# Basic concepts Lecture 1a Course leader: Oleg Sysoev Jer: Oleg Sysc

#### Course topics

#### Block 1

- Basic concepts in machine learning. Software for ML. Classification and regression
- Dimensionality reduction and model selection
- Kernel methods (SVM) and neural networks

#### Block 2

Mixture models and ensemble methods

#### Course organization

- 1 topic= 3-4 lectures (Zoom) +1 lab (2h\* 3, campus)+seminar (zoom)
- Course given as
  - 732A99 (9 ECTS): Block 1+Block 2
  - 732A68 (9 ECTS): Block 1+Block 2
  - TDDE01 (6 ECTS): Block 1

#### Labs

- Sign-up at LISAM, exactly 3 persons! (otherwise group can be split)
- Take around 8h, group report
- Recommended strategy: one person has main responsibility for one assignment in the lab.
- Statement of Contribution: describe clearly how each member contributed to the group report (which member which assignment). Without it lab is automatically failed.
- Deadlines
- To pass exam, each individual needs to have experience of solving all lab tasks → make sure to try all tasks before the exam!
- Published a couple of days in advance try doing before attending to the first lab session!
- Submission via LISAM

#### Course organization

#### Lectures

- Available as PowerPoint or PDF, normally at LISAM
  - Write in the chat if you have questions during the lectures

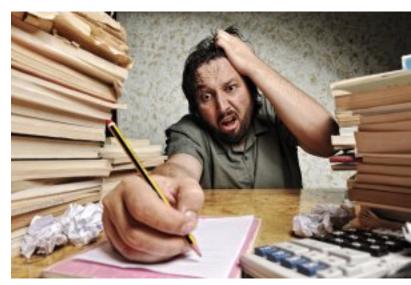
#### Seminars

- Obligatory attendance of all seminars
- Zoom
- Speaker and opponent groups
- Discussion of the latest lab
- Presentation schedule will be published on LISAM (Seminar.PDF)

## Course organization

- Examination
  - laboratory part + computer-based exam

- Lecture 1b is 'Basic Statistics'
- Lecture 1c is 'Introduction to R'



http://www.ewagseduction.com/wp-content/uploads/2014/11/stressful.in

# What is Machine Learning?

- Machine learning is a subfield of **computer science** that evolved from the study of **pattern recognition** and computational learning theory in **artificial intelligence**.
- Machine learning explores the study and construction of algorithms that can learn from and make predictions on data. Such algorithms operate by building a model from example inputs in order to make data-driven predictions or decisions, rather than following strictly static program instructions.

Wikipedia (Oct 15, 2016).

# Machine Learning and Statistics

- ML=intersection of computer science, statistics and artificial intelligence.
  - Related: data mining, knowledge discovery and data science.
- ML uses mainly statistical (probabilistic) models for analyzing data.
  - Data mining and knowledge discovery tend to use less rigorous, but often effective, algorithms.
  - ML is not a discovery of a hidden information (Data Mining)
- ML vs Statistics: ML has a heavier focus on prediction, and lesser on interpretation.
- ML applications often involve large sets → computational complexity of algorithms is important.
  - Statistics often does not care about runtime

# Why probability models?

- Probability models and statistical inference provide a framework
- A principled way to think about any problem in machine learning
  - Probabilistic model → Estimation → Prediction
- Probabilistic models quantify uncertainties.
  - Deterministic answers may often be inappropriate



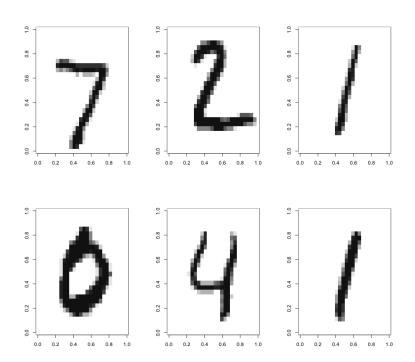
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The currency exchange rate tomorrow will be 10.41!

# Why probability models?

As robotics is now moving into the open world, the issue of uncertainty has become a major stumbling block for the design of capable robot systems. Managing uncertainty is possibly the most important step towards robust real-world robot systems.

## Example: classifying hadwritten digits



#### Example: classifying hadwritten digits

Training data: 60000 images.

Test data: 10000 images.

Features: intensities (0-255, scaled to 0-1) in the

 $28 \times 28 = 784$  pixels as features.

#### **Methods:**

- Multinomial regression with LASSO prior
- Support vector machines
- Neural Networks (deep?)

## Example: classifying hadwritten digits

Confusion matrix

#### **PREDICTION**

## T R U T H

```
      0
      1
      2
      3
      4
      5
      6
      7
      8
      9

      0
      966
      0
      8
      1
      1
      7
      9
      2
      4
      6

      1
      0
      1121
      1
      1
      0
      2
      3
      13
      7
      7

      2
      2
      2
      957
      13
      5
      4
      4
      21
      7
      0

      3
      0
      2
      9
      947
      0
      29
      1
      3
      12
      10

      4
      0
      0
      12
      1
      940
      5
      5
      9
      8
      32

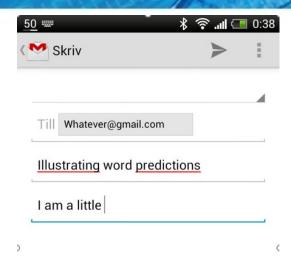
      5
      6
      1
      3
      19
      1
      816
      9
      1
      24
      9

      6
      4
      4
      13
      1
      7
      12
      926
      0
      10
      1

      7
      1
      0
      9
      10
      2
      2
      0
      954
      5
      13

      8
      1
      4
      17
      11
      2
      10
      1
      3
```

## Example: smartfone typing predictions





#### Example: smartfone typing predictions

Assume a simple (Markov) model of a sentence:

$$p(w_1, ..., w_n) = p(w_1)p(w_2|w_1) ... p(w_n|w_{n-1})$$

- Intuition:
  - p(person|crazy) = 0.1
  - p(horse|crazy) = 0.0001

Highest P(?|Donald)?

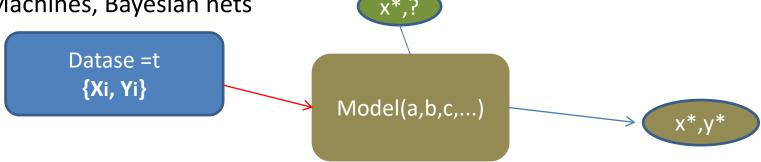
- Probability for sentence depends only on  $p(w_n|w_{n-1})$
- How to compute ? Investigate a lot of data!

$$p(w_k|w_{k-1}) = \frac{\# cases \ w_k \ follows \ w_{k-1}}{\# cases \ w_{k-1}}$$

- In practice, more advanced model used
  - Neural networks for ex.

## Types of learning

- Supervised learning (classification, regression)
  - Compute parameters from data
  - Given features of a new object, predict target (generalize beyond seen training data)
  - Classification (Y=categorical), Regression (Y=continuous)
- Most of ML models: Neural Nets, Decision Trees, Support Vector Machines, Bayesian nets



# Types of learning

- Unsupervised learning (→Data Mining)
  - No target
  - Aim is to extract interesting information about
    - Relations of parameters to each other
    - Grouping of objects

Ex: clustering, density estimation, association analysis

## Types of learning

- **Semi-supervised**: targets are known only for some observations.
- Active learning. Strategies for deciding which observations to label
- Reinforcement learning. Find suitable actions to maximize the reward. True targets are discovered by trial and error.
- Transfer learning: use knowledge from some domain to train better models in a similar domain

## Basic ML ingridients

- Data T: observations (cases)
  - Features  $x_1, \dots x_p$
  - Targets  $y_1, \dots, y_r$

Case	$x_1$	$x_2$	y
1			
2			

- Mathematical Model  $P(x|w_1,...w_k)$  or  $P(y|x,w_1,...w_k)$ 
  - Example: Linear regression  $p(y|x, w) = N(w_0 + w_1 x, \sigma^2)$
- Learning algorithm (data  $\rightarrow$  get parameters  $\widehat{w}$  or p(w|D))
  - Maximum likelihood, Bayesian estimation...
- Prediction of new data  $x_*$  by using the fitted model

## Types of data sets

- Training data (training set T): used for learning the model
  - Supervised learning:  $w_i$  in  $P(y|x, w_1, ..., w_k)$  estimated using T

X	Υ
1.1	M
2.3	F

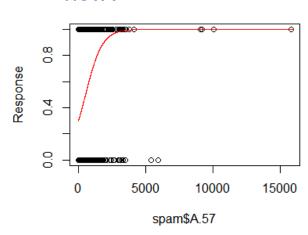
- Test data (test set T\*): used for predictions
  - Supervised learning: estimate  $p(y_*)$  or  $\widehat{y_*}$  for new  $x_*$

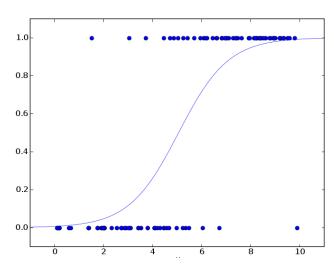
X	Υ
1.3	?
2.9	?

## Logistic regression

- Data  $y_i \in \{Spam, Not Spam\}, x_i = \#of \ a \ word$
- Model:  $p(y = Spam|w, x) = \frac{1}{1 + e^{-w_0 w_1 x}}$
- Learning algorithm: maximum likelihood
- Prediction :  $p(spam) = p(Y = spam | x_*)$

We can also make point predictions -how?

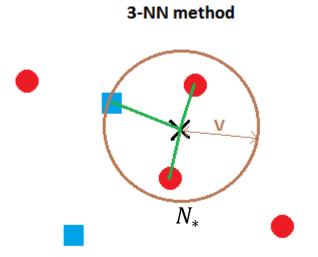




## K-nearest neighbor model

Can be classification or regression

- Basic idea:
  - For given  $x_*$ , find K nearest observations
  - Classification: majority voting
  - Regression: compute mean
- K is called hyperparameter



# K-nearest neighbor algorithm

```
Data: Training data \{\mathbf{x}_i, y_i\}_{i=1}^n and test input \mathbf{x}_{\star}
```

**Result:** Predicted test output  $\widehat{y}(\mathbf{x}_{\star})$ 

- 1 Compute the distances  $\|\mathbf{x}_i \mathbf{x}_{\star}\|_2$  for all training data points  $i = 1, \dots, n$
- 2 Let  $\mathcal{N}_{\star} = \{i : \mathbf{x}_i \text{ is one of the } k \text{ data points closest to } \mathbf{x}_{\star}\}$
- 3 Compute the prediction  $\widehat{y}(\mathbf{x}_{\star})$  as

$$\widehat{y}(\mathbf{x}_{\star}) = \begin{cases} \text{Average}\{y_j : j \in \mathcal{N}_{\star}\} & \text{(Regression problems)} \\ \text{MajorityVote}\{y_j : j \in \mathcal{N}_{\star}\} & \text{(Classification problems)} \end{cases}$$

# K-nearest neighbor model

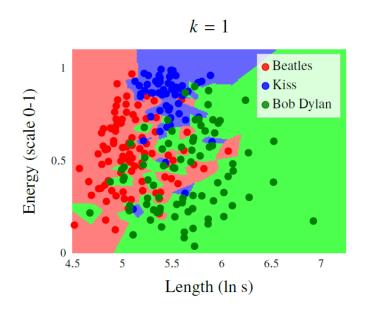
- Data  $T = \{(x_i, y_i), i = 1, ..., n\}$
- Model: W same size as T
- Learning algorithm: Set W=T, compute distances in W
- Prediction:

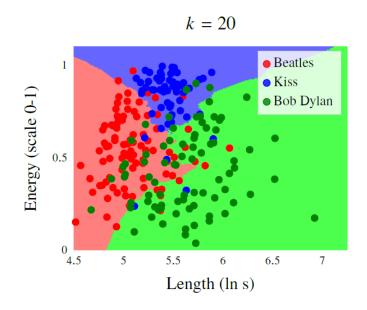
$$-y_* = \frac{1}{|N_*|} \sum_{i \in N_*} y_i$$
$$-y_* = MajorityVote_{i \in N_*}(y_i)$$

## K-nearest neigbor example

#### Classification

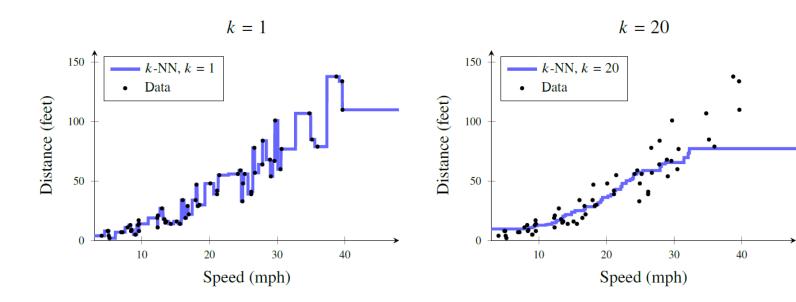
Music data, x1=song length, x2=a signal processing characteristic





# K-nearest neighbor example

- Regression
  - Car data: x1 speed when brake signal given, x2 distance until full stop



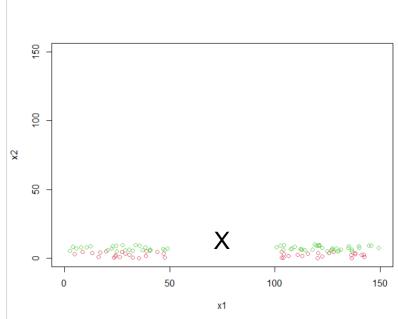
How to choose K?

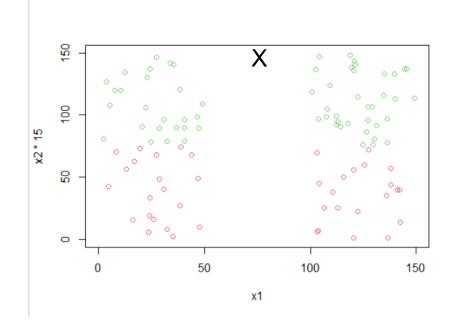
How to define distance?

## K-nearest neighbor model

- Feature preprocessing: scaling
  - Important, for ex when defining distance

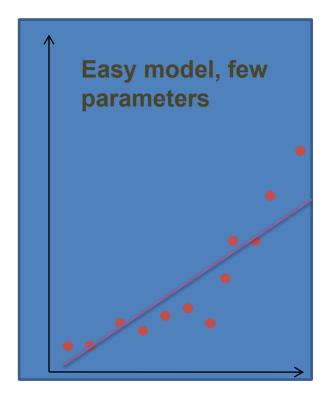
- Usual preprocessing: 
$$x'_{ij} = \frac{x_{ij} - mean(x_{ij}|i=1,...n)}{std(x_{ij}|i=1,...n)}$$

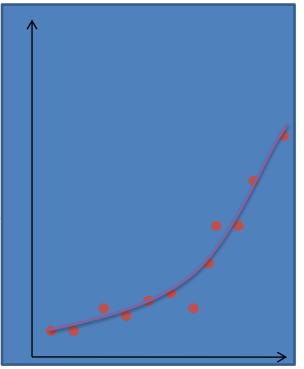


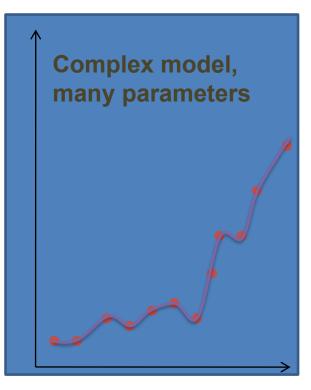


# Overfitting

Which model feels appropriate?

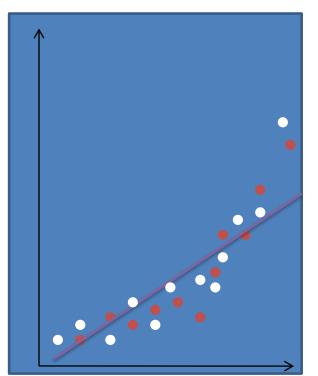


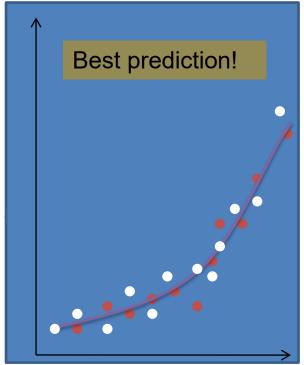


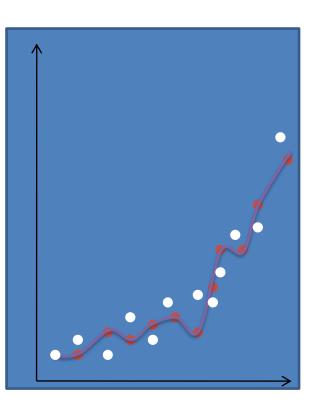


# Overfitting

#### Now new data from the same process

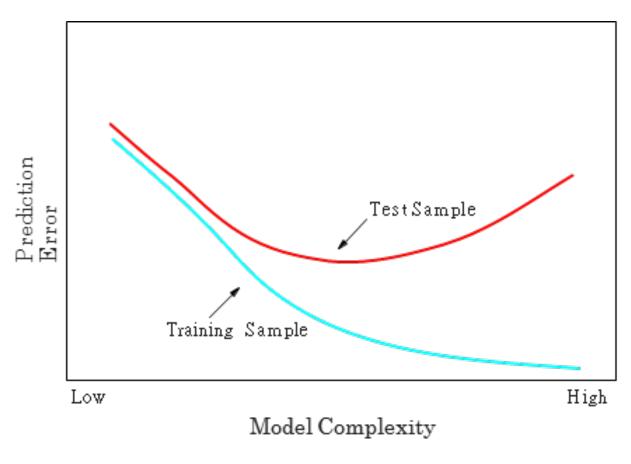






# Overfitting

#### • Observed:



#### Model selection

- Given several models  $M_1$ , ...  $M_m$
- Divide data set into training and test data

Training	Test
----------	------

- Fit models  $M_i$  to training data  $\rightarrow$  get parameter values
- Use fitted models to predict test data and compare test errors  $R(M_1)$ , ...  $R(M_m)$
- Model with lowest prediction error is best

#### **Comment:**

Approach works well for moderate/large data

#### Holdout method

Divide into training, validation and test sets

Training Validation Test

Choose proportions in some way

 Test set is used to test a performance on a new data

#### Holdout in R

- How to partition into train/test?
  - Use set.seed(12345) in the labs to get identical results

```
n=dim(data)[1]
set.seed(12345)
id=sample(1:n, floor(n*0.7))
train=data[id,]
test=data[-id,]
```

How to partition into train/valid/test?

```
n=dim(data)[1]
set.seed(12345)
id=sample(1:n, floor(n*0.4))
train=data[id,]
id1=setdiff(1:n, id)
set.seed(12345)
id2=sample(id1, floor(n*0.3))
valid=data[id2,]
id3=setdiff(id1,id2)
test=data[id3,]
```

# Typical error functions

Regression, MSE:

$$R(Y, \widehat{Y}) = \frac{1}{N} \sum_{i=1}^{N} (Y_i - \widehat{Y}_i)^2$$

Classification, misclassification rate

$$R(Y, \widehat{Y}) = \frac{1}{N} \sum_{i=1}^{N} I(Y_i \neq \widehat{Y}_i)$$

• Classification, cross-entropy for M classes  $C_1, \dots, C_M$ :

$$R(Y, \hat{p}(Y)) = -\sum_{i=1}^{N} \sum_{m=1}^{M} I(Y_i = C_m) \log \hat{p}(Y_i = C_m)$$

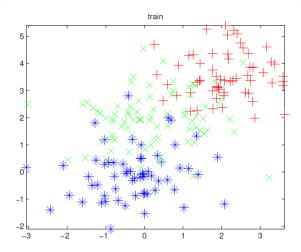
## Model types

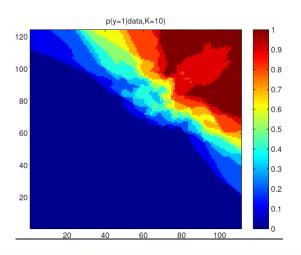
#### Parametric models

- Have certain number of parameters independently of the size of training data
- Assumption about of the data distribution
- Ex: logistic regression

#### Nonparametric models

- Number of parameters (complexity) changes with training data
  - Example: K-NN classifier

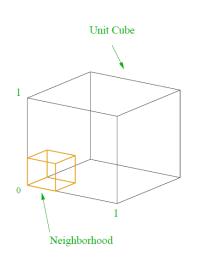


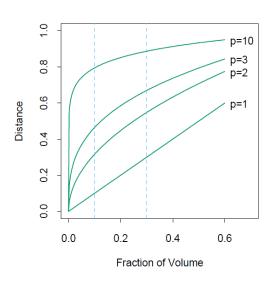


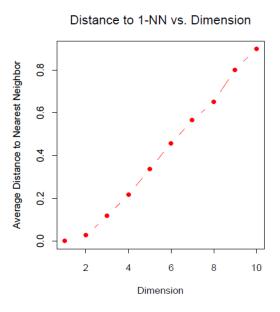
## Curse of dimensionality

- Given data *T*:
  - Features  $x_1, \dots x_p$
  - Targets  $y_1, \dots, y_r$
- When p increases models using "proximity" measures work badly
- Curse of dimensionality: A point has no "near neighbors" in high dimensions → using class labels of a neighbor can be misleadning
  - Distance-based methods affected

# Curse of dimensionality







# Curse of dimensionality

Hopeless? No!

- Real data normally has much lower effective dimension
  - Dimensionality reduction techniques
- Smoothness assumption
  - small change in one of x's should lead to small change in  $y \rightarrow$  interpolation