

# Advanced Microeconomics

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## Lecture 18: Contract, law, and enforcement in static settings

Essential reading:

- Watson (2013): Strategy – an introduction to game theory, chapter 13
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# The role of contracts

- Contracting institutions such as the legal system govern a wide variety of relationships in our society
  - contracts for firms and workers that specify wages and other aspects of the employment relationship
  - contracts of homeowners with building contractors
  - contracts of firms with suppliers and customers
  - contracts of nations about trade (WTO) and security (NATO) issues
- Contracting may help to
  - alleviate strategic uncertainty
  - avoid inefficient coordination
    - esp. when there are multiple equilibria
  - align incentives
    - ie. mitigate conflicts between joint and individual decisions

**Definition:** A **contract** is an agreement about behavior that is intended to be enforced.

- A contractual relationship consists of two phases:
  - Contracting phase, in which players set the terms of their contracts
    - Focus of lecture on Principal-agent model
  - Implementation phase, in which contract is carried out and enforced
    - Focus in this lecture: enforcement of contract
- Methods of contract enforcement: a contract is
  - **self-enforced**, if the players have the individual incentives to abide by the terms of the contract
  - **externally enforced**, if there is an external player, such as a judge or arbitrator, that enforces behavior in accordance with contract

# An example

- Remodeling of a house requires effort of an architect and a building constructor
- Both decide simultaneously whether investing (costly) effort in the project ( $I$ ) or not investing ( $N$ )
  - Investing by the architect facilitates the work of the constructor
  - Investing by the constructor improves quality of remodeling
    - We assume that architect is also the owner of the home; hence he benefits from quality of the remodeling
    - Game below is called the *underlying game*

		Constructor	
		I	N
Architect/Owner	I	$Z_1, Z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0

# Example: self-enforcing

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0

- Assumptions:
  - $z_1 + z_2 > x_1 + y_2, y_1 + x_2, 0$
  - Parties can make monetary transfers
    - Hence  $(I, I)$  is the only efficient outcome of the game
- Question: can the parties enforce a contract specifying that  $(I, I)$  will be played?
- If  $z_1 < x_1$  and/or  $z_2 < x_2$ , then an agreement to play  $(I, I)$  is not *self-enforcing*
  - i.e., it is not a Nash equilibrium

## Example: external enforcement

- Thus  $(I, I)$  needs to be externally enforced
- Suppose a court imposes transfers  $\alpha, \beta, \gamma$  if outcome is not  $(I, I)$ 
  - This is called the *induced game*
- We distinguish two contractual settings
  - Court allows people to write *complete contracts* as they see fit and enforces them verbatim
  - Court puts constraints on the set of feasible contracts and parties write *incomplete contracts*

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0

Architect/Owner

		Constructor	
		I	N
Architect/Owner	I		
	N		

# Example: external enforcement

- Thus  $(I, I)$  needs to be externally enforced
- Suppose a court imposes transfers  $\alpha, \beta, \gamma$  if outcome is not  $(I, I)$ 
  - $\alpha, \beta, \gamma \in \mathbb{R}$ , i.e., transfers can be positive or negative
  - This is called the *induced game*
- We distinguish two contractual settings
  - a) Court allows people to write *complete contracts* as they see fit and enforces them verbatim
  - b) Court puts constraints on the set of feasible contracts and parties write *incomplete contracts*

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1 + \beta, x_2 - \beta$
	N	$x_1 + \alpha, y_2 - \alpha$	$\gamma, -\gamma$

# Complete contracting in discretionary environments

- Suppose the players can write a **complete contract** specifying  $\alpha, \beta, \gamma$
- The contract induces  $(I, I)$  if
  - and the court enforces the contract,
  - which requires that the contract is **fully verifiable**
    - ie. the court must be able to verify whether the players have chosen  $I$  or  $N$

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1+\beta, x_2-\beta$
	N	$x_1+\alpha, y_2-\alpha$	$\gamma, -\gamma$

# Complete contracting in discretionary environments

- Suppose the players can write a **complete contract** specifying  $\alpha, \beta, \gamma$
- The contract induces  $(I, I)$  if
  - $z_1 \geq x_1 + \alpha$  and  $z_2 \geq x_2 - \beta$ ,
  - and the court enforces the contract,
  - which requires that the contract is **fully verifiable**
    - ie. the court must be able to verify whether the players have chosen  $I$  or  $N$

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1 + \beta, x_2 - \beta$
	N	$x_1 + \alpha, y_2 - \alpha$	$\gamma, -\gamma$

# Contracting in discretionary environments

- But: full verifiability is more often the exception than the rule
  - E.g.: court may be able to judge quality of work, but not whether defects have been caused by failure of architect or constructor
  - In this example of **limited verifiability**, the court cannot distinguish between  $(I, N)$ ,  $(N, I)$  and  $(N, N)$ , which yields game below
  - $(I, I)$  a Nash equilibrium if  $\underline{z_1} > \underline{x_1}$  and  $\underline{y_1} > \underline{x_2}$
  - Summation yields *necessary* condition
    - which may easily be violated (e.g. with payoffs as in prisoners' dilemma)

		Constructor	
	I	$z_1, z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0
Architect/Owner			
	I		
	N		

# Contracting in discretionary environments

- But: full verifiability is more often the exception than the rule
  - E.g.: court may be able to judge quality of work, but not whether defects have been caused by failure of architect or constructor
  - In this example of **limited verifiability**, the court cannot distinguish between  $(I, N)$ ,  $(N, I)$  and  $(N, N)$ , which yields game below
  - $(I, I)$  a Nash equilibrium if  $z_1 \geq x_1 + \alpha$  and  $z_2 \geq x_2 - \alpha$
  - Summation yields *necessary* condition  $z_1 + z_2 \geq x_1 + x_2$ 
    - which may easily be violated (e.g. with payoffs as in prisoners' dilemma)

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1 + \alpha, x_2 - \alpha$
	N	$x_1 + \alpha, y_2 - \alpha$	$\alpha, -\alpha$

- Often players write **incomplete contracts**
  - It may be expensive to list all contingencies
  - Players may count on court to “complete” a contract during litigation
- Often courts impose transfers on the basis of certain legal principles, rather than on the basis of the contract document
- Legal principle of **expectation damage**:
  - court imposed transfer of money from defendant to plaintiff so as to give the plaintiff the payoff he would have received had the contract been fulfilled
    - the players’ expectations are  $z_1, z_2$

Architect/Owner	I	N
	$z_1, z_2$	$y_1, x_2$
	$x_1, y_2$	0,0

# Expectation damages

- **expectation damage:** court imposed transfer of money from defendant to plaintiff so as to give the plaintiff the payoff he would have received had the contract been fulfilled, i.e.  $z_1, z_2$
- If architect breaches, it must pay constructor
- If constructor breaches, it must pay architect
- This yields induced game below

	Constructor	
Architect/Owner	I	N
	$z_1, z_2$	$y_1, x_2$
I	$x_1, y_2$	0,0
N		

  

	Constructor	
Architect/Owner	I	N
I		
N		

# Expectation damages

- If architect breaches, it must pay constructor  $z_2 - y_2$
- If constructor breaches, it must pay architect  $z_1 - y_1$
- This yields induced game below
  - $(I, I)$  a Nash equilibrium if  $z_1 = y_1$  and  $z_2 = y_2$
  - Rearranging yields conditions for  $(I, I)$  to be efficient:  
 $z_1 \geq y_1$  and  $z_2 \geq y_2$
- Result: under expectation damage  $(I, I)$  is enforceable if and only if  $(I, I)$  is efficient

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0

Architect/Owner

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$z_1, x_2 - z_1 + y_1$
	N	$x_1 - z_2 + y_2, z_2$	0,0

# Expectation damages

- If architect breaches, it must pay constructor  $z_2 - y_2$
- If constructor breaches, it must pay architect  $z_1 - y_1$
- This yields induced game below
  - $(I, I)$  a Nash equilibrium if  $z_1 \geq x_1 - z_2 + y_2$  and  $z_2 \geq x_2 - z_1 + y_1$
  - Rearranging yields conditions for  $(I, I)$  to be efficient:  

$$z_1 + z_2 \geq x_1 + y_2 \text{ and } z_2 + z_1 \geq x_2 + y_1$$
- Result: under expectation damage  $(I, I)$  is enforceable if and only if  $(I, I)$  is efficient

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$z_1, x_2 - z_1 + y_1$
	N	$x_1 - z_2 + y_2, z_2$	0,0

- Hence expectation damages alleviate tension between individual and joint incentives
- But: the court needs a great deal of information
  - Who breached the contract
  - Exact payoff structure
- Legal principle of **reliance damages**: court imposes transfer that returns the plaintiff to the state in which she would have been but for the contract
  - Suppose we take the Nash equilibrium payoff  $(0, 0)$  as the “no contract” value
    - ie. for original game we assume  $y_i \leq 0, i = 1, 2$

		Constructor	
		I	N
Architect/Owner	I	$Z_1, Z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0

- **reliance damages:** court imposes transfer that returns the plaintiff to the state in which she would have been but for the contract, here:  $(0,0)$ 
  - yields induced game below
  - $(I, I)$  is a Nash equilibrium in the induced game if and only if
  - In words: damages from not-investing,  $y_i < 0$ , must be sufficiently large
  - Advantage: easier to implement because court does not need to know payoff for  $(I, I)$

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0
Architect/Owner		I	N
	I		
	N		

- **reliance damages:** court imposes transfer that returns the plaintiff to the state in which she would have been but for the contract, here: (0,0)

- yields induced game below
- $(I, I)$  is a Nash equilibrium in the induced game if and only if

$$z_1 \geq x_1 + y_2 \text{ and } z_2 \geq x_2 + y_1$$

- In words: damages from not-investing,  $y_i < 0$ , must be sufficiently large
- Advantage: easier to implement because court does not need to know payoff for  $(I, I)$

		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$y_1, x_2$
	N	$x_1, y_2$	0,0
		Constructor	
		I	N
Architect/Owner	I	$z_1, z_2$	$0, x_2+y_1$
	N	$x_1+y_2, 0$	0,0