

Simulation_data_generate

1. Choose different cox distributions to generate data
2. Choose different beta
3. Create functions to simplify codes
4. Visualization 4.1 KM-curve vs. fitted curve 4.2 beta ~ MSE with different parameters to generate data 4.3 ...
5. discussion: description, pros and cons ...

```
## -- Attaching packages ----- tidyverse 1.3.1 --
## v ggplot2 3.3.5      v purrr  0.3.4
## v tibble  3.1.4      v dplyr  1.0.7
## v tidyr   1.1.3      v stringr 1.4.0
## v readr   2.0.1      v forcats 0.5.1

## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()

##
## Attaching package: 'pracma'

## The following object is masked from 'package:purrr':
##
##   cross

## Loading required package: ggpubr

##
## Attaching package: 'survminer'

## The following object is masked from 'package:survival':
##
##   myeloma
```

Generate survival data

```
set.seed(666)

# Generate survival data
genn_dat <- function(n, lambda, beta, gamma, alpha, dist) {
  # Generate key for each observation
  id <- seq(1:n)

  # Predictor X (treatment = 1; control = 0)
  x <- rbinom(n, size = 1, prob = 0.5)

  ## --- Generate Survival Time T ---
  U <- runif(n)
  # Use exponential distribution
  expo <- function(U, lambda, x, beta) {
```

```

    -log(U) / (lambda * exp(x * beta))
  }

  # Use weibull distribution
  weibull <- function(U, lambda, x, gamma, beta) {
    (-log(U) / (lambda * exp(x * beta))) ^ (1 / gamma)
  }

  # --- To be modified (add cox function) ---
  # Use 'Cox' distribution -- gompertz
  gompertz <- function(U, alpha, lambda, x, beta) {
    (1 / alpha) * (1 - alpha * log(U) / (lambda * exp(x * beta)))
  }

  # Select different baseline functions
  if (dist == "expo") {
    surv_t <- expo(U, lambda, x, beta)}
  else if (dist == "weibull") {
    surv_t <- weibull(U, lambda, x, gamma, beta)
  }
  else {
    surv_t <- gompertz(U, alpha, lambda, x, beta)
  }

  return(
    df = data.frame(
      id = id,
      treatment = x,
      time = surv_t
    )
  )
}

```

Fit models

```

# Set the truth (beta = 0.5)

# --- MODIFY sample size or beta ---
# Generate data from exponential
set.seed(666)
dat <- genn_dat(n = 10000, lambda = 2, beta = 0.5, gamma = 3, dist = "weibull")

fit_km <- survfit(Surv(dat$time) ~ dat$treatment, data = dat)
# Fit exponential model
fit_expo <- flexsurvreg(Surv(dat$time) ~ as.factor(dat$treatment), dist = "exponential", data = dat)
- fit_expo$coefficients[-1]

## as.factor(dat$treatment)1
## -0.1700936

# Weibull
fit_weibull <- survreg(Surv(dat$time) ~ dat$treatment, dist = "weibull")
- fit_weibull$coefficients[-1] / fit_weibull$scale

```

```
## dat$treatment
##      0.5099349

# `Cox` -- gompertz
fit_cox <- coxph(Surv(dat$time) ~ dat$treatment)
summary(fit_cox)

## Call:
## coxph(formula = Surv(dat$time) ~ dat$treatment)
##
##      n= 10000, number of events= 10000
##
##              coef exp(coef) se(coef)      z Pr(>|z|)
## dat$treatment 0.51013   1.66551  0.02068 24.67  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##              exp(coef) exp(-coef) lower .95 upper .95
## dat$treatment      1.666      0.6004      1.599      1.734
##
## Concordance= 0.561 (se = 0.003 )
## Likelihood ratio test= 606.9 on 1 df,  p=<2e-16
## Wald test               = 608.6 on 1 df,  p=<2e-16
## Score (logrank) test = 620.4 on 1 df,  p=<2e-16
```

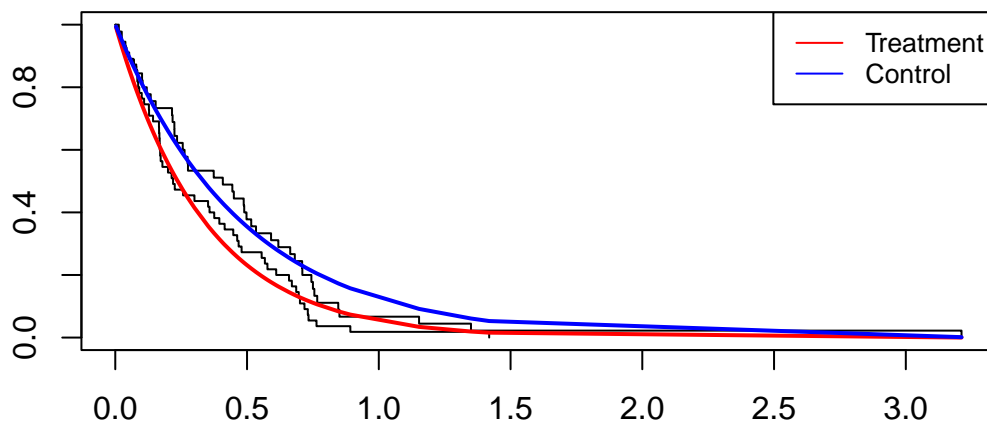
Visualization(beta = 0.5)

1. data-exponential(lambda = 2)

```
## Generate Data
set.seed(666)
dat_1 <- genn_dat(n = 100, lambda = 2, beta = 0.5, dist = "expo")
s_1 <- with(dat_1, Surv(time))

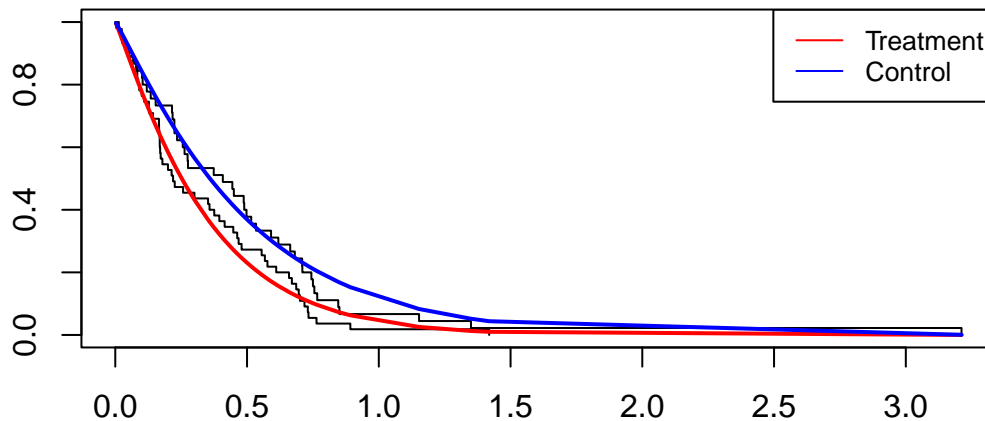
## Exponential
fit_expo_1 = flexsurvreg(s_1 ~ as.factor(treatment), dist = 'exponential', data = dat_1)
plot(fit_expo_1, col = c('red', 'blue'), main = "Exponential proportional-hazards model")
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Exponential proportional-hazards model



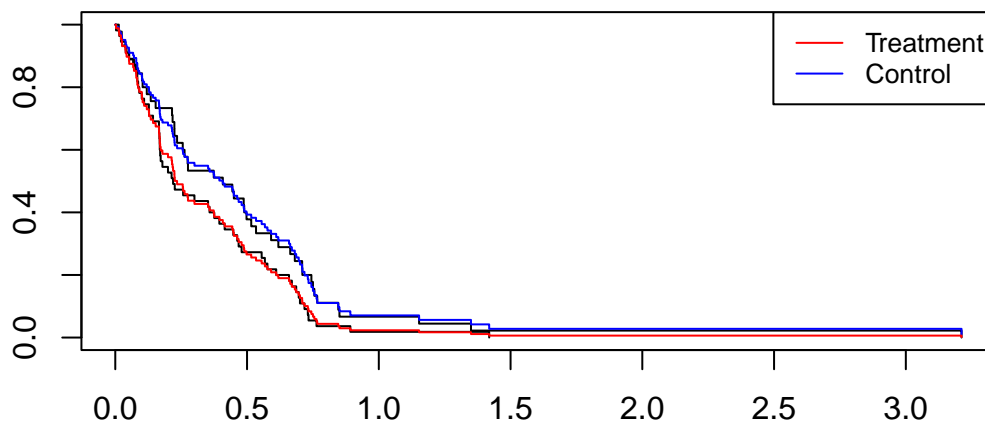
```
## Weibull
fit_wei_1 = flexsurvreg(s_1 ~ as.factor(treatment), dist = 'weibull', data = dat_1)
plot(fit_wei_1, col = c('red', 'blue'), main = "Weibull proportional-hazards model")
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Weibull proportional-hazards model



```
## Cox
fit_km_1 = survfit(s_1 ~ treatment, data = dat_1)
plot(fit_km_1, conf.int = F, main = "Cox proportional-hazards model")
fit_cox_1 = coxph(s_1 ~ as.factor(treatment), data = dat_1)
lines(survfit(fit_cox_1, newdata = data.frame(treatment = 0)), col = "blue", conf.int = F)
lines(survfit(fit_cox_1, newdata = data.frame(treatment = 1)), col = "red", conf.int = F)
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Cox proportional-hazards model



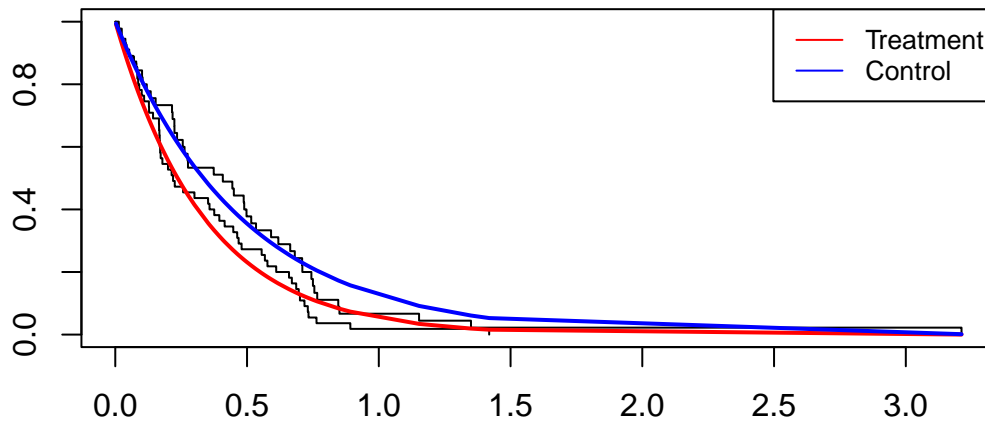
2. data-weibull(lambda = 2, gamma = 1)

```
## Generate Data
set.seed(666)
dat_2 <- genn_dat(n = 100, lambda = 2, beta = 0.5, gamma = 1, dist = "weibull")
s_2 = with(dat_2, Surv(time))
```

```
## Exponential
```

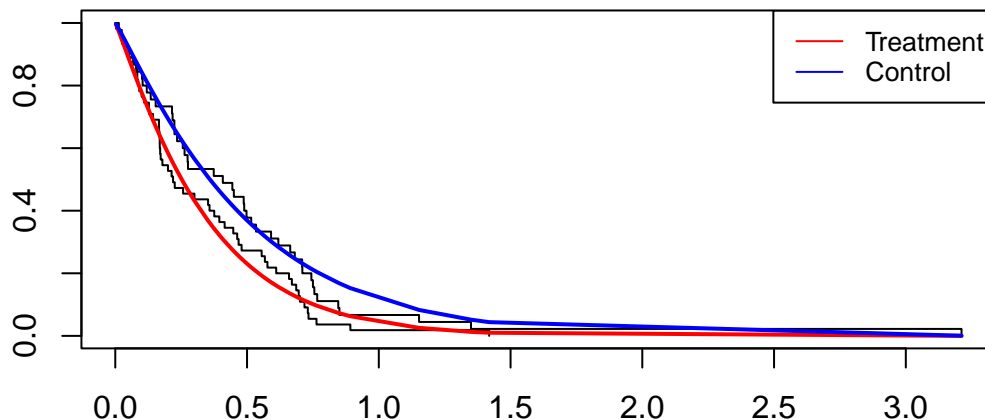
```
fit_expo_2 = flexsurvreg(s_2 ~ as.factor(treatment), dist = 'exponential', data = dat_2)
plot(fit_expo_2, col = c('red', 'blue'), main = "Exponential proportional-hazards model")
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Exponential proportional-hazards model



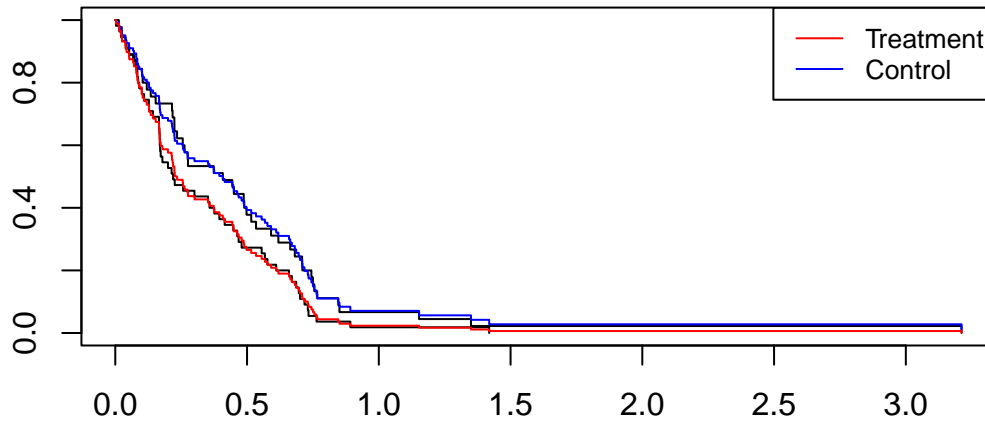
```
## Weibull
fit_wei_2 = flexsurvreg(s_2 ~ as.factor(treatment), dist = 'weibull', data = dat_2)
plot(fit_wei_2, col = c('red', 'blue'), main = "Weibull proportional-hazards model")
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Weibull proportional-hazards model



```
## Cox
fit_km_2 = survfit(s_2 ~ treatment, data = dat_2)
plot(fit_km_2, conf.int = F, main = "Cox proportional-hazards model")
fit_cox_2 = coxph(s_2 ~ as.factor(treatment), data = dat_2)
lines(survfit(fit_cox_2, newdata = data.frame(treatment = 0)), col = "blue", conf.int = F)
lines(survfit(fit_cox_2, newdata = data.frame(treatment = 1)), col = "red", conf.int = F)
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Cox proportional-hazards model

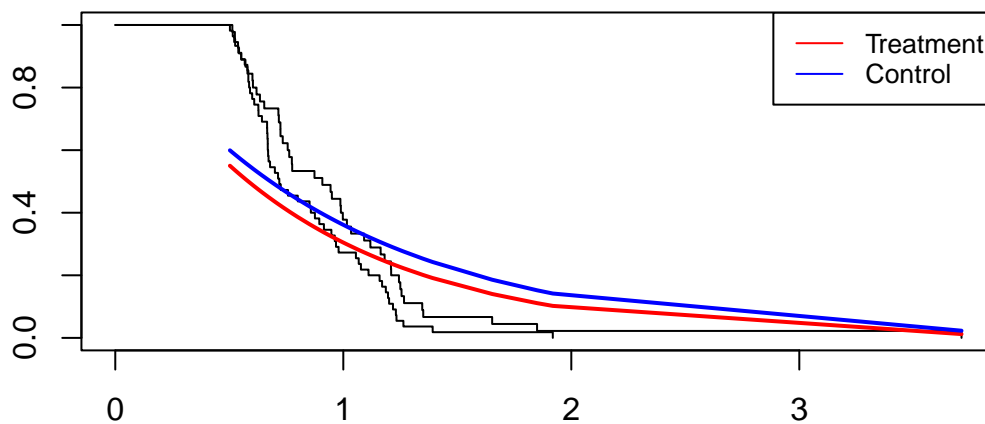


3. `data-gompertz(alpha = 2, lambda = 2)`

```
## Generate Data
set.seed(666)
dat_3 <- genn_dat(n = 100, lambda = 2, beta = 0.5, alpha = 2, dist = "gompertz")
s_3 = with(dat_3, Surv(time))

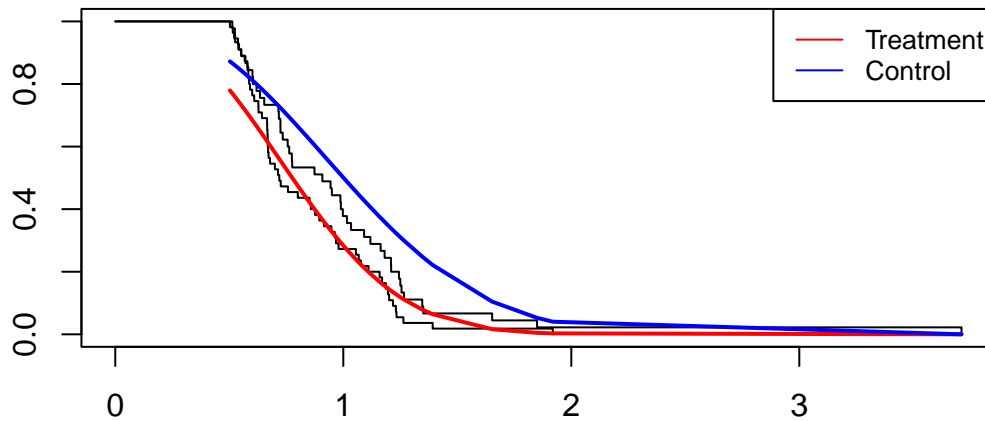
## Exponential
fit_expo_3 = flexsurvreg(s_3 ~ as.factor(treatment), dist = 'exponential', data = dat_3)
plot(fit_expo_3, col = c('red', 'blue'), main = "Exponential proportional-hazards model")
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Exponential proportional-hazards model



```
## Weibull
fit_wei_3 = flexsurvreg(s_3 ~ as.factor(treatment), dist = 'weibull', data = dat_3)
plot(fit_wei_3, col = c('red', 'blue'), main = "Weibull proportional-hazards model")
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Weibull proportional-hazards model



```
## Cox
fit_km = survfit(s_3 ~ treatment, data = dat_3)
plot(fit_km, conf.int = F, main = "Cox proportional-hazards model")
fit_cox_3 = coxph(s_3 ~ as.factor(treatment), data = dat_3)
lines(survfit(fit_cox_3, newdata = data.frame(treatment = 0)), col = "blue", conf.int = F)
lines(survfit(fit_cox_3, newdata = data.frame(treatment = 1)), col = "red", conf.int = F)
legend("topright", legend = c('Treatment', 'Control'), col = c('red', 'blue'), lty = 1, cex = 0.8)
```

Cox proportional-hazards model

