

Implementing Tuple Variables in Gecode

Bachelor Thesis

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Abstract

This is the abstract

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2 Introduction

2.1 Constraint Programming

Constraint programming (CP) is a method to solve problems by first modeling the problem with different types of variables and then adding constraints that the variables must fulfill. The variables have an initial domain of possible values. The CP solver then uses the constraints to remove impossible values. A very typical problem suitable for constraint programming is sudoku. The most intuitive model is a 9×9 matrix of integer variables. The general constraints for all standard sudokus is that every cell has a domain of $\{1..9\}$, and that all cells in a row, column and box must be different. For a specific sudoku constraints are added to require specific cells to have specific values.

The available data types limits the options to model a specific problem. With more data types a specific problem can be modeled in different ways. There is a famous problem called Queens. The problem is to place eight queens on a chess board in such a way that no queen threatens another. If only boolean variables were available we would have to model the problem with 64 boolean variables. If we instead use integer variables we can use the fact that all rows will have exactly one queen when we model the problem. This could be solved with booleans by redundant constraints, but it is more efficient to implement the constraints directly in the model.

2.2 Terminology

- Constraint - A condition that may be hard or soft. Hard constraints must be satisfied, but soft conditions are optional. The latter are used for optimisation problems.

- Propagator - In its simplest form it just tells if there exists a solution in current domain according to the specific constraint the propagator handles, but in reality it also performs pruning.
- Pruning - Removing values from the domain of a variable with a propagator.
- Searching - The brute force searching one want to avoid. It's basically done by assigning a variable to a value in it's domain and rerun all propagators.
- Brancher - When no propagator can prune anything searching is needed. This is done with a brancher, which splits the domain in two or more parts, creating a search tree.
- Variable - In CP a variable has a domain of values. The goal is to reduce the domain to size one.
- Domain - The set of possible values for a variable. The domain can be exact or approximate. All values that should be in an exact domain representation should also be in any approximation.
- Assigned Variable - A variable with domain size exactly one is called assigned.
- Failed Variable - A variable with domain size zero is called failed.
- Solution - A state where all variables are assigned and all hard constraints are satisfied.
- Fixpoint - A propagator is at a fixpoint when it can't prune the domain more by running again before the variables has been modified.
- Subsumed - A subsumed propagator is done. No matter what happens to the variables it can not prune more values.

2.3 Gecode

Gecode is an open source CP solver programmed in C++ and is licensed under the MIT license. It is flexible and supports customization of most parts, including data types, branchers and propagators. It is suitable for both education and professional use. In this thesis, Gecode 4.3.2 was used.

For more information, consult the homepage. <http://www.gecode.org>

3 Background

3.1 The need for Tuple Variables

When using a CP solver, one wants to avoid brute force searching. This is done by intelligently choosing model and constraints. By doing this the variable domains can be pruned to smaller sizes. For example, if two variables x and y have domains $dom(x) = \{1, 2, 3\}$ and $dom(y) = \{2, 3, 4\}$, and the constraint $y < x$ is applied the domains can be pruned to $dom(x) = \{3\}$ and $dom(y) = \{2\}$. If we instead have the same variables but add the constraint $x \neq y$ nothing would be pruned, since for all values in both domains there exists solutions. In this example the problem was modeled with two integer variables, but if the problem instead would be modeled with one tuple variable pruning would be possible. Then we would have a tuple variable t with domain $dom(t) = \{\langle 1, 2 \rangle, \langle 1, 3 \rangle, \langle 1, 4 \rangle, \langle 2, 2 \rangle, \langle 2, 3 \rangle, \langle 2, 4 \rangle, \langle 3, 2 \rangle, \langle 3, 3 \rangle, \langle 3, 4 \rangle\}$ and pruning with

the same constraint would yield $dom(t) = \{\langle 1, 2 \rangle, \langle 1, 3 \rangle, \langle 1, 4 \rangle, \langle 2, 3 \rangle, \langle 2, 4 \rangle, \langle 3, 2 \rangle, \langle 3, 4 \rangle\}$. This shrinks the size of the search tree from 9 to 7.

If we instead look at the case where $dom(x), dom(y) = \{1..1000\}$ and the constraint $x = y$ the benefits are more obvious. Using integer variables no values can be pruned. If tuple variables were used, the size of the domain would shrink from 10^6 to 10^3 . This indicates that tuple variables can be quite useful.

The main benefit of a tuple is the possibility to link variables together. The most obvious case is when dealing with coordinates, but it can be generalized to any case where it is interesting to see if a combination of two variables are part of a solution.

4 Tuple Variable

4.1 Creating a New Variable

4.1.1 Specification File

Creating the specification file is the first thing that needs to be done when designing a new variable. Caution should be taken, because this step may be very hard to modify later. A simple specification file could look like this.

```
[ General ]
Name:      IntTuple
Namespace: MPG::IntTuple
[ ModEvent ]
Name:      FAILED=FAILED
[ ModEvent ]
Name:      VAL=ASSIGNED
[ ModEvent ]
Name:      NONE=NONE
[ PropCond ]
Name:      NONE=NONE
[ PropCond ]
Name:      VAL=ASSIGNED
ScheduledBy: VAL
[ End ]
```

As can be seen, there are three sections. The specification file must start with the [General] section and end with [End]. There are also sections for modification events and propagation conditions. When the specification file is written a configuration script is used to generate base classes from the specification file.

The [General] section is pretty straight forward. This is where the name and namespace of the variable is specified. Both name and namespace are arbitrary. In Gecode the standard variables have namespace Gecode::VarName and in the examples in the documentation they instead have the namespace MPG::VarName.

The [ModEvent] section describes the modification events. For all variables, modification events for NONE, FAILED and ASSIGNED are required. More modification events may be added to avoid unnecessary executions of propagators.

The [PropCond] section describes how the propagators are scheduled. For all variables, propagator conditions for NONE and ASSIGNED are required.

4.1.2 Variable Implementation

The variable implementation class would with the specification file in the previous section be called `IntTupleImp` and inherit from the class `IntTupleVarBase` generated from the specification file. It has to implement a function called `assigned` that returns true if the variable is assigned.

4.1.3 Variable Class

The variable class is the class that is used when modeling the actual problem and inherits from the variable implementation. It is a read only user interface, and a programmer that does not program any custom branchers or propagators will not use anything else than this. This class would be called `IntTupleVar`.

4.1.4 Deltas

4.1.5 Views

The variable implementation class does implement methods for modification of the variable, but the variable class does not give access to these. Instead these are called from a view, which is a read and write interface to the implementation class.

4.1.6 Propagators

A propagator implements constraints and prunes variables. They interact with the views and not variable class and have four possible return values.

- `ES_FAILED` - There are no values in the domain that satisfies the constraint. The variable is failed.
- `ES_FIX` - The propagator is at a fixpoint. It is impossible for the propagator to prune more values before the domain has changed for any of the variables the propagator depend on by either a brancher or another propagator.
- `ES_NOFIX` - The propagator may be at a fixpoint, but it is not guaranteed. Running it once more may or may not prune some values. Unless it is at a fixpoint for sure, this should be used.
- `ES_SUBSUMED` - The propagator is done. Regardless of any changes made to the variable this particular propagator will not be able to do anything more.

The propagator must implement `ES_FAILED` and at least one of the others. `ES_NOFIX` is safe to return in the sense that it does not promise anything. Furthermore, the propagator needs the following methods:

- `post` - The method for posting a constraint, which basically is saying that a certain constraint should be used.
- `disposal` - This works as a destructor. The only reason to not have a regular destructor is that destructors in C++ can't take arguments.
- `copy` - A method to copy the propagator.
- `cost` - Estimates the cost to run the propagator. This does not affect the correctness, but may improve efficiency by making it easier for the Gecode engine to schedule cheap propagators before expensive ones.

- propagate - The method which does the actual work. It prunes domains and determines the status to return.

A propagator must also subscribe to variables, that is, telling Gecode when the propagator should be awoken. For instance, a propagator that says that x should be less than y should subscribe to the maximum value of x and minimum value of y .

Consistency A propagator can work with different consistencies. Bound consistency means that the propagator ensures that the bounds (min and max value for an integer variable) satisfies the constraint. If if $dom(x) = 1, 5, 7, 8$ and $dom(y) = 1, 3, 7$ and the constraint $x = y$ is applied, the propagator would yield $dom(x) = 1, 5, 7$ and $dom(y) = 1, 3, 7$ with bounds consistency, since there are solutions to $x = 1, x = 7, y = 1$ and $y = 7$. $x = 5$ and $y = 3$ is not considered. Pruning the whole domain does in general cost more execution time.

4.1.7 Branchers

When there are no propagators able to prune any variables the CP solver must start searching. The branchers determines how this is done. The simplest brancher just puts the first value in the first branch and the rest of the values in a second branch. Another way is to pick a random value in the domain, but more sophisticated ways exist. For the IntPair variable only a simple brancher is implemented. The domain of IntPair is just a long sorted list, and the brancher picks the first value.

A brancher must implement the following methods:

- status
- choice
- commit
- print
- ngl

4.2 Implementation of Exact IntPair

The exact version does not approximate the domain, that is, the implementation is a long list of all integer pairs that's currently in the domain.

The specification is as follows.

[General]	
Name:	IntPair
Namespace:	Gecode::IntPair
[ModEvent]	
Name:	FAILED=FAILED
[ModEvent]	
Name:	NONE=NONE
[ModEvent]	
Name:	VAL=ASSIGNED
[PropCond]	

Name:	NONE=NONE
[PropCond]	
Name:	VAL=ASSIGNED
ScheduledBy:	VAL
[PropCond]	
Name:	BND
ScheduledBy:	VAL, BND, XBND, YBND, XMIN, YMIN, XMAX, YMAX
[PropCond]	
Name:	XBND
ScheduledBy:	VAL, BND, XMIN, XMAX
[PropCond]	
Name:	YBND
ScheduledBy:	VAL, BND, YMIN, YMAX
[PropCond]	
Name:	XMIN
ScheduledBy:	VAL, BND, XMIN, XBND
[PropCond]	
Name:	XMAX
ScheduledBy:	VAL, BND, XMAX, XBND
[PropCond]	
Name:	YMIN
ScheduledBy:	VAL, BND, YMIN, YBND
[PropCond]	
Name:	YMAX
ScheduledBy:	VAL, BND, YMAX, YBND
[End]	

4.3 Restrictions

To keep things simple only two-dimensional integer tuples are considered, so called Pairs.

4.4 Implementation of Rectangle IntPair

This version of IntPair approximates the domain by just storing four pairs. The benefit is vastly less use of memory, but the drawback is that it can't be pruned as efficient as the exact version. Another benefit for future work is that an approximation is possible to extend to float numbers.

4.5 Performance Test

5 Related Work

5.1 Implementation of bit-vector variables in a CP solver

5.2 A propagator design framework for constraints over sequences

6 Conclusions and future work

6.1 Rewrite the implementation in such a way that it may be accepted in a new Gecode release

All big software libraries have coding standards. There is plenty of work to rewrite the code for IntPairs in such a way that it satisfies Gecodes standard.

6.2 Test different implementations with different domain representations

6.3 Extend the tuples to arbitrary dimensions and not just pairs

This would require a complete rewrite of the variable implementation.

6.4 Extend the tuples to floats

6.5 Reach better performance for a specific problem with an array of pair variables than with two arrays of integer variables

7 Git repository

<http://github.com/patwotrik/gecode-tuples>

8 Links

https://en.wikipedia.org/wiki/Eight_queens_puzzle

9 Legal

This document is licensed under GPL v3 and may be redistributed as GPL v3 or later.

References

- [1] Calculus, Adams
- [2] Operating systems and its concepts, Galvin