

# Modelling impaired and enhanced learning with enhanced plasticity

Subhaneil Lahiri

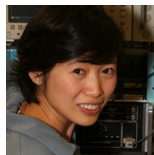
with: Barbara Nguyen-Vu, Grace Zhao, Aparna Suvrathan, Han-Mi Lee, Surya Ganguli, Carla Shatz and Jennifer Raymond

Stanford University

December 3, 2014



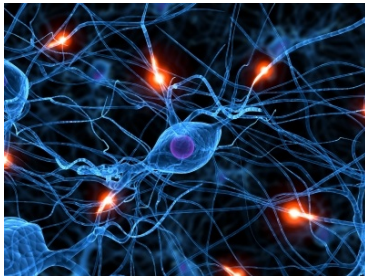
Barbara Nguyen-Vu



Grace Zhao

# Introduction

Learning requires synaptic plasticity.

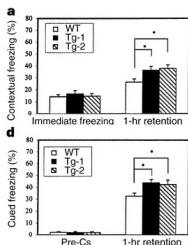


Can we enhance learning by enhancing plasticity?

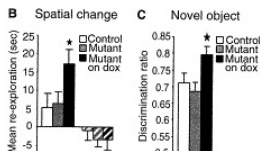


# Enhanced plasticity *can* enhance learning

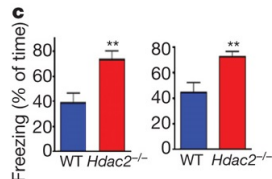
## Overexpress NR2B



## Inhibit CN



## Knockout Hdac2



## Fear conditioning

[Tang et al. (1999)]

## Novel object recog.

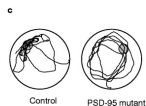
[Malleret et al. (2001)]

## Fear conditioning

[Guan et al. (2009)]

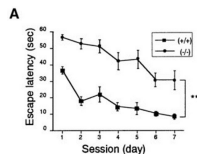
# Enhanced plasticity can *impair* learning

Mutate PSD-95



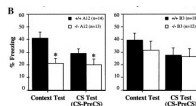
Water maze

Knockout PTP $\delta$



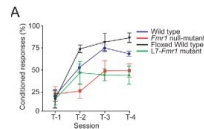
Water maze

Delete Tmod2



Fear cond.

Knockout FMR1



Eyeblink

[Migaud et al. (1998)][Uetani et al. (2000)] [Cox et al. (2003)] [Koekkoek et al. (2005)]

also: [Hayashi et al. (2004), Rutten et al. (2008)]

# Overview

Sometimes enhanced plasticity  $\rightarrow$  enhanced learning.  
Sometimes enhanced plasticity  $\rightarrow$  impaired learning.

Why? How? When?



# Overview

Sometimes enhanced plasticity → enhanced learning.  
Sometimes enhanced plasticity → impaired learning.

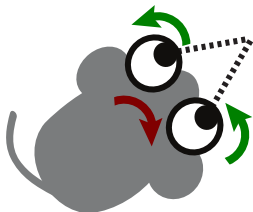


Why? How? When?

Mice with enhanced cerebellar plasticity can show **both** impaired and enhanced learning.

Simple synapses **cannot** explain behaviour. **Complex synapses** are required.  
→ predictions for synaptic physiology.

# Vestibulo-Occular Reflex



Eye movements compensate for head movements  
 $\Rightarrow$  stabilise image on retina.

Requires control of VOR gain =  $\frac{\text{eye velocity}}{\text{head velocity}}$ .

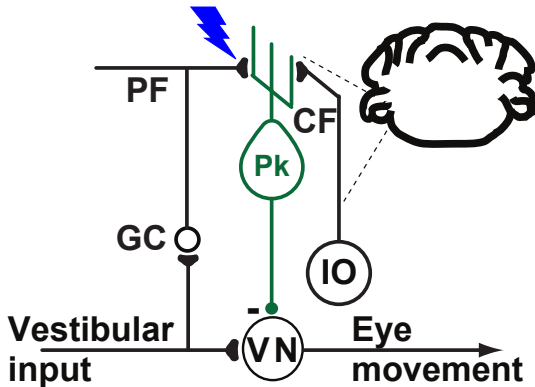
Needs to be adjusted as eye muscles age, etc.

# Vestibulo-Ocular Reflex training

## VOR Increase Training



## VOR Decrease Training



VOR increase: LTD in PF-P<sub>k</sub> synapses.  
VOR decrease: different mechanism,  
also reverses LTD in PF-P<sub>k</sub>.

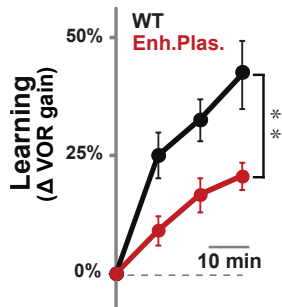
[Marr (1969), Albus (1971), Ito (1972)]



# Enhanced plasticity impairs learning

**Expectation:** enhanced LTD → enhanced learning.

**VOR Increase  
Training**



**Experiment:** enhanced plasticity → impaired learning.

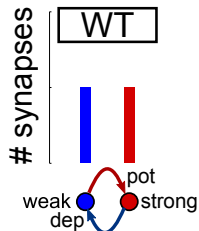
Knockout of MHC-I K<sup>b</sup>D<sup>b</sup> molecules in PF-Pk synapses

→ lower threshold for LTD

[McConnell et al. (2009)]

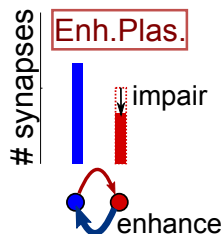
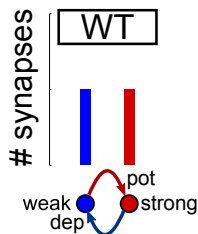
# Depletion hypothesis

Learning rate  $\sim$  intrinsic plasticity rate  $\times$  # synapses available for LTD.



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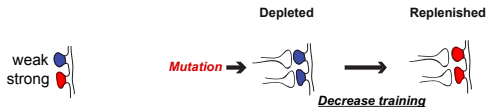


**Question 1:** depletion effect competes with enhanced intrinsic plasticity.  
When is depletion effect stronger?

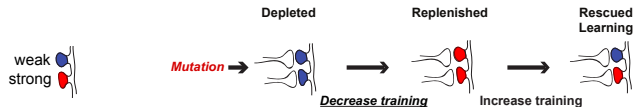
# Replenishment by reverse-training



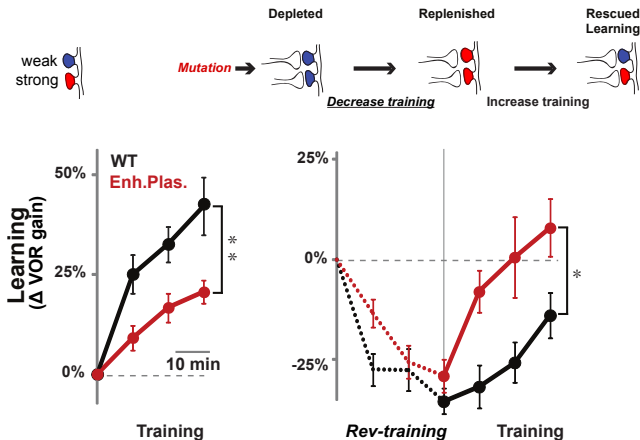
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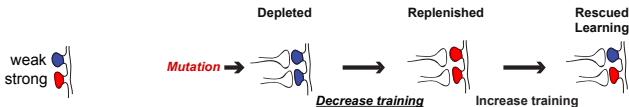
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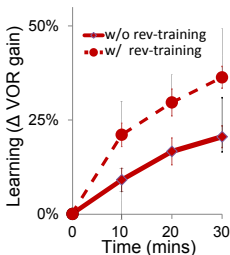
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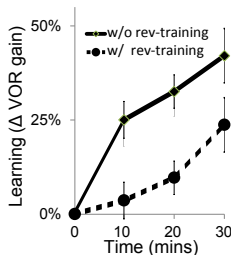
# Replenishment by reverse-training



Enh. Plast.



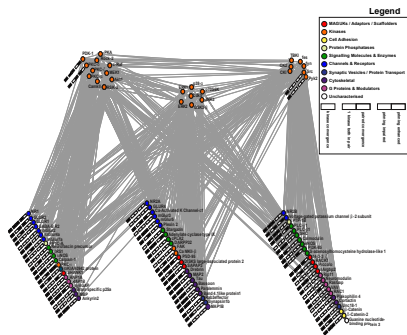
WT



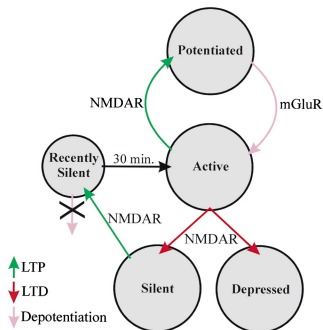
**Question 2:** How can replenishment ever impair learning?



# Synapses are complex



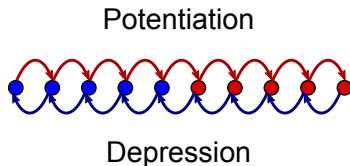
[Coba et al. (2009)]



[Montgomery and Madison (2002)]

# Models of complex synaptic dynamics

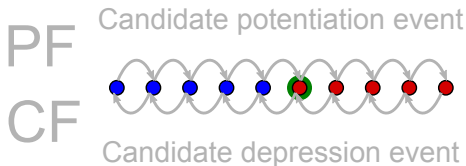
- Internal functional state of synapse  $\rightarrow$  synaptic weight.
  - Candidate plasticity events  $\rightarrow$  transitions between states
- weak  
● strong



[Fusi et al. (2005), Fusi and Abbott (2007), Barrett and van Rossum (2008)]  
[Smith et al. (2006), Lahiri and Ganguli (2013)]

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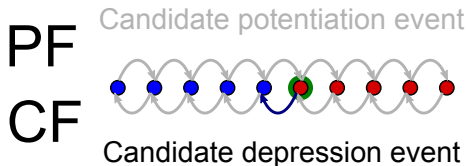
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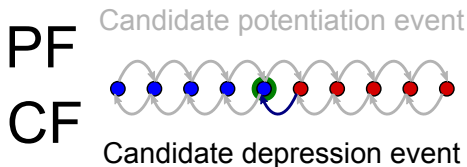
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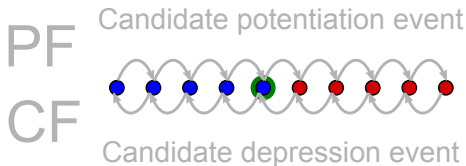
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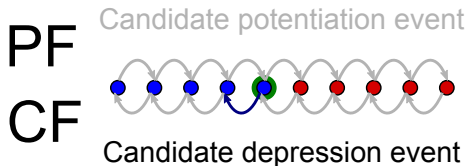
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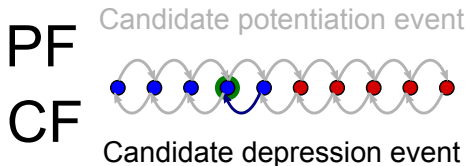
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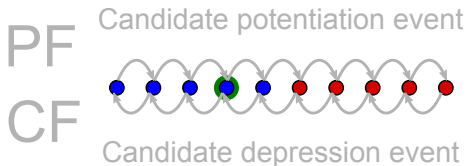


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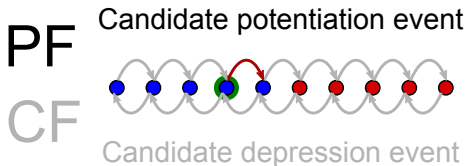
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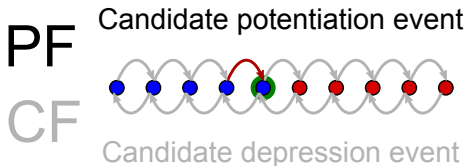
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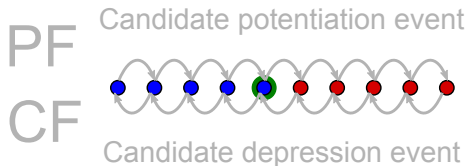
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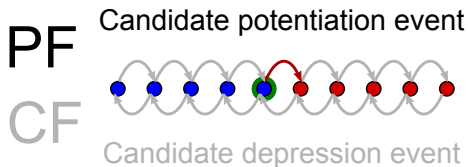
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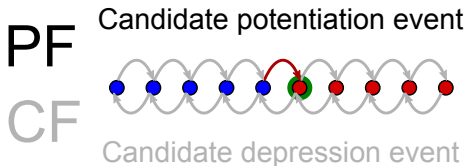
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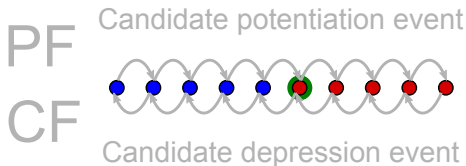
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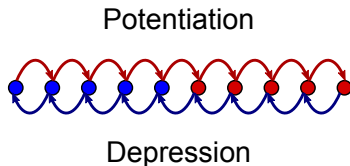
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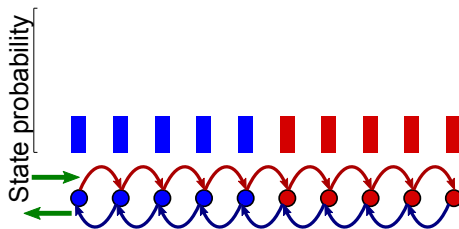
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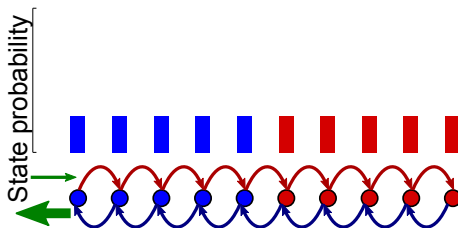
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# Modelling VOR experiments

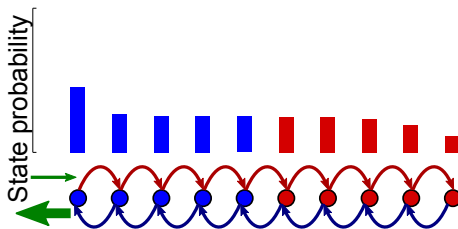


# Modelling VOR experiments



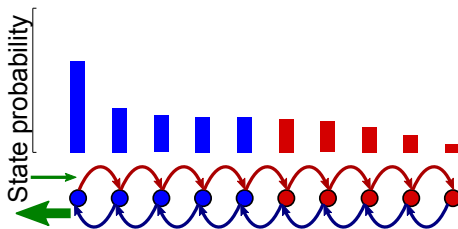
Training: different CF activity  $\Rightarrow$   
change frequency of pot/dep events.

# Modelling VOR experiments



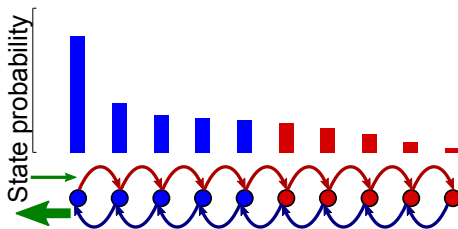
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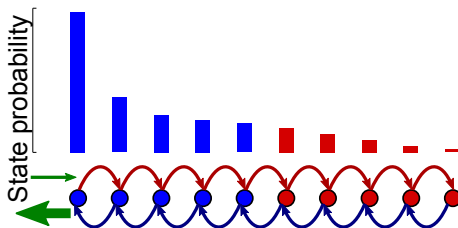
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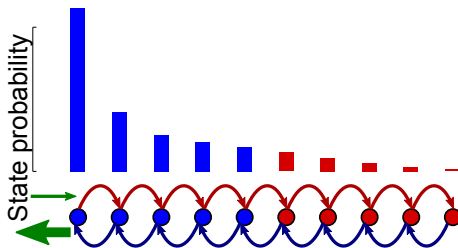
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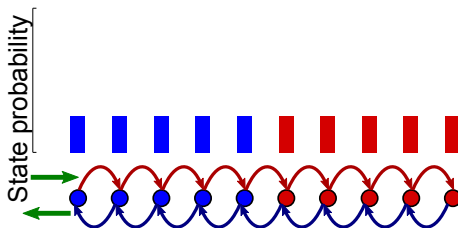
# Modelling VOR experiments



Training: different CF activity  $\Rightarrow$   
change frequency of pot/dep events.

Learning: decrease in average synaptic weight.

# Modelling VOR experiments



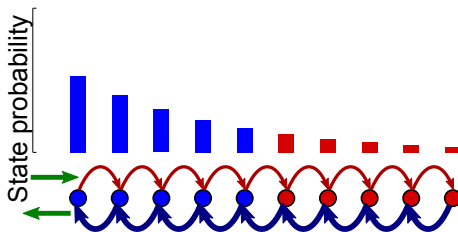
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Mutation: lower threshold for LTD  $\Rightarrow$   
increase transition probability for depression events.



# Modelling VOR experiments



Training: different CF activity  $\Rightarrow$   
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Learning: decrease in average synaptic weight.

Mutation: lower threshold for LTD  $\Rightarrow$   
increase transition probability for depression events.

# Questions

Depletion effect competes with enhanced intrinsic plasticity.

**Question 1:** When is the depletion effect stronger?

Reverse training impairs learning in wild-type.

**Question 2:** How can replenishment *ever* impair learning?

Enhanced plasticity → enhanced/impaired learning

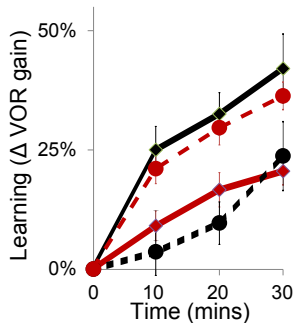
**Big question:** Why?

# Simple synapses cannot explain the data

Multistate synapse

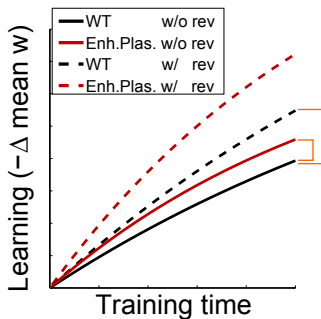
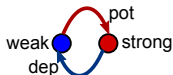


VOR Increase Training

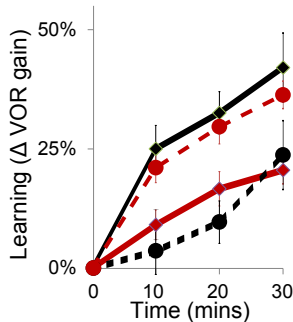


# Simple synapses cannot explain the data

## Binary synapse

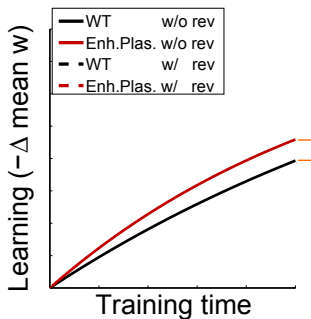
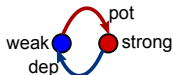


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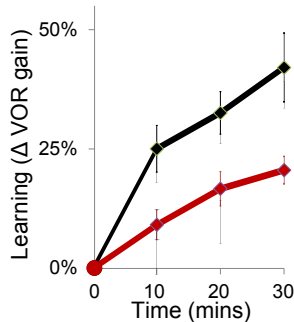


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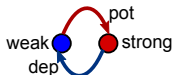


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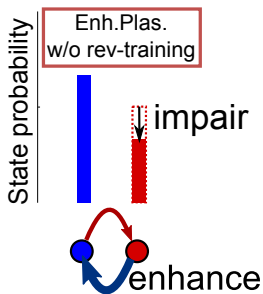


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## Binary synapse



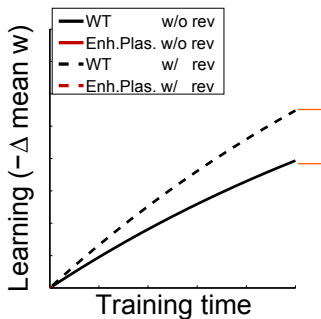
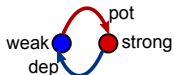
## Initial distribution



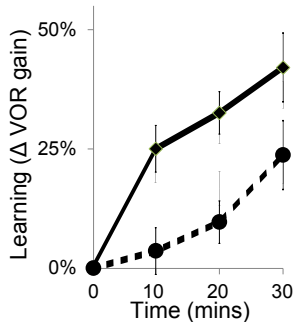
depletion effect  
<  
enhanced plasticity  
 $\Rightarrow$  enhanced learning

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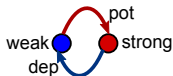


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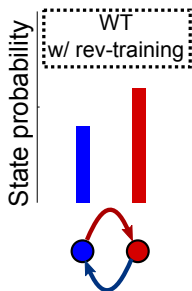


# Simple synapses cannot explain the data

## Binary synapse



## Initial distribution



reverse training



replenishment

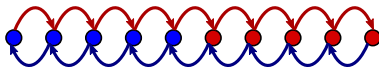


enhanced learning

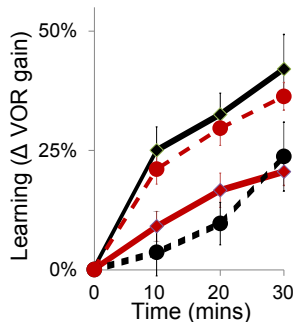
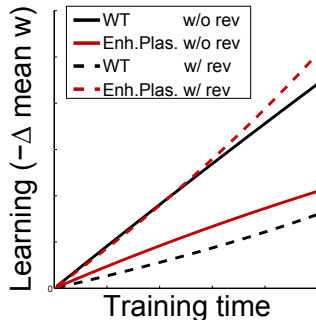


# Complex metaplastic synapses can explain the data

## Serial synapse



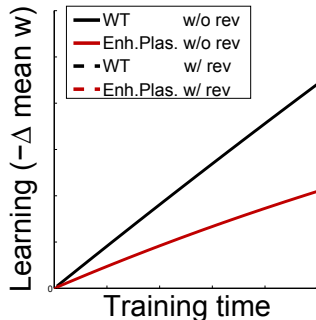
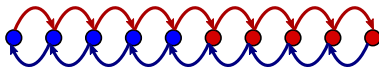
## VOR Increase Training



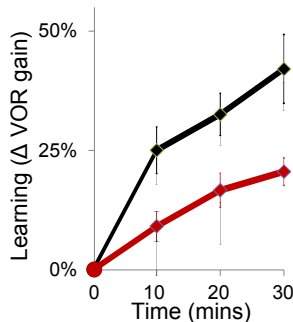
[Leibold and Kempter (2008), Ben-Dayan Rubin and Fusi (2007)]

# Complex metaplastic synapses can explain the data

## Serial synapse



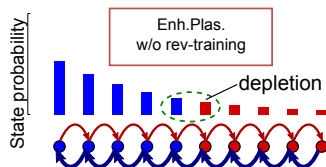
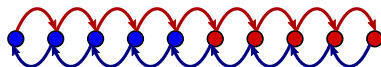
## VOR Increase Training



[Leibold and Kempter (2008), Ben-Dayan Rubin and Fusi (2007)]

# Complex metaplastic synapses can explain the data

## Serial synapse



amplified depletion

>

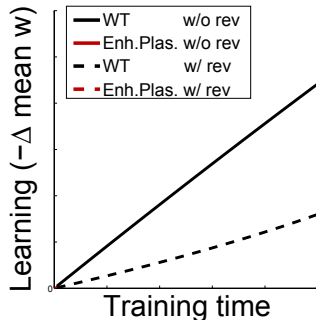
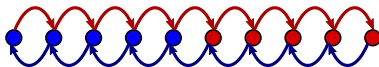
enhanced plasticity

⇒ impaired learning

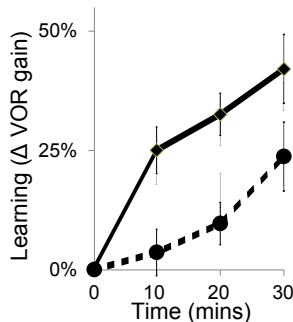
[Leibold and Kempter (2008), Ben-Dayan Rubin and Fusi (2007)]

# Complex metaplastic synapses can explain the data

## Serial synapse



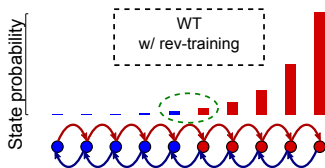
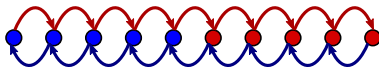
## VOR Increase Training



[Leibold and Kempter (2008), Ben-Dayan Rubin and Fusi (2007)]

# Complex metaplastic synapses can explain the data

## Serial synapse

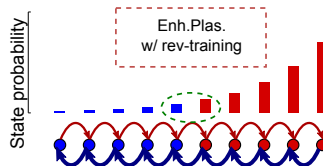
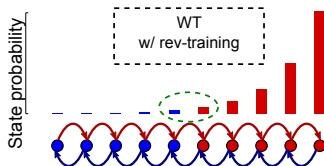
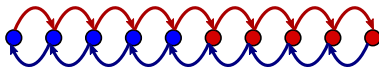


reverse training  
+  
“stubborn” metaplasticity  
⇒ impaired learning

[Leibold and Kempter (2008), Ben-Dayan Rubin and Fusi (2007)]

# Complex metaplastic synapses can explain the data

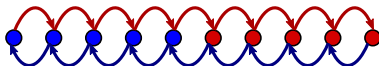
## Serial synapse



[Leibold and Kempter (2008), Ben-Dayan Rubin and Fusi (2007)]

# Complex metaplastic synapses can explain the data

## Serial synapse



starting point:  
labile states



enhanced plasticity  
 $\Rightarrow$  impaired learning

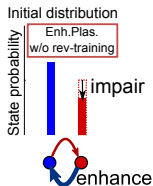
starting point:  
stubborn states



enhanced plasticity  
 $\Rightarrow$  enhanced learning

[Leibold and Kempter (2008), Ben-Dayan Rubin and Fusi (2007)]

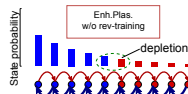
# Enhanced plasticity can enhance or impair learning



Intrinsic plasticity  
dominates depletion

↓

enhanced plasticity  
enhances learning



Depletion dominates  
intrinsic plasticity

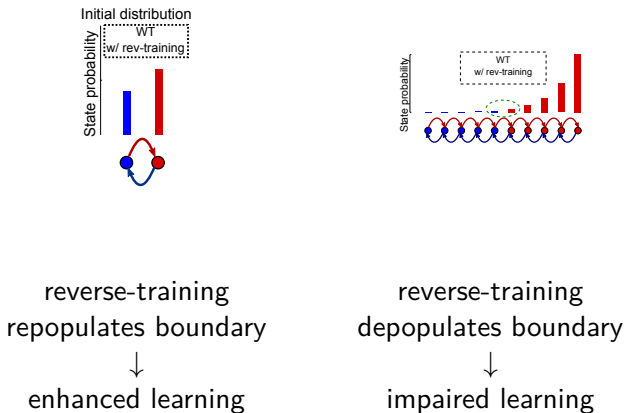
↓

enhanced plasticity  
impairs learning

**Key feature 1:** Synaptic complexity that amplifies depletion effect.

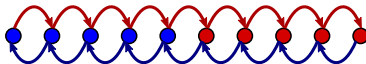


# Reverse-training can impair or enhance learning



**Key feature 2:** Synaptic stubbornness – metaplasticity where repeated potentiation impairs subsequent depression.

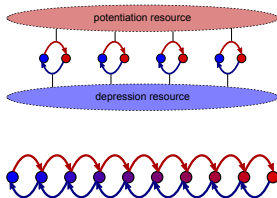
# Essential features



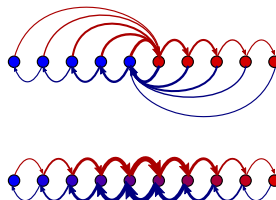
The success of the serial model relies on two features:

- Complexity - needed for depletion to dominate enhanced plasticity,
- Stubbornness - repeated potentiation impairs subsequent depression.

Fail:



Succeed:



[Amit and Fusi (1994), Fusi et al. (2005)]

# Conclusions

- Diverse behavioural patterns:  
Enhanced plasticity → enhance/impair learning (prior experience).  
Reverse-training → enhance/impair learning (plasticity rates).
- enhanced LTD vs. depletion → learning outcome.
- Predictions for synaptic physiology:  
Complexity: necessary to amplify depletion.  
Stubbornness: repeated potentiation impairs subsequent depression.
- We used behaviour to constrain the dynamics of synaptic plasticity.



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Barbara Nguyen-Vu

Grace Zhao

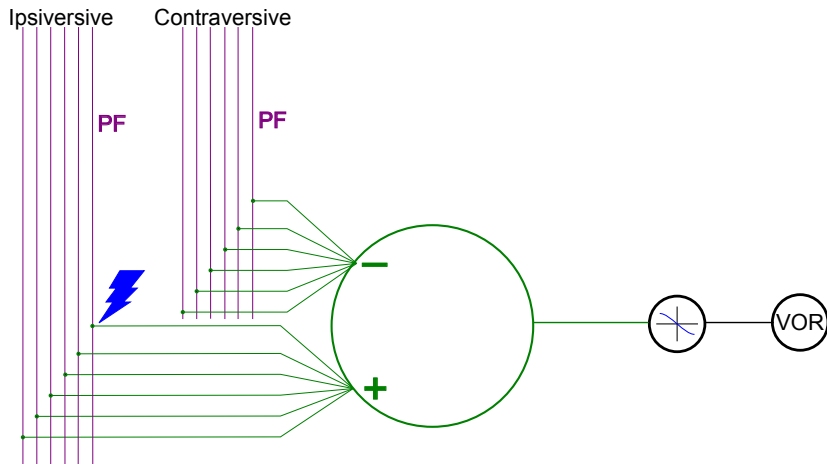
Aparna Suvrathan

**Carla Shatz**

Han-Mi Lee

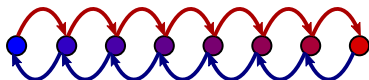
**Funding:** Swartz Foundation, Stanford Bio-X Genentech fellowship.

# Model of circuit

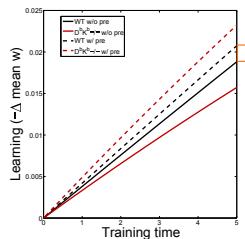
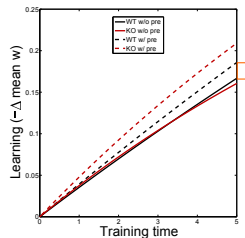
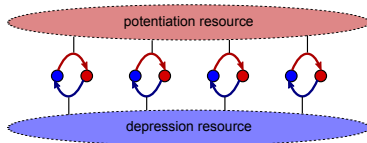


# Other models that fail

## Multistate synapse



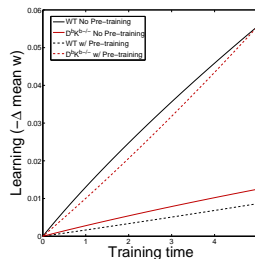
## Pooled resource model



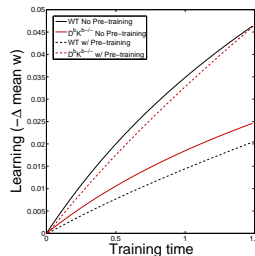
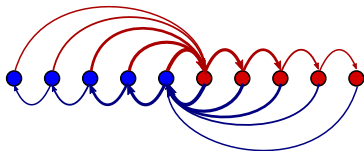
[Amit and Fusi (1994)]

# Other models that work

Non-uniform multistate model

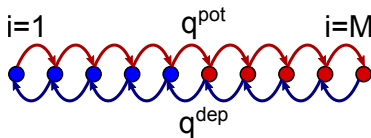


Cascade model



[Fusi et al. (2005)]

# Mathematical explanation



Serial synapse:  $\mathbf{p}_i^\infty \sim \mathcal{N} \left( \frac{q^{\text{pot}}}{q^{\text{dep}}} \right)^i$ .

Learning rate  $\sim \mathbf{p}_{M/2}^\infty \left( \frac{q^{\text{dep}}}{q^{\text{pot}}} \right) = \mathcal{N} \left( \frac{q^{\text{pot}}}{q^{\text{dep}}} \right)^{\frac{M}{2}-1}$ .

For  $M > 2$ : larger  $q^{\text{dep}} \implies$  slower learning.

For  $M = 2$ : larger  $q^{\text{dep}} \implies$  larger  $\mathcal{N} \implies$  faster learning.



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