**2D TEz MOM Analysis**

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**Abstract – A two dimensional method of moments (MOM) simulation is presented. A normally incident plane impinges upon an infinitely long perfect electric conducting cylinder.**

1. **INTRODUCTION**
2. **FORMULATION**
   1. **Discretization**

Unlike other methods in computational electromagnetics, the geometrical mesh does not include the free space environment. The discretization occurs on the boundaries of the objects of interest. Figure XX shows an example of a cylinder divided into 8 segments with their midpoints represented by circles.

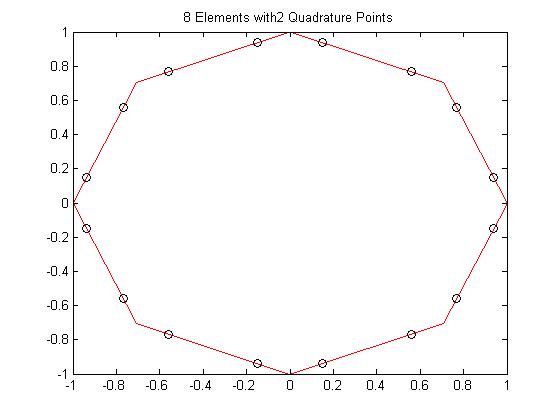


Figure 1 Circular Mesh of 8 segments with midpoints

* 1. **Boundary Conditions (D- EFIE, B-MFIE)**

For a TEz incident plane wave, the boundary conditions on the surface of the cylinder are determined by equations (2.2.1) and (2.2.2). The fields outside of the cylinder are represented with a subscript of 2 whereas the fields inside the cylinder are represented with a subscript of 1. The problem calls for a perfectly conducting cylinder which makes the fields inside the cylinder identically equal to zero.

* 1. **Fundamental Equations (D-EFIE,B-MFIE)**
     1. **MFIE**

The magnetic field integral equation begins with the boundary condition shown in equation (2.2.1). The exterior field is comprised of both the incident and scattered magnetic field. The tangential component of the exterior field is equal to the surface current at the boundary of the PEC cylinder as seen from equation (2.3.1).

The use of the magnetic vector potential, A, is used to determine the scattered magnetic field. The magnetic vector potential in Equation (2.3.2) uses an outward propagating Green’s function equal to a first order Hankel function of the second kind.

The scattered field is now evaluated from equation (2.3.3). A singularity occurs if the Green’s function is equal to zero. To account for the singularity, a principle value integral is used and the subsequent incident magnetic field integral equation is found by equation (2.3.4).

Source coordinates are differentiated from the observer coordinates with the use of a prime. The use of the letter, , represented the parameterized tangential components on the surface of the PEC cylinder.

The surface current, , can then be approximated by equation (2.3.4) where represents the pulse basis functions used upon each element. A solution can be obtained with the use of testing functions which are considered in a subsequent section.

* + 1. **EFIE**
    2. **Point Matching**
    3. **N-Point Quadrature**
  1. **Matrix Formulation (D-EFIE, B-MFIE)**
     1. **Singularity Extraction**

As mentioned previously, a principle value integral was needed for the magnetic field integral equation. Any method used will have a singularity if the source and observer cells overlap. After applying the principle value integral, the entries Z[i,i] will be equal to a value of -1/2. If the source and observer distance is within a tolerance, ε, the singularity extraction in equation (2.4.1) is used. A small argument approximation for the Hankel function was used to numerically extract the singularity. The resultant of this extraction was then added to the integral of the small argument approximation which was determined analytically.

1. **RESULTS**
   1. **Error**

Analytic solutions for both the surface current and bistatic echo width are shown in equations (3.1.1) and (3.1.2) respectively. The simulation results determine the coefficients for the surface current on each element which can be easily referenced to an angular dependence on the surface of the cylinder.

After the current coefficients are determined, bistatic echo width can be implemented from equation (3.1.3). As seen from equation (3.1.3), Far-field approximations are made when echo width is considered.

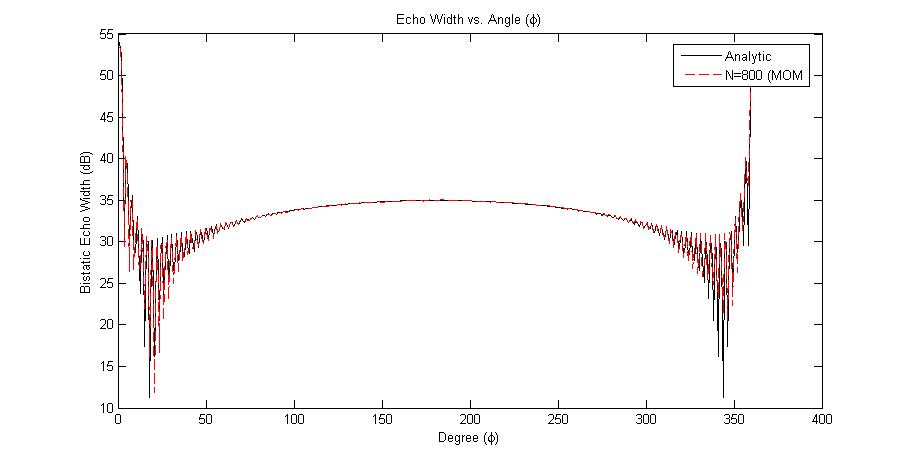
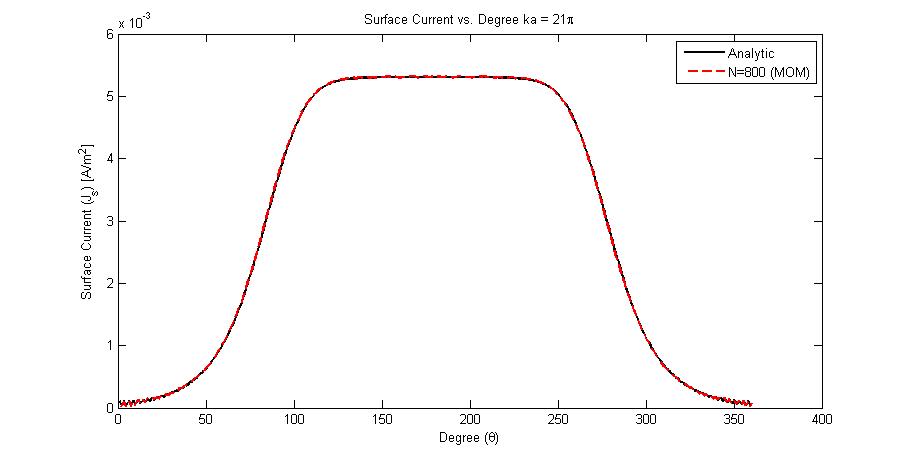


Figure 2 Left: Surface Current Right: Echo Width

* 1. **Convergence**

1. **Future Work**
   1. **CFIE**

Without the use of triangular basis functions for the MFIE method, a combined field integral equation (CFIE) cannot be determined. Internal resonances of the PEC cylinder correspond to ambiguous results solely relying on the use of MFIE. A test of iteration number versus frequency of interest for the MFIE alone might show internal resonances if there are anomalous iteration numbers.

* 1. **TMz**

1. **CONCLUSION**
2. **REFERENCES**
3. J. Jin, *The Finite Element Method in Electromagnetics*, 2nd edition, Wiley, 2002.