-B[m-2]))<=0) --m;
      B[m++]=A[i];
   }
   int k = m;
   per(i,0,n-1){
      while(m > k && sgn((B[m-1]-B[m-2])/(A[i]-B[m-2]))<=0) --m;
      B[m++]=A[i];
   }
   B.resize(m);
   if(sz(B) > 1) B.pop_back();
   return B;
}
T area(polygon A) { // multiple 2 with integer type
   T res=0;
   rep(i,0,sz(A)) res+=A[i]/(A[(i+1)%sz(A)]);
   return fabs(res) / 2;
}
bool isconvex(polygon A){ // counter-clockwise
   bool ok=1;int n=sz(A);
   rep(i,0,2) A.pb(A[i]);
   rep(i,0,n) ok&=((A[i+1]-A[i])/(A[i+2]-A[i]))>=0;
   return ok;
}
int inPpolygon(P p,polygon A){ // -1 : on , 0 : out , 1 : in
   int res=0;
   rep(i,0,sz(A)){
      P u=A[i],v=A[(i+1)%sz(A)];
      if(onPS(p,u,v)) return -1;
      T cross = sgn((v-u)/(p-u)) , d1 = sgn(u.y-p.y) , d2 = sgn(v.y-p.y);
      if(cross > 0 && d1 <= 0 && d2 > 0) ++res;
      if(cross < 0 && d2 <= 0 && d1 > 0) --res;
   }
   return res != 0;
}
T diameter(polygon A) { // longest distance
   int n=sz(A);if(n <= 1) return 0;
   int l=0,r=0;rep(i,1,n) (A[i]<A[l])&&(l=i),(A[r]<A[i])&&(r=i);
   db res=abs(A[l]-A[r]);int i=l,j=r;
   do (++((A[(i+1)%n]-A[i])/(A[(j+1)%n]-A[j])>=0?j:i))%=n,
      res=max(res,abs(A[i]-A[j]));
   while(i!=l||j!=r);
   return res;
}
polygon convexCut(polygon A,P s,P t){ // counter-clockwise , left hand of st
   int n=sz(A);
   polygon B;
   rep(i,0,n){
      P u=A[i],v=A[(i+1)%n];
      int d1 = sgn((t-s)/(u-s)) , d2 = sgn((t-s)/(v-s));
```

```
      if(d1 >= 0) B.pb(u);
      if(d1 * d2 < 0) B.pb(insLL(L(u,v),L(s,t)));
   }
   return B;
}
// sz(A) <= 100,000
namespace NearestPoints{
   T solve(int l,int r,vector<P>&p){
      if(l == r) return 1e100;
      int m=(l+r)>>1;
      T Xm = p[m].x , lim = min(solve(l,m,p) , solve(m+1,r,p));
      inplace_merge(p.begin()+l,p.begin()+m+1,p.begin()+r+1,[&](P a,P b){return a.y<b.y
      ;});
      vector<P> V;
      rep(i,l,r+1) if(fabs(p[i].x - Xm) <= lim) V.pb(p[i]);
      rep(i,0,sz(V)) rep(j,i+1,sz(V)){
         if(fabs(V[j].y - V[i].y) >= lim) break;
         T dis = abs(V[i]-V[j]);
         lim = min(lim,dis);
      }
      return lim;
   }
   T solve(vector<P> A){
      sort(all(A),[&](P a,P b){return a.x<b.x;});
      return solve(0,sz(A)-1,A);
   }
}
struct C{
   P o;T r;C(){} C(P o,T r):o(o),r(r){}
   bool operator == (const C&b) const {return o==b.o&&sgn(r-b.r)==0;}
   // 通过圆心角（弧度）求圆上坐标
   P point(T rad) {return P(o.x + cos(rad) * r, o.y + sin(rad) * r);}
};
// 注意相等关系
// 相离4: 外切3: 相交2: 内切1: 内含0:
int relCC(C A,C B){
   T dis = abs(A.o - B.o);
   if(sgn(dis - (A.r + B.r)) == 1) return 4;
   if(sgn(dis - (A.r + B.r)) == 0) return 3;
   if(sgn(dis - fabs(A.r - B.r)) == 1) return 2;
   if(sgn(dis - fabs(A.r - B.r)) == 0) return 1;
   return 0;
}
vector<P> insCL(C c,L a){
   db x = (a.s-c.o)*(a.t-a.s) , y = norm(a.t-a.s);
   db d = x * x - y * (norm(a.s-c.o) - c.r*c.r);
   vector<P> res;
   if(sgn(d) < 0) return res;
   d = max(d,0.);
   P mid = a.s - (a.t - a.s) * (x / y);
   P del = (a.t - a.s) * (sqrt(d) / y);
   return {mid - del,mid + del}; // dir : a.s -> a.t
}
vector<P> insCC(C a,C b){
   vector<P> res;
   T x = norm(a.o - b.o);
   if(sgn(x)==0) return res;
   T  y = ((a.r * a.r - b.r * b.r) / x + 1) / 2 ,
      d = a.r * a.r / x - y * y;
   if(sgn(d) < 0) return res;
   d = max(d,0.);
   P mid = (b.o - a.o) * y + a.o ,
     del = ((b.o - a.o) * sqrt(d)).rot90();
   return {mid - del , mid + del};// counter-clockwise along a
}
vector<P> tanCP(C c,P p){
   db x = norm(p - c.o) , d = x - c.r * c.r;
   vector<P> res;
   if(sgn(d) < 0) return res;
   d = max(d,0.);
   P mid = c.o + (p - c.o) * (c.r * c.r / x) ,
     del = ((p-c.o)*(c.r*sqrt(d)/x)).rot90();
   return {mid - del ,mid + del}; // counter-clockwise
}
vector<pair<P,P> > tanCC(C c1,C c2){// need to unique
   vector<pair<P,P> > res;
   // extan
   if(!sgn(c1.r-c2.r)){
      P dir = c2.o-c1.o;
      dir = (dir*(c1.r/abs(dir))).rot90();
      res.pb({c1.o+dir,c2.o+dir});
      res.pb({c1.o-dir,c2.o-dir});
   } else {
      P p = (c2.o * c1.r - c1.o * c2.r) / (c1.r - c2.r);
      vector<P> ps = tanCP(c1 , p) , qs = tanCP(c2 , p);
      rep(i,0,min(sz(ps),sz(qs))) res.pb({ps[i],qs[i]});
   }
   // intan
   P p = (c1.o * c2.r + c2.o * c1.r) / (c1.r + c2.r);
   vector<P> ps = tanCP(c1 , p) , qs = tanCP(c2 , p);
   rep(i,0,min(sz(ps),sz(qs))) res.pb({ps[i],qs[i]});
   return res;
}
db areaCT(db r,P s,P t) { // need divide 2, maybe less than 0
   vector<P> p = insCL(C(P(0,0),r),L(s,t));
   if(!sz(p)) return r*r*rad(s,t);
   bool b1 = sgn(norm(s)-r*r) == 1 , b2 = sgn(norm(t)-r*r) == 1;
   if(b1 && b2) {
      if(sgn((s-p[0])*(t-p[0])) <= 0 && sgn((s-p[1])*(t-p[1])) <= 0)
         return r*r*(rad(s,p[0]) + rad(p[1],t)) + (p[0]/p[1]);
      else return r*r*rad(s,t);
   } else if(b1) return r*r*rad(s,p[0])+(p[0]/t);
   else if(b2) return r*r*rad(p[1],t)+(s/p[1]);
   return (s/t);
}
db areaCPoly(db r, polygon A) { // need divide 2, counter-clockwise
   db ans = 0;
   rep(i, 0, sz(A)) ans += areaCT(r, A[i], A[(i + 1) % sz(A)]);
   return ans;
}
```

```
P inC(P A,P B,P C){
   db a = abs(B - C) , b = abs(C - A) , c = abs(A - B);
   return (A * a + B * b + C * c) / (a + b + c);
}
P outC(P A,P B,P C){
   P b = B - A , c = C - A;
   db dB = norm(b) , dC = norm(c) , d = b / c * 2;
   return A - P(b.y * dC - c.y * dB , c.x * dB - b.x * dC) / d;
}
P othroC(P A,P B,P C){
   P b = B - A , c = C - A;
   db Y = b.y * c.y * (B - C).y,
       a = c / b,
       xx = (Y + c.x * b.y * B.x - b.x * c.y * C.x) / a,
       yy = -b.x * (xx - C.x) / b.y + c.y;
   return P(xx , yy);
}
C Mincir(P *p,int n){
   random_shuffle(p , p + n);
   P o = p[0];db r = 0;
   rep(i,1,n) {
      if(sgn(abs(o-p[i])-r) <= 0) continue;
      o = p[i] , r = 0;
      rep(j,0,i) {
         if(sgn(abs(o-p[j])-r) <= 0) continue;
         o = (p[i] + p[j]) / 2 , r = abs(o-p[j]);
         rep(k,0,j) {
            if(sgn(abs(o-p[k])-r) <= 0) continue;
            o = outC(p[i],p[j],p[k]) , r = abs(o-p[k]);
         }}}
   return C(o,r);
}
namespace CircleIntersection{
   struct E{
      P p;T ang;int delta;
      E(){} E(P p,T ang,int delta):p(p),ang(ang),delta(delta){}
      bool operator < (const E&b) const {return ang<b.ang;}
   };
   bool overlap(C a,C b) {return sgn(a.r-b.r-abs(a.o-b.o))>=0;}
   void solve(C *c,int n,T *ans) {
      memset(ans , 0 , sizeof(T) * (n + 1));
      rep(i,0,n) {
         int cnt=1;
         vector<E> evt;
         rep(j,0,i) if(c[i]==c[j]) cnt++;
         rep(j,0,n) if(j!=i&&!(c[i]==c[j])&&overlap(c[j],c[i])) cnt++;
         rep(j,0,n) if(j!=i){
            vector<P> pts=insCC(c[i],c[j]);
            if(sz(pts)) {
               T a[2];
               rep(j,0,2) a[j]=(pts[j]-c[i].o).arg();
               evt.pb(E(pts[0],a[0],1));
               evt.pb(E(pts[1],a[1],-1));
               cnt += a[0] > a[1];
            }
         }
         if(!sz(evt)) ans[cnt] += pi*c[i].r*c[i].r;
         else{
            sort(all(evt));
            evt.pb(evt.front());
            rep(j,0,sz(evt)-1) {
               cnt+=evt[j].delta;
               ans[cnt] += evt[j].p / evt[j+1].p / 2;
               db ang = evt[j + 1].ang - evt[j].ang;
               if(ang < 0) ang += pi * 2;
               ans[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r / 2;
            }}}}
namespace ConvecIntersection{
   const int N = 1005;
   struct Rec {
      P d[10];int dn;// d[dn] = d[0]
      P operator [] (const int&n) {return d[n];}
   }r[N];
   typedef pair<db,int> pdi;
   int n;pdi res[1000005];
   db getLoc(P a,P b,P p){
      if(sgn(b.x - a.x)) return (p.x - a.x) / (b.x - a.x);
      return (p.y - a.y) / (b.y - a.y);
   }
   db work() {
      db rt=0;
      rep(i,0,n) rep(j,0,r[i].dn){
         int sz=0;
         res[sz++] = pdi(0,0);res[sz++] = pdi(1,0);
         rep(t,0,n) {
            if(t == i) continue;
            rep(g,0,r[t].dn) {
               int du = sgn((r[i][j+1] - r[i][j]) / (r[t][g] - r[i][j]));
               int dv = sgn((r[i][j+1] - r[i][j]) / (r[t][g+1] - r[i][j]));
               if(!du && !dv) {
                  if(sgn((r[i][j+1] - r[i][j]) * (r[t][g+1] - r[t][g])) < 0 || i < t){
                     res[sz++] = pdi(getLoc(r[i][j] , r[i][j+1] , r[t][g]) , 1);
                     res[sz++] = pdi(getLoc(r[i][j] , r[i][j+1] , r[t][g+1]) , -1);
                  }} else {
                     db s1 = (r[i][j] - r[t][g]) / (r[t][g+1] - r[t][g]);
                     db s2 = (r[t][g+1] - r[t][g]) / (r[i][j+1] - r[t][g]);
                     if(du >= 0 && dv < 0) res[sz++] = pdi(s1 / (s1 + s2) , 1);
                     else if(du < 0 && dv >= 0) res[sz++] = pdi(s1 / (s1 + s2) , -1);
                  }}}
         sort(res , res + sz);
         int cnt = 0; --sz;
         rep(t,0,sz) {
            cnt += res[t].se;
            if(cnt == 0 && sgn(res[t].fi - res[t+1].fi)) {
               db a = res[t].fi;
               if(a < 0) a = 0; if(a > 1) break;
               db b = res[t+1].fi;
               if(b < 0) continue; if(b > 1) b = 1;
               rt += ((r[i][j+1] - r[i][j]) * a + r[i][j]) / ((r[i][j+1]-r[i][j]) * b +
               r[i][j]);
```

```
            }}}
      return rt / 2;}}
```

4.3 3. GeoAdd

```
/*
 * 平面图欧拉定理：V + F − E = 2
 */
 bool cmp(const pii &a, const pii &b) { // 级角排序
   int o = a > pii(0, 0), t = b > pii(0, 0);
   if(o != t) return o < t;
   return det(a, b) > 0;
}
bool isSSr(const L &a, const L &b){ // 线段规范相交
   db c1 = det(a.t − a.s, b.s − a.s), c2 = det(a.t − a.s, b.t − a.s),
       c3 = det(b.t − b.s, a.s − b.s), c4 = det(b.t − b.s, a.t − b.s);
   return sign(c1) * sign(c2) < 0 && sign(c3) * sign(c4) < 0;
}
bool isSS(L a,L b){ // 线段不规范相交
   db c1 = det(a.t − a.s, b.s − a.s), c2 = det(a.t − a.s, b.t − a.s),
       c3 = det(b.t − b.s, a.s − b.s), c4 = det(b.t − b.s, a.t − b.s);
   return sign(c1) * sign(c2) <= 0 && sign(c3) * sign(c4) <= 0 &&
      sign(max(a.s.x, a.t.x) − min(b.s.x, b.t.x)) >= 0 &&
      sign(max(b.s.x, b.t.x) − min(a.s.x, a.t.x)) >= 0 &&
      sign(max(a.s.y, a.t.y) − min(b.s.y, b.t.y)) >= 0 &&
      sign(max(b.s.y, b.t.y) − min(a.s.y, a.t.y)) >= 0;
}
db disSS(L a, L b){ // 线段到线段距离
   if(isSS(a, b)) return 0;
   return min(min(disToSeg(b, a.s), disToSeg(b, a.t)), min(disToSeg(a, b.s), disToSeg(a,
    b.t)));
}
// 判断直线线段是否相交（端点也算）
bool isLS(P a1, P a2, P b1, P b2) {
    db c1 = det(a2 − a1, b1 − a1), c2 = det(a2 − a1, b2 − a1);
    return sign(c1) * sign(c2) <= 0;
}
P outC(P A, P B, P C) { // 外心
   P b = B − A, c = C − A;
   db dB = b.len2(), dC = c.len2(), d = 2 * det(b, c);
   return A − P(b.y * dC − c.y * dB, c.x * dB − b.x * dC) / d;
}
bool isconvex(vector<P> A) { // 判断是否是凸包逆时针
   bool ok = 1;
   int n = sz(A);
   rep(i, 0, 2) A.pb(A[i]);
   rep(i, 0, n) ok &= det(A[i + 1] − A[i], A[i + 2] − A[i]) >= 0;
   return ok;
}
db diameter(vector<P> A) { // 求凸包最远点对
   int n = sz(A);
   if(n <= 1) return 0;
   int l = 0, r = 0;
   rep(i, 1, n) (A[i] < A[l]) && (l = i), (A[r] < A[i]) && (r = i);
   db res = (A[l]−A[r]).len();
   int i = l, j = r;
   do (++(det(A[(i + 1) % n]− A[i], A[(j + 1) % n] − A[j]) >= 0 ? j : i)) %= n,
      res = max(res, (A[i] − A[j]).len());
   while(i != l || j != r);
   return res;
}
// sz(A) <= 100,000
namespace NearestPoints { // 点集中最近点对
   db solve(int l, int r, vector<P> &p) {
      if(l == r) return 1e100;
      int m = l + r >> 1;
      db Xm = p[m].x, lim = min(solve(l, m, p), solve(m + 1, r, p));
      inplace_merge(p.begin() + l, p.begin() + m + 1, p.begin() + r + 1, [&](P a, P b){
      return a.y < b.y;});
      vector<P> V;
      rep(i, l, r + 1) if(fabs(p[i].x − Xm) <= lim) V.pb(p[i]);
      rep(i, 0, sz(V)) rep(j, i + 1, sz(V)) {
         if(fabs(V[j].y − V[i].y) >= lim) break;
         T dis = (V[i] − V[j]).len();
         lim = min(lim, dis);
      }
      return lim;
   }
   db solve(vector<P> A) {
      sort(all(A), [&](P a, P b){return a.x < b.x;});
      return solve(0, sz(A) − 1, A);
   }
}
// 注意相等关系
// 相离4: 外切3: 相交2: 内切1: 内含0:
int relCC(C A, C B) { // 两圆关系
   db dis = (A.o − B.o).len();
   if(sign(dis − (A.r + B.r)) == 1) return 4;
   if(sign(dis − (A.r + B.r)) == 0) return 3;
   if(sign(dis − fabs(A.r − B.r)) == 1) return 2;
   if(sign(dis − fabs(A.r − B.r)) == 0) return 1;
   return 0;
}
vector<P> tanCC(const C &c1, const C &c2) { // 求圆与圆的切点
   vector<P> res;
   db dis = (c1.o − c2.o).len();
   if(sign(dis − (c1.r + c2.r)) == 0) {
      res.pb(c1.o + (c2.o − c1.o) * c1.r / (c1.r + c2.r));
   }
   if(sign(dis − fabs(c1.r − c2.r) == 0)) {
      res.pb(c1.o + (c2.o − c1.o) * c1.r / (c1.r − c2.r));
   }
   return res;
}
db rad(P p1, P p2) { return atan2l(det(p1, p2), dot(p1, p2)); } // p1 与 p2 的夹角，有方
向
db areaCT(db r,P s,P t) { // 求圆与三角形交面积，需要除2
   P p1, p2;
   bool f = isCL(C(P(0, 0), r), L(s, t), p1, p2);
   if(!f) return r * r * rad(s, t);
```

```
   bool b1 = sign(s.len2() - r * r) == 1 , b2 = sign(t.len2() - r * r) == 1;
   if(b1 && b2) {
      if(sign(dot(s - p1, t - p1)) <= 0 && sign(dot(s - p2, t - p2) <= 0))
         return r * r * (rad(s, p1) + rad(p2, t)) + det(p1, p2);
      else return r * r * rad(s, t);
   } else if(b1) return r * r * rad(s, p1) + det(p1, t);
   else if(b2) return r * r * rad(p2, t) + det(s, p2);
   return det(s, t);
}
db areaCPoly(C c, vector<P> p) { // 求圆与多边形交面积
   int n = sz(p);
   db ans = 0;
   rep(i, 0, n) {
      P u = p[i], v = p[(i + 1) % n];
      ans += areaCT(c.r, u - c.o, v - c.o);
   }
   return fabs(ans) / 2;
}
C Mincir(P *p,int n){ // ? 最小圆覆盖
   random_shuffle(p , p + n);
   P o = p[0];db r = 0;
   rep(i,1,n) {
      if(sgn(abs(o-p[i])-r) <= 0) continue;
      o = p[i] , r = 0;
      rep(j,0,i) {
         if(sgn(abs(o-p[j])-r) <= 0) continue;
         o = (p[i] + p[j]) / 2 , r = abs(o-p[j]);
         rep(k,0,j) {
            if(sgn(abs(o-p[k])-r) <= 0) continue;
            o = outC(p[i],p[j],p[k]) , r = abs(o-p[k]);
         }}}
   return C(o,r);
}
namespace CircleIntersection{ // ?
   struct E{
      P p;T ang;int delta;
      E(){} E(P p,T ang,int delta):p(p),ang(ang),delta(delta){}
      bool operator < (const E&b) const {return ang<b.ang;}
   };
   bool overlap(C a,C b) {return sgn(a.r-b.r-abs(a.o-b.o))>=0;}
   void solve(C *c,int n,T *ans) {
      memset(ans , 0 , sizeof(T) * (n + 1));
      rep(i,0,n) {
         int cnt=1;
         vector<E> evt;
         rep(j,0,i) if(c[i]==c[j]) cnt++;
         rep(j,0,n) if(j!=i&&!(c[i]==c[j])&&overlap(c[j],c[i])) cnt++;
         rep(j,0,n) if(j!=i){
            vector<P> pts=insCC(c[i],c[j]);
            if(sz(pts)) {
               T a[2];
               rep(j,0,2) a[j]=(pts[j]-c[i].o).arg();
               evt.pb(E(pts[0],a[0],1));
               evt.pb(E(pts[1],a[1],-1));
               cnt += a[0] > a[1];
            }
         }
         if(!sz(evt)) ans[cnt] += pi*c[i].r*c[i].r;
         else{
            sort(all(evt));
            evt.pb(evt.front());
            rep(j,0,sz(evt)-1) {
               cnt+=evt[j].delta;
               ans[cnt] += evt[j].p / evt[j+1].p / 2;
               db ang = evt[j + 1].ang - evt[j].ang;
               if(ang < 0) ang += pi * 2;
               ans[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r / 2;
            }}}}
namespace ConvecIntersection{ // ?
   const int N = 1005;
   struct Rec {
      P d[10];int dn;// d[dn] = d[0]
      P operator [] (const int&n) {return d[n];}
   }r[N];
   typedef pair<db,int> pdi;
   int n;pdi res[1000005];
   db getLoc(P a,P b,P p){
      if(sgn(b.x - a.x)) return (p.x - a.x) / (b.x - a.x);
      return (p.y - a.y) / (b.y - a.y);
   }
   db work() {
      db rt=0;
      rep(i,0,n) rep(j,0,r[i].dn){
         int sz=0;
         res[sz++] = pdi(0,0);res[sz++] = pdi(1,0);
         rep(t,0,n) {
            if(t == i) continue;
            rep(g,0,r[t].dn) {
               int du = sgn((r[i][j+1] - r[i][j]) / (r[t][g] - r[i][j]));
               int dv = sgn((r[i][j+1] - r[i][j]) / (r[t][g+1] - r[i][j]));
               if(!du && !dv) {
                  if(sgn((r[i][j+1] - r[i][j]) * (r[t][g+1] - r[t][g])) < 0 || i < t){
                     res[sz++] = pdi(getLoc(r[i][j] , r[i][j+1] , r[t][g]) , 1);
                     res[sz++] = pdi(getLoc(r[i][j] , r[i][j+1] , r[t][g+1]) , -1);
                  }} else {
                     db s1 = (r[i][j] - r[t][g]) / (r[t][g+1] - r[t][g]);
                     db s2 = (r[t][g+1] - r[t][g]) / (r[i][j+1] - r[t][g]);
                     if(du >= 0 && dv < 0) res[sz++] = pdi(s1 / (s1 + s2) , 1);
                     else if(du < 0 && dv >= 0) res[sz++] = pdi(s1 / (s1 + s2) , -1);
                  }}}
         sort(res , res + sz);
         int cnt = 0; --sz;
         rep(t,0,sz) {
            cnt += res[t].se;
            if(cnt == 0 && sgn(res[t].fi - res[t+1].fi)) {
               db a = res[t].fi;
               if(a < 0) a = 0; if(a > 1) break;
               db b = res[t+1].fi;
               if(b < 0) continue; if(b > 1) b = 1;
```

```
            rt += ((r[i][j+1] - r[i][j]) * a + r[i][j]) / ((r[i][j+1]-r[i][j]) * b +
            r[i][j]);
        }}}
    return rt / 2;}}
```

4.4 MaxAreaTri

```
// O(n ^ 2)
void maxAreaTri(P *p, int n, P &a, P &b, P &c) {
   int i = 0, j = 1, k = 2;
   a = p[i], b = p[j], c = p[k];
   T res = area(a, b, c), cur = res, tmp;
   do {
      while(1) {
         while(cur <= (tmp = area(p[i], p[j], p[(k + 1) % n]))) (++k) %= n, cur = tmp;
         if(cur <= (tmp = area(p[i], p[(j + 1) % n], p[k]))) (++j) %= n, cur = tmp;
         else break;
      }
      if(cur > res) a = p[i], b = p[j], c = p[k], res = cur;
      (++i) %= n;
      if(i == j) (++j) %= n;
      if(j == k) (++k) %= n;
      cur = area(p[i], p[j], p[k]);
   } while(i);
}
```

5 Graph

5.1 1. DCC

```
// cactus: n multi by 2
// key is cuts
// dcc i->j , i(points) , j(bcc_block)
// st is stack
// _st is top of stack
// _ is number of dcc
// can handle isolate point and not connected graph and muti edge
// can handle self circle ?
namespace DCC{
    const int N = 202020;
    vi key , dcc[N];
    int dfn[N] , low[N] , st[N] , _st , _;
    void dfs(int c,int dep,const vi g[]){
        int cc=0,out=1<dep;st[_st++]=c;
        dfn[c]=low[c]=dep;
        for(auto t:g[c])
            if(!dfn[t]){
                dfs(t,dep+1,g);
                low[c]=min(low[c],low[t]);
                if(low[t]>=dfn[c]){
                    if(++out==2) key.pb(c);
                    while(st[--_st]!=t) dcc[st[_st]].pb(_);
                    dcc[c].pb(_);dcc[t].pb(_++);
                }
            } else if(dfn[t] != dfn[c] - 1 || cc++)
                low[c] = min(low[c] , dfn[t]);
    }
    int solve(int n,const vi g[]){// n is size of points
        fill_n(dfn,n,_=0);
        fill_n(low,n,_st=0);
        fill_n(dcc,n,key=vi());
        rep(i,0,n) if(!dfn[i]) dfs(i,1,g);
        rep(i,0,n) if(sz(dcc[i]) == 0) dcc[i].pb(_++);
        return _;
    }
}
```

5.2 2. BCC

```
// key contains the id of edges
// _ starts from 0
namespace BCC{
    const int N = 202020;
    vi key , bcc[N];
    int dfn[N] , low[N] , id[N] , st[N] , _st , _;
    void dfs(int c,int dep,vector<pii> g[]){
        int cc=0;st[_st++]=c;
        dfn[c]=low[c]=dep;
        for(auto e:g[c]){
            int t=e.fi;
            if(!dfn[t]){
                dfs(t,dep+1,g);
                low[c]=min(low[c],low[t]);
                if(low[t]>dfn[c]) key.pb(e.se);
            } else if(dfn[t] != dfn[c] - 1 || cc++)
                low[c] = min(low[c] , dfn[t]);
        }
        if(low[c]==dfn[c]){
            do{id[st[--_st]]=_;}while(st[_st]!=c);
            _++;
        }
    }
    int solve(int n,vector<pii> g[]){
        fill_n(dfn,n,_=0);
        fill_n(low,n,_st=0);
        fill_n(bcc,n,key=vi());
        rep(i,0,n) if(!dfn[i]) dfs(i,1,g);
        rep(i,0,n) for(auto j:g[i]) if(id[i]!=id[j.fi])
            bcc[id[i]].pb(id[j.fi]);
        return _;
    }
};
```

5.3 3. SCC

```
// _ starts from 0
namespace SCC{
```

```
    const int N = 100050;
    int dfn[N],low[N],id[N],st[N],_st,_,cc;
    void dfs(int c,vi g[]){
        dfn[c]=low[c]=++cc;
        st[_st++]=c;
        for(auto t:g[c])
            if(!dfn[t])
                dfs(t,g),low[c]=min(low[c],low[t]);
            else if(!id[t])
                low[c] =min(low[c],dfn[t]);
        if(low[c]==dfn[c]){
            ++_;
            do{id[st[--_st]]=_;}while(st[_st]!=c);
        }
    }
    vi ng[N];
    int solve(int n,vi g[]){
        fill_n(dfn,n,cc=0);
        fill_n(low,n,_st=0);
        fill_n(id,n,_=0);
        rep(i,0,n) if(!dfn[i]) dfs(i,g);
        rep(i,0,n) --id[i];
        fill_n(ng,_,vi());
        rep(i,0,n) for(auto j:g[i]) if(id[i]!=id[j]) ng[id[i]].pb(id[j]);
        return _;
    }
}
```

5.4 4. MaxMatch

```
namespace MaxMatch{
    const int N = 5050;
    int link[N],vis[N];
    int dfs(int c,vi g[]){
        for(auto t : g[c])
            if(!vis[t]){
                vis[t] = true;
                if(link[t]==-1||dfs(link[t],g))
                    return link[t]=c,1;
            }
        return 0;
    }
    int solve(int n,int m,vi g[]){
        fill_n(link,m,-1);
        int ret=0;
        rep(i,0,n){
            memset(vis,0,m*sizeof(int));
            ret += dfs(i,g);
        }
        return ret;
    }
}
```

5.5 5. KM

```
/*
 * 输入保证左边点数 <= 右边点数
 */
// init!! , id starts from 0
template<class T>
struct KM {
    static const int N = 505;
    static const T inf = ~0U>>2;
    int n, m, left[N], pre[N], used[N];
    T g[N][N], Lx[N], Ly[N], slack[N];
    void ini(int _n, int _m) {
        n = _n , m = _m;
        rep(i,0,n) rep(j,0,m) g[i][j] = -inf;
    }
    void go(int now) {
        rep(i,0,m+1) used[i]=0,slack[i]=inf;
        left[m] = now;int u,v;
        for(u=m;~left[u];u=v){
            used[u] = 1;
            T d = inf;
            rep(i,0,m) if(!used[i]){
                T tmp = Lx[left[u]] + Ly[i] - g[left[u]][i];
                if(tmp < slack[i]) slack[i] = tmp, pre[i] = u;
                if(slack[i] < d) d = slack[v=i];
            }
            rep(i,0,m+1) if(used[i]) Lx[left[i]] -= d , Ly[i] += d;
                else slack[i] -= d;
        }
        for(;u!=m;left[u]=left[pre[u]],u=pre[u]);
    }
    T run() {
        fill_n(Lx,n,0);fill_n(Ly,m,0);
        fill_n(left,m,-1);
        rep(i,0,n) go(i);
        T ans = 0;
        rep(i,0,n) ans += Lx[i];
        rep(i,0,m) ans += Ly[i];
        return ans;
    }
};
```

5.6 6. 生成树计数与欧拉回路方案数

```
// d[][]:
//     i!=j d[i][j]=0
//     i==j d[i][j]=in_deg(i)
// b[][]:
//     from i to j has b[i][j] directed edges
// a[][] = d[][] - b[][]

// 无向图生成树个数： a[][] 任何一个 n-1 阶主子式的绝对值
// 有向图以 i 为根的生成树个数： a[][] 去掉第 i 行第 i 列的行列式的绝对值

int det(int n) { // det(a[1..n-1][1..n-1])
```

```
   int ans=1;
   rep(i, 1, n) {
      rep(j, i+1, n) while(a[j][i]) {
         int t = a[i][i] / a[j][i];
         rep(k, i, n) a[i][k] = sub(a[i][k], mul(a[j][k], t)), swap(a[i][k], a[j][k]);
         ans = P - ans;
      }
      if(a[i][i] == 0) return 0;
      ans = mul(ans, a[i][i]);
   }
   return ans;
}

// 有向图要记得判断每个点的出度入度是否相等
// 无向图需要转换成有向图
// tw(G): 以 w 为根的生成树个数
// ec(G) = tw(G) * pi((deg[v] - 1)!)
// ans = ec(G) * deg[w]; 如果求的不是本质不同的，就还需要这个
// 本质相同：    1231341 1341231
// 本质不同：    1231341 1312341
```

5.7 7. Dijkstra

```
int n, dis[N];
void Dijkstra(int st) {
   priority_queue<pii> q;
   fill_n(dis + 1, n, inf);
   dis[st] = 0;
   q.push(mp(0, st));
   while(!q.empty()) {
      pii u = q.top();q.pop();
      if(dis[u.se] != -u.fi) continue;
      for(auto v : g[u.se]) {
         if(dis[v.fi] > dis[u.se] + v.se) {
            dis[v.fi] = dis[u.se] + v.se;
            q.push(mp(-dis[v.fi], v.fi));
         }
      }
   }
}
```

5.8 DualMST

对偶图最小生成树，等于平面图所有边边权和减去平面图最大生成树。

5.9 EulerianPath

```
vi ans;
bool vis[N];
vector<pii> g[N];

void dfs(int u) {
   for(auto v : g[u]) if(!vis[abs(v.se)]) {
      vis[abs(v.se)] = 1;
      dfs(v.fi);
      ans.pb(-v.se);
   }
}
```

5.10 MMST

```
// 曼哈顿最小距离生成树
// 这份代码处理的区域是 Y 轴右转 45 度
namespace MMST {
#define lb(x) ((x) & -(x))
   const int N = 101010, inf = 1e9 + 7;

   vector<pair<int, pii> > E;
   vi V;

   pii mi[N];
   void init() { rep(i, 1, sz(V) + 1) mi[i] = mp(inf, inf); }
   void upd(int p, pii c) {
      p = sz(V) + 1 - p;
      for( ; p <= sz(V); p += lb(p)) mi[p] = min(mi[p], c);
   }
   pii qry(int p) {
      p = sz(V) + 1 - p;
      pii ans = mp(inf, inf);
      for( ; p >= 1; p ^= lb(p)) ans = min(ans, mi[p]);
      return ans;
   }
   int F(int x) { return lower_bound(all(V), x) - V.begin() + 1; }
   void _solve(vector<pair<pii, int> > v) {
      V.clear();
      rep(i, 0, sz(v)) v[i].fi.se -= v[i].fi.fi, V.pb(v[i].fi.se);
      sort(all(V));
      V.erase(unique(all(V)), V.end());
      sort(all(v));
      reverse(all(v));
      init();
      for(auto u : v) {
         pii t = qry(F(u.fi.se));
         int s = u.fi.fi * 2 + u.fi.se;
         if(t.se != inf) E.pb(mp(t.fi - s, mp(t.se, u.se)));
         upd(F(u.fi.se), mp(s, u.se));
      }
   }
   void solve(vector<pair<pii, int> > v) {
      _solve(v);
      rep(i, 0, sz(v)) swap(v[i].fi.fi, v[i].fi.se);
      _solve(v);
      rep(i, 0, sz(v)) v[i].fi.fi *= -1;
      _solve(v);
      rep(i, 0, sz(v)) swap(v[i].fi.fi, v[i].fi.se);
      _solve(v);
   }
}
```

5.11 ManhattanDistance

```
(x, y) -> (x + y, x - y)            Manhattan distance -> Chebyshev distance
(x, y) -> (x + y >> 1, x - y >> 1)  Chebyshev distance -> Manhattan distance
```

6 Math

6.1 BerlekampMassey

```
// O(len^2)
vi BM(vi s) {
   vi C(1, 1), B(1, 1);
   int L = 0, m = 1, b = 1;
   rep(n, 0, sz(s)) {
      ll d = 0;
      rep(i, 0, L+1) (d += 1ll * C[i] * s[n-i]) %= P;
      if(d == 0) ++m;
      else {
         vi T = C;
         ll c = P - d * kpow(b, P - 2) % P;
         while(sz(C) < sz(B) + m) C.pb(0);
         rep(i, 0, sz(B)) C[i + m] = add(C[i + m], mul(c, B[i]));
         if(2 * L <= n) {
            L = n + 1 - L, B = T, b = d, m = 1;
         } else {
            ++m;
         }
      }
   }
   reverse(all(C));
   rep(i, 0, sz(C)) C[i] = P - C[i];
   return vi(C.begin(), C.end() - 1);
}
```

6.2 Fib

```
// sum(fib[1..n]) + 1=fib[n + 2]
// gcd(fib[n], fib[m]) = fib[gcd(n, m)]
```

6.3 GaussDB

```
namespace GaussDB{
   static const int N=210;
   double mat[N][N];//增广矩阵
   double x[N];//解集
   bool free_x[N];//标记是否是不确定的变元
   const double eps = 1e-7;
   int Gauss(int equ, int var){
      int k;
      int max_r, col;
      int free_index, free_num;
      memset(free_x, 1, sizeof(free_x));
      memset(x, 0, sizeof(x));
      for(k=col=0; k<equ&&col<var; ++k, ++col){
         max_r=k;
         rep(i, k+1, equ)
            if(fabs(mat[i][col])-mat[max_r][col]>eps) max_r=i;
         if(max_r!=k)
            rep(j, k, var+1)swap(mat[max_r][j], mat[k][j]);
         if(fabs(mat[k][col]<eps)){--k;continue;}
         rep(i, k+1, equ){
            if(fabs(mat[i][col])<=eps) continue;
            double tmp=mat[i][col]/mat[k][col];
            rep(j, col, var+1)
               mat[i][j]-=mat[k][j]*tmp;
         }

      }
      rep(i, k, equ)
         if(fabs(mat[i][var]>eps)) return 0;//无解
      if(k<var){
         for(int i=k-1; i>=0; --i){
            free_num=0;
            rep(j, 0, var){
               if(fabs(mat[i][j])>eps&&free_x[j]){
                  free_num+=1;
                  free_index=j;
               }
            }
            if(free_num>1) continue;
            double tmp=mat[i][var];
            rep(j, 0, var){
               if(j!=free_index&&fabs(mat[i][j])>eps)
                  tmp-=mat[i][j]*x[j];
            }
            free_x[free_index]=0;
            x[free_index]=tmp/mat[i][free_index];
         }
         return var-k;//自由变元个数
      }
      for(int i=var-1; i>=0; --i){
         double tmp=mat[i][var];
         rep(j, i+1, var){
            if(fabs(mat[i][j])>eps)
               tmp-=x[j]*mat[i][j];
         }
         x[i]=tmp/mat[i][i];
      }
      return 1;
   }
}
```

6.4 GaussInt

```
namespace Gauss{
   static const int N=210;
   int a[510][N];
   int kpow(int a, int b){
      int r=1;
      while(b>0){
         if(b&1)r=r*a%P;
         a=a*a%P;
         b>>=1;
      }
      return r;
   }
   int solve(int n, int m){//n=equ, m=var 同 Gaussxor
      int i=0, x=0;
      for(; i<n&&x<m; i++, x++){
         int r=i;
         while(r<n&&!a[r][x])r++;
         if(r>=n){
            i--;
            continue;
         }
         if(r!=i)
            rep(j, 0, m+1)swap(a[r][j], a[i][j]);
         int inv=kpow(a[i][x], P-2);
         for(int k=m; k>=x; k--)a[i][k]=a[i][k]*inv%P;
         rep(j, 0, n)
            if(i!=j&&a[j][x])
               for(int k=m; k>=x; k--)
                  a[j][k]=(a[j][k]-a[i][k]*a[j][x]%P+P)%P;
      }
      rep(k, i, n)if(a[k][m])return -1;
      return m-i;
   }
   void out(int n, int m){
      rep(i, 0, n){
         rep(j, 0, m)cout<<a[i][j]<<' ';
         cout<<endl;
      }
   }
};
```

6.5 GaussXor

```
//对 2 取模的 01 方程组
namespace Gause{
   static const int N=310;
   //有 equ 个方程， var 个变元。增广矩阵行数为 equ 列数为, [0..var]
   int equ,var;
   bitset<N> a[N]; //增广矩阵 modif
   int x[N]; //解集
   int free_x[N];//用来存储自由变元（多解枚举自由变元可以使用）
   int free_num;//自由变元的个数
   //返回值为 -1 表示无解，为 0 是唯一解，否则返回自由变元个数
   int Gauss(){
      int max_r,col,k;// k 为增广矩阵的秩
      free_num = 0;
      for(k=0, col=0; k<equ&&col<var; k++, col++){
         max_r = k;
         for(int i=k+1; i<equ; i++){
            if(abs(a[i][col])>abs(a[max_r][col]))
               max_r=i;
         }
         if(a[max_r][col]==0){
            k--;
            free_x[free_num++]=col;//这个是自由变元
            continue;
         }
         if(max_r!=k){
            swap(a[k],a[max_r]);
         }
         for(int i=k+1; i<equ; i++){
            if(a[i][col]!=0)
               a[i]^=a[k];
         }
      }
      for(int i=k; i<equ; i++)
         if(a[i][col]!=0)
            return -1;//无解
      if(k<var) return var-k;//自由变元个数
      //唯一解，回代
      for(int i=var-1; i>=0; i--){
         x[i]=a[i][var];
         for(int j=i+1; j<var; j++)
            x[i]^=(a[i][j]&&x[j]);
      }
      return 0;
   }
}
```

6.6 LinearBasis

```
struct Base{
    ll a[63];
    Base() {memset(a,0,sizeof(a));}
    void ins(ll x){
        for(int i=62;~i;--i) {
            if(x>>i&1) {
                if(a[i]) x^=a[i];
                else{ a[i]=x; break; }
            }
        }
    }
};
```

6.7 LinearRecursion

```
// a_{m} = \sum_{j=0}^{-m1}a_{j}*c_{j} O(m^2lgn)
int linear_recurrence(ll n, int m, vi a, vi c) {
   vector<ll> v(m, 0), u(m<<1, 0);
```

```
   v[0] = 1;
   for(ll x = 0, W = n ? 1ll<<(63 - __builtin_clzll(n)) : 0; W; W >>= 1, x <<= 1) {
      fill(all(u), 0);
      int b = !!(n & W); if(b) x++;
      if(x < m) u[x] = 1;
      else {
         rep(i, 0, m) rep(j, 0, m) (u[i + b + j] += v[i] * v[j]) %= P;
         per(i, m, 2*m) rep(j, 0, m) (u[i - m + j] += c[j] * u[i]) %= P;
      }
      copy(u.begin(), u.begin() + m, v.begin());
   }
   ll ans = 0;
   rep(i, 0, m) (ans += v[i] * a[i]) %= P;
   return ans;
}
```

6.8 Polya

```
/*

* Burnside's lemma

* 首先列出所有可能的染色方案，然后找出每个置换下保持不变的方案（不动点）数。
* 等价类数目：所有置换的不动点数的平均值。

* Polya enumeration theorem

* 一个循环的颜色需相同

*/
```

6.9 Prepare

```
// 模数不是素数，需要做除法
(a / b) % P = a % (P * b) / b

// 矩阵乘法
// 没有交换律，有结合律。
// 左乘向量取行，右乘取列。

// inv O(n)
inv[1] = 1;
rep(i, 2, N) inv[i] = mul(inv[P%i], P - P/i);

// p O(n)
vi p;
bool vis[N];
for(int i = 2; i < N; ++i) {
    if(!vis[i]) p.pb(i);
    for(int j = 0; j < sz(p) && i * p[j] < N; ++j) {
        vis[i * p[j]] = 1;
        if(i % p[j] == 0) break;
    }
}

// phi O(n)
int cntp, p[N], phi[N], vis[N];
phi[1]=1;
rep(i,2,N) {
    if(!vis[i]) p[cntp++]=i, phi[i]=i-1;
    for(int j=0;j<cntp&&p[j]*i<N;++j) {
        vis[p[j]*i]=1;
        if(i%p[j]==0) {
            phi[p[j]*i]=phi[i]*p[j]%P;
            break;
        } else {
            phi[p[j]*i]=phi[i]*(p[j]-1)%P;
        }
    }
}
```

7 Others

7.1 BitOperation

```
// 枚举子集
for(int i = x; i; (--i) & x) {
    //
}
// 统计子集的答案
rep(i, 0, n) {
    rep(j, 0, 1 << n) if(j >> i & 1) {
        upd(s[j], s[j ^ (1 << i)]);
    }
}
// 统计超集的答案
rep(i, 0, n) {
    for(int j = (1 << n) - 1; ~j; --j) if(!(j >> i & 1)) {
        upd(s[j], s[j | (1 << i)]);
    }
}

//
int __builtin_ffs (unsigned int x)
int __builtin_ffsl (unsigned long)
int __builtin_ffsll (unsigned long long)
Returns one plus the index of the least significant 1-bit of x, or if x is zero, returns
 zero.

//
int __builtin_clz (unsigned int x)
Returns the number of leading 0-bits in x, starting at the most significant bit position
. If x is 0, the result is undefined.

//
int __builtin_ctz (unsigned int x)
Returns the number of trailing 0-bits in x, starting at the least significant bit
position. If x is 0, the result is undefined.
```

```
//
int __builtin_popcount (unsigned int x)
Returns the number of 1-bits in x.

//
int __builtin_parity (unsigned int x)
Returns the parity of x, i.e. the number of 1-bits in x modulo 2.
```

7.2 Bitset

```
// Base
   b.any();   // has 1 ?
   b.none();  // all 0 ?
   b.count(); // cnt of 1

   b.set();   // all to 1
   b.reset(); // all to 0
   b.flip();  // all = 0 <-> 1

   b.set(p);  // b[p] = 1
   b.test(p); // b[p] is 1
   b.reset(p);// b[p] = 0
   b.flip(p); // b[p] = 0 <-> 1

// Black tech
   // __builtin_ctz in bitst
   b._Find_first();

   // travel all 1
   for (int i = b._Find_first(); i < sz(b); i = b._Find_next(i));
```

7.3 FastMul

```
inline ll mul(ll a,ll b){
   return (a * b - (ll)((long double)a * b / P + 0.5) * P + P) % P;
}
```

7.4 Strtok

```
char s[111];
gets(s);
vector<string> a;
for(char* p=strtok(s," .,()");p;p=strtok(NULL," .,())) a.pb(p);
```

7.5 ToNfa

```
const int N=510,Q=201000;

char s1[N],s2[N];
int q[Q],pre[N][N][2],pc[N][N][2],d[N][N][2],hd,tl;

struct node {
   vector<node*> nxt;
   vector<int> ch;
   void link(node *p,int c) { nxt.pb(p);ch.pb(c);}
}nd1[N],nd2[N],*Cur;

struct nfa { node *st,*ed;} Nd1[N],Nd2[N],*cur;

inline void upd(int a,int b,int &_a,int &_b) { if (a<_a) _a=a,_b=b;}
nfa *solve(int l,int r,char *s) {
   nfa *p=cur++;p->st=Cur++;p->ed=Cur++;
   if (l==r) p->st->link(p->ed,s[l]-'a');
   else {
      int pro=0,mp=inf,mw=-1;
      per(i,l,r+1) {
         if (s[i]=='(') pro-=3;
         if (s[i]==')') pro+=3;
         else if (s[i]=='*') upd(pro+2,i,mp,mw);
         else if (s[i]=='|') upd(pro,i,mp,mw);
         else if (i!=l&&s[i-1]!='(') upd(pro+1,i,mp,mw);
      }
      if (mp>=3) {
         nfa *p1=solve(l+1,r-1,s);
         p->st->link(p1->st,-1);
         p1->ed->link(p->ed,-1);
      } else if (mp==2) {
         assert(mw==r);
         nfa *p1=solve(l,r-1,s);
         p->st->link(p1->st,-1);
         p1->ed->link(p->st,-1);
         p->st->link(p->ed,-1);
      } else if (mp==1) {
         nfa *p1=solve(l,mw-1,s),*p2=solve(mw,r,s);
         p->st->link(p1->st,-1);
         p1->ed->link(p2->st,-1);
         p2->ed->link(p->ed,-1);
      } else {
         nfa *p1=solve(l,mw-1,s),*p2=solve(mw+1,r,s);
         p->st->link(p1->st,-1);
         p->st->link(p2->st,-1);
         p1->ed->link(p->ed,-1);
         p2->ed->link(p->ed,-1);
      }
   }
   return p;
}

void add(int x,int y,int _x,int _y,int _z,int c) {
   int _d=d[_x][_y][_z]+(c!=-1),z=_z||(c!=-1);
   if (d[x][y][z]>_d) {
      d[x][y][z]=_d;pc[x][y][z]=c;
      pre[x][y][z]=(_x<<20)+(_y<<10)+_z;
      if (c==-1) q[--hd]=(x<<20)+(y<<10)+z;
      else q[tl++]=(x<<20)+(y<<10)+z;
   }
}
```

```
void print(int x,int y,int z) {
   if (x==0&&y==0&&z==0) return;
   else {
      int Pre=pre[x][y][z];
      print(Pre>>20,(Pre>>10)&1023,Pre&1);
      if (pc[x][y][z]!=-1) putchar(pc[x][y][z]+'a');
   }
}
int main() {
   // read
   scanf("%s%s", s1, s2);
   // regular expression -> nfa
   cur=Nd1,Cur=nd1,solve(0,strlen(s1)-1,s1);
   cur=Nd2,Cur=nd2,solve(0,strlen(s2)-1,s2);
   // dp
   memset(d,0x20,sizeof(d));d[0][0][0]=0;
   hd=tl=100000;
   q[--hd]=0;
   while (hd<tl) {
      int x=q[hd]>>20,y=(q[hd]>>10)&1023,z=q[hd]&1;hd++;
      rep(i,0,nd1[x].nxt.size()) rep(j,0,nd2[y].nxt.size()) if (nd1[x].ch[i]==nd2[y].ch[
      j]&&nd1[x].ch[i]!=-1)
         add(nd1[x].nxt[i]-nd1,nd2[y].nxt[i]-nd2,x,y,z,nd1[x].ch[i]);
      rep(i,0,nd1[x].nxt.size()) if (nd1[x].ch[i]==-1)
         add(nd1[x].nxt[i]-nd1,y,x,y,z,-1);
      rep(i,0,nd2[y].nxt.size()) if (nd2[y].ch[i]==-1)
         add(x,nd2[y].nxt[i]-nd2,x,y,z,-1);
   }
   if (d[1][1][1]>=1000000) puts("Correct");
   else puts("Wrong"),print(1,1,1);
}
```

7.6 duipai

```
#!/bin/bash
while true; do
    ./gen > gen.in
    ./sol <gen.in >sol.out
    ./j <gen.in >j.out
    if diff sol.out j.out; then
        printf "AC\n"
    else
        printf "Wa\n"
        exit 0
    fi
done

// sh check.sh
```

8 String

8.1 1. StringHash

```
// id starts from 1
const int mod=1e9+7;
ull base[N],ha[N];
char s[N];
void init() {
   base[0]=1;
   rep(i,1,N) base[i]=base[i-1]*mod;
}
void Hash() {
   int len=strlen(s+1);
   ha[0]=0;
   rep(i,1,len+1) ha[i]=ha[i-1]*mod+s[i];
}
ull getHa(int l,int r) {
   return ha[r]-ha[l-1]*base[r-l+1];
}
```

8.2 2. Exkmp

```
/*
 * s 串的每个后缀与 t 串的最长公共前缀
 * t:  a  b  a
 * nt: 0  0  1
 * s:  a  b  a  c  a  b  a
 * ns: 3  0  1  0  3  0  1
 */
void exkmp(char *s,int *z,char *t,int *p){
    int lens = strlen(s);
    int lent = strlen(t);
    p[0]=0;
    for(int i=0,x=0,y=0;i<lens;++i){
        z[i] = i <= y ? min(y-i,p[i-x]) : 0;
        while(i + z[i] < lens && z[i] < lent && s[i + z[i]] == t[z[i]]) ++z[i];
        if(y <= i + z[i]) x = i, y = i + z[i];
    }
}

void Exkmp(){
    scanf("%s%s",s,t);
    exkmp(t+1,nt+1,t,nt);
    exkmp(s,ns,t,nt);
}
```

8.3 3. Kmp

```
/*
t:  a  b  a
nt:-1 -1  0
s:  a  b  a  c  a  b  a
ns: 0  1  2 -1  0  1  2
*/
void kmp(char *s,int *ns,char *t,int *nt){
    int lens = strlen(s);
```

```
    int lent = strlen(t);
    nt[0] = -1;
    for(int i=0,j=-1;i<lens;++i){
        while(j >= 0 && s[i] != t[j + 1]) j = nt[j];
        if(s[i] == t[j + 1]) ++j;
        ns[i] = j;
        if(j + 1 == lent) j = nt[j];
    }
}
void KMP(){
    scanf("%s%s",s,t);
    kmp(t+1,nt+1,t,nt);
    kmp(s,ns,t,nt);
}
```

8.4 4. ACAutomaton

```
/*
* [0,L) , N-1 is virtual , 0 is rt
* init!!
* addation: end[] end[c]|=end[fail[c]]
*/
struct Trie{
    static const int N = 101010 , M = 26;
    int ne[N][M] , fail[N] , fa[N] , rt , L;
    void ini(){ fill_n(ne[fail[0] = N-1],M,0);L = 0;rt = newnode();}
    int newnode(){ fill_n(ne[L],M,0); return L++; }
    void add(char *s){
        int p = rt;
        for(int i=0;s[i];++i){
            int c = s[i] - 'a';// modify
            if(!ne[p][c]) ne[p][c] = newnode() , fa[L-1] = p;
            p = ne[p][c];
        }
    }
    void Build(){
        vi v;v.pb(rt);
        rep(i,0,sz(v)){
            int c = v[i];
            rep(i,0,M) ne[c][i] ?
                v.pb(ne[c][i]) , fail[ne[c][i]] = ne[fail[c]][i] :
                ne[c][i] = ne[fail[c]][i];
        }
    }
};
```

8.5 5. SAIS

```
/**
 * Ensure that str[n] is the unique lexicographically smallest character in str.
 * time complexity: O(n)
 */
namespace SA {
   const static int N = 100000 + 10;
   int sa[N], rk[N], ht[N], s[N<<1], t[N<<1], p[N], cnt[N], cur[N];
#define pushS(x) sa[cur[s[x]]--] = x
#define pushL(x) sa[cur[s[x]]++] = x
#define inducedSort(v) std::fill_n(sa, n, -1); std::fill_n(cnt, m, 0);      \
   for (int i = 0; i < n; i++) cnt[s[i]]++;                                  \
   for (int i = 1; i < m; i++) cnt[i] += cnt[i-1];                           \
   for (int i = 0; i < m; i++) cur[i] = cnt[i]-1;                            \
   for (int i = n1-1; ~i; i--) pushS(v[i]);                                  \
   for (int i = 1; i < m; i++) cur[i] = cnt[i-1];                            \
   for (int i = 0; i < n; i++) if (sa[i] > 0 &&  t[sa[i]-1]) pushL(sa[i]-1); \
   for (int i = 0; i < m; i++) cur[i] = cnt[i]-1;                            \
   for (int i = n-1;  ~i; i--) if (sa[i] > 0 && !t[sa[i]-1]) pushS(sa[i]-1)
   void sais(int n, int m, int *s, int *t, int *p) {
      int n1 = t[n-1] = 0, ch = rk[0] = -1, *s1 = s+n;
      for (int i = n-2; ~i; i--) t[i] = s[i] == s[i+1] ? t[i+1] : s[i] > s[i+1];
      for (int i = 1; i < n; i++) rk[i] = t[i-1] && !t[i] ? (p[n1] = i, n1++) : -1;
      inducedSort(p);
      for (int i = 0, x, y; i < n; i++) if (~(x = rk[sa[i]])) {
         if (ch < 1 || p[x+1] - p[x] != p[y+1] - p[y]) ch++;
         else for (int j = p[x], k = p[y]; j <= p[x+1]; j++, k++)
            if ((s[j]<<1|t[j]) != (s[k]<<1|t[k])) {ch++; break;}
         s1[y = x] = ch;
      }
      if (ch+1 < n1) sais(n1, ch+1, s1, t+n, p+n1);
      else for (int i = 0; i < n1; i++) sa[s1[i]] = i;
      for (int i = 0; i < n1; i++) s1[i] = p[sa[i]];
      inducedSort(s1);
   }
   template<typename T>
      int mapCharToInt(int n, const T *str) {
         int m = *max_element(str, str+n);
         std::fill_n(rk, m+1, 0);
         for (int i = 0; i < n; i++) rk[str[i]] = 1;
         for (int i = 0; i < m; i++) rk[i+1] += rk[i];
         for (int i = 0; i < n; i++) s[i] = rk[str[i]] - 1;
         return rk[m];
      }
   template<typename T>
      void suffixArray(int n, const T *str) {
         int m = mapCharToInt(++n, str);
         sais(n, m, s, t, p);
         for (int i = 0; i < n; i++) rk[sa[i]] = i;
         for (int i = 0, h = ht[0] = 0; i < n-1; i++) {
            int j = sa[rk[i]-1];
            while (i+h < n && j+h < n && s[i+h] == s[j+h]) h++;
            if (ht[rk[i]] = h) h--;
         }
      }
};
// 出现 i 次的子串有 c[i] 个
namespace S {
   int top;
   int sta[N<<1], cnt[N<<1];
   ll c[N];
   inline int gao(int k) {
```

```
    int cc = 0;
    while(top && sta[top] > k) {
       cc += cnt[top];
       cnt[top] = 0;
       c[cc] += sta[top] - max(k, sta[top-1]);
       --top;
    }
    return cc;
  }
  inline void push(int x, int y) {
    if(!top || sta[top] != x) sta[++top] = x;
    cnt[top] += y;
  }
  inline void build(int n) {
    top = 0;
    fill_n(c+1, n, 0);
    rep(i, 1, n+1) {
       int lcp = SA::ht[i], cc = gao(lcp);
       push(lcp, cc);
       push(n - SA::sa[i], 1);
    }
    gao(0);
  }
};
```

8.6 6. DoublingArray

```
namespace Doubling{
    static const int N = 101010;
   // sa[0~n]: 排名第的后缀是以i sa[i] 开头
   // h[1~n]:S[sa[i-1]] 与 S[sa[i]] 的最长公共前缀长度为 h[i]
    int t[N] , wa[N] , wb[N] , sa[N] , h[N];
    void sort(int *x,int *y,int n,int m){
        rep(i,0,m) t[i] = 0;
        rep(i,0,n) t[x[y[i]]]++;
        rep(i,1,m) t[i] += t[i-1];
        per(i,0,n) sa[--t[x[y[i]]]] = y[i];
    }
    bool cmp(int *x,int a,int b,int d){
        return x[a] == x[b] && x[a+d] == x[b+d];
    }
    void da(int *s,int n,int m){
        int *x=wa,*y=wb;
        rep(i,0,n) x[i] = s[i] , y[i] = i;
        sort(x , y , n , m);
        for(int j=1,p=1;p<n;m=p,j<<=1){
            p = 0;rep(i,n-j,n) y[p++] = i;
            rep(i,0,n) if(sa[i] >= j) y[p++] = sa[i] - j;
            sort(x , y , n , m);
            swap(x , y);p = 1;x[sa[0]] = 0;
            rep(i,1,n) x[sa[i]] = cmp(y,sa[i],sa[i-1],j)?p-1:p++;
        }
    }
    void cal_h(int *s,int n,int *rk){
        int j,k=0;
        for(int i=1;i<=n;++i) rk[sa[i]] = i;
        for(int i=0;i<n;h[rk[i++]] = k)
            for(k&&--k,j=sa[rk[i]-1];s[i+k]==s[j+k];++k);
    }
}
// rank[0~n-1]: 以 i 开头的后缀排名 rank[i]
struct DA{ // [0,n] , in[n] = 0 , n load
    static const int N = 101010;
    int p[18][N] , rk[N] , in[N] , Log[N] , n;
    void Build(){
        Doubling::da(in,n+1,300);
        Doubling::cal_h(in,n,rk);
        Log[0] = -1;for(int i=1;i<=n;++i) Log[i] = Log[i-1] + (i==(i&(-i)));
        for(int i=1;i<=n;++i) p[0][i] = Doubling::h[i];
        for(int j=1;1<<j<=n;++j){
            int lim = n+1-(1<<j);
            for(int i=1;i<=lim;++i)
                p[j][i] = min(p[j-1][i] , p[j-1][i+(1<<j>>1)]);
        }
    }
    // 某两个后缀的最长公共前缀
    int lcp(int a,int b){
        a = rk[a] , b = rk[b];
        if(a > b) swap(a , b);++a;
        int t = Log[b-a+1];
        return min(p[t][a] , p[t][b-(1<<t)+1]);
    }
};
```

8.7 7. SuffixAutomaton

```
/*
 * [0,L] , 0 is virtual , 1 is rt , init!!
 * [l[par[s]] + 1, l[s]]
 * 好像暴力向上跳的复杂度是对的。
 */
struct SAM {
    static const int N = ::N << 1, M = 26;
    int par[N], l[N], ne[N][M];
    int rt, last, L;
    void add(int c) {
        int p = last;
        /* ex
      if(ne[p][c] && l[ne[p][c]] == l[p] + 1) {
         last = ne[p][c];
         return ;
      }
      */
      int np = ++L;
        fill(ne[np], ne[np] + M, 0);
        l[np] = l[p] + 1;
        last = np;
        while(p && !ne[p][c]) ne[p][c] = np, p = par[p];
        if(!p) par[np] = rt;
        else{
```

```
            int q = ne[p][c];
            if(l[q] == l[p] + 1) par[np] = q;
            else {
                int nq = ++L;
                l[nq] = l[p] + 1;
                copy(ne[q], ne[q] + M, ne[nq]);
                par[nq] = par[q];
                par[q] = par[np] = nq;
                while(p && ne[p][c] == q) ne[p][c] = nq, p = par[p];
            }
        }
    }
    void ini() {
        rt = last = L = 1;
        fill(ne[rt], ne[rt] + M, 0);
        l[0] = -1;
    }
};
// BucketSort
rep(i, 1, L + 1) ++cnt[l[i]];
rep(i, 1, L + 1) cnt[i] += cnt[i - 1];
rep(i, 1, L + 1) cur[cnt[l[i]]--] = i;
```

8.8 8. Manacher

```
/*
 * length of pa is two size of str
 * i: [0, n)     pa[i<<1] : odd string 整个回文长度为 2*pa[i<<1]-1
 * i: [0, n - 1) pa[i<<1|1] : even string 整个回文长度为 2*pa[i<<1]
 * N>2*n
*/
void Manacher(char *s,int n,int *pa){
    pa[0] = 1;
    for(int i=1,j=0;i<(n<<1)-1;++i){
        int p = i >> 1 , q = i - p , r = ((j + 1)>>1) + pa[j] - 1;
        pa[i] = r < q ? 0 : min(r - q + 1 , pa[(j<<1) - i]);
        while(0 <= p - pa[i] && q + pa[i] < n && s[p - pa[i]] == s[q + pa[i]])
            pa[i]++;
        if(q + pa[i] - 1 > r) j = i;
    }
}
```

8.9 9. PalindromicTree

```
// [0,p) , 0(even) and 1(odd) is virtual , init!!
struct Palindromic_Tree {
   static const int N = ::N , M = 26;
   int ne[N][M] , fail[N] , len[N] , S[N] , last , n , p, cnt[N], las[N];
   int newnode(int l){
      fill(ne[p] , ne[p] + M , 0);
      len[p] = l;
      las[p] = n;
      cnt[p] = 0;
      return p++;
   }
   void ini(){
      p = 0;newnode(0);newnode(-1);
      S[n = last = 0] = -1;
      fail[0] = 1;
   }
   int get_fail(int x){
      while(S[n - len[x] - 1] != S[n]) x = fail[x];
      return x;
   }
   void add(int c){
      S[++n] = c;
      int cur = get_fail(last);
      if(!ne[cur][c]){
         int now = newnode(len[cur] + 2);
         fail[now] = ne[get_fail(fail[cur])][c];
         ne[cur][c] = now;
      }
      last = ne[cur][c];
      cnt[last]++;
   }
   void build() {
      for(int i = p - 1; ~i; --i) cnt[fail[i]] += cnt[i];
   }
}pam;
```

9 Tree

9.1 Centroid

```
// id starts from 1
namespace Centriod {
    const int N = ::N;
    bool vis[N];
   int sz[N];
    void dfssz(int c,int fa,int Sz,int &rt){
        sz[c] = 1;
        for(auto t : g[c]) if(!vis[t]&&t!=fa) dfssz(t,c,Sz,rt) , sz[c]+=sz[t];
        if(!rt && sz[c]*2>Sz) rt=c;
    }
    void dfs(int c){
        int rt=0;dfssz(c,0,0,rt);dfssz(c,0,sz[c],rt=0);
        vis[rt] = true;
        /*
         * calc
         * 注意计算以 rt 为起点的路径、只包含 rt 的路径
        * 注意 v != vis[rt]
        */
        for(auto t : g[rt]) if(!vis[t]) dfs(t);
    }
};
```

9.2 DsuOnTree

```
// id starts with 1
namespace QuerySubtree{
    static const int N = ::N;
    int sz[N] , wson[N] , par[N];
    void dfs(int c,int fa,vi g[]){
        sz[c]=1;par[c]=fa;int &s=wson[c]=0;
        for(auto t:g[c]) if(t!=fa)
            dfs(t,c,g),sz[c]+=sz[t],(sz[t]>=sz[s])&&(s=t);
    }
    void solve(int c,int fa,bool iswson,vi g[]){
        for(auto t : g[c]) if(t != wson[c] && t != fa) solve(t , c , false , g);
        if(wson[c]) solve(wson[c] , c , true , g);
        for(auto t : g[c]) if(t != wson[c] && t != fa) {
            // query
            // add
        }
        if(!iswson) ;// del
    }
    void solve(vi g[]){
        dfs(1,0,g);
        solve(1,0,false,g);
    }
}
```

9.3 HeavyChain

```
// id starts with 1
struct HeavyChain{
   static const int N = ::N;
   int sz[N], wson[N], top[N], dep[N], id[N], _, par[N], who[N];
   void dfs(int c, int fa, vi g[]){
      sz[c] = 1;
      par[c] = fa;
      dep[c] = dep[fa] + 1;
      int &s = wson[c] = top[c] = 0;
      for(auto t : g[c]) if(t != fa) {
         dfs(t, c, g);
         sz[c] += sz[t];
         if(sz[t] >= sz[s]) s = t;
      }
   }
   void dfs2(int c, int fa, vi g[]){
      id[c] = ++_;
      who[_] = c;
      int s = wson[c];
      if(!top[c]) top[c] = c;
      if(s) top[s] = top[c], dfs2(s, c, g);
      for(auto t : g[c]) if(t != fa && t != s) dfs2(t, c, g);
   }
   void Query(int a, int b){
      int fa = top[a], fb = top[b];
      while(fa != fb){
         if(dep[fa] < dep[fb]) swap(a, b), swap(fa, fb);
         // Cal id[fa] .. id[a]
         a = par[fa]; fa = top[a];
      }
      if(dep[a] < dep[b]) swap(a, b);
      // Cal id[b] .. id[a]
      // b is lca
   }
   void Build(vi g[]){
      dfs(1, 0, g);
      _=0;
      dfs2(1, 0, g);
   }
}hc;
```

9.4 LongChain

```
struct LongChain{
   static const int N = ::N;
   int wson[N] , top[N] , dep[N] , lg[N];
   int jump[N][20] , id[N] , who[N] , rwho[N] , _;
   void dfs(int c,int fa,vi g[]){
      dep[c]=1;int &s=wson[c]=top[c]=0;
      jump[c][0]=fa;rep(i,1,20) jump[c][i]=jump[jump[c][i-1]][i-1];
      for(auto t:g[c]) if(t!=fa)
         dfs(t,c,g),dep[c]=max(dep[t]+1,dep[c]),(dep[t]>=dep[s])&&(s=t);
   }
   void dfs2(int c,int fa,int rc,vi g[]){
      if(!top[c]) top[c]=c,rc=c;
      who[id[c]=++_]=c;rwho[_]=rc;
      int s=wson[c];
      if(s) top[s]=top[c],dfs2(s,c,jump[rc][0],g);
      for(auto t:g[c]) if(t!=fa&&t!=s) dfs2(t,c,t,g);
   }
   void Build(vi g[]){
      dfs(1,0,g);_=0;dfs2(1,0,1,g);
      rep(i,2,N) lg[i]=lg[i>>1]+1;
   }
   void solve(int c, int fa, vi g[]) {
      for(auto t : g[c]) if(t != fa) solve(t, c, g);
      if(wson[c]) {
         // upd c by wson[c], O(1) or O(log(n))
      } else {
         // c is leaf
      }
      for(auto t : g[c]) if(t != fa && t != wson[c]) {
         // brute force upd c by t
      }
      // 注意统计以 c 为起点的链的答案，注意深度的限制（两棵子树都要注意）
   }
   // kth_par should exist
   int kth_par(int x,int k){
      if(k==0) return x;
      int j0=1<<lg[k];
      int p0=jump[x][lg[k]];
      int j1=k-j0;
      int del=id[p0]-id[top[p0]];
```

```
        if(del>=j1) return who[id[p0]-j1];
        else return rwho[id[top[p0]]+j1-del];
    }
}hc;
```