

Learning and memory with complex synaptic plasticity

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Introduction

Synaptic plasticity is often modelled as the change of a single number. But, there is a complex dynamical system inside a synapse.

We will study the entire space of a broad class of models of complex synapses to find upper bounds on their performance.

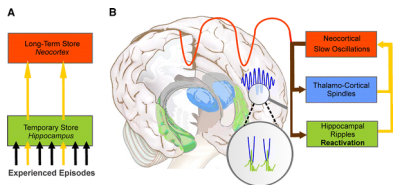
This leads to understanding of what structures are useful for storing memories for different timescales.

Timescales of memory

Memories stored in different places
for different timescales

[Squire and Alvarez (1995)]

[McClelland et al. (1995)]



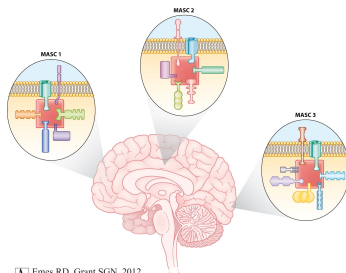
[Born and Wilhelm (2012)]

Also: Cerebellar cortex → nuclei.

[Attwell et al. (2002)]

[Cooke et al. (2004)]

Different synapses have different
molecular structures.



[Emes RD, Grant SGN, 2012.
Annu. Rev. Neurosci. 35:111–31]

[Emes and Grant (2012)]

Storage capacity of synaptic memory

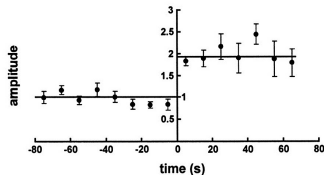
A classical perceptron has a capacity $\propto N$, ($\#$ synapses).

Requires synapses' dynamic range also $\propto N$.

With discrete, finite synapses:

\implies new memories overwrite old,

\implies stability-plasticity dilemma.



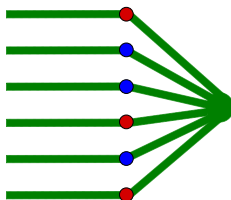
[Petersen et al. (1998), O'Connor et al. (2005)]

When we store new memories rapidly, memory capacity $\sim \mathcal{O}(\log N)$.

[Amit and Fusi (1992), Amit and Fusi (1994)]

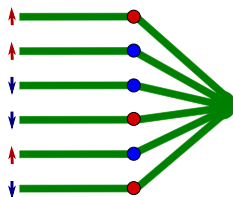
Recognition memory

Synapses given a sequence of patterns (pot & dep) to store



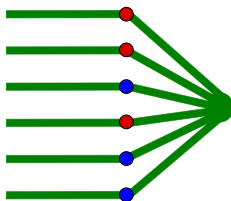
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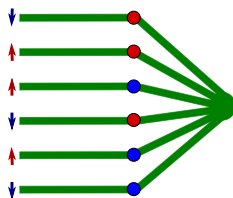
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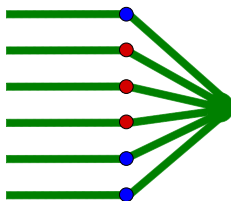
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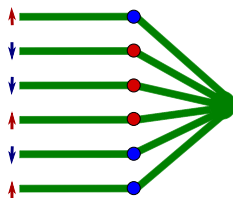
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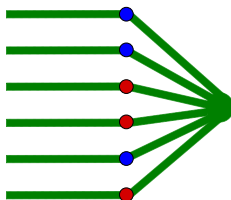
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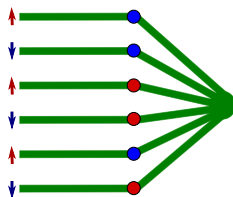
Recognition memory

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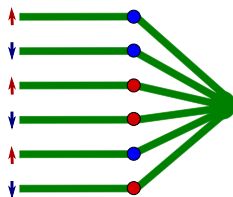
Synapses given a sequence of patterns (pot & dep) to store



Later: presented with a pattern. Has it been seen before?

Recognition memory

Synapses given a sequence of patterns (pot & dep) to store



Later: presented with a pattern. Has it been seen before?

Compare $\vec{s} \cdot \vec{w}(t)$ to threshold.

[?]

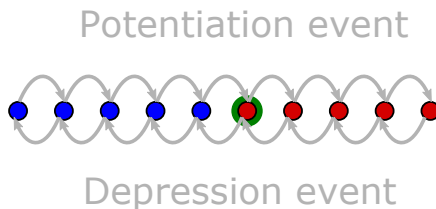
$$\text{SNR}(t) = \frac{\langle \vec{s} \cdot \vec{w}(t) \rangle - \langle \vec{s} \cdot \vec{w}(\infty) \rangle}{\sqrt{\text{Var}(\vec{s} \cdot \vec{w}(\infty))}}, \quad \overline{\text{SNR}}(\tau) = \int d\tau \frac{e^{-t/\tau}}{\tau} \text{SNR}(t).$$

Models of complex synaptic dynamics



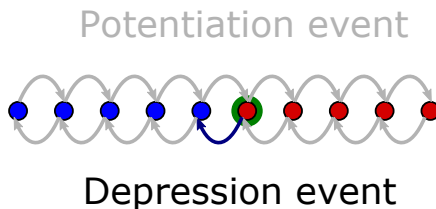
Models of complex synaptic dynamics

- Internal functional state of synapse \rightarrow synaptic weight.
 - Candidate plasticity events \rightarrow transitions between states
- weak ● strong



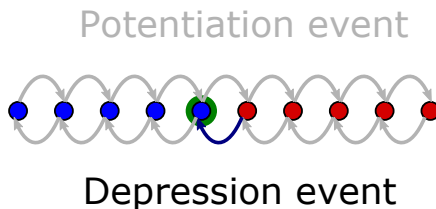
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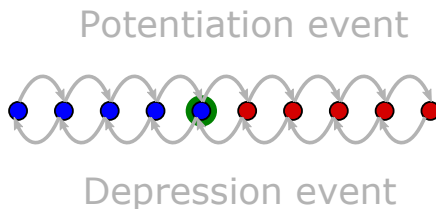
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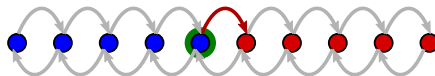
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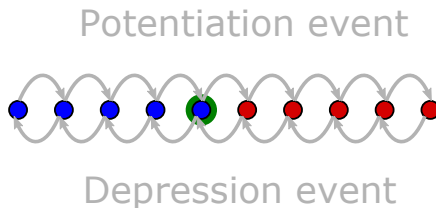
Potential event



Depression event

Models of complex synaptic dynamics

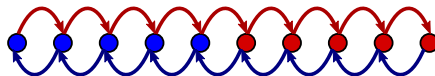
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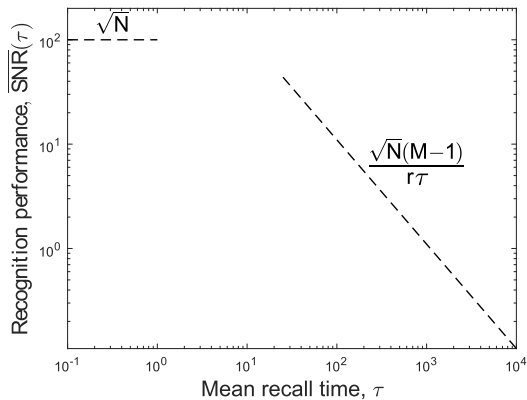
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Potentiation



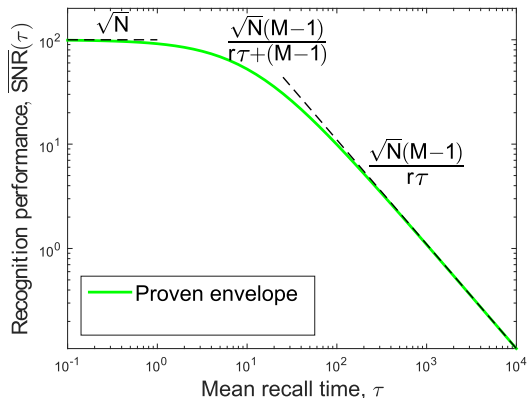
Depression

Proven envelope: memory frontier



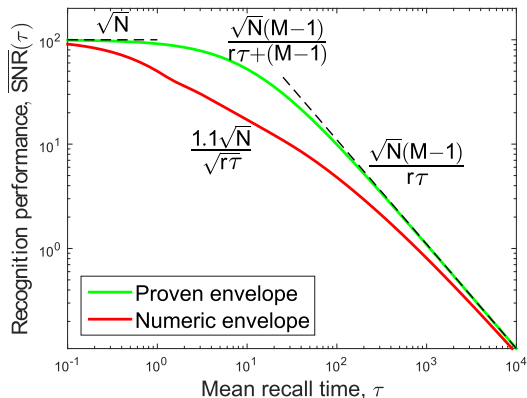
Proven envelope: memory frontier

Upper bound on memory curve at *any* timescale.

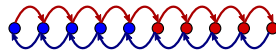


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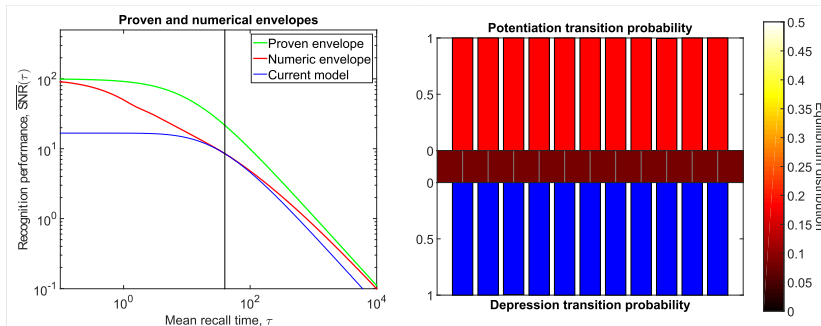
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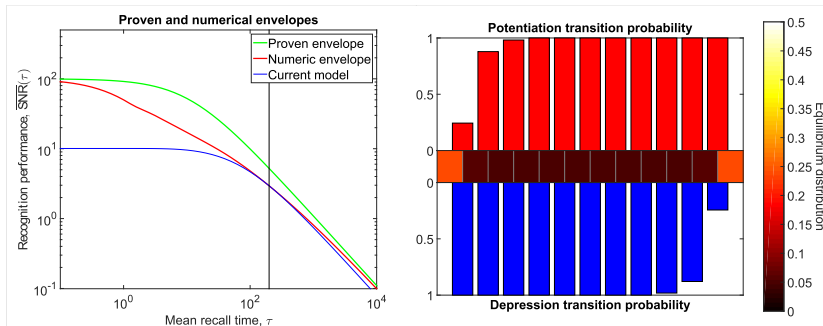
Serial topology:



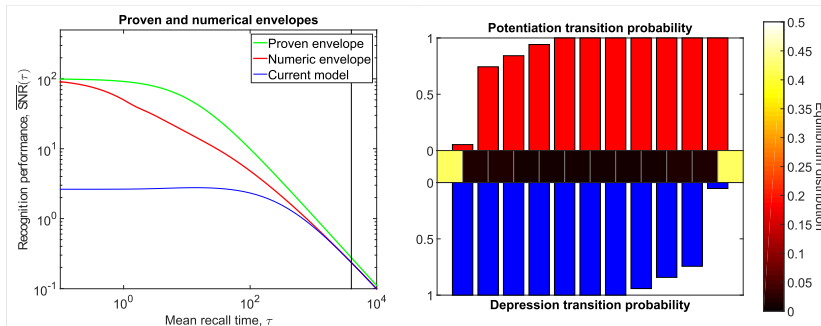
Models that maximise memory for one timescale



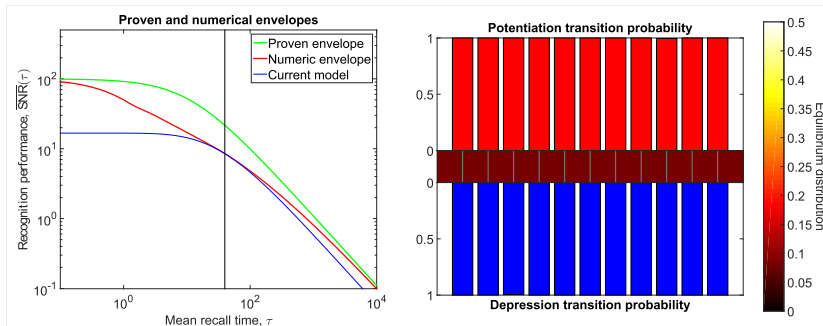
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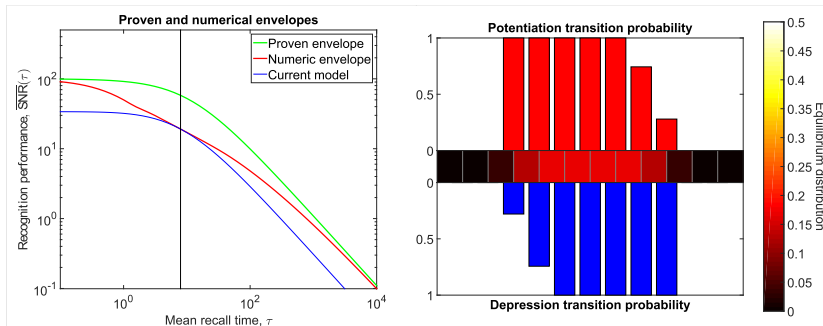
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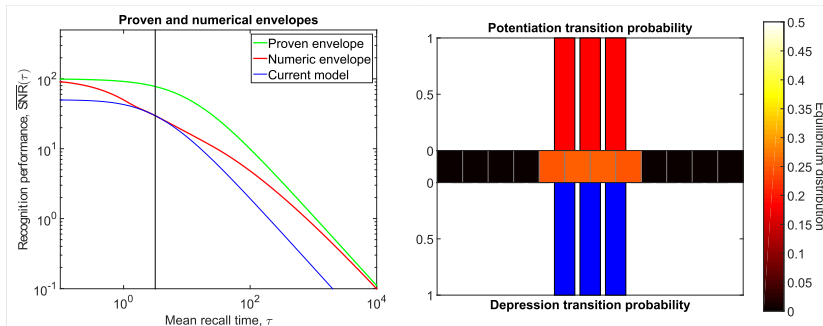
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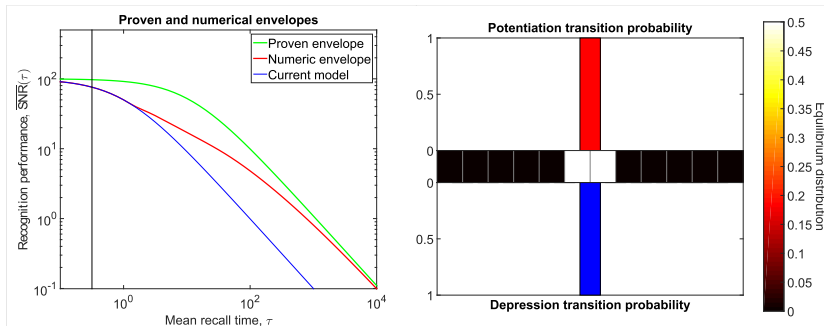
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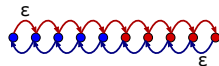
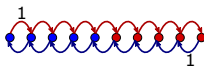


Synaptic structures for different timescales of memory

Real synapses limited by molecular building blocks.
Evolution had larger set of priorities.

What can we conclude?

Short timescales \longrightarrow Intermediate timescales \longrightarrow Long timescales

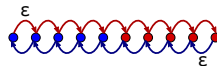
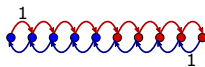


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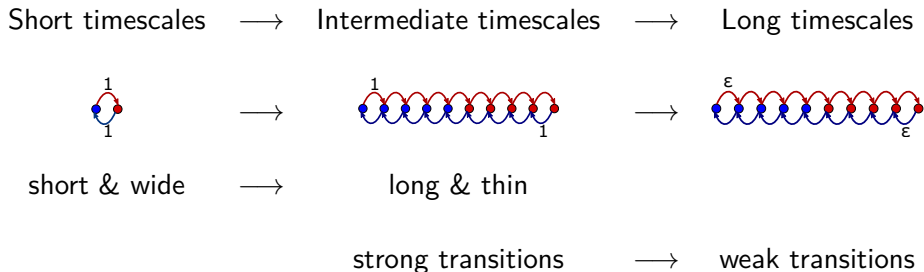
short & wide \longrightarrow

long & thin

Synaptic structures for different timescales of memory

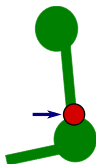
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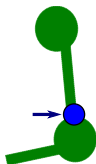
Proposed Experimental design

Subject a synapse to a sequence of candidate plasticity events.
Observe the changes in synaptic efficacy.



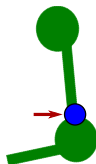
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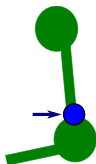
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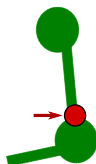
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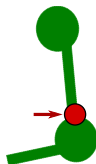
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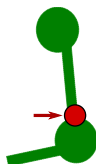
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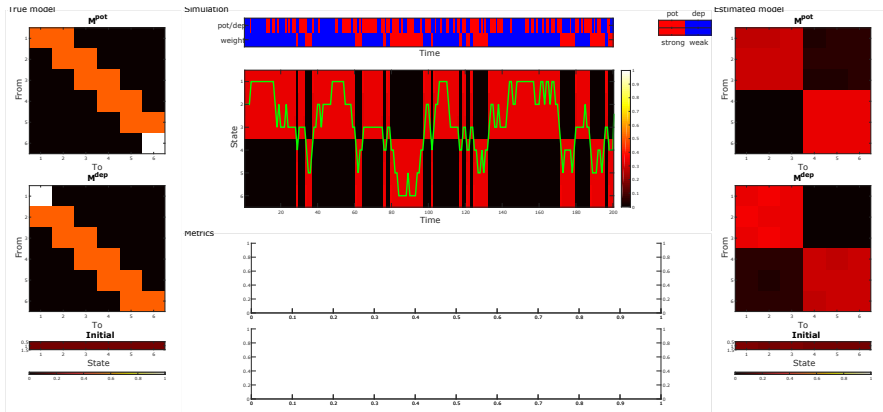
EM algorithms:

Sequence of hidden states \rightarrow estimate transition probabilities

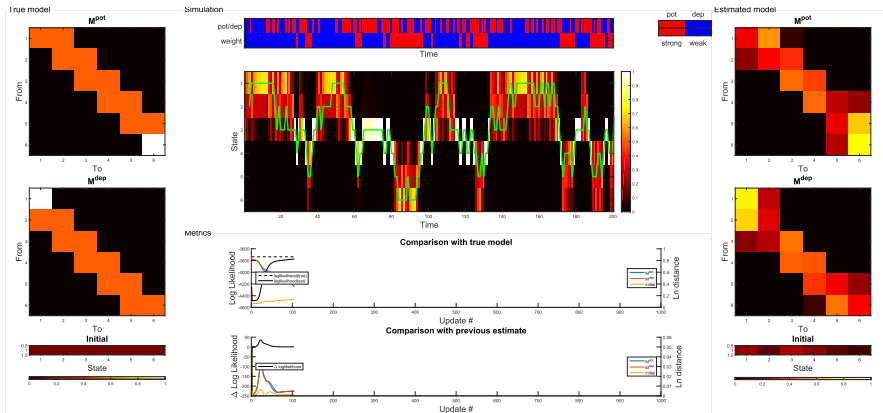
Transition probabilities \rightarrow estimate sequence of hidden states

[Baum et al. (1970), Rabiner and Juang (1993), Dempster et al. (2007)]

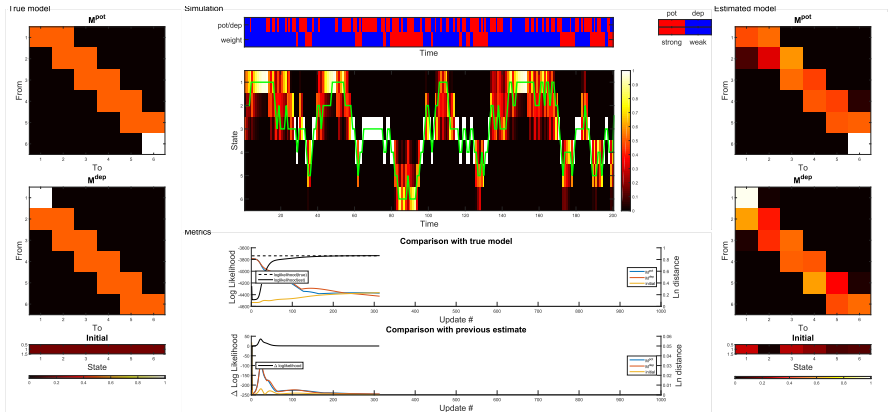
Fitting algorithm



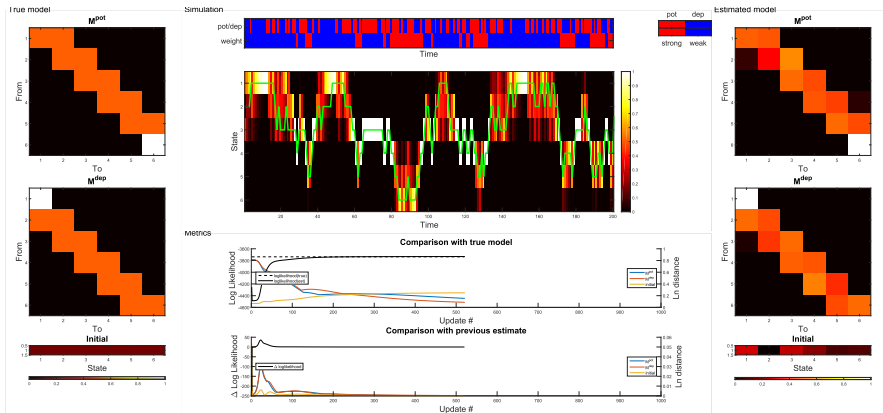
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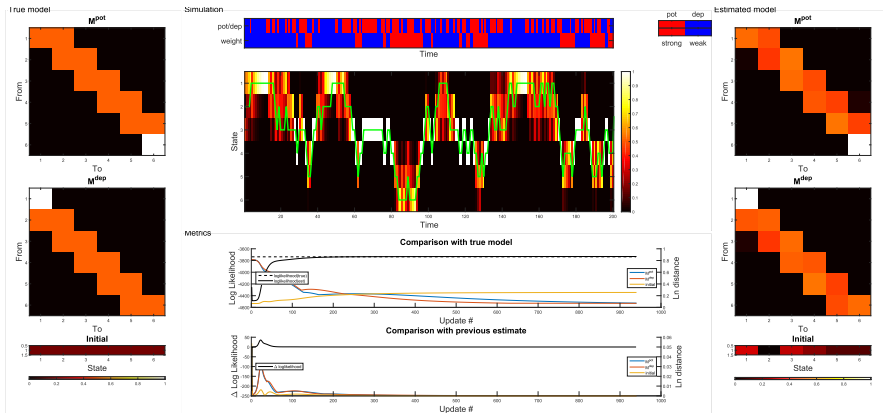
Fitting algorithm



Fitting algorithm



Fitting algorithm



- We have formulated a general theory of learning and memory with complex synapses.
- We find a memory envelope: a single curve that cannot be exceeded by the memory curve of *any* synaptic model.
- We understood which types of synaptic structure are useful for storing memories for different timescales.

Acknowledgements

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- Surya Ganguli
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- David Sussillo
- Jascha Sohl-Dickstein

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Springer, 1960.

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Technical detail: ordering states

Let \mathbf{T}_{ij} = mean first passage time from state i to state j . Then:

$$\eta = \sum_j \mathbf{T}_{ij} \mathbf{p}_j^\infty,$$

is independent of the initial state i (Kemeney's constant).

[Kemeny and Snell (1960)]

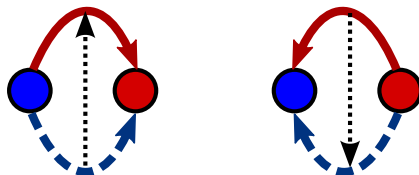
We define:

$$\eta_i^+ = \sum_{j \in \text{strong}} \mathbf{T}_{ij} \mathbf{p}_j^\infty, \quad \eta_i^- = \sum_{j \in \text{weak}} \mathbf{T}_{ij} \mathbf{p}_j^\infty.$$

They can be used to arrange the states in an order (increasing η^- or decreasing η^+). [back](#)

Technical detail: upper/lower triangular

With states in order:



Endpoint: potentiation goes right, depression goes left.

[back](#)