Assignment #9: 图论: 遍历, 及 树算

Updated 1739 GMT+8 Apr 14, 2024

2024 spring, Complied by 23工院 武昱达

编程环境

PyCharm Professional Edition

1. 题目

04081: 树的转换

http://cs101.openjudge.cn/dsapre/04081/

思路:

```
1 # for a generic_tree, we make its left son as its left son
   # and make its right brother its right son, then a generic
   # tree is shifted to a binary tree.
 4
 5
        0
      / | \
 6
 7
     1 2 3
                                     1
                   ===>
 8
9
10
11
12
                                       5
13
14
    class TreeNode:
15
        def __init__(self,value):
16
17
            self.value = value
           self.children=[]
18
19
            self.parent=None
20
            self.bro=None
21
            self.left=None
22
           self.right=None
23
        def get_max_H(self):
24
            if not self.children:return 1
25
            return max(child.get_max_H() for child in self.children)+1
26
        def get_new_max_h(self):
27
            if self.left==None and self.right==None:
28
                return 1
29
            if self.left==None and self.right:
                return self.right.get_new_max_h()+1
30
31
            if self.right==None and self.left:
32
                return self.left.get_new_max_h()+1
            if self.left and self.right:
33
```

```
34
                 return
    max(self.left.get_new_max_h(),self.right.get_new_max_h())+1
35
36
    num=0
    def build_generic_tree(1:list,current_node):
37
38
        global num
39
        if len(1) == 0:
40
            return
        if 1[0]=="d":
41
42
            num += 1
43
            node = TreeNode(num)
            if current_node.children:
44
                 current_node.children[-1].bro=node
45
46
            current_node.children.append(node)
            node.parent=current_node
47
            build_generic_tree(l[1:],node)
48
        if 1[0]=='u':
49
50
            build_generic_tree([1:],current_node.parent)
51
        return current_node
52
53
    def build_new_tree(root, last_root, is_left:bool):
54
        new_root=TreeNode(root.value)
55
        if last_root:
            if is_left:last_root.left=new_root
56
57
            else:last_root.right=new_root
58
59
        if root.children:
60
            build_new_tree(root.children[0],new_root,True)
61
        if root.bro:
            build_new_tree(root.bro,new_root,False)
62
63
        return new_root
64
65
    root=TreeNode(0)
66
67
    build_generic_tree(list(input()), root)
68
    new_root=build_new_tree(root,None,False)
69
    print('{} => {}'.format(root.get_max_H()-1,new_root.get_new_max_h()-1))
```

代码运行截图 (至少包含有"Accepted")

#44384037提交状态 查看 提交 统计 提问

状态: Accepted

#: 44384037 题目: 04081 提交人: 23n2300011119 (武)

内存: 3744kB 时间: 30ms 语言: Python3

基本信息

提交时间: 2024-03-24 17:44:39

08581: 扩展二叉树

http://cs101.openjudge.cn/dsapre/08581/

思路:

涉及一步循环地找空祖先节点。

```
1
    from collections import deque
 2
    class TreeNode:
 3
        def __init__(self,val):
 4
            self.val=val
 5
            self.left=None
 6
            self.right=None
 7
            self.parent=None
 8
 9
    def fill_tree(root, node):
10
        node.parent=root
        if root.left==None:root.left=node
11
12
        else:root.right=node
13
14
    # 函数的功能是建成以root为根的树,并把他连接到parent节点上。
15
    def build_tree(d:deque,parent:TreeNode):
        if not d:return
16
17
        cur_node=TreeNode(d.popleft())
18
19
        while parent.left and parent.right:
20
            parent=parent.parent
21
        cur_node.parent=parent
22
        fill_tree(parent,cur_node)
23
        if cur_node.val=='.':
24
25
            build_tree(d,parent)
26
        else:build_tree(d,cur_node)
```

```
27
28
    def post_search(root):
29
        if root.val == '.':
             return ""
30
31
        output=[]
32
        output.extend(post_search(root.left))
33
        output.extend(post_search(root.right))
34
        output.append(root.val)
        return "".join(output)
35
36
37
    def in_search(root):
38
        if root.val=='.':
             return ""
39
40
        output=[]
41
        output.extend(in_search(root.left))
42
        output.append(root.val)
        output.extend(in_search(root.right))
43
44
        return "".join(output)
45
    raw=deque(input())
46
47
    root=TreeNode(raw.popleft())
48
    build_tree(raw,root)
49
    print(in_search(root))
50
    print(post_search(root))
```

代码运行截图 (至少包含有"Accepted")

#44698772提交状态

查看 提交 统计 提问

基本信息

#: 44698772 题目: 08581

内存: 3712kB

语言: Python3

时间: 29ms

提交人: 23n2300011119 (武)

提交时间: 2024-04-18 20:07:32

```
状态: Accepted
```

```
源代码
 from collections import deque
 class TreeNode:
    def __init__(self, val):
         self.val=val
         self.left=None
        self.right=None
        self.parent=None
 def fill_tree(root, node):
     node.parent=root
     if root.left==None:root.left=node
     else:root.right=node
 # 函数的功能是建成以root为根的树,并把他连接到parent节点上。
 def build_tree(d:deque,parent:TreeNode):
     if not d:return
     cur_node=TreeNode(d.popleft())
     while parent.left and parent.right:
        parent=parent.parent
     cur node.parent=parent
     fill_tree (parent, cur_node)
     if cur_node.val=='.':
        build_tree(d,parent)
```

22067: 快速堆猪

http://cs101.openjudge.cn/practice/22067/

思路:

懒删除堆实现。

```
import heapq
 1
 2
    from collections import defaultdict
 3
    p_stack,p_heap,is_out=[],[],defaultdict(int)
 4
    while True:
 5
        try:
 6
             tmp=input()
             if tmp=="min":
 8
                 if p_stack:
 9
                     while True:
10
                          a=heapq.heappop(p_heap)
11
                          if not is_out[a]:
                              heapq.heappush(p\_heap,a)
12
13
                              print(a)
14
                              break
15
                          else:
                              is\_out[a]=1
16
17
                              continue
18
             elif tmp=="pop":
19
                 if p_stack:
20
                     is_out[p_stack.pop()]+=1
21
             else:
22
                 _,num=map(str,tmp.split())
23
                 p_stack.append(int(num))
24
                 heapq.heappush(p_heap,int(num))
25
        except EOFError:
26
             break
```

代码运行截图 (AC代码截图,至少包含有"Accepted")

```
#44097967提交状态
                                                                                 查看
                                                                                        提交
                                                                                               统计
                                                                                                       提问
状态: Accepted
                                                                         基本信息
源代码
                                                                               #: 44097967
                                                                             题目: 22067
 import heapq
                                                                            提交人: 23n2300011119 (武)
 from collections import defaultdict
                                                                             内存: 7644kB
 p_stack,p_heap,is_out=[],[],defaultdict(int)
 while True:
                                                                             时间: 366ms
     try:
                                                                             语言: Python3
        tmp=input()
                                                                          提交时间: 2024-03-06 21:42:26
        if tmp=="min":
            if p stack:
                while True:
                    a=heapq.heappop(p_heap)
                    if not is_out[a]:
                        heapq.heappush(p_heap,a)
                        print(a)
                        break
                    else:
                        is_out[a]-=1
                        continue
         elif tmp=="pop":
            if p_stack:
                is_out[p_stack.pop()]+=1
             _, num=map(str,tmp.split())
            p_stack.append(int(num))
            heapq.heappush(p_heap,int(num))
     except EOFError:
        break
```

04123: 马走日

dfs, http://cs101.openjudge.cn/practice/04123

思路:

写DFS的时候务必在写代码之前明确几件事情:

- 1. 函数的作用
- 2. 需要传入几个参数
- 3. 哪些是可以global的,哪些是传入的
- 4. 参数的意义。如这里的path, 我的定义是:

对某一层dfs, path是计算当前起点以后总共的访问路径数。

那么返回时返回条件就应该是path==X*Y,因为当前起点已经被计算进来了。

dfs的作用是从起点开始遍历所有尚未遍历的点。

在这一定义下,初始时必须把起点visited标记为True,于实际意义相对应。

代码

```
1
    d=[(-1,-2),(-2,-1),(1,-2),(2,-1),(2,1),(1,2),(-1,2),(-2,1)]
 2
    res=0
 3
    def dfs(X,Y,path,start):
        global res
 4
 5
        if path==X*Y:
 6
             res+=1
 7
             return
 8
9
        x, y = start
10
        for dx, dy in d:
11
             if 0 \le x + dx \le X and 0 \le y + dy \le Y and not visited[x + dx][y + dy]:
                 visited[x+dx][y+dy]=True
12
13
                 dfs(X,Y,path+1,(x+dx,y+dy))
14
                 visited[x+dx][y+dy]=False
15
    for i in range(T:=int(input())):
16
17
        X,Y,x,y=map(int,input().split())
        res=0
18
        visited=[[False for j in range(Y)] for i in range(X)]
19
20
        visited[x][y]=True
21
        dfs(X,Y,1,(x,y))
22
        print(res)
```

代码运行截图 (AC代码截图,至少包含有"Accepted")

状态: Accepted

```
#: 44700558
                                                                                  题目: 04123
d=[(-1,-2),(-2,-1),(1,-2),(2,-1),(2,1),(1,2),(-1,2),(-2,1)]
                                                                                提交人: 23n2300011119 (武)
                                                                                 内存: 4028kB
def dfs(X,Y,path,start):
    global res
                                                                                 时间: 2812ms
    if path==X*Y:
                                                                                  语言: Python3
        res+=1
                                                                              提交时间: 2024-04-18 22:27:47
       return
    x, y = start
    for dx, dy in d:
       if 0 \le x + dx \le x and 0 \le y + dy \le y and not visited[x+dx][y+dy]:
            {\tt visited[x+dx][y+dy]=True}
            dfs(X, Y, path+1, (x+dx, y+dy))
            visited[x+dx][y+dy]=False
for i in range(T:=int(input())):
   X,Y,x,y=map(int,input().split())
    res=0
    visited=[[False for j in range(Y)] for i in range(X)]
    visited[x][y]=True
    dfs(X,Y,1,(x,y))
    print(res)
```

基本信息

28046: 词梯

bfs, http://cs101.openjudge.cn/practice/28046/

思路: bucket, BFS

```
1
    from collections import deque
 2
    class Vertex:
 3
        def __init__(self,id):
 4
             self.id=id
 5
             self.neighbors={}
             self.previous=None
 6
 7
             self.color='white'
 8
        def __str__(self):
            return '*'+self.id
 9
10
    class Graph:
        def __init__(self):
11
12
            self.vertices={}
13
             self.num_vertices=0
14
        def add_vertex(self,id):
15
16
             self.vertices[id]=Vertex(id)
17
             self.num_vertices+=1
18
        def add_edge(self,v1_id,v2_id):
19
20
            # v1_start, v2_end
            if v1_id not in self.vertices:
21
                 self.vertices[v1_id]=Vertex(v1_id)
22
            if v2_id not in self.vertices:
23
24
                 self.vertices[v2_id]=Vertex(v2_id)
25
            v1,v2=self.vertices[v1_id],self.vertices[v2_id]
            v1.neighbors[v2_id]=v2
26
27
             self.num_vertices+=1
28
29
    n,graph,buckets=int(input()),Graph(),{}
```

```
30
    words=[input() for _ in range(n)]
31
    for word in words:
32
        for bit in range(1,len(word)+1):
33
            tag=word[:bit-1]+'_'+word[bit:]
            bucket=buckets.setdefault(tag,set())
34
35
            bucket.add(word)
36
    # for i,j in buckets.items():
          print(i,j)
37
    for bucket in buckets.values():
38
39
        for i in bucket:
            tmp=bucket-{i}
40
            for j in tmp:
41
42
                graph.add_edge(i,j)
43
44
45
    start,goal=map(str,input().split())
46
    # BFS,这里不用函数实现
47
    q=deque()
    q.append(graph.vertices[start])
48
    current=graph.vertices[start]
49
50
    # 注: 标黑色用于把回头路堵死; 标灰色用于把更长的可行路径堵死。
51
    # 由于更长的可行路径被堵死且最短路径唯一, 所以每个点的前驱若有有则仅有一个。
    while q and current.id!=goal:
52
53
        current=q.popleft()
54
        for vert in current.neighbors.values():
55
            if vert.color=='white':
                vert.color='grey'
56
57
                vert.previous=current
                q.append(vert)
58
59
        current.color='black'
60
61
    def traverse(start:Vertex):
62
        output=[start.id]
63
        current=start
64
        while current.previous:
65
            output.append(current.previous.id)
66
            current=current.previous
        return " ".join(output[::-1])
67
68
    if current.id==goal:
69
70
        print(traverse(graph.vertices[goal]))
71
    else:
        print("NO")
72
```

#44718761提交状态 查看 提交 统计 提问

状态: Accepted

```
基本信息
源代码
                                                                                         #: 44718761
                                                                                       题目: 28046
 from collections import deque
                                                                                     提交人: 23n2300011119 (武)
 class Vertex:
     def __init__(self,id):
    self.id=id
                                                                                       内存: 9444kB
                                                                                       时间: 87ms
         self.neighbors={}
                                                                                       语言: Python3
          self.previous=None
                                                                                    提交时间: 2024-04-20 14:34:05
          self.color='white
     def __str__(self):
    return '*'+self.id
 class Graph:
     def __init__(self):
          self.vertices={}
          self.num_vertices=0
     def add_vertex(self,id):
          self.vertices[id]=Vertex(id)
          self.num_vertices+=1
     def add_edge(self,v1_id,v2_id):
          # v1_start,v2_end
if v1 id not in self.vertices:
```

28050: 骑士周游

dfs, http://cs101.openjudge.cn/practice/28050/

思路:

启发式算法+马走日DFS

```
1
    d=[(-1,-2),(-2,-1),(1,-2),(2,-1),(2,1),(1,2),(-1,2),(-2,1)]
 2
    def avail(vert):
 3
         x,y=vert
 4
         return (0 \le x \le x \text{ and } 0 \le y \le y \text{ and not } visited[x][y])
 5
 6
    def ordered_by_avail(start):
         x,y=start
 8
         steps=[]
 9
         for dx, dy in d:
10
             next_step=(x+dx,x+dy)
             available=0
11
12
             for step in d:
13
                  ddx,ddy=step
14
                  if avail((x+dx+ddx,y+dy+ddy)):available+=1
15
             steps.append((available,(dx,dy)))
16
         steps.sort(key=lambda x:x[0])
17
         return [i[1] for i in steps]
18
19
    def dfs(X,Y,path,start):
20
         if path==X*Y:
21
             print('success')
22
             exit()
23
24
         x, y = start
25
         new_d=ordered_by_avail(start)
         for dx, dy in new_d:
26
27
             if avail((x+dx,y+dy)):
28
                  visited[x+dx][y+dy]=True
```

```
29
                dfs(X,Y,path+1,(x+dx,y+dy))
30
                visited[x+dx][y+dy]=False
31
32
    X=Y=int(input())
    x,y=map(int,input().split())
33
34
    visited=[[False for j in range(Y)] for i in range(X)]
35
    visited[x][y]=True
    dfs(X,Y,1,(x,y))
36
    print('fail')
37
```

代码运行截图 (AC代码截图,至少包含有"Accepted")

#44719775提交状态 查看 提交 统计 提问

```
状态: Accepted
                                                                                                     基本信息
                                                                                                             #: 44719775
                                                                                                           题目: 28050
  d = \left[ \; \left(-1,-2\right) \; , \; \left(-2,-1\right) \; , \; \left(1,-2\right) \; , \; \left(2,-1\right) \; , \; \left(2,1\right) \; , \; \left(1,2\right) \; , \; \left(-1,2\right) \; , \; \left(-2,1\right) \; \right]
                                                                                                        提交人: 23n2300011119 (武)
 def avail(vert):
                                                                                                          内存: 4044kB
      x,y=vert
                                                                                                          时间: 81ms
      return (0 <=x<X and 0<=y<Y and not visited[x][y])
                                                                                                          语言: Pvthon3
  def ordered_by_avail(start):
                                                                                                      提交时间: 2024-04-20 15:12:29
      x,y=start
      steps=[]
      for dx, dy in d:
           next_step=(x+dx,x+dy)
available=0
           for step in d:
                ddx,ddy=step
if avail((x+dx+ddx,y+dy+ddy)):available+=1
           steps.append((available,(dx,dy)))
      steps.sort(key=lambda x:x[0])
      return [i[1] for i in steps]
  def dfs(X,Y,path,start):
      if path==X*Y:
          print('success')
            exit()
      x, y = start
      new_d=ordered_by_avail(start)
      for dx,dy in new_d:
    if avail((x+dx,y+dy)):
                 {\tt visited[x+dx][y+dy]=True}
                dfs(X,Y,path+1,(x+dx,y+dy))
visited[x+dx][y+dy]=False
 X=Y=int(input())
  x,y=map(int,input().split())
  visited=[[False for j in range(Y)] for i in range(X)]
  visited[x][y]=True
 dfs(X,Y,1,(x,y))
 print('fail')
```

2. 学习总结和收获

当图变得越来越抽象(指从计概的矩阵变成点和边的集合),过程写得越来越规范,实现的复杂度越来越低,但是随之而来的是代码量越来越大......

本周题目难度不小, 前面的题比较熟悉, 暂且不提。

两个图算法的题目,词梯巧妙在用桶的方法快速建图(夏佬狂喜),骑士周游巧妙在利用启发式算法大幅降低时间成本。

学习下来,能感受到自己变抽象了,也变强了。