

2013-06-05

Complex synapses

A general theory of learning and memory with Complex
Synapses
based on work with Surya Ganguli

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June 5, 2013

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We often model synaptic plasticity as the change of a single number (synaptic weight). In reality, there is a complex dynamical system inside a synapse.

Semi-realistic models of synaptic memory have terrible storage without synaptic complexity.

We will study the entire space of a broad class of models of complex synapses to find upper bounds on their performance.

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Complex synapses

└ Introduction

1. amplitude of psp.
2. finite number of values.

We often model synaptic plasticity as the change of a single number (synaptic weight). In reality, there is a complex dynamical system inside a synapse.

Semi-realistic models of synaptic memory have terrible storage without synaptic complexity.

We will study the entire space of a broad class of models of complex synapses to find upper bounds on their performance.

└ Concepts

Learning rule: how activity \rightarrow potentiation/depression.
e.g. Hebb rule, STDP, Hopfield outer product, perceptron rule,...

Plasticity mechanism: how synapse responds to potentiation/depression.
e.g. Binary switch, Cascade model, Multistate model,...

Synaptic transmission: how synaptic state affects neural activity
e.g. Hopfield attractor,...

Learning rule: how activity \rightarrow potentiation/depression.

e.g. Hebb rule, STDP, Hopfield outer product, perceptron rule,...

Plasticity mechanism: how synapse responds to potentiation/depression.

e.g. Binary switch, Cascade model, Multistate model,...

Synaptic transmission: how synaptic state affects neural activity.

e.g. Hopfield attractor,...

1. Avoid confusion: separate concepts
2. Talk exclusively about second one.
3. Abstract away other two.

1 Why complex synapses?

2 Modelling synaptic complexity

3 Upper bounds

4 Envelope memory curve

1. review terrible properties of simple synapses.
2. mathematical formalism of model, quantify performance (memory decay over time)
3. upper bounds on single numbers that depend on whole memory curve (decay over time)
4. upper bounds at finite times

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Complex synapses

- Why complex synapses?

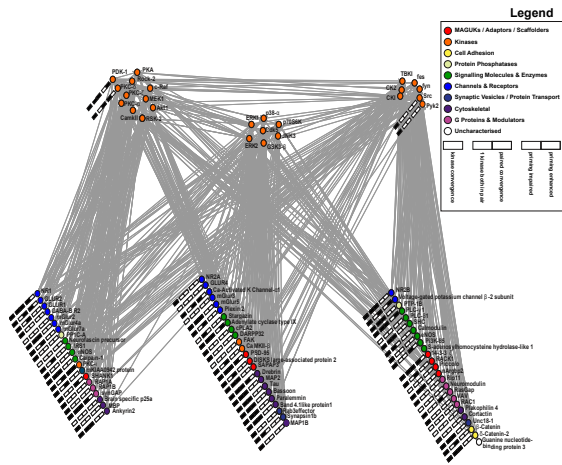
Section 1

Why complex synapses?

Section 1

Why complex synapses?

Complex synapse



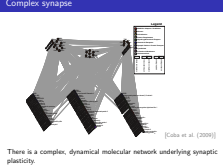
[Coba et al. (2009)]

There is a complex, dynamical molecular network underlying synaptic plasticity.

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Complex synapses

- Why complex synapses?
- Complex synapse



1. Molecular network, post-synaptic density, from Seth Grant
2. Does this matter?
3. Could just be the machinery for changing synaptic weight
4. link back to questions on "There"

Storage capacity of synaptic memory

A classical perceptron (used as a recognition memory device) has a capacity $\propto N$, the number of synapses.

Requires synapses' dynamic range also $\propto N$.

If we restrict synaptic weight to a fixed, finite set of values,
 \implies tradeoff between learning and forgetting:
new memories overwriting old.

If we wish to store new memories rapidly, memory capacity $\sim \mathcal{O}(\log N)$.
[Amit and Fusi (1992), Amit and Fusi (1994)]

To circumvent this tradeoff, need to go beyond model of a synapse as a single number.

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Complex synapses

└ Why complex synapses?

└ Storage capacity of synaptic memory

1. very plastic: learn easy, forget easy
2. little plasticity, remember better, learn harder
3. or sparse $\sim \log N/N$
4. one way around limit: complexity

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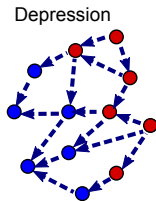
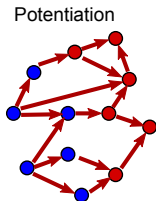
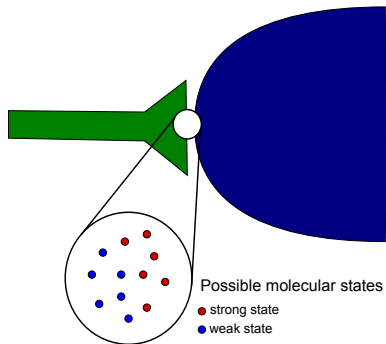
Complex synapses
└─ Modelling synaptic complexity

Section 2

Modelling synaptic complexity

Section 2

Modelling synaptic complexity

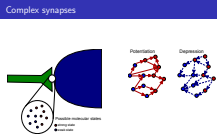


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Complex synapses

└ Modelling synaptic complexity

└ Complex synapses



1. functional states, not molecules
2. synaptic weight depends on state
3. many states can have same weight
4. stochastic transitions

- No spatial/temporal correlations in plasticity events.
- Potentiating/depressing plasticity events \sim Poisson processes.
- Potentiation and depression are described by Markov processes.
- Synaptic weights can only take values ± 1 .
- Ideal observer: read weights directly.

[Fusi et al. (2005), Fusi and Abbott (2007), Barrett and van Rossum (2008)]

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Complex synapses

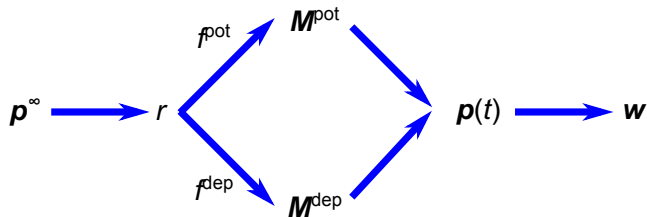
└ Modelling synaptic complexity

└ Simplifying assumptions

1. allows us to concentrate on synapse, not neuron/network
2. No firing system
3. don't care if STDP...
4. looks like binary synapse from outside. Inside...
5. ideal observer reads weights, not electrical activity: don't model neurons/network
6. upper bound on electrical activity readout

- No spatial/temporal correlations in plasticity events.
 - Potentiating/depressing plasticity events \sim Poisson processes.
 - Potentiation and depression are described by Markov processes.
 - Synaptic weights can only take values ± 1 .
 - Ideal observer: read weights directly.
- [Fusi et al. (2005), Fusi and Abbott (2007), Barrett and van Rossum (2008)]

There are N identical synapses with M internal functional states.



$$\frac{d\mathbf{p}(t)}{dt} = r\mathbf{p}(t)\mathbf{W}^F, \quad \mathbf{W}^F = f^{\text{pot}}\mathbf{M}^{\text{pot}} + f^{\text{dep}}\mathbf{M}^{\text{dep}} - \mathbf{I},$$

$$\mathbf{p}^{\infty}\mathbf{W}^F = 0.$$

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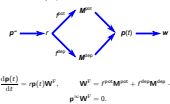
Complex synapses

└ Modelling synaptic complexity

└ Dynamics

Dynamics

There are N identical synapses with M internal functional states.



$$\frac{d\mathbf{p}(t)}{dt} = r\mathbf{p}(t)\mathbf{W}^F, \quad \mathbf{W}^F = f^{\text{pot}}\mathbf{M}^{\text{pot}} + f^{\text{dep}}\mathbf{M}^{\text{dep}} - \mathbf{I},$$

$$\mathbf{p}^{\infty}\mathbf{W}^F = 0.$$

1. stoch process has steady state.
2. Prior activity puts it in this state. row vec.
3. plasticity events at rate r
4. fraction pot/dep
5. probs changed by Markov matrices, prob $i \rightarrow j$
6. Readout: synaptic weight vec when in each state.
7. Memory at $t = 0$, keep track of pot/dep
8. subsequent: average over pot/dep

\vec{w} is the N -element vector of synaptic weights.

$$\text{Signal} = \langle \vec{w}_{\text{ideal}} \cdot \vec{w}(t) - \vec{w}_{\text{ideal}} \cdot \vec{w}(\infty) \rangle,$$

$$\text{Noise} = \sqrt{\text{Var}(\vec{w}_{\text{ideal}} \cdot \vec{w}(\infty))} \sim \sqrt{N}.$$

We find:

$$\text{SNR}(t) = \sqrt{N}(2f^{\text{pot}}f^{\text{dep}})\mathbf{p}^\infty \left(\mathbf{M}^{\text{pot}} - \mathbf{M}^{\text{dep}} \right) \exp(rt\mathbf{W}^{\text{F}}) \mathbf{w}.$$

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Complex synapses

└ Modelling synaptic complexity

└ Memory curve

1. of different synapses
2. ideal observer reads weights, not states
3. upper bound on electrical activity readout
4. ideal: pot→strong...
5. use $\vec{w}_{\text{ideal}} \cdot \vec{w}(\infty)$ as null model
6. Noise: ignore correction when asymmetric. No effect.
7. Using \mathbf{W}^{F} averages over pot/dep sequence (proof: expand)

\vec{w} is the N -element vector of synaptic weights.

$$\text{Signal} \sim \langle \vec{w}_{\text{ideal}} \cdot \vec{w}(t) - \vec{w}_{\text{ideal}} \cdot \vec{w}(\infty) \rangle,$$

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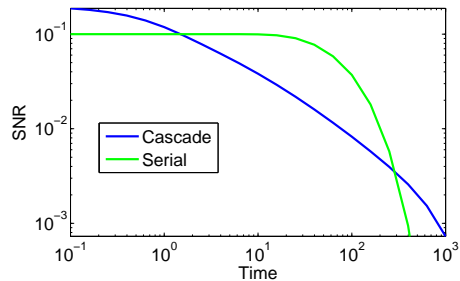
Example models

Two example models of complex synapses.



[Fusi et al. (2005), Leibold and Kempster (2008)]

These have different memory storage properties

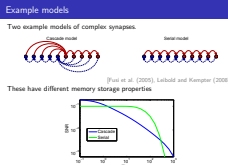


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Complex synapses

└ Modelling synaptic complexity

└ Example models



1. previous work, also: Benna-Fusi
2. Multistate good at one time, bad at others,
3. Cascade, less well at that time, better over range of times.

- Can we understand the space of *all possible* synaptic models?
- How does structure (topology) of model \rightarrow function (memory curve)?
- What are the limits on what can be achieved?
- Which transition topologies saturate these limits?

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Complex synapses

└ Modelling synaptic complexity

└ Questions

Questions

- Can we understand the space of all possible synaptic models?
- How does structure (topology) of model \rightarrow function (memory curve)?
- What are the limits on what can be achieved?
- Which transition topologies saturate these limits?

1. not just individual models
2. understand net (link on topology)
3. avoid using word “optimal”. depends on what want to do.

Memory curve given by

$$\text{SNR}(t) = \sqrt{N}(2f^{\text{pot}}f^{\text{dep}}) \mathbf{p}^\infty \left(\mathbf{M}^{\text{pot}} - \mathbf{M}^{\text{dep}} \right) \exp \left(rt \mathbf{W}^F \right) \mathbf{w}.$$

Constraints: $\mathbf{M}_{ij}^{\text{pot/dep}} \in [0, 1], \quad \sum_j \mathbf{M}_{ij}^{\text{pot/dep}} = 1.$

Eigenmode decomposition:

$$\text{SNR}(t) = \sqrt{N} \sum_a \mathcal{I}_a e^{-rt/\tau_a}.$$

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Complex synapses

└ Modelling synaptic complexity

└ Constraints

1. prefactors don't do anything, ignore
2. prior state, encoding, forgetting, readout
3. difficult to to apply
4. what are constraints on these?

Memory curve given by

$$\text{SNR}(t) = \sqrt{N}(2f^{\text{pot}}f^{\text{dep}}) \mathbf{p}^\infty \left(\mathbf{M}^{\text{pot}} - \mathbf{M}^{\text{dep}} \right) \exp \left(rt \mathbf{W}^F \right) \mathbf{w}.$$

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Section 3

Upper bounds

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Complex synapses
└ Upper bounds

Section 3

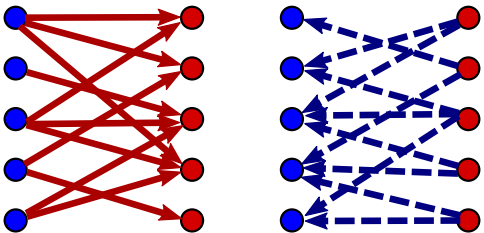
Upper bounds

Initial SNR as flux

Initial SNR is closely related to flux between strong & weak states

$$\text{SNR}(0) \leq \frac{4\sqrt{N}}{r} \Phi_{-+}.$$

Max when potentiation guarantees $\mathbf{w} \rightarrow +1$,
depression guarantees $\mathbf{w} \rightarrow -1$.



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Complex synapses

└ Upper bounds

└ Initial SNR

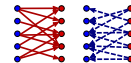
└ Initial SNR as flux

Initial SNR as flux

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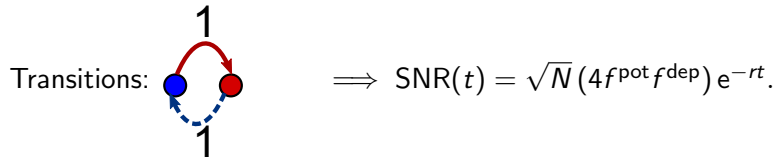
Max when potentiation guarantees $\mathbf{w} \rightarrow +1$,
depression guarantees $\mathbf{w} \rightarrow -1$.



1. flux = eq prob \times trans prob
2. usually saturated: pot never dec, dep never inc
3. transitions out of one node sum to 1
4. equivalent to two-state model: doesn't matter which strong/weak state, same prob of going to other set.

Two-state model

Two-state model equivalent to previous slide:



Maximal initial SNR:

$$\text{SNR}(0) \leq \sqrt{N}.$$

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Complex synapses
└ Upper bounds
└ Initial SNR
└ Two-state model

Two-state model

Two-state model equivalent to previous slide:



Maximal initial SNR:

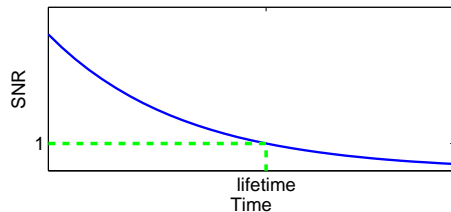
$$\text{SNR}(0) \leq \sqrt{N}.$$

1. decays very quickly
2. $f^{\text{pot}} = \frac{1}{2}$
3. Initial SNR not a good thing to optimise.

Area under memory curve

Memory lifetime bounded by area under SNR curve:

$$\text{SNR}(\text{lifetime}) = 1 \\ \Rightarrow \text{lifetime} < \mathcal{A}.$$



This area has an upper bound:

$$\mathcal{A} \leq \sqrt{N(M-1)}/r.$$

Saturated by a model with linear chain topology.

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Complex synapses

└ Upper bounds

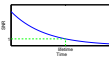
└ Area under memory curve

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Area under memory curve

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Saturated by a model with linear chain topology.

1. lifetime = area under green j area under blue
2. capacity $\sim r$ lifetime, #new memories before we forget original.
3. reminder: $N = \text{\#synapses}$, $M = \text{\#states}$
4. proof next slide

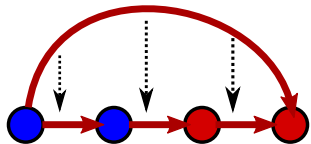
Proof of area bound

For any model, we can construct perturbations that

- preserve equilibrium distribution,
- increase area.

details

e.g. decrease “shortcut” transitions, increase bypassed “direct” ones.
Endpoint: linear chain



The area of this model is

$$A = \frac{2\sqrt{N}}{r} \sum_k \mathbf{p}_k^\infty |k - \langle k \rangle|.$$

Max: equilibrium probability distribution concentrated at both ends.

[Barrett and van Rossum (2008)]



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Complex synapses

└ Upper bounds

└ Area under memory curve

└ Proof of area bound

Proof of area bound

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Max: equilibrium probability distribution concentrated at both ends.

[Barrett and van Rossum (2008)]

1. relies on order & technical condition
2. max given \mathbf{p}^∞
3. now max wrt. \mathbf{p}^∞
4. keep c.o.m. in middle
5. similar result, slightly different conditions: linear weights, mutual info

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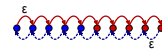
Complex synapses

└ Upper bounds

└ Area under memory curve

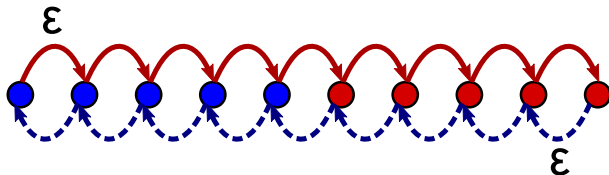
└ Saturating model

Make end states "sticky"



Has long decay time, but terrible initial SNR.

Make end states "sticky"



Has long decay time, but terrible initial SNR.

1. Difficult to get out of end state.
2. Area not a good thing to optimise

SNR curve: $SNR(t) = \sqrt{N} \sum_a \mathcal{I}_a e^{-rt/\tau_a}$.

subject to constraints:

$$\sum_a \mathcal{I}_a \leq 1, \quad \sum_a \mathcal{I}_a \tau_a \leq M - 1.$$

We can maximise wrt. \mathcal{I}_a, τ_a .

SNR curve:

$$SNR(t) = \sqrt{N} \sum_a \mathcal{I}_a e^{-rt/\tau_a}.$$

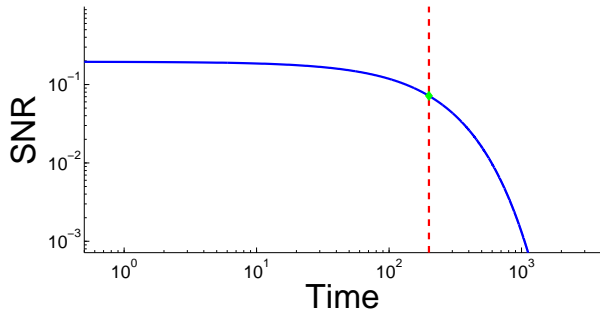
subject to constraints:

$$\sum_a \mathcal{I}_a \leq 1, \quad \sum_a \mathcal{I}_a \tau_a \leq M - 1.$$

We can maximise wrt. \mathcal{I}_a, τ_a .

1. from eigenmode decomposition
2. from initial, area bounds

Constructing the envelope



Maximise SNR at one time

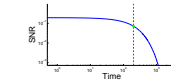
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Complex synapses

└ Envelope memory curve

└ Constructing the envelope

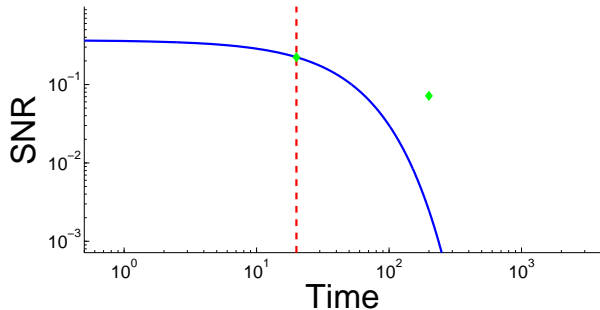
Constructing the envelope



Maximise SNR at one time

1. One exp. only constrains SNR at that time, not others

Constructing the envelope



Another time

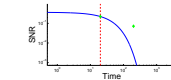
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Complex synapses

└ Envelope memory curve

└ Constructing the envelope

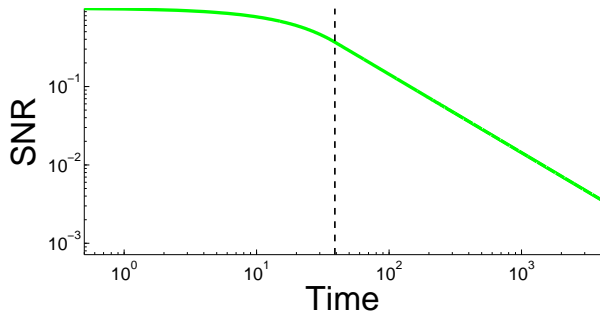
Constructing the envelope



Another time

1. One exp. only constrains SNR at that time, not others
2. get another bound

Constructing the envelope



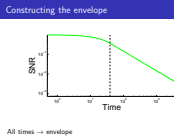
All times \rightarrow envelope

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Complex synapses

└ Envelope memory curve

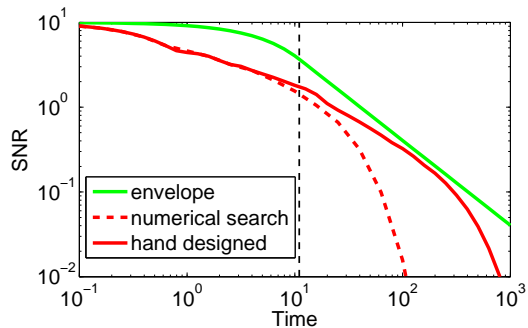
└ Constructing the envelope



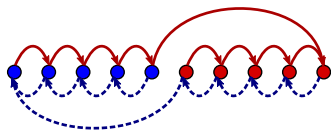
All times \rightarrow envelope

1. One exp. only constrains SNR at that time, not others
2. get another bound
3. vary time of max. no curve can cross this.
4. Regions: init(1); area(1,2)
5. Early: exp; Late: power-law, $\sim t^{-1}$
6. is it tight? can any constrained set of exps be achieved?

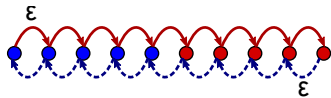
Achievable envelope



Early times:



Late times:

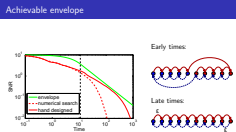


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Complex synapses

└ Envelope memory curve

└ Achievable envelope



1. Best we've found, by numerical opt and hand chosen models.
2. Models on next slide
3. vary length, keeping deterministic
4. Area maximising.

Lifetime of a memory bounded by where envelope crosses 1

$$\text{lifetime} \leq \frac{\sqrt{N}(M-1)}{er},$$

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Complex synapses
└ Envelope memory curve
└ Lifetime bound

Lifetime bound

Lifetime of a memory bounded by where envelope crosses 1

$$\text{lifetime} \leq \frac{\sqrt{N}(M-1)}{er},$$

1. Independent synapses?

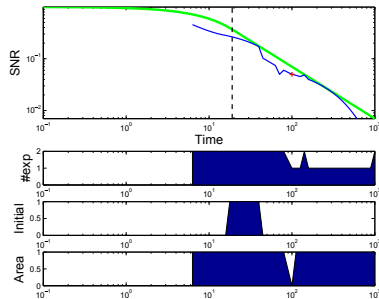
Two-time envelope

Maximise $\text{SNR}(t_1)$ subject to constraint $\text{SNR}(t_2) = S_2$.

For t_1 close to t_2 , get single exponential.

Far away, get two exponentials.

See tradeoff between $\text{SNR}(t_1)$ and $\text{SNR}(t_2)$.



Complex synapses

└ Envelope memory curve

└ Two-time envelope

1. Max at multiple times, \rightarrow multiple timescales? cascade? Benna-Fusi?
2. only implemented first 2 constraints
3. numerics not working. 2 exp solution need to solve 2 transcendental equations.

Two-time envelope

Maximise $\text{SNR}(t_1)$ subject to constraint $\text{SNR}(t_2) = S_2$.

For t_1 close to t_2 , get single exponential.
Far away, get two exponentials.

See tradeoff between $\text{SNR}(t_1)$ and $\text{SNR}(t_2)$.



- We have formulated a general theory of learning and memory with complex synapses.
- The area under the memory curve of any model $<$ linear chain with same equilibrium distribution.
- We find a memory envelope: a single curve that cannot be exceeded by the memory curve of *any* synaptic model.
- Synaptic complexity (M internal states) raises the memory envelope linearly in M for times $> \mathcal{O}(M^2)$.

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Complex synapses
└ Envelope memory curve
└ Summary

Summary

- We have formulated a general theory of learning and memory with complex synapses.
- The area under the memory curve of any model $<$ linear chain with same equilibrium distribution.
- We find a memory envelope: a single curve that cannot be exceeded by the memory curve of any synaptic model.
- Synaptic complexity (M internal states) raises the memory envelope linearly in M for times $> \mathcal{O}(M^2)$.

Thanks to:

- Surya Ganguli
- Stefano Fusi
- Marcus Benna
- David Sussillo
- Jascha Sohl-Dickstein

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Complex synapses

└ Envelope memory curve

└ Acknowledgements

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1. Last slide!

References I



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└ Envelope memory curve

└ References

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Complex synapses

└ Envelope memory curve

└ References

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Complex synapses

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Technical detail: ordering states

Let \mathbf{T}_{ij} = mean first passage time from state i to state j . Then:

$$\eta = \sum_j \mathbf{T}_{ij} \mathbf{p}_j^\infty,$$

is independent of the initial state i (Kemeney's constant).

[Kemeny and Snell (1960)]

We define:

$$\eta_i^+ = \sum_{j \in \text{strong}} \mathbf{T}_{ij} \mathbf{p}_j^\infty, \quad \eta_i^- = \sum_{j \in \text{weak}} \mathbf{T}_{ij} \mathbf{p}_j^\infty.$$

They can be used to arrange the states in an order (increasing η^- or decreasing η^+). [back](#)

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Complex synapses

└ Envelope memory curve

└ Technical detail: ordering states

1. Measure “distance” to the strong/weak states.
2. sum to constant, \implies two orders same

Technical detail: ordering states

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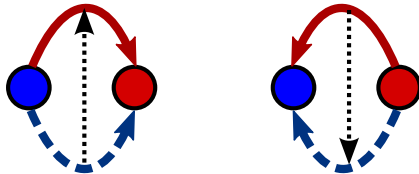
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Technical detail: upper/lower triangular

With states in order:



Endpoint: potentiation goes right, depression goes left.

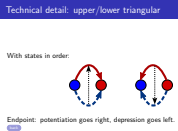
[back](#)

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Complex synapses

└ Envelope memory curve

└ Technical detail: upper/lower triangular



1. pot & dep with same initial & final state
2. pot/dep matrices are upper/lower triangular.
3. one other pert. too technical, even for bonus slide!