Understanding impaired learning with enhanced plasticity

based on work in preparation with: T.D. Barbara Nguyen-Vu, Grace Q. Zhao, Han-Mi Lee, Surya Ganguli, Carla J. Shatz, Jennifer L. Raymond

Subhaneil Lahiri

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1. Acknowledge Barbara and Grace

Introduction

Learning requires synaptic plasticity.
Expect enhanced plasticity $\rightarrow$ enhance learning.

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2. Want to understand when and why
3. Depends on circumstance. Rich pattern of behaviour
4. Develop understanding of when and why learning is enhanced/impaired

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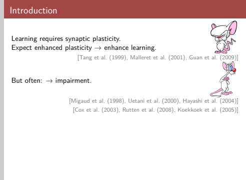
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Simple synapses cannot explain behaviour.
→ Necessary & sufficient conditions on complex synapses to replicate this.

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Outline

- Motor learning
  - Cerebellar learning of mice with enhanced plasticity
  - Complex synaptic models
- (Memory capacity of complex synapses)

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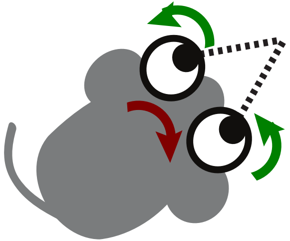
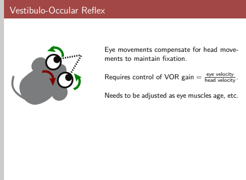
Vestibulo-Occular Reflex



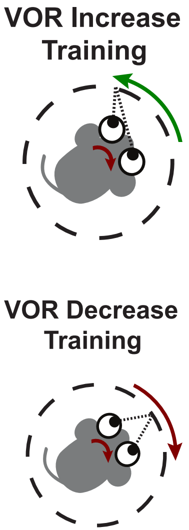
Eye movements compensate for head movements to maintain fixation.

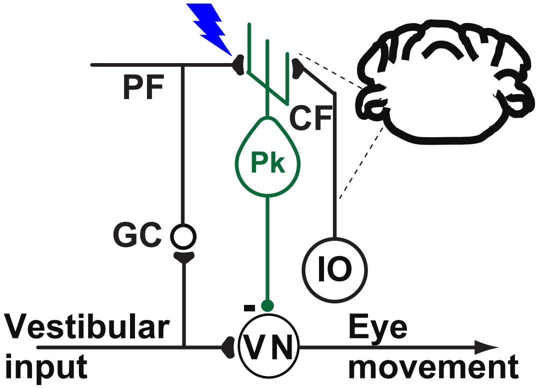
Requires control of VOR gain $= \frac{\text{eye velocity}}{\text{head velocity}}$.

Needs to be adjusted as eye muscles age, etc.



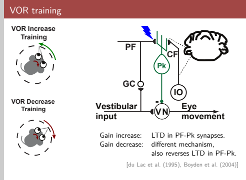
VOR training





Gain increase: LTD in PF-Pk synapses.
Gain decrease: different mechanism, also reverses LTD in PF-Pk.

[du Lac et al. (1995), Boyden et al. (2004)]



1. trick brain into thinking VOR gain needs adjusting my moving visual stimulu
2. anti-phase → increase gain
3. in phase → decrease gain
4. Gain change involves cerebellum
5. If we enhanced plasticity here: expect enhanced learning

Enhanced plasticity impairs learning

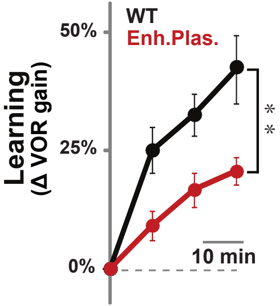
Knockout of MHC-I D^bK^b molecules in PF-Pk synapses

[McConnell et al. (2009)]

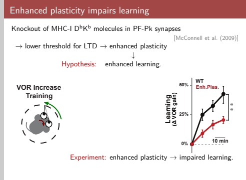
→ lower threshold for LTD → enhanced plasticity

↓

Hypothesis: enhanced learning.



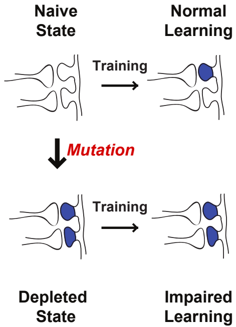
Experiment: enhanced plasticity → impaired learning.

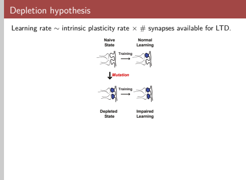


1. Major Histocompatibility Complex - involved in synaptic plasticity (Carla Shatz lab)
2. Easier LTD → expect better learning
3. Impairment of learning
4. Looking at change of VOR gain during gain-up training

Depletion hypothesis

Learning rate $\sim$ intrinsic plasticity rate $\times$ # synapses available for LTD.





1. Our model: baseline activity $\to$ saturation $\to$ less depression possible
2. Saturation has to compete with enhanced plsaticity. Which will win?

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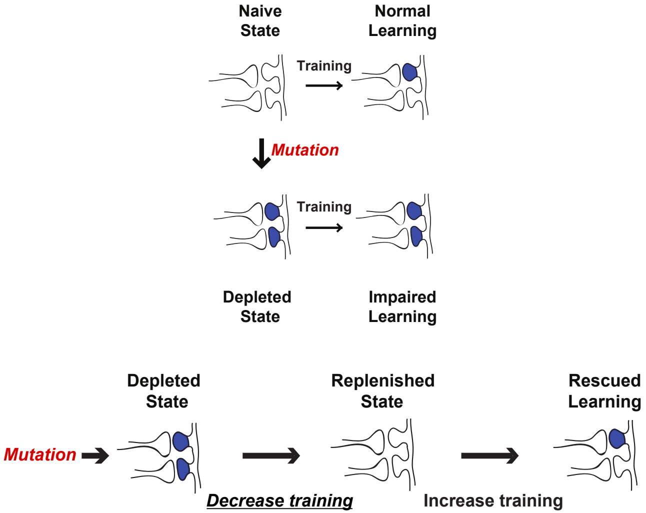
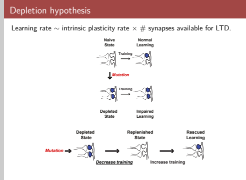
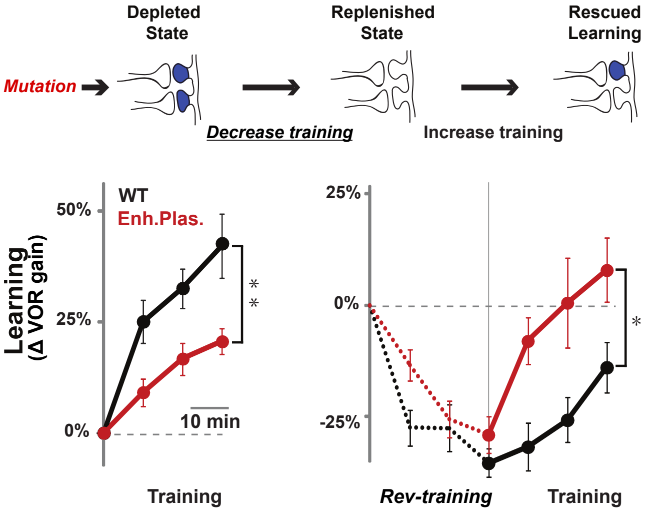
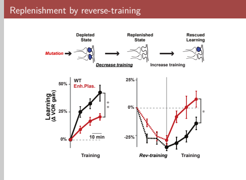




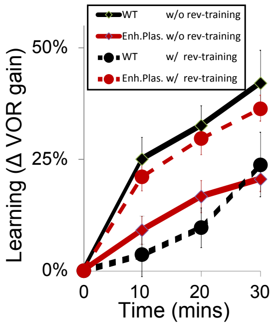
1. Our model: baseline activity $\to$ saturation $\to$ less depression possible
2. Saturation has to compete with enhanced plsaticity. Which will win?
3. Prediction: replenish with rev-training $\to$ rescue

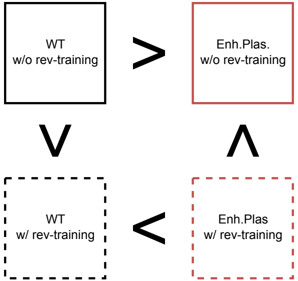


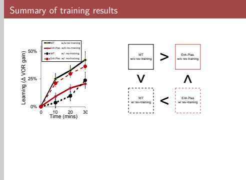


1. precede gain inc training w/ gain dec rev-training: reverses LTD
2. but behaviour from elsewhere → not modelled
3. Focus on gain inc part

Summary of training results







1. Restricted to gain inc for comparison
2. Solid: no pre. Dashed: with pre
3. Initial slope only

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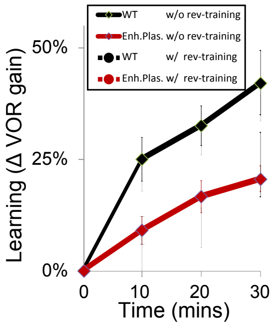
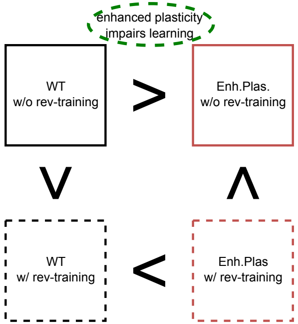
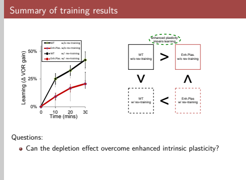




Questions:

- Can the depletion effect overcome enhanced intrinsic plasticity?



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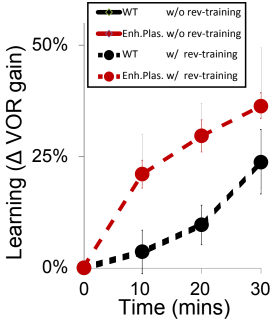

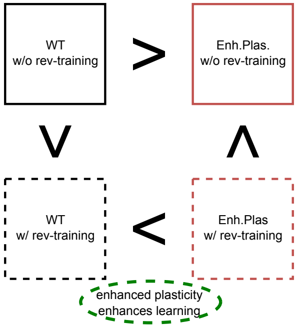

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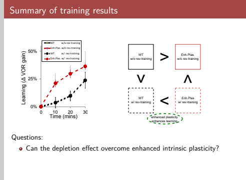

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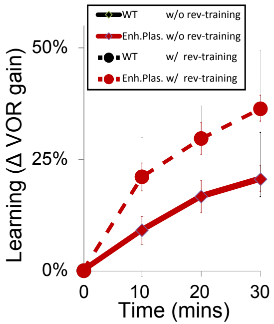

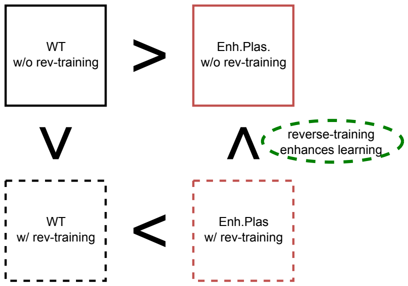

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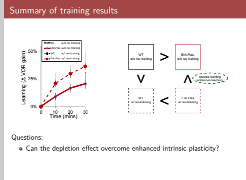

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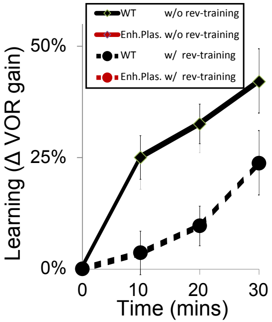

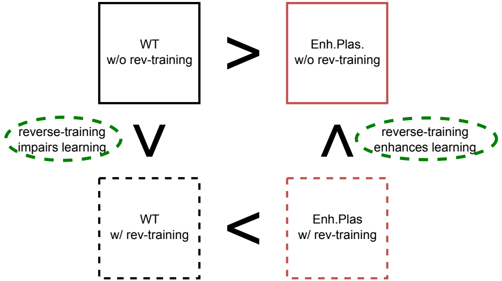

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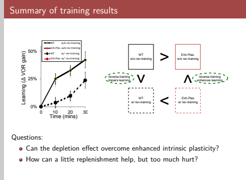
- How can a little replenishment help, but too much hurt?



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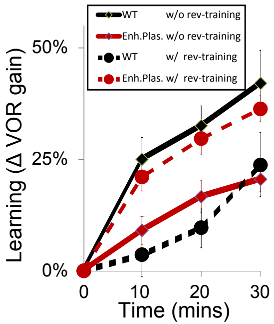

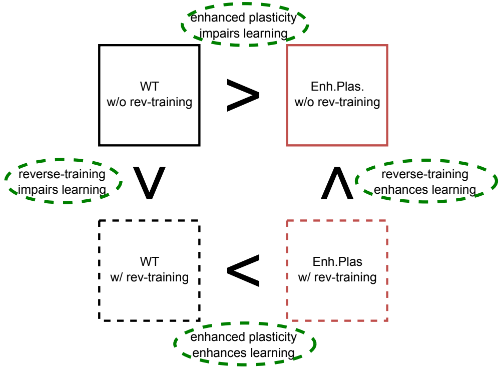

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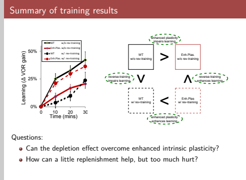

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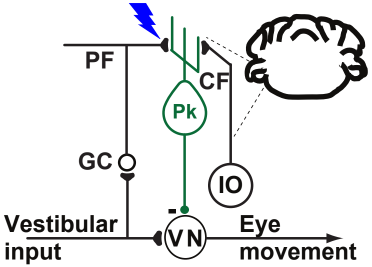
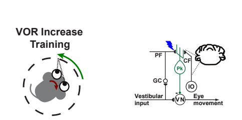
9. Summarize: Enh.Plas. can impair/enhance. Rev can impair/enhance
10. Diagonal comparisons: parameter fitting. Depend on size of mut vs. rev

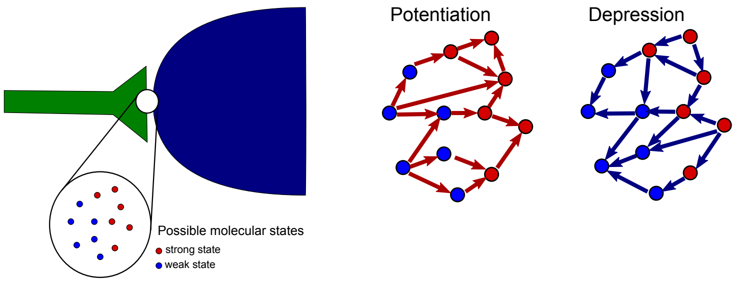
Behaviour to synapses





1. Focus on synapses. See if we can understand this behaviour.

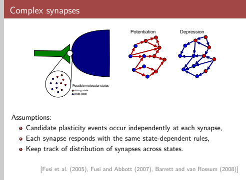
Complex synapses



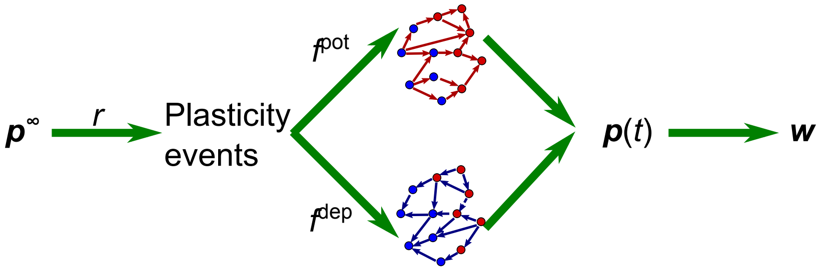
Assumptions:

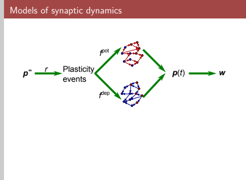
- Candidate plasticity events occur independently at each synapse,
- Each synapse responds with the same state-dependent rules,
- Keep track of distribution of synapses across states.

[Fusi et al. (2005), Fusi and Abbott (2007), Barrett and van Rossum (2008)]

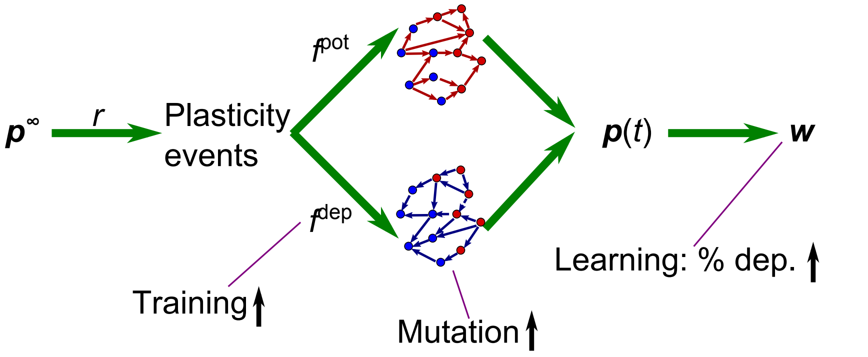


1. Not just synaptic weight, internal dynamical system
2. Important for memory: simple synapses – terrible storage, rescued by complexity
3. Multiple functional states w/ different weights
4. Stochastic transitions between states
5. allows us to concentrate on synapse, not neuron/network
6. This is a question about synaptic populations after all.





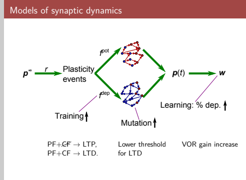
1. stoch process has steady state distribution.
2. Prior activity puts it in this state. row vec.
3. plasticity events at rate r
4. fraction pot/dep
5. probs changed by Markov matrices, prob $i \to j$
6. Readout: synaptic weight vec when in each state.



PF+$\cancel{CF}$ → LTP,
PF+CF → LTD.

Lower threshold for LTD

VOR gain increase



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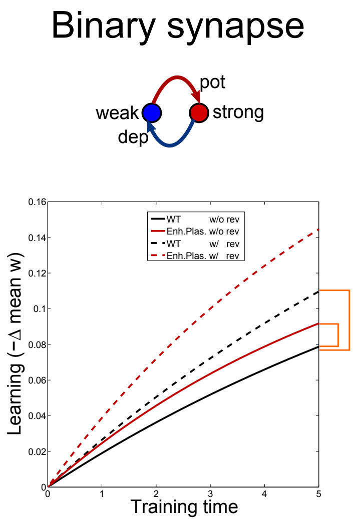
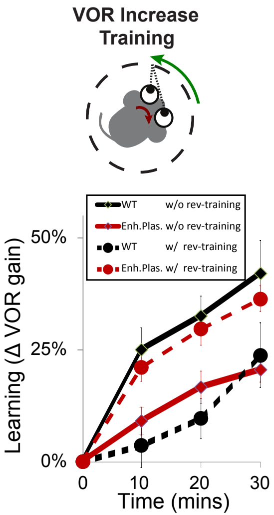
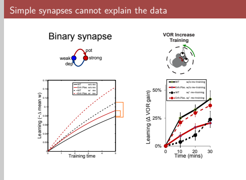
5. probs changed by Markov matrices, prob $i \to j$
6. Readout: synaptic weight vec when in each state.
7. Mutation: lower threshold → increase transition probs
8. Training: Changes statistics of LTP/LTD. Only parameters we have. Don't care about r.
9. Learning: Only output we have. Don't keep track of synaptic identity.

Simple synapses cannot explain the data

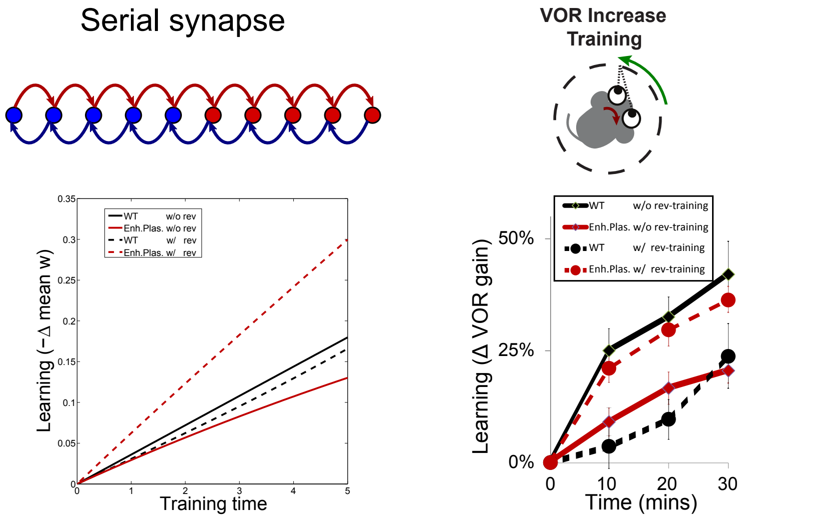




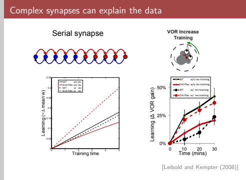


1. Binary fails – mathematical proof for any params
2. Enh.Plas: faster depression wins over bias
3. pre: reduces/reverses bias. always helps.

Complex synapses can explain the data

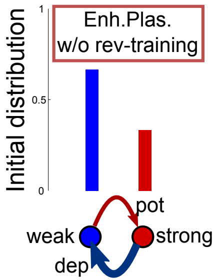


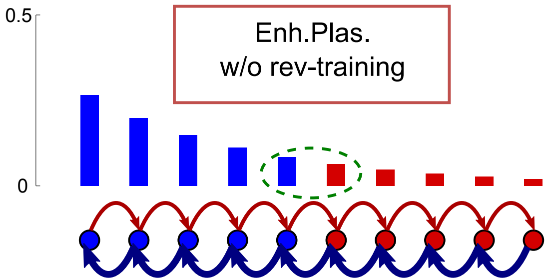
[Leibold and Kempter (2008)]



1. Serial: still only two weights. Works.
2. Understand by looking at distributions before training

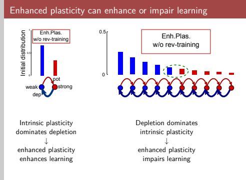
Enhanced plasticity can enhance or impair learning





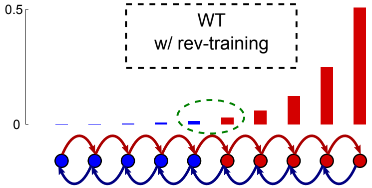
Intrinsic plasticity dominates depletion
↓
enhanced plasticity enhances learning

Depletion dominates intrinsic plasticity
↓
enhanced plasticity impairs learning

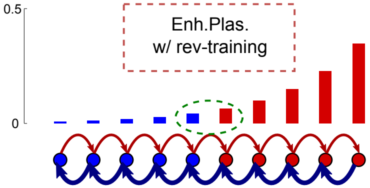


1. Binary: enhanced plasticity → bias
2. Not enough to overcome faster depression
3. Serial: Only get signal from boundary
4. Exponential decay depopulates boundary, enhances effect of bias

Reverse-training can impair or enhance learning



reverse-training
depopulates boundary
↓
impaired learning



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repopulates boundary
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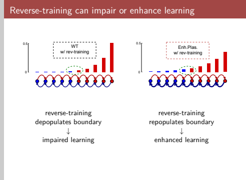
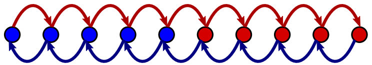
enhanced learning



1. rev-training: little repopulates boundary
2. Too much pushes to other side, depopulates boundary
3. this effect is absent in any simple synapse

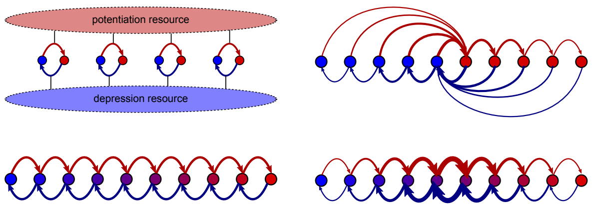
Essential features



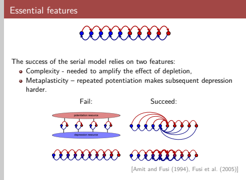
The success of the serial model relies on two features:

- Complexity - needed to amplify the effect of depletion,
- Metaplasticity – repeated potentiation makes subsequent depression harder.

Fail: Succeed:



[Amit and Fusi (1994), Fusi et al. (2005)]



1. due to exponential decay
2. push away from boundary where signal generated
3. borne out by other models that fail/succeed

Conclusions

- We find diverse behavioural patterns in these mutant mice:
  Enhanced plasticity $\rightarrow$ enhance/impair learning depending on prior experience.
  Reverse-training $\rightarrow$ enhance/impair learning depending on plasticity rates.
- We can explain these behavioural patterns using synaptic models.
- Key required synaptic properties are:
  Synaptic complexity: necessary to amplify depletion.
  Synaptic stubbornness: repeated potentiation makes subsequent depression harder.
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Tradeoff: learning vs. remembering

What about memory?

- Simple synapses have poor memory storage capacity.
  Synaptic complexity is needed for rescue.
  [Amit and Fusi (1992), Amit and Fusi (1994)]

- Trade-off between learning and remembering:
  Too rigid $\rightarrow$ difficult to learn new memories.
  Too plastic $\rightarrow$ new memories quickly overwrite old.

- Exploring the *entire* space of complex synaptic models
  $\rightarrow$ upper bounds on their storage ability
  & the models that saturate them.

  [Lahiri and Ganguli (submitted)]

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The frontiers of complex synaptic memory

We have N synapses with M internal states each.

We study the decay of one memory over time due to corruption by subsequent memories.

We prove that, no matter what the structure, no synaptic model can have:

- initial fidelity (SNR) greater than $\sqrt{N}$.
- memory lifetime greater than $\sim \sqrt{N}M$.
- fidelity decay slower than $\sim \sqrt{N}M/t$.

At late times, fidelity is maximised by a model with a simple chain structure.

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Impaired learning with enhanced plasticity

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