
Logic and Computer Design Fundamentals

Chapter 5 – Digital Hardware Implementation

Part 2 – Programmable Implementation Technologies

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Overview

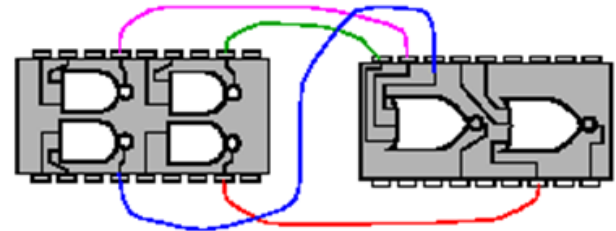
- **Part 1 – The Design Space**
- **Part 2 – Programmable Implementation Technologies**
 - **Why Programmable Logic?**
 - **Programming Technologies**
 - **Read-Only Memories (ROMs)**
 - **Programmable Logic Arrays (PLAs)**
 - **Programmable Array Logic (PALs)**
 - **Field Programmable Gate Array (FPGAs)**

Constructing Digital Circuits

Hand Wired Circuits

Cirri 1970-85

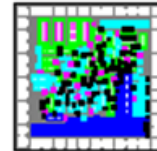
- Make 2 to 4 silicon gates in a package.
- Connect with wires.



VLSI circuits

Start with a silicon wafer and make:

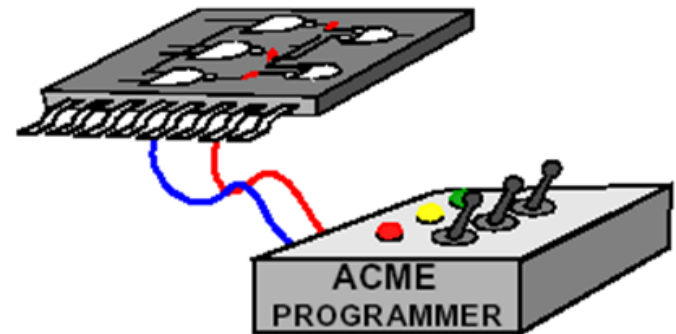
- the gates
 - the interconnections on top
- both made together.



Field Programmable circuits


Start with a silicon wafer and make:

- gates with no connections.
- Make connections later using:
 - 1) electrical means
 - blow fuses, grow anti fuses
 - use memory to hold connections
 - 2) deposit metal lines on top of silicon.



Why Programmable Logic?

- **Facts:**

- It is most economical to produce an IC in large volumes 
- Many designs required only small volumes of ICs

- **Need an IC that can be:**

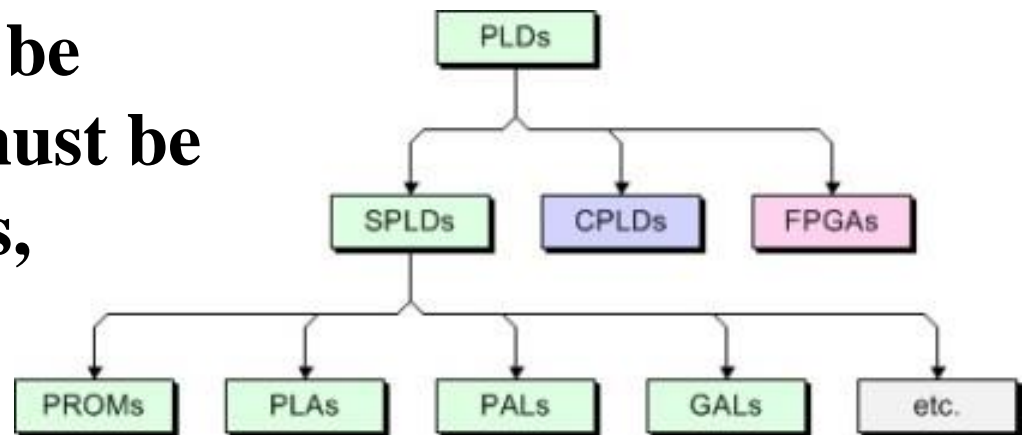
- Produced in large volumes
- Handle many designs required in small volumes

- **A programmable logic part can be:**

- made in large volumes
- programmed to implement large numbers of different low-volume designs

Programmable Logic Device


- A programmable logic device (PLD) is an electronic component used to build **reconfigurable** digital circuits.
- Unlike a logic gate, which has a fixed function, a PLD has an **undefined function** at the time of manufacture.
- Before the PLD can be used in a circuit it must be **programmed**, that is, **reconfigured**.

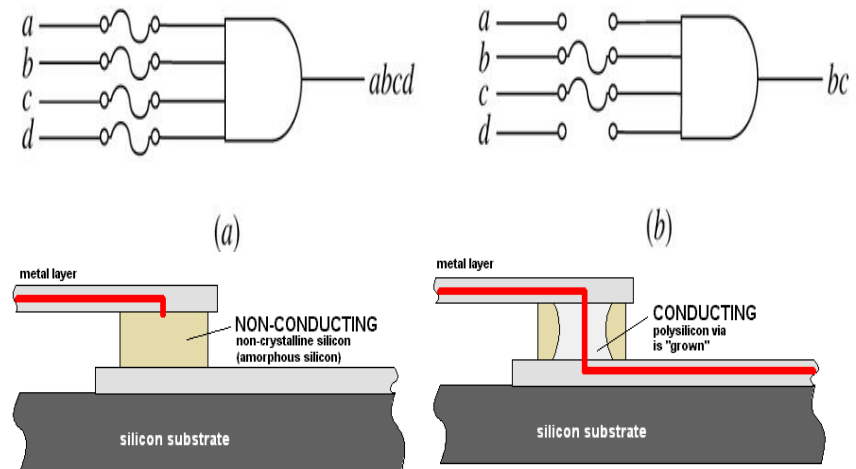


Programmable Logic - More Advantages

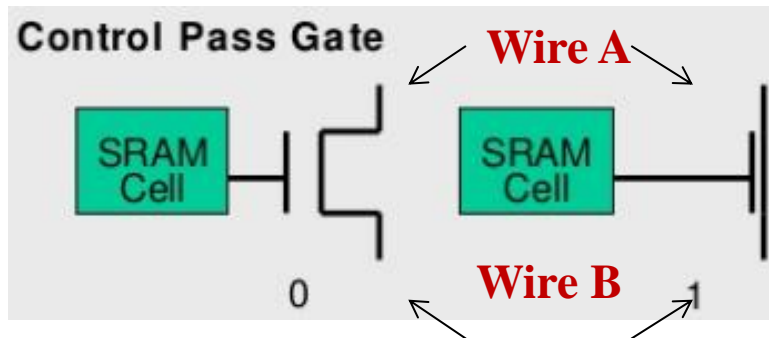
- Many programmable logic devices are *field-programmable*, i. e., can be programmed outside of the manufacturing environment
- Most programmable logic devices are *erasable* and *reprogrammable*.
 - Allows “updating” a device or correction of errors
 - Allows reuse the device for a different design - the ultimate in re-usability!
 - Ideal for course laboratories
- Programmable logic devices can be used to prototype design that will be implemented for sale in regular ICs.
 - Complete Intel Pentium designs were actually prototyped with specialized systems based on large numbers of VLSI programmable devices!

Programming Technologies

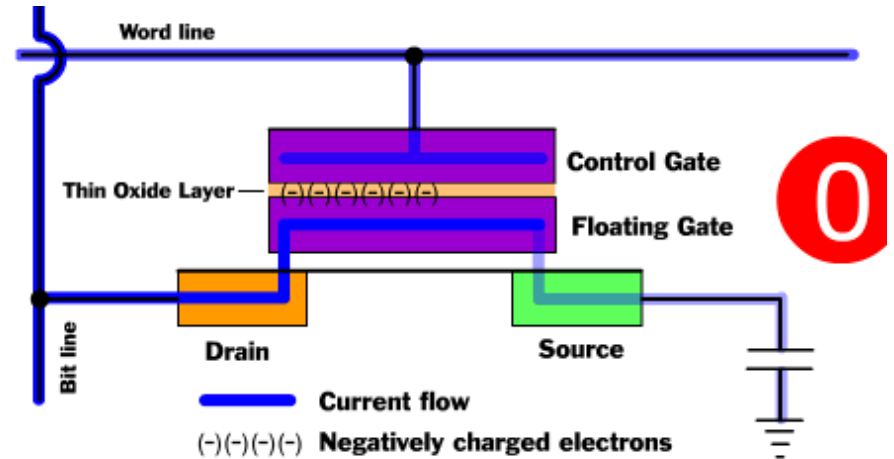
- Programming technologies are used to:
 - Control connections
 - Control transistor switching
 - Build lookup tables
- The technologies
 - Control connections
 - Mask programming
 - Fuse 
 - Antifuse



Programming Technologies (continued)



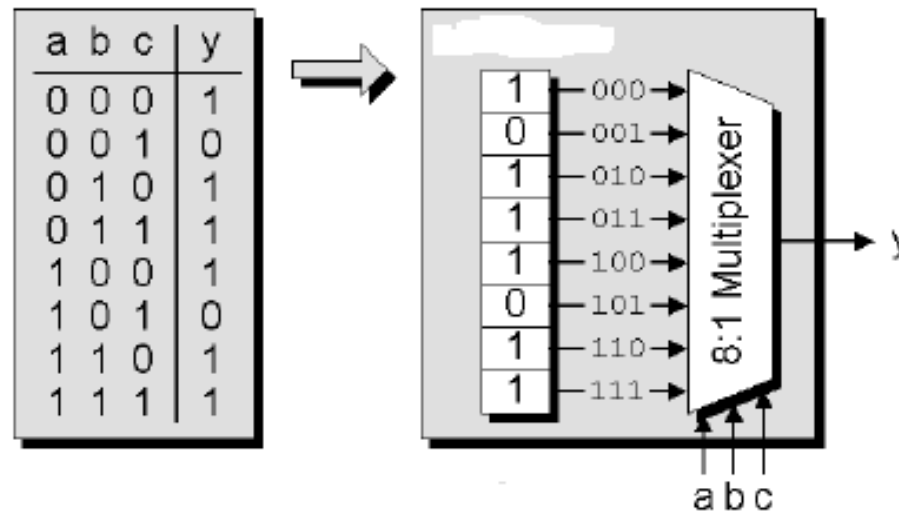
disconnect connect



- The technologies
 - Transistor Switching Control
 - Single-bit storage element
 - Stored charge on a **floating** gate
 - Erasable
 - Electrically erasable
 - Flash (as in Flash Memory)

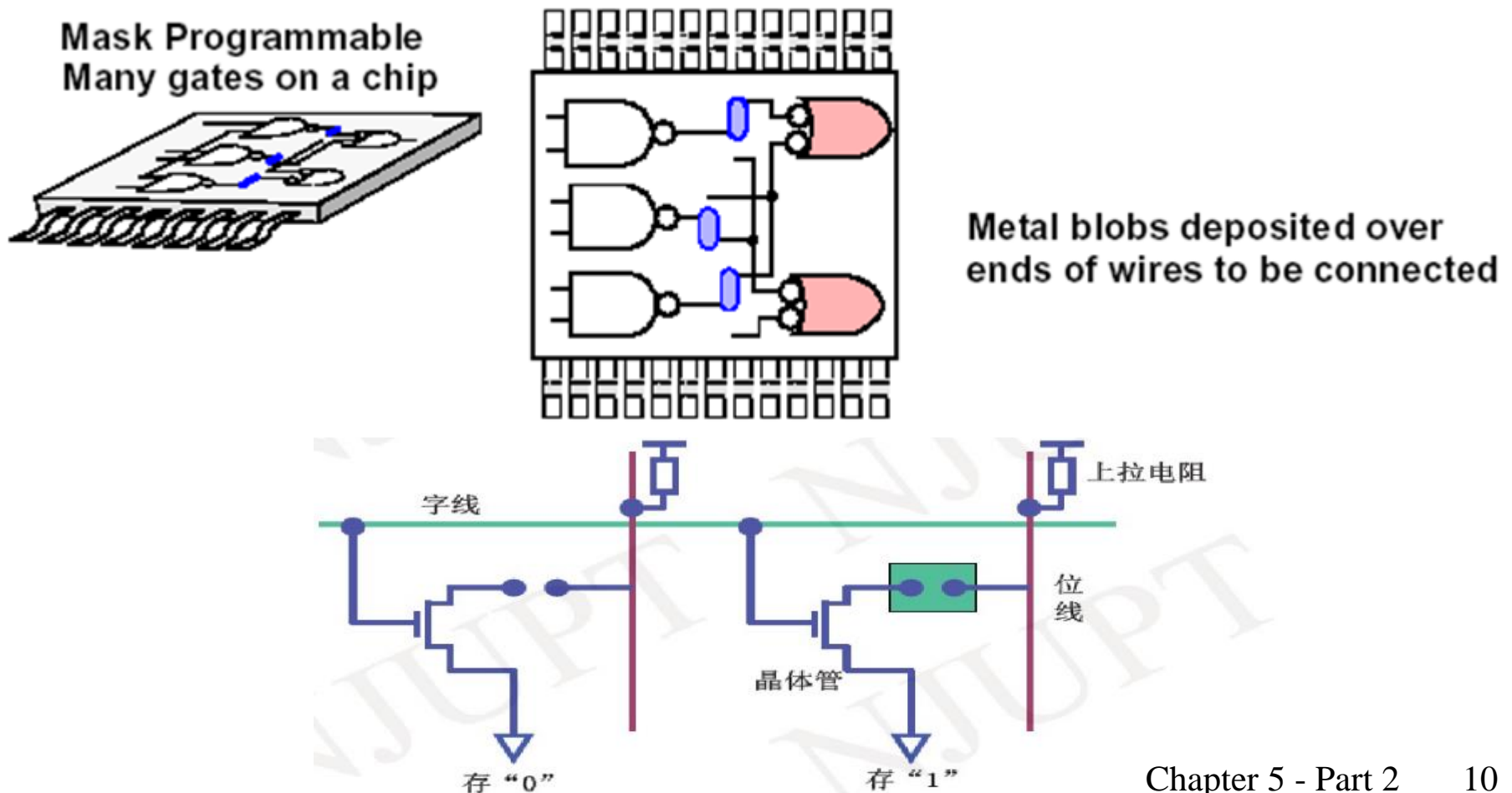
Programming Technologies (continued)

- The technologies
 - Build lookup tables
 - Storage elements 



Technology Characteristics

- **Permanent** - Cannot be erased and reprogrammed
 - **Mask programming (by manufacturers)**

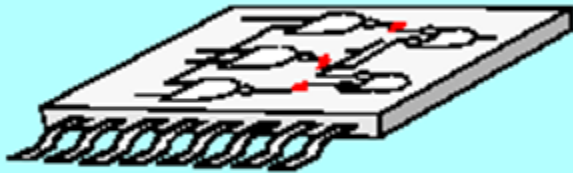


Technology Characteristics

- **Permanent** - Cannot be erased and reprogrammed
 - **Fuse**
 - **Antifuse**

(by users)

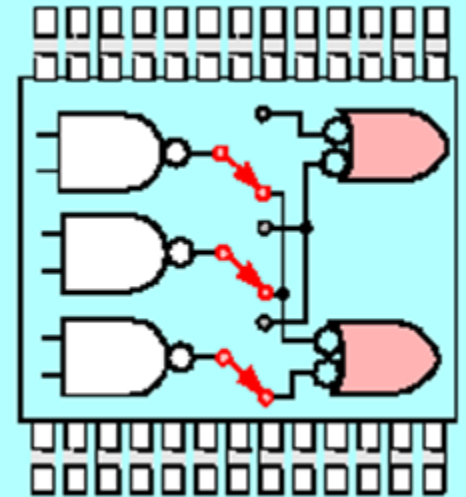
2. Electrically Programmable
Many gates on a chip



Electrically Controlled
Switches

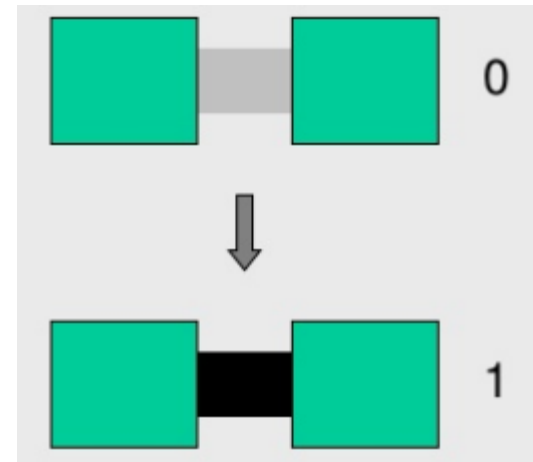
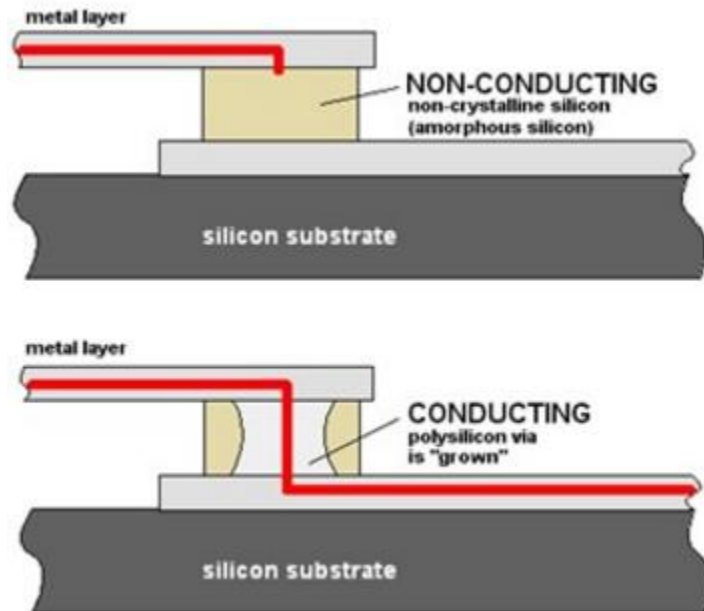
Fuses; blow to remove
unwanted connections

Antifuses; grow to
make connections



Antifuse technology

- Two metal layers sandwich a layer of non-conductive, **amorphous silicon**. When voltage is applied to this middle layer, the amorphous silicon is turned into **polysilicon**, which is conductive.



Technology Characteristics

■ Reprogrammable

- Volatile - Programming lost if chip power lost

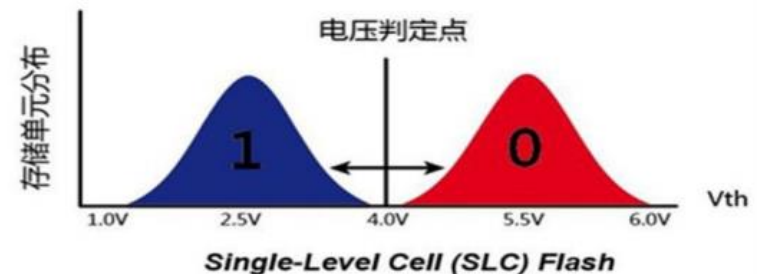
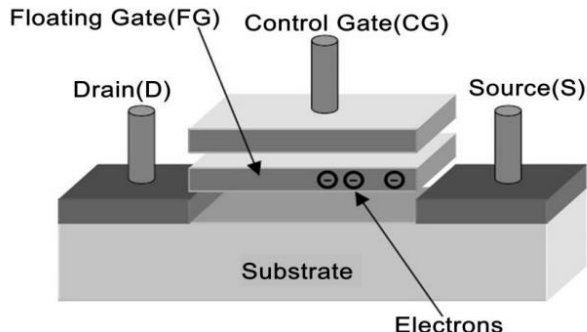
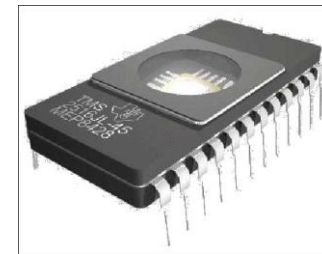
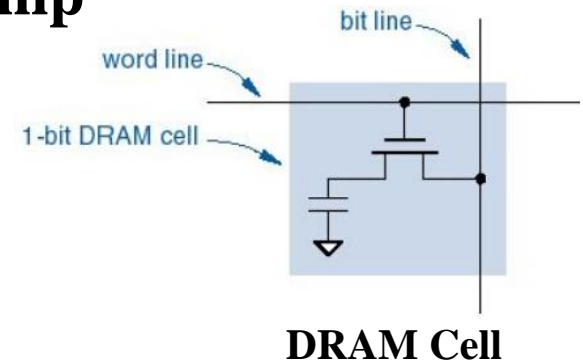
- Single-bit storage element

- Non-Volatile

- Erasable

- Electrically erasable

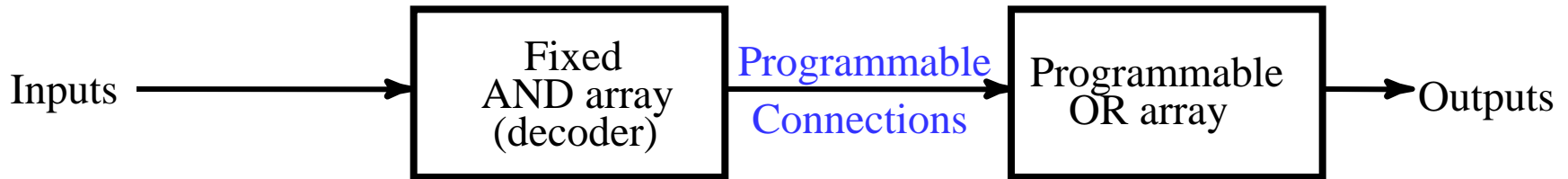
- Flash (as in Flash Memory)



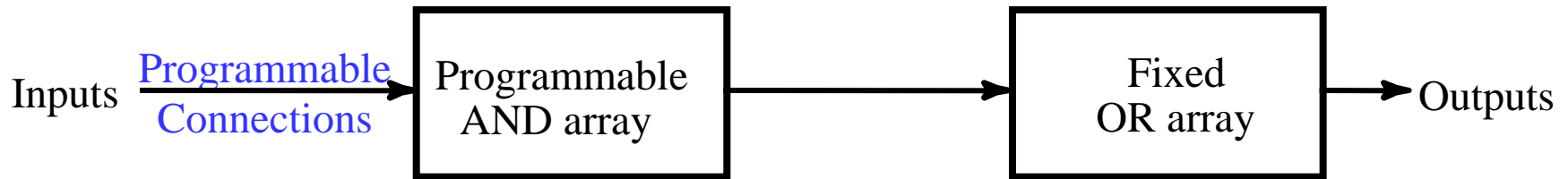
Programmable Configurations

- *Read Only Memory (ROM)* - a **fixed array of AND** gates and a **programmable array of OR** gates
- *Programmable Array Logic (PAL)[®]* - a **programmable array of AND** gates feeding a **fixed array of OR** gates.
- *Programmable Logic Array (PLA)* - a **programmable array of AND** gates feeding a **programmable array of OR** gates.
- *Complex Programmable Logic Device (CPLD) /Field-Programmable Gate Array (FPGA)* - complex enough to be called “architectures” - See VLSI Programmable Logic Devices reading supplement

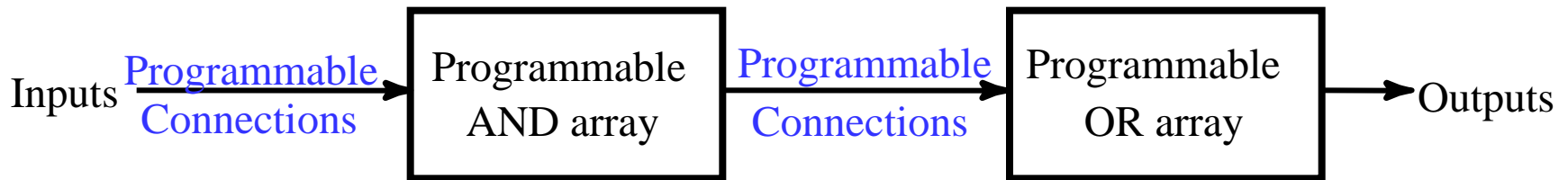
ROM, PAL and PLA Configurations



(a) Programmable read-only memory (PROM)

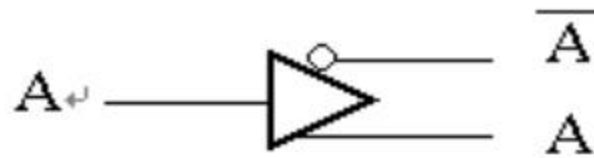


(b) Programmable array logic (PAL[®]) device



(c) Programmable logic array (PLA) device

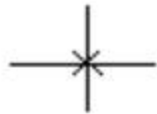
Logical symbols



Buffer



wire connecting
(not programmable)

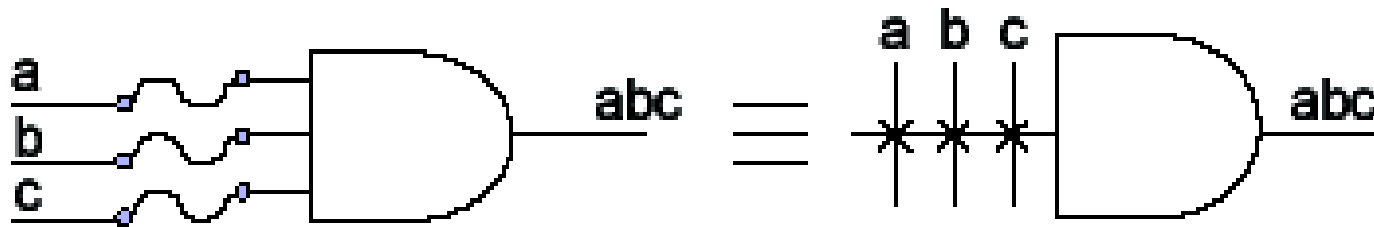


wire connecting
(programmable)

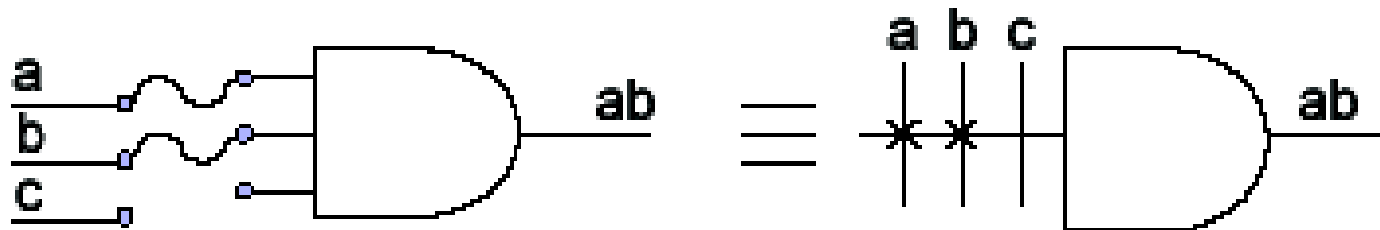


Disconnection
(erasable)

Logical symbols (continued)

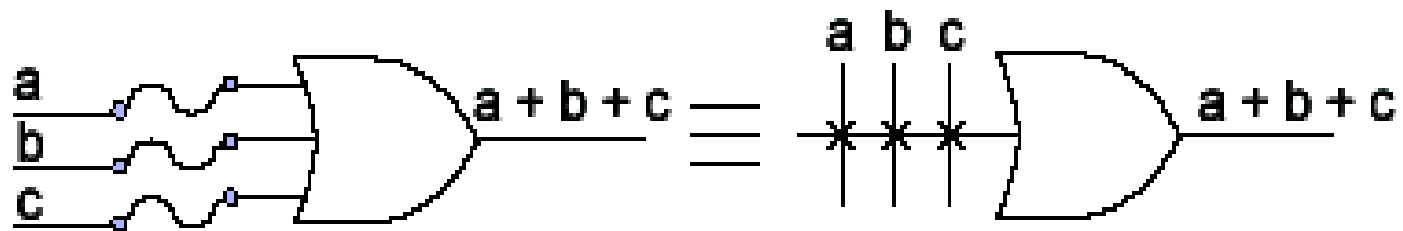


AND gate before programming

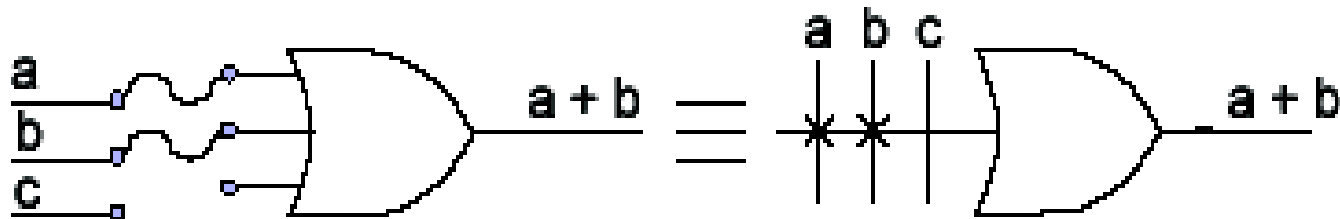


AND gate after programming

Logical symbols (continued)

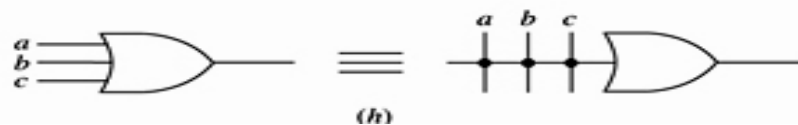
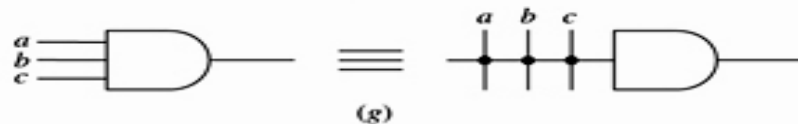
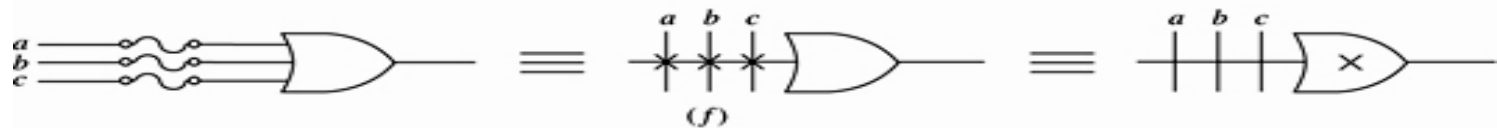
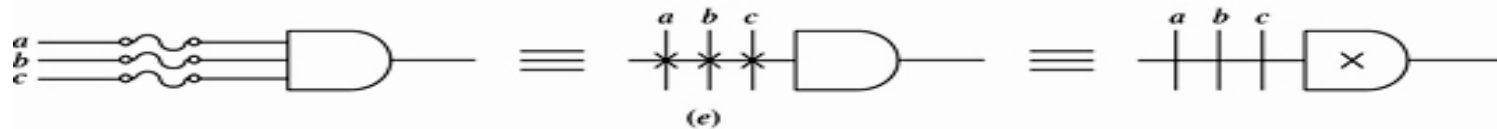
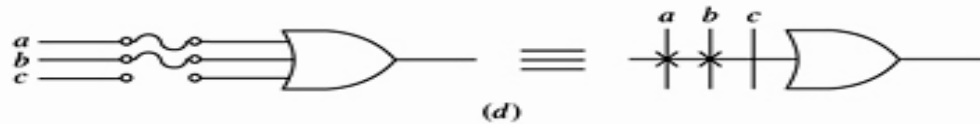
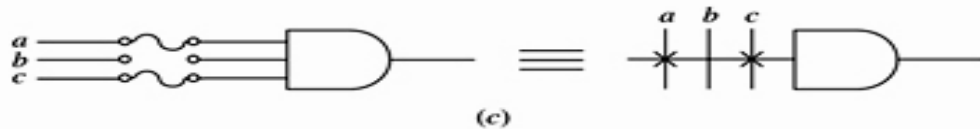
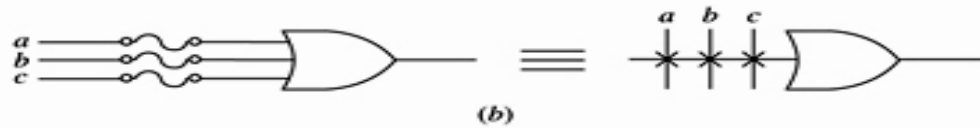
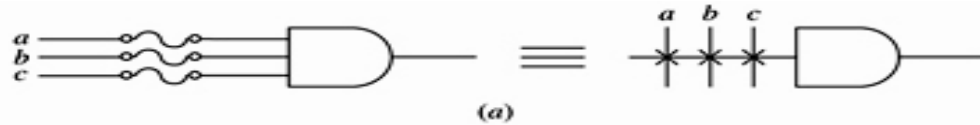


OR gate before programming



OR gate after programming

Logical symbols (continued)



Read Only Memory

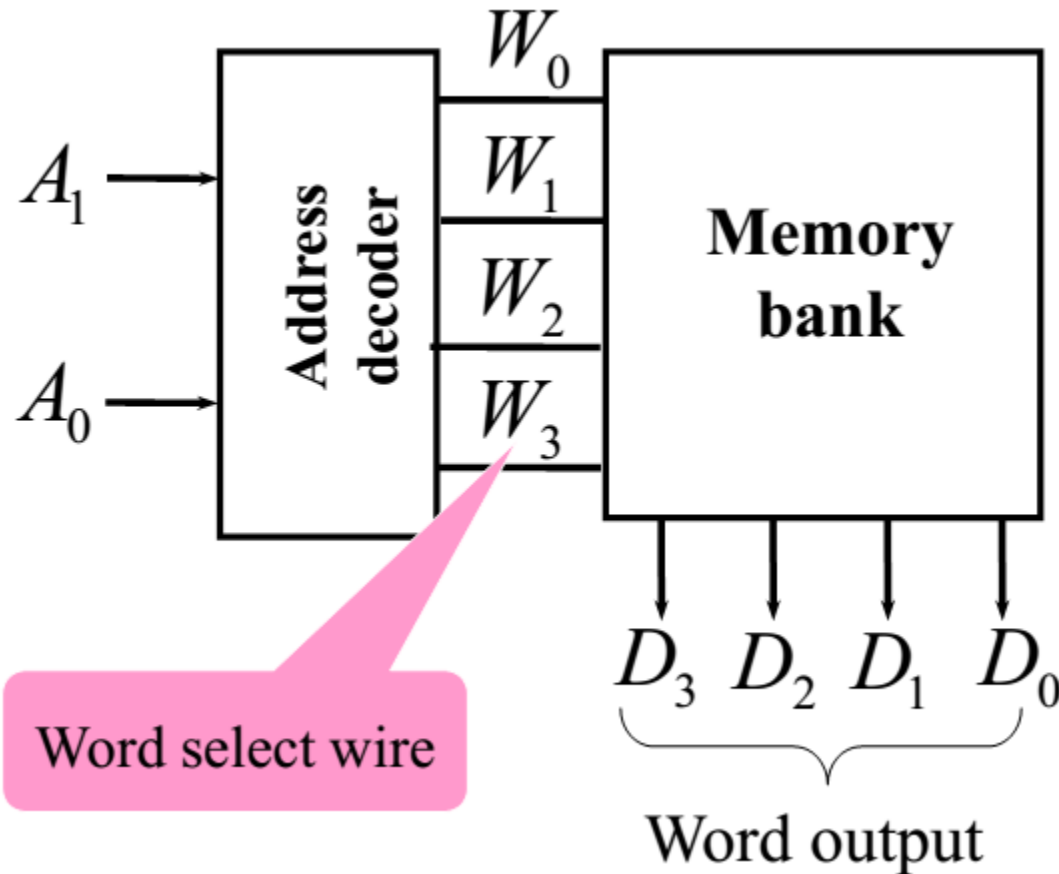
- **Read Only Memories (ROM) or Programmable Read Only Memories (PROM) have:**
 - **N input lines,**
 - **M output lines, and**
 - **2^N decoded minterms.**
- **Fixed AND array with 2^N outputs implementing all N-literal minterms.**
- **Programmable OR Array with M outputs lines to form up to M sum of minterm expressions.**

Read Only Memory

- A program for a ROM or PROM is simply a multiple-output truth table
 - If a 1 entry, a connection is made to the corresponding minterm for the corresponding output
 - If a 0, no connection is made
- Can be viewed as a *memory* with the inputs as *addresses* of *data* (output values), hence ROM or PROM names!

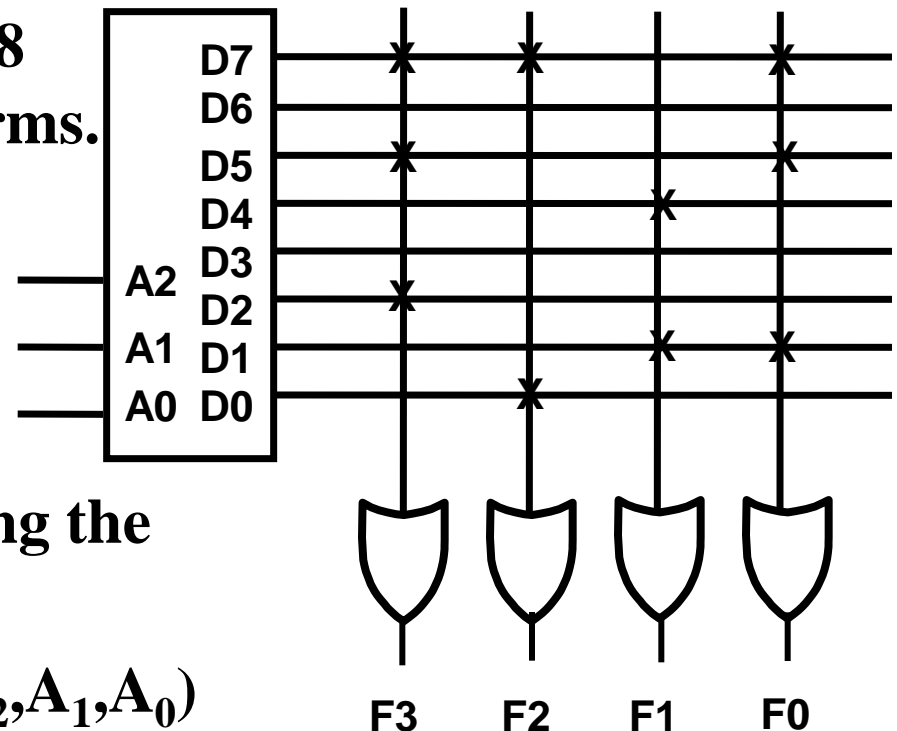
The general structure of ROM

- ROM size = $2^2 \times 4 = 16\text{bit}$



Read Only Memory Example

- Example: An 8×4 ROM (N=3 input lines, M=4 output lines)
- The **fixed "AND" array** is a “decoder” with 3 inputs and 8 outputs implementing minterms.
- The **programmable “OR” array** uses a single line to represent all inputs to an OR gate. An “X” in the array corresponds to attaching the minterm to the OR
- Read Example: For input $(A_2, A_1, A_0) = 001$, output is $(F_3, F_2, F_1, F_0) = 0011$.
- What are functions F_3, F_2, F_1 and F_0 in terms of (A_2, A_1, A_0) ?



Example: Square of 3-bit input number

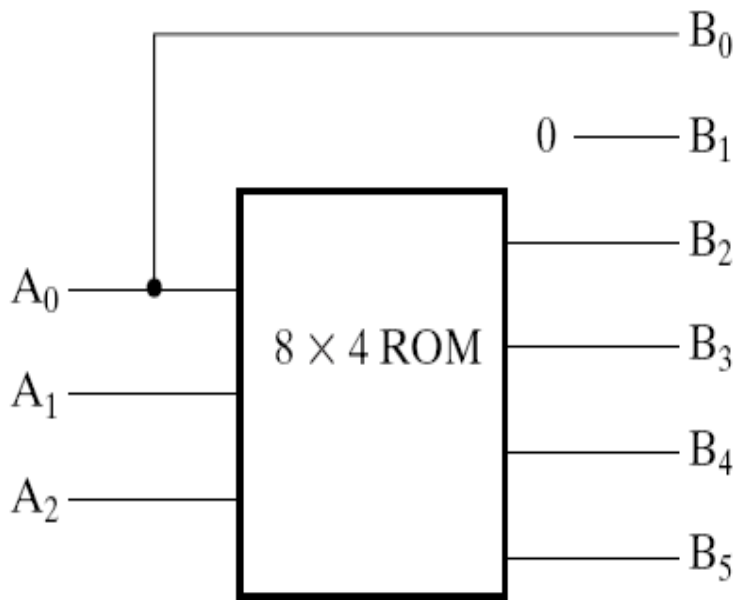
Inputs			Outputs						Decimal
A ₂	A ₁	A ₀	B ₅	B ₄	B ₃	B ₂	B ₁	B ₀	
0	0	0	0	0	0	0	0	0	0
0	0	1	0	0	0	0	0	1	1
0	1	0	0	0	0	1	0	0	4
0	1	1	0	0	1	0	0	1	9
1	0	0	0	1	0	0	0	0	16
1	0	1	0	1	1	0	0	1	25
1	1	0	1	0	0	1	0	0	36
1	1	1	1	1	0	0	0	1	49

How to choose ROM? $B_1 = 0$
 $B_0 = A_0$

8 × 4 ROM

Example: Square of 3-bit input number

- 8 × 4 bit ROM are selected ROM Truth Table**

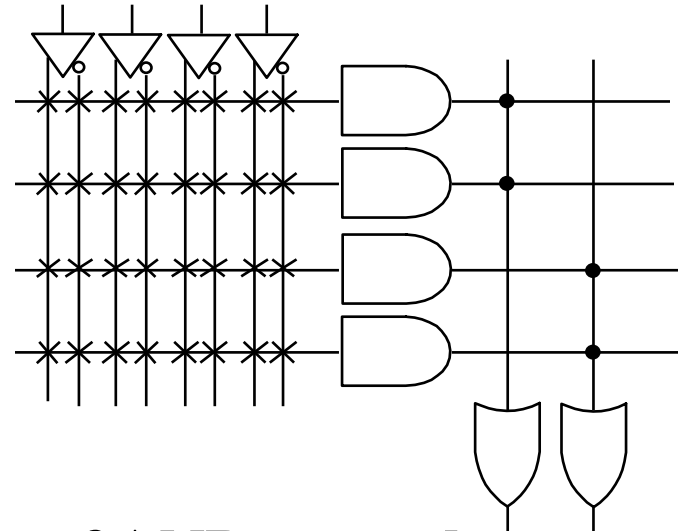


A_2	A_1	A_0	B_5	B_4	B_3	B_2
0	0	0	0	0	0	0
0	0	1	0	0	0	0
0	1	0	0	0	0	1
0	1	1	0	0	1	0
1	0	0	0	1	0	0
1	0	1	0	1	1	0
1	1	0	1	0	0	1
1	1	1	1	1	0	0

- **Are B_0 and B_1 reprogrammable?**

Programmable Array Logic (PAL)

- The PAL is the opposite of the ROM, having a **programmable set of ANDs combined with fixed ORs**.
- **PAL does not provide full decoding of the variables and does not generate all the minterms.**
- The decoder is replaced by an array of AND gates that can be programmed to **generate product terms** of the input variables.
- The product terms are then selectively connected to OR gates to provide the sum of products for the required Boolean functions.



Programmable Array Logic (PAL)

(continued)

■ Disadvantage

- ROM guaranteed to implement any M functions of N inputs. PAL may **have too few inputs to the OR gates**.

■ Advantages

- For given internal complexity, a PAL can have larger N and M
- Some PALs have outputs that can be complemented, adding POS functions
- No multilevel circuit implementations in ROM (without external connections from output to input). PAL has outputs from OR terms as internal inputs to all AND terms, making implementation of **multi-level circuits** easier.

Programmable Array Logic Example

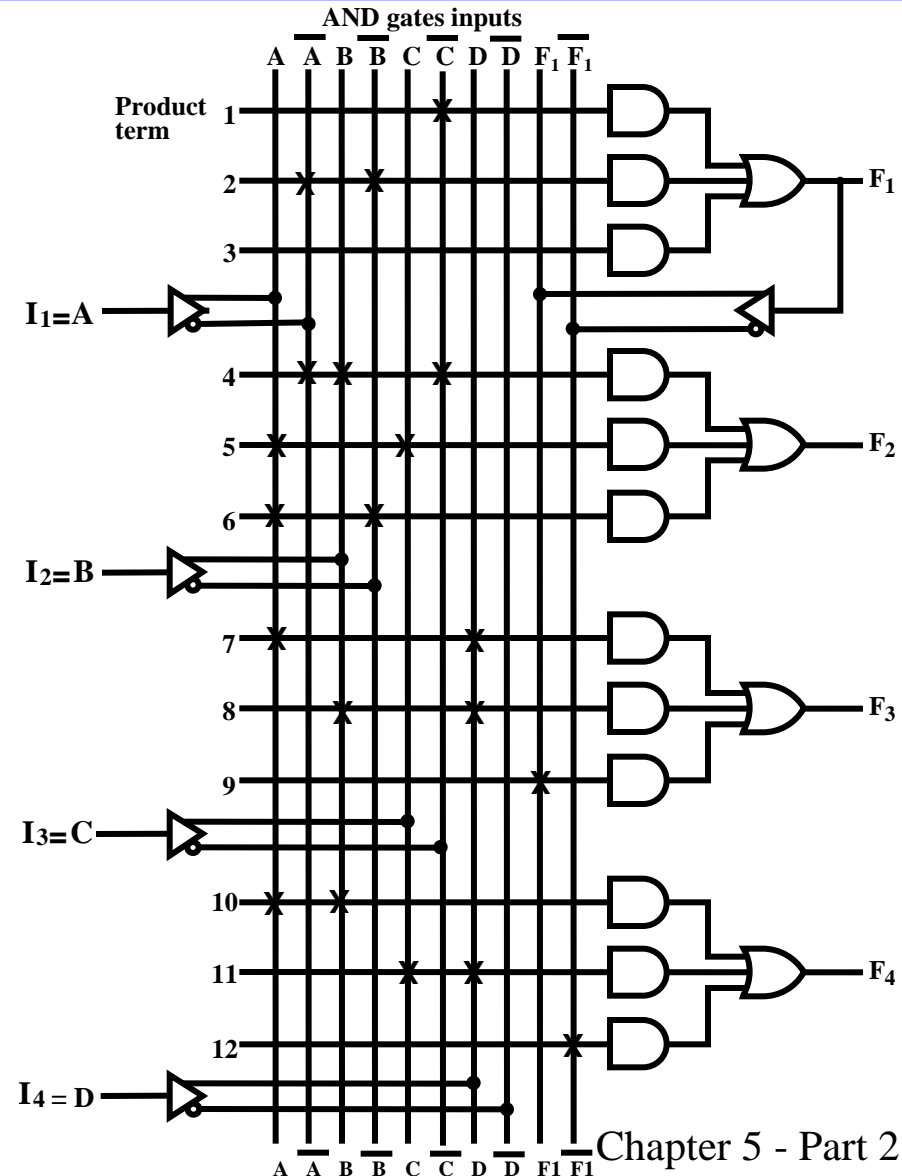
- 4-input, 4-output PAL with fixed, 3-input OR terms
- What are the equations for F1 through F4?

$$F1 = \overline{\overline{A}}\overline{\overline{B}} + \overline{C}$$

$$F2 = \overline{A}B\overline{C} + AC + A\overline{B}$$

$$F3 = AD + BD + \overline{F1}$$

$$F4 = AB + CD + \overline{F1}$$



Programmable Array Logic

- Design requires fitting functions within the limited number of ANDs per OR gate
- Single function optimization is the first step to fitting
- Otherwise, if the number of terms in a function is greater than the number of ANDs per OR gate, then **factoring** is necessary

Programmable Array Logic Example

- Equations: $F1 = A\bar{B}\bar{C} + \bar{A}B\bar{C} + \bar{A}\bar{B}C + ABC$
 $F2 = AB + BC + AC$

- F1 must be factored since four terms

- Factor out last two terms as W

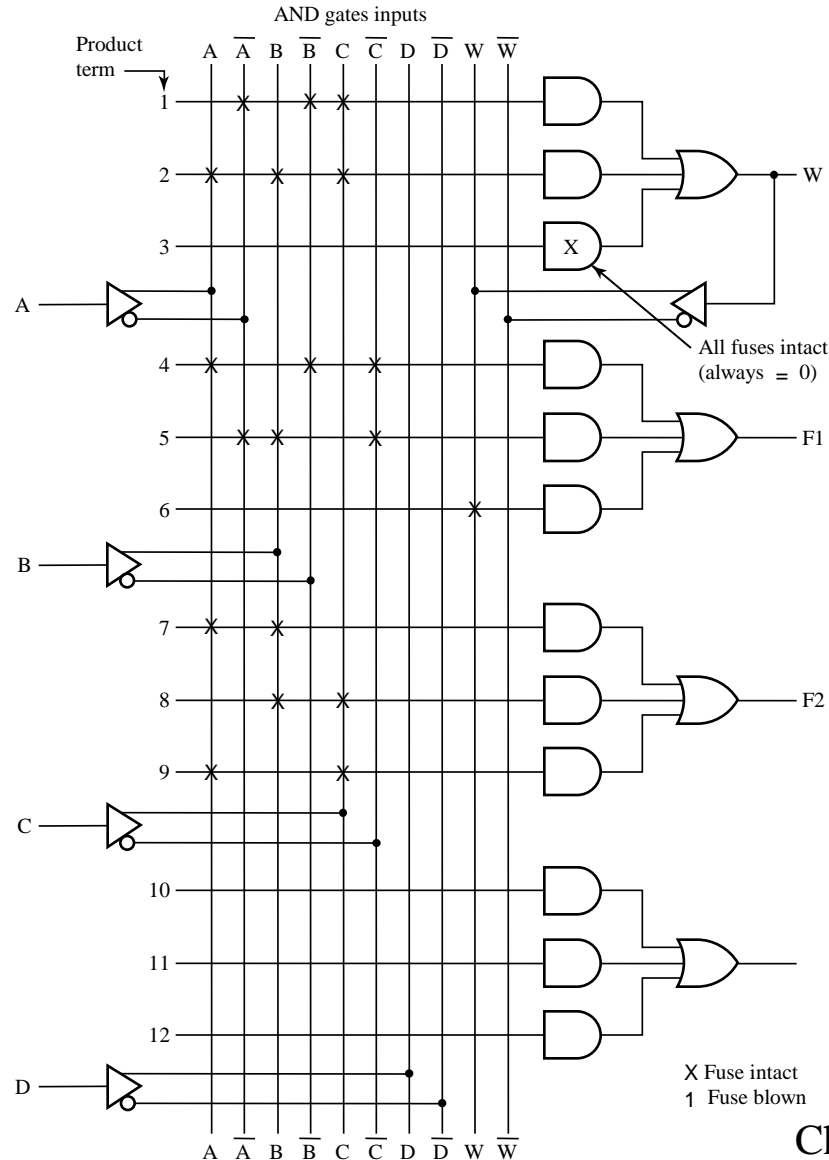
Product term	AND Inputs					Outputs
	A	B	C	D	W	
1	0	0	1	—	—	$W = \bar{A}\bar{B}C + ABC$
2	1	1	1	—	—	
3	—	—	—	—	—	
4	1	0	0	—	—	$F1 = X = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + W$
5	0	1	0	—	—	
6	—	—	—	—	1	
7	1	1	—	—	—	$F2 = Y = AB + BC + AC$
8	—	1	1	—	—	
9	1	—	1	—	—	
10	—	—	—	—	—	
11	—	—	—	—	—	
12	—	—	—	—	—	

Programmable Array Logic Example

$$W = \overline{A}\overline{B}C + ABC$$

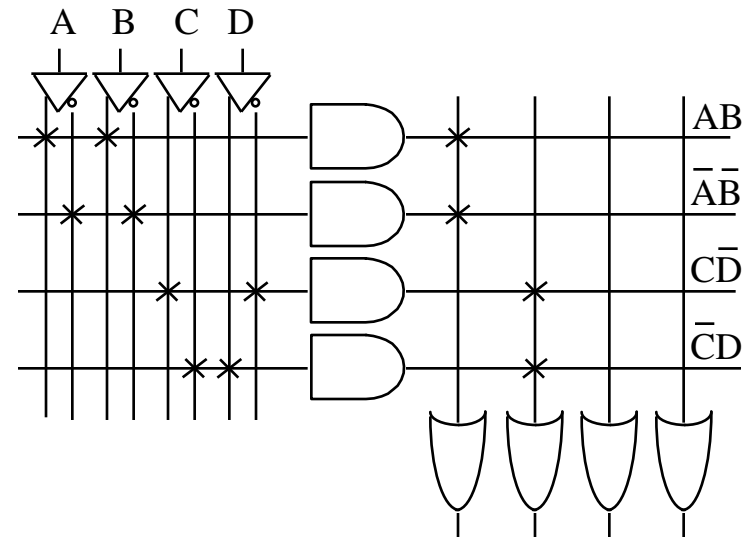
$$F1 = X = \overline{A}\overline{B}C + \overline{A}BC + W$$

$$F2 = Y = AB + BC + AC$$



Programmable Logic Array (PLA)

- Compared to a ROM and a PAL, a PLA is the most flexible having a programmable set of ANDs combined with a programmable set of ORs.
- Advantages
 - A PLA can have large N and M permitting implementation of equations that are impractical for a ROM (because of the number of inputs, N, required)
 - A PLA has all of its product terms connectable to all outputs, overcoming the problem of the limited inputs to the PAL ORs
 - Some PLAs have outputs that can be complemented, adding POS functions

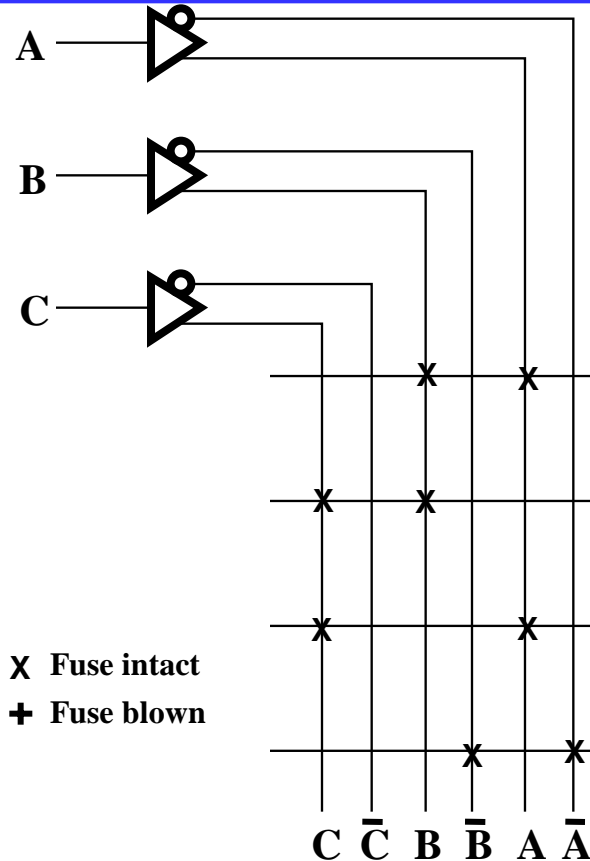


Programmable Logic Array (PLA)

■ Disadvantages

- Often, the product term count limits the application of a PLA.
- Two-level multiple-output optimization is required to reduce the number of product terms in an implementation, helping to fit it into a PLA.
- Multi-level circuit capability available in PAL not available in PLA. PLA requires external connections to do multi-level circuits.

Programmable Logic Array Example



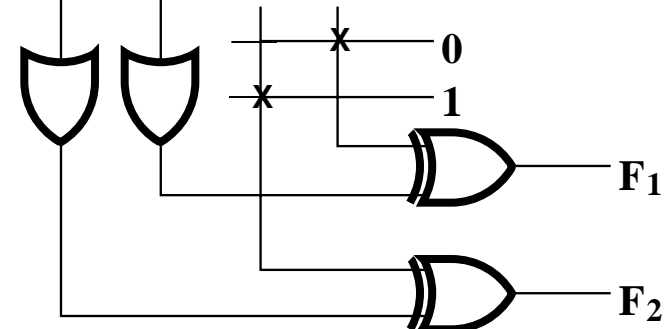
X Fuse intact
+ Fuse blown

- What are the equations for F₁ and F₂?
- Could the PLA implement the functions without the XOR gates?

$$F_1 = AB + BC + AC$$

$$F_2 = \overline{AB} + \overline{A\bar{B}} \\ = \overline{A}B + A\bar{B}$$

- 3-input, 2-output PLA with 4 product terms

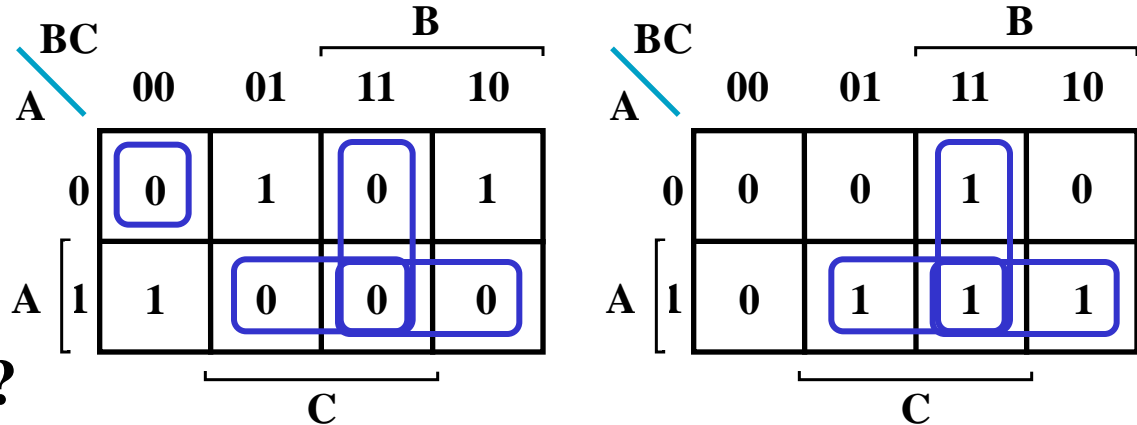


Programmable Logic Array

- The set of functions to be implemented **must fit the available number of product terms**
- The number of literals per term is less important in fitting
- The best approach to fitting is **multiple-output, two-level optimization** (which has not been discussed)
- Since output inversion is available, terms can implement either a function or its complement
- For small circuits, K-maps can be used to visualize product term sharing and use of complements
- For larger circuits, software is used to do the optimization including use of complemented functions

Programmable Logic Array Example

- K-map specification
- How can this be implemented with four terms?



- Complete the programming table

$$F_1 = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C}$$

$$\bar{F}_1 = AB + AC + BC + \bar{A}\bar{B}\bar{C}$$

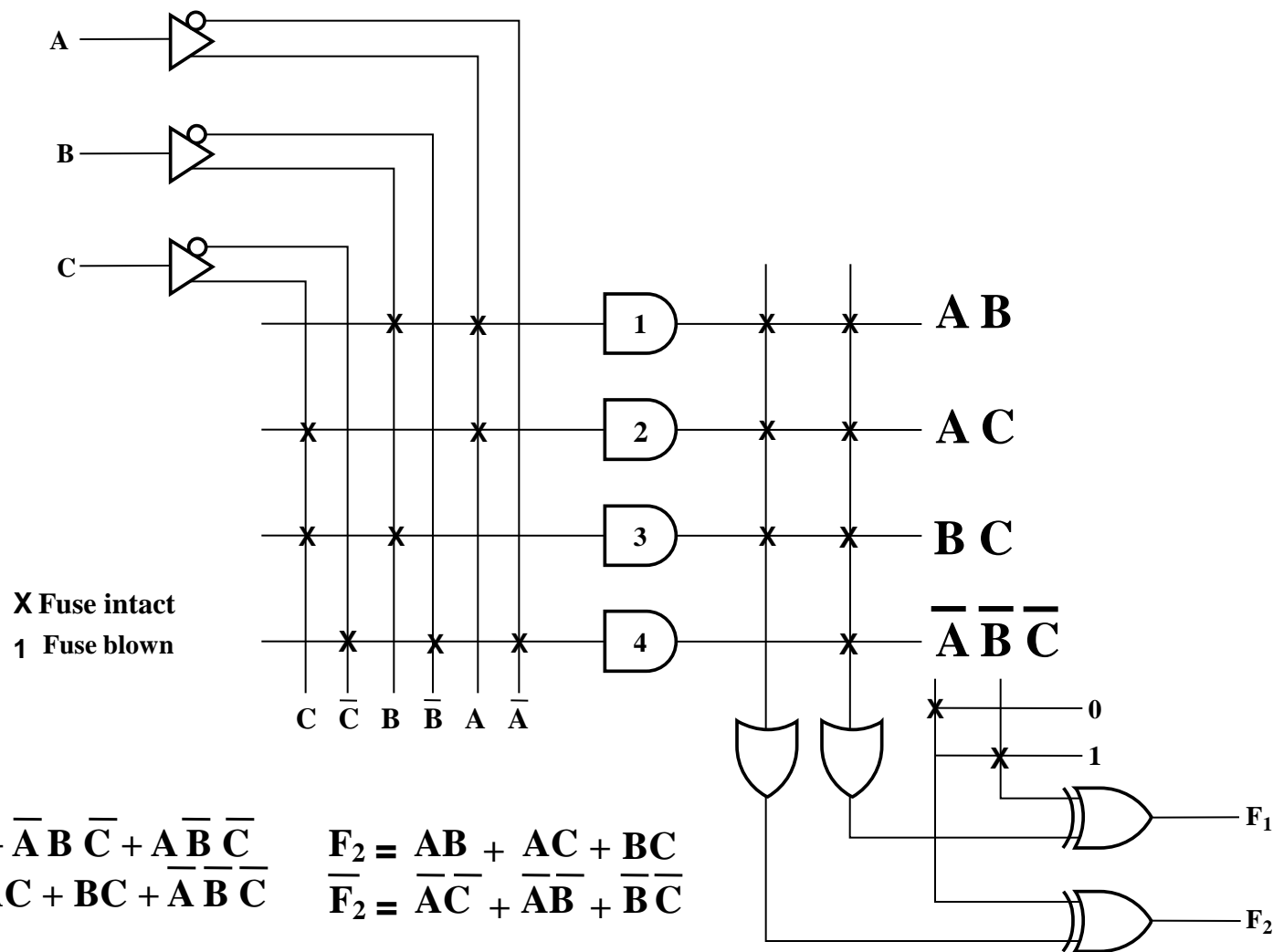
$$F_2 = AB + AC + BC$$

$$\bar{F}_2 = \bar{A}\bar{C} + \bar{A}\bar{B} + \bar{B}\bar{C}$$

PLA programming table

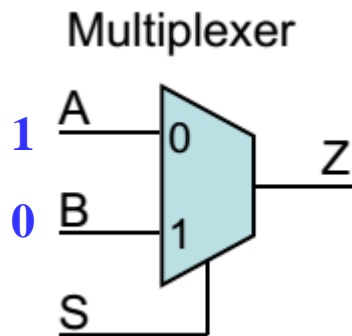
	Product term	Outputs				
		Inputs (C)			(T)	
		A	B	C	\bar{F}_1	F_2
AB	1	1	1	–	1	1
AC	2	1	–	1	1	1
BC	3	–	1	1	1	1
$\bar{A}\bar{B}\bar{C}$	4	0	0	0	1	–

Programmable Logic Array Example



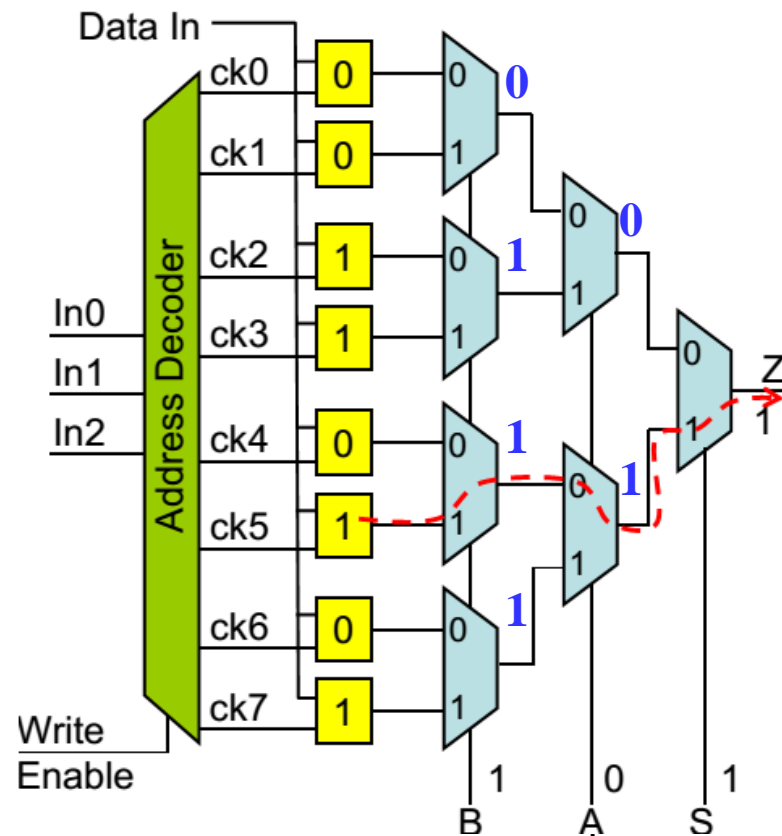
Lookup Tables

- Lookup tables (LUTs) are used for implementing logic in Field-Programmable Gate Arrays (FPGAs) and Complex Logic Devices (CPLDs)
- Lookup tables implement truth table in small memories (usually SRAM).



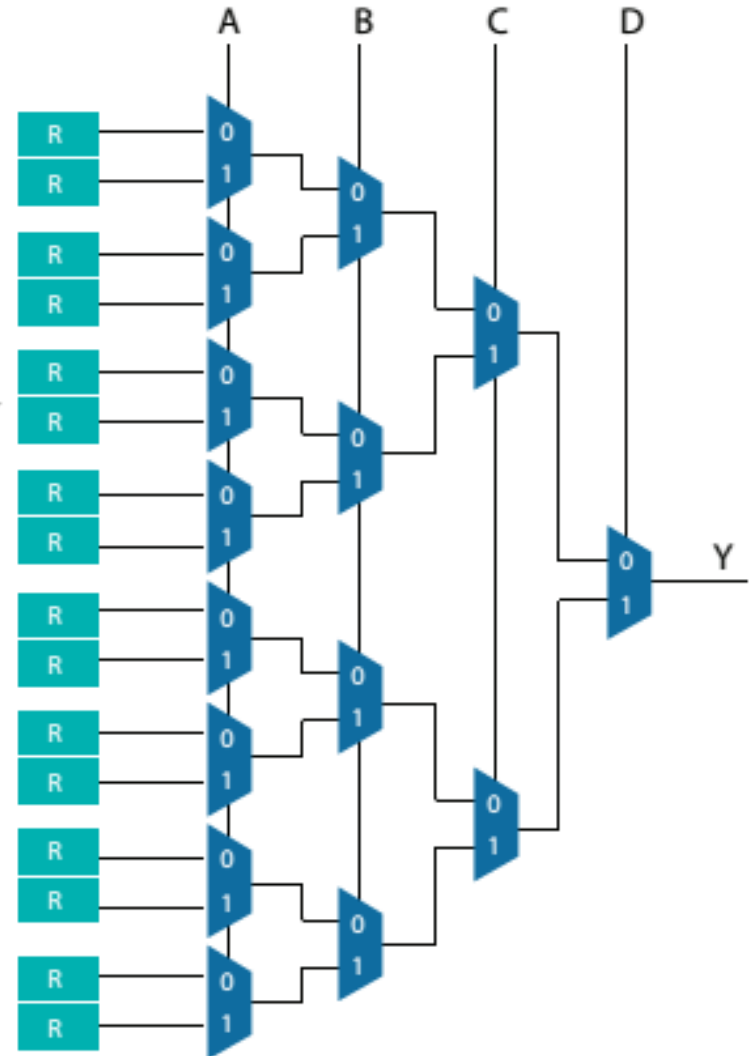
Truth table

S	Z
0	1
1	0



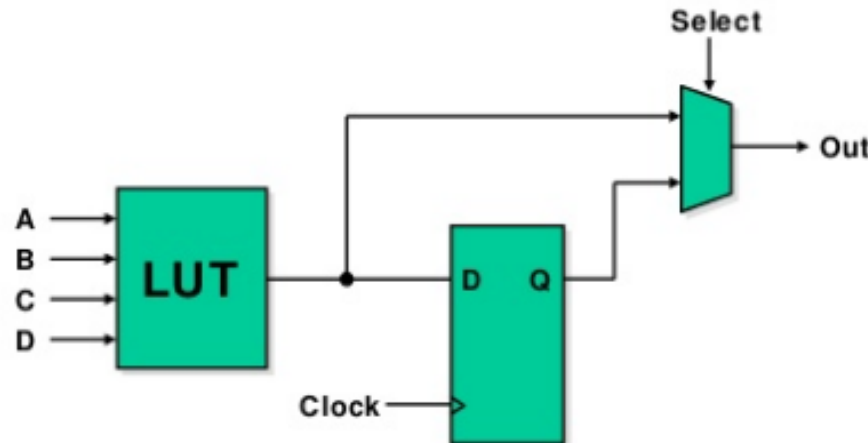
Lookup Tables (continued)

- Larger LUTs can be built out of smaller ones.
- For example, a 4-LUT can be built with 16 bits of SRAM and a 16-to-1 multiplexer implemented as a tree of 2-to-1 multiplexers.



Lookup Tables (continued)

- Lookup tables are typically small, often with four inputs, one output, and 16 entries.
- Since lookup tables store truth tables, it is possible to implement any 4-input function.
- Thus, the design problem is how to optimally decompose a set of given functions into a set of 4-input two-level functions.



Lookup Table Example

- Equations to be implemented:

$$F_1(A,B,C,D,E,F,G,H,I) = ABCDE + FGHI$$

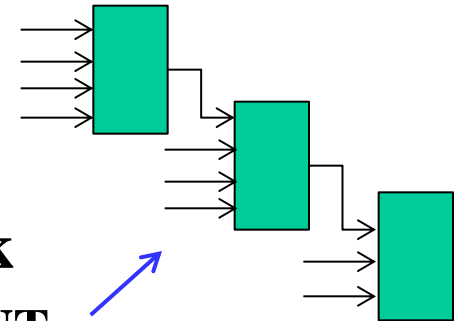
$$F_2(A,B,C,D,E,F,G,H,I) = ABCEF + FGHI$$

- Compute the number of LUT: Factoring k

- Number of inputs = 9 $k = \lceil 9/4 \rceil = 3$ need 3 LUT

- Divide these 2 functions into function group with 4 variables, each group contains 3 functions

- Need at most 6 LUT
- If common LUT exists, the number of LUT can be reduced by 2



$$F_1 = (\text{ABC})DE + (\text{FGHI})DE$$

$$X_1(A,B,C) = \text{ABC}$$

$$F_1(D,E,X_1,X_2) = X_1DE + X_2DE$$

$$F_2 = (\text{ABC})EF + \text{FGHI}$$

$$X_2(F,G,H,I) = \text{FGHI}$$

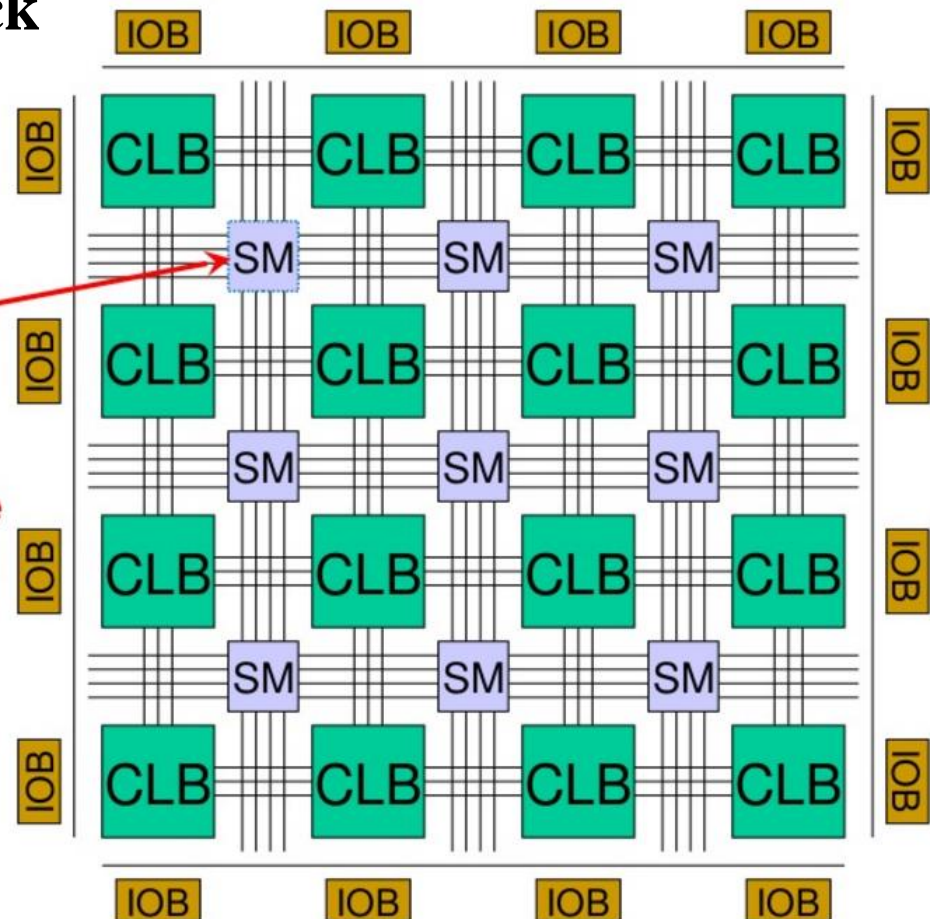
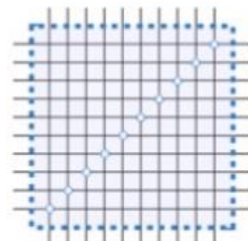
$$F_2(E,F,X_1,X_2) = X_1EF + X_2$$

Programmable Gate Array: FPGA

- The internal structure is composed of three parts:

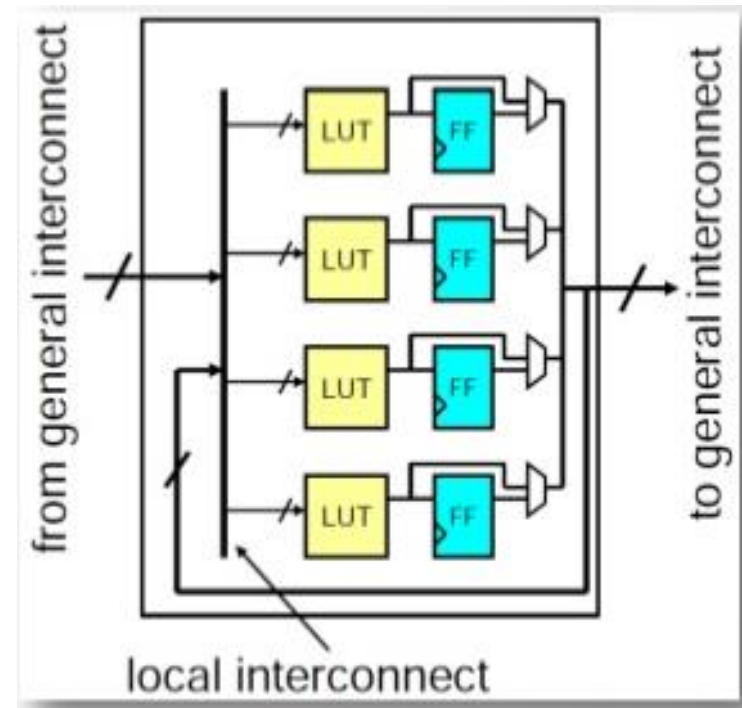
- Programmable logic block (CLB)
- Programmable switch box/matrix (SM)
- Programmable input output module (IOB)

Programmable
Switch Matrix



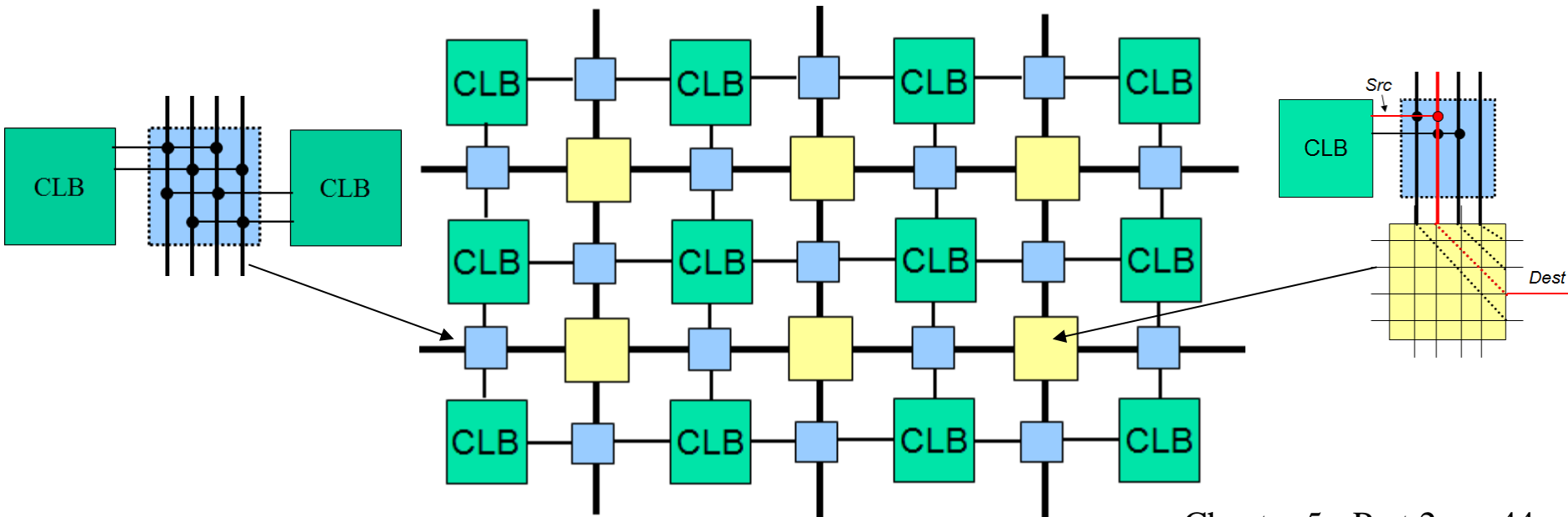
Configurable Logic Block

- **Configuration Logic Block (CLB) is the basic logic unit in a FPGA.**
 - ▣ The storage cells in the LUTs are volatile
 - ▣ Using PROM to hold data permanently
 - ▣ The storage cells are loaded from PROM when the chip initializes the switch box/matrix



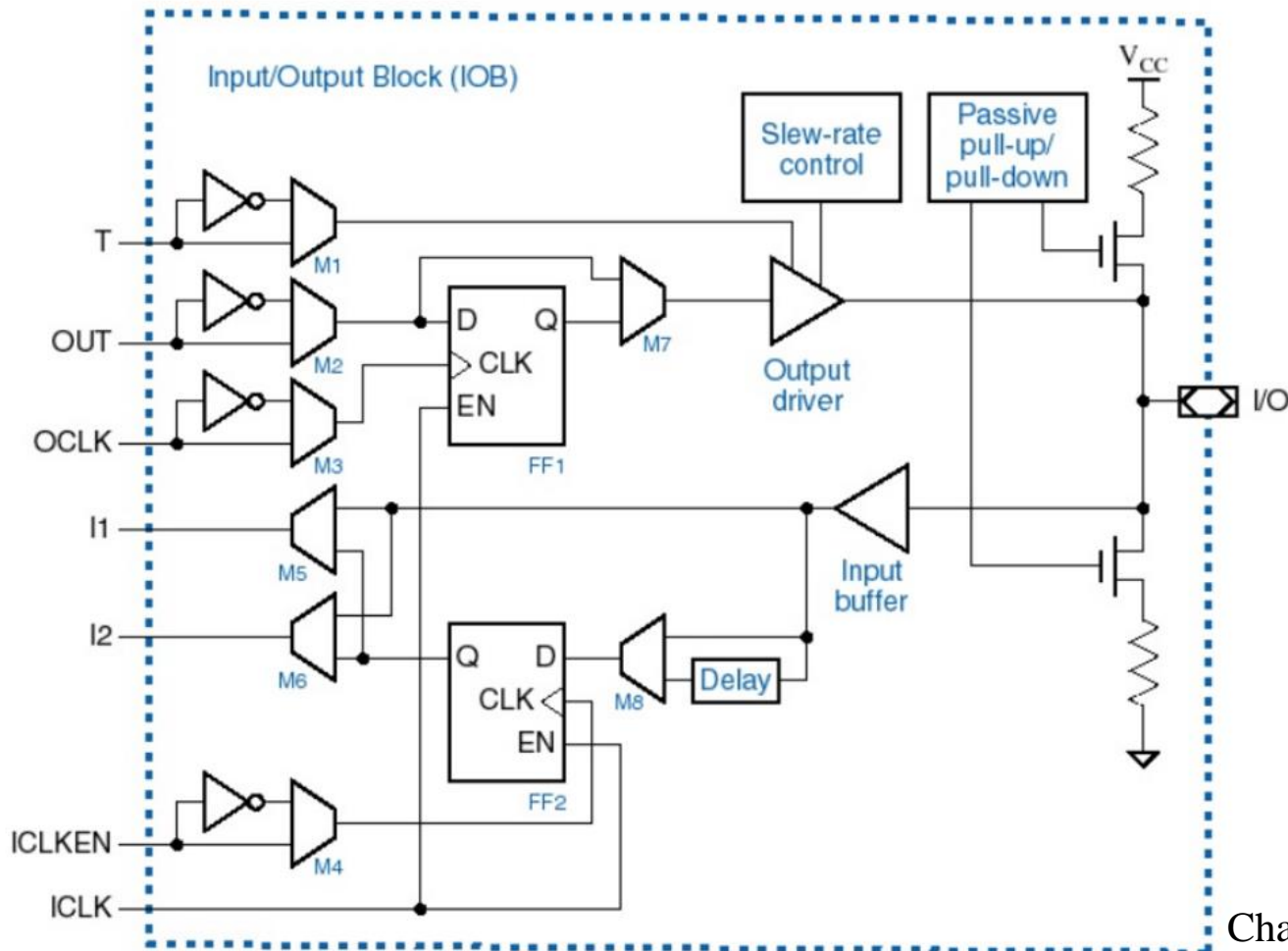
Reconfigurable Interconnect

- Connection box allows inputs and outputs of CLB to connect to different wires.
- Connection box characteristics:
 - **Flexibility**: how many wires a single wire can connect to
 - **Topology**: which wires can be connected
 - **Routability**: how many circuits that can be routed



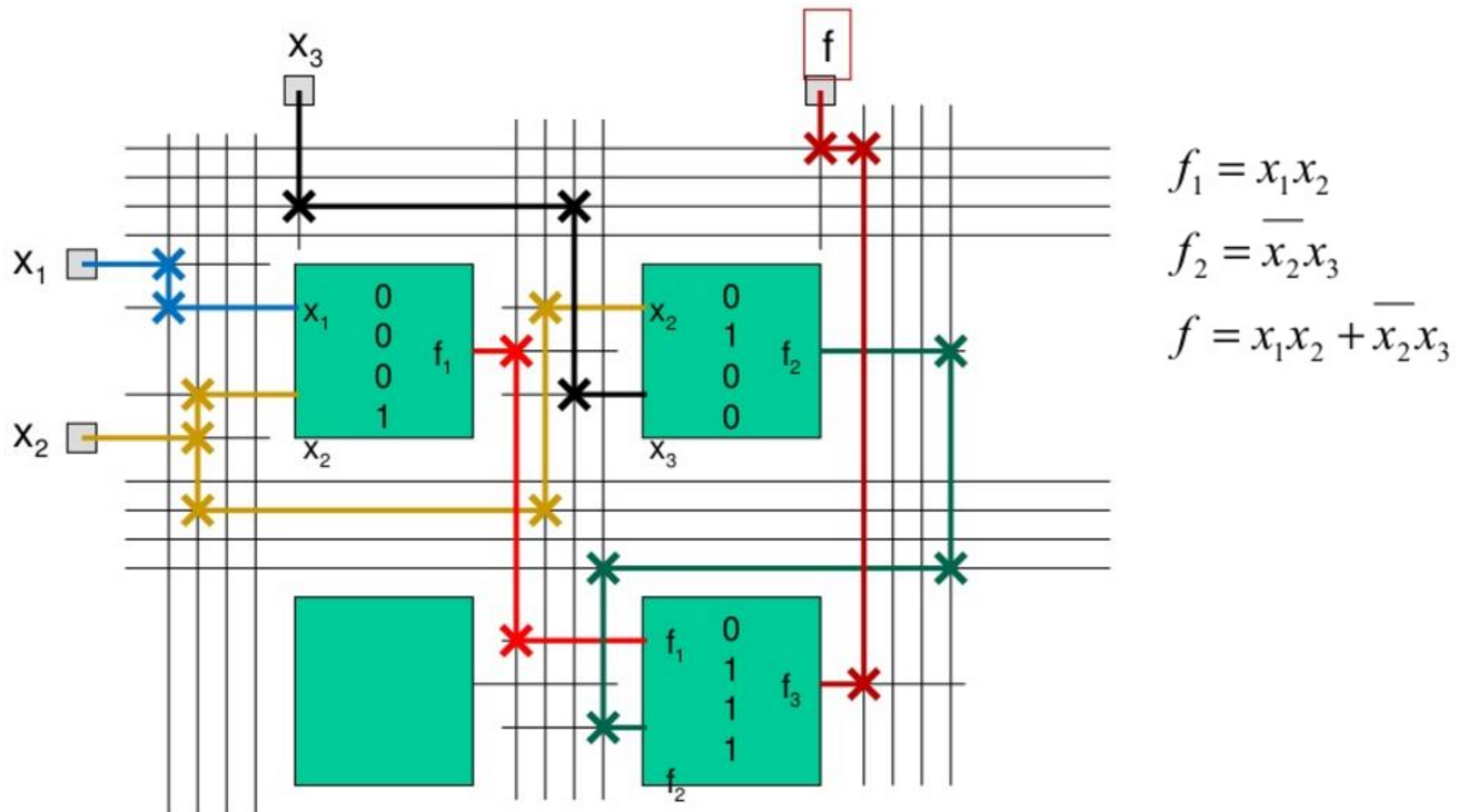
Programmable input/output module

- I/O blocks are special logic blocks at periphery of device for external connections.



Programming FPGAs

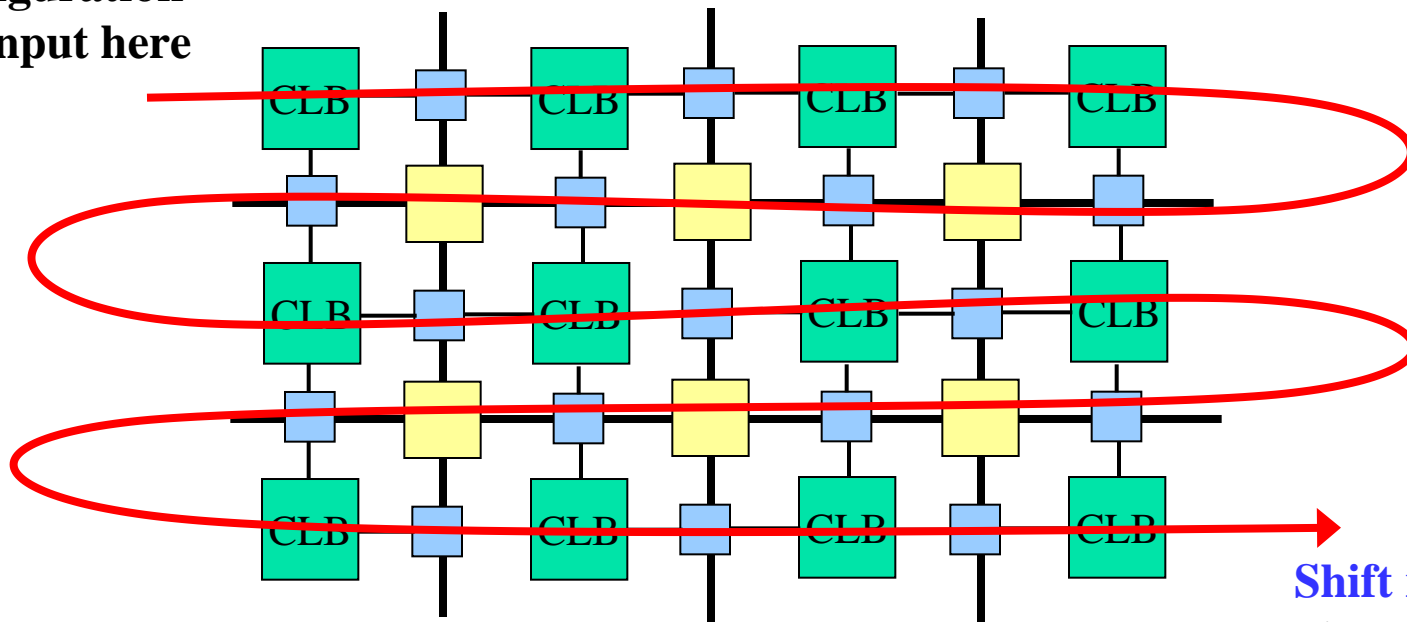
- An example of programming an FPGA



Programming FPGAs (continued)

- FPGAs are programmed and configured with a “**bitfile**” that contains bits to fill LUTs.

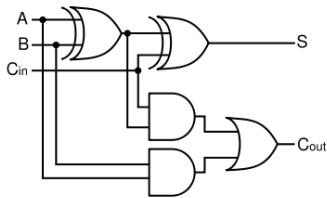
Configuration
bits input here



Shift register shifts
bits to appropriate
location in FPGA

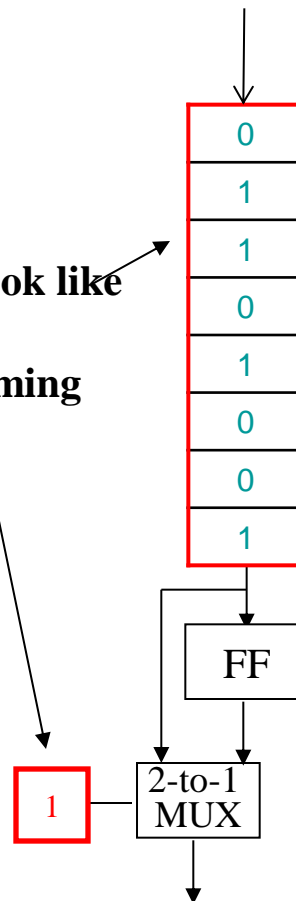
Programming FPGAs (continued)

- An example of programming CLB with 3-input, 1-output LUT to implement sum output of full adder

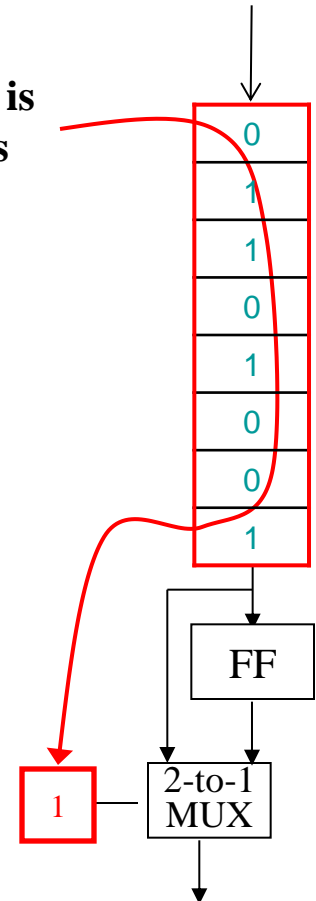


In			Out
A	B	Cin	S
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

Should look like this after programming



Assume data is shifted in this direction



Combinational Function Implementation

- **Implementation techniques:**
 - **Decoders and OR gates**
 - **Multiplexers**
 - **ROMs**
 - **PALs**
 - **PLAs**
 - **Lookup Tables**
- **Can be referred to as structured implementation methods** since a specific underlying structure is assumed in each case.

Decoder and OR Gates Example

- Implement a binary Adder

- Finding sum of minterms expressions

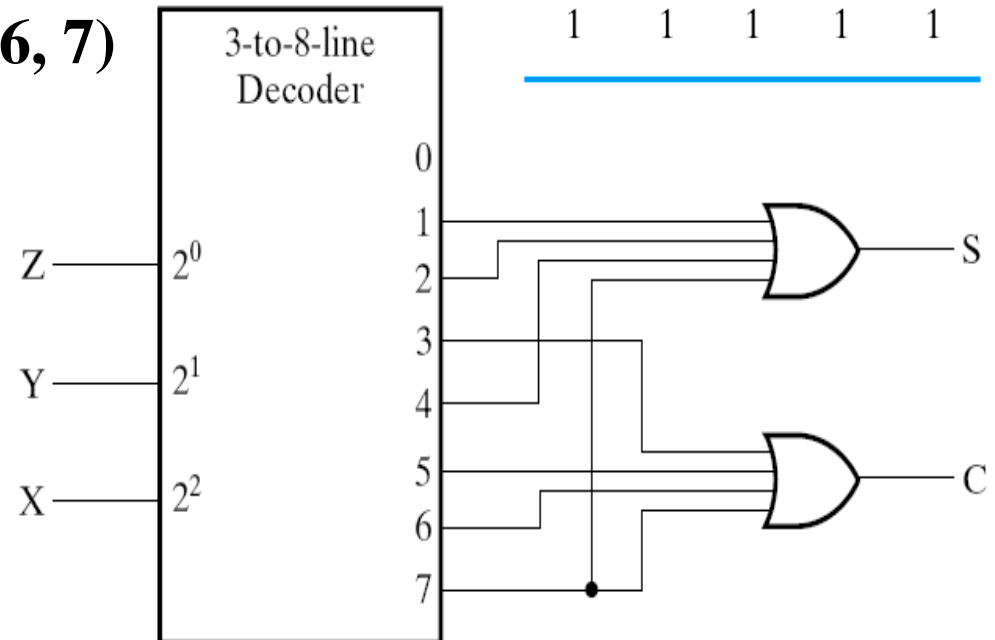
$$S(X, Y, Z) = \Sigma_m(1, 2, 4, 7)$$

$$C(X, Y, Z) = \Sigma_m(3, 5, 6, 7)$$

Find circuit

Truth Table

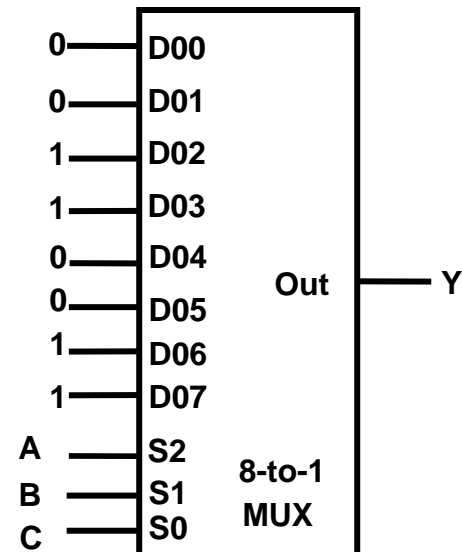
X	Y	Z	C	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1



Multiplexer Example: Gray to Binary Code

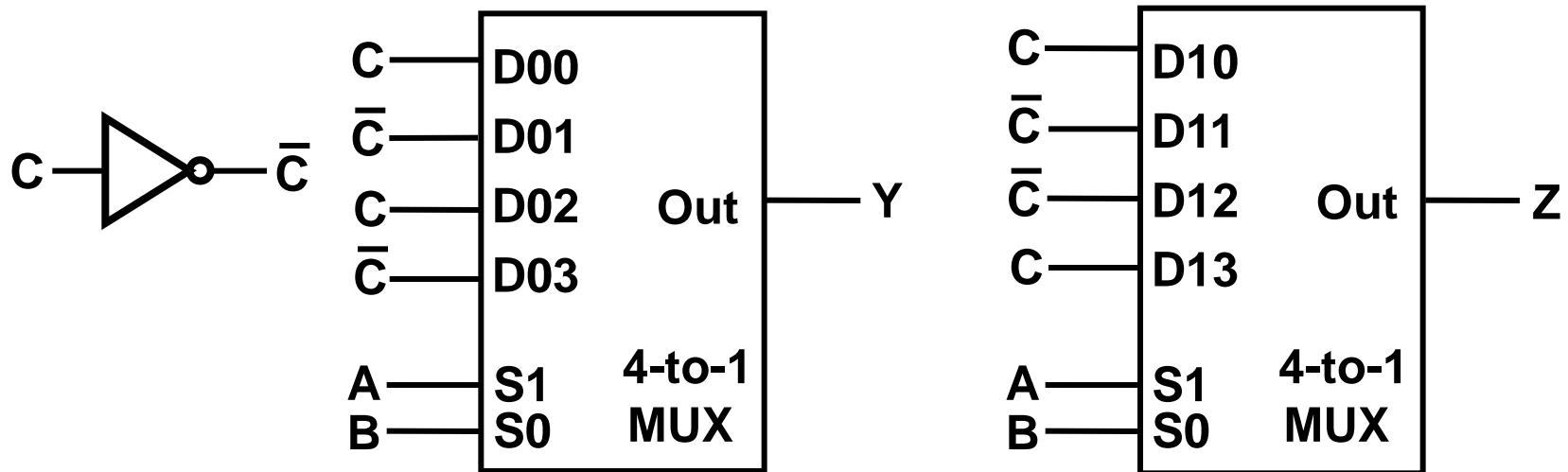
- Design a circuit to convert a 3-bit Gray code to a binary code.
- Label the outputs of the multiplexer with the output variables. Value-fix the information inputs to the multiplexer using the values from the truth table.

Gray			Binary		
A	B	C	x	y	z
0	0	0	0	0	0
1	0	0	0	0	1
1	1	0	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	1	1	1	0	1
1	0	1	1	1	0
0	0	1	1	1	1



Gray to Binary (continued)

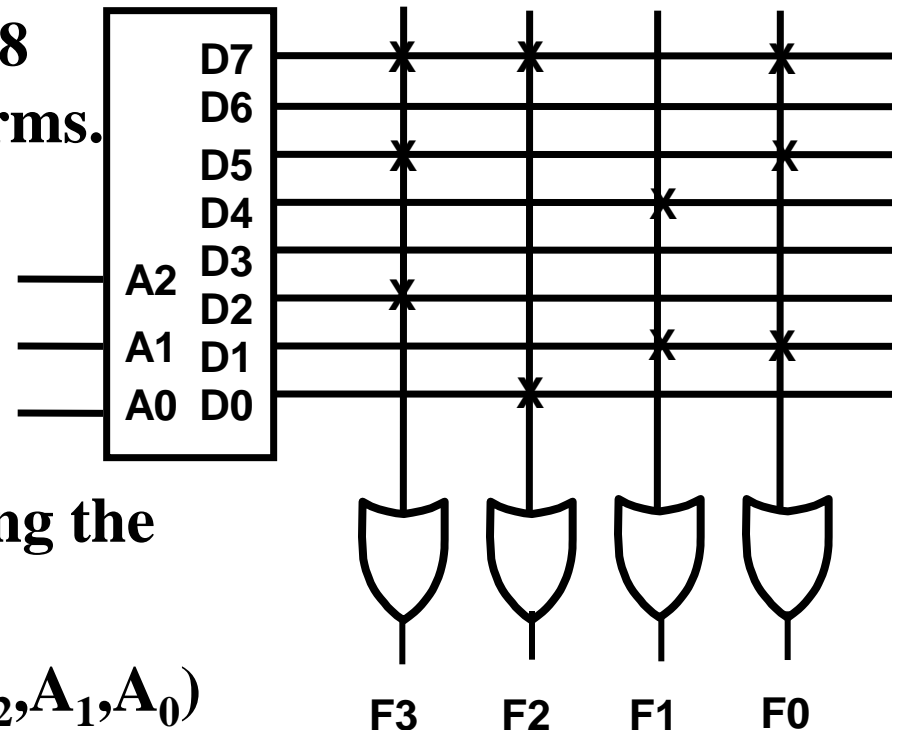
- Assign the variables and functions to the multiplexer inputs:



- This approach reduces the cost by almost half, which requires less control poles for a multiplexer.
- This result is no longer ROM-like.

Read Only Memory Example

- Example: An 8×4 ROM (N=3 input lines, M=4 output lines)
- The **fixed "AND" array** is a “decoder” with 3 inputs and 8 outputs implementing minterms.
- The **programmable “OR” array** uses a single line to represent all inputs to an OR gate. An “X” in the array corresponds to attaching the minterm to the OR
- Read Example: For input $(A_2, A_1, A_0) = 001$, output is $(F_3, F_2, F_1, F_0) = 0011$.

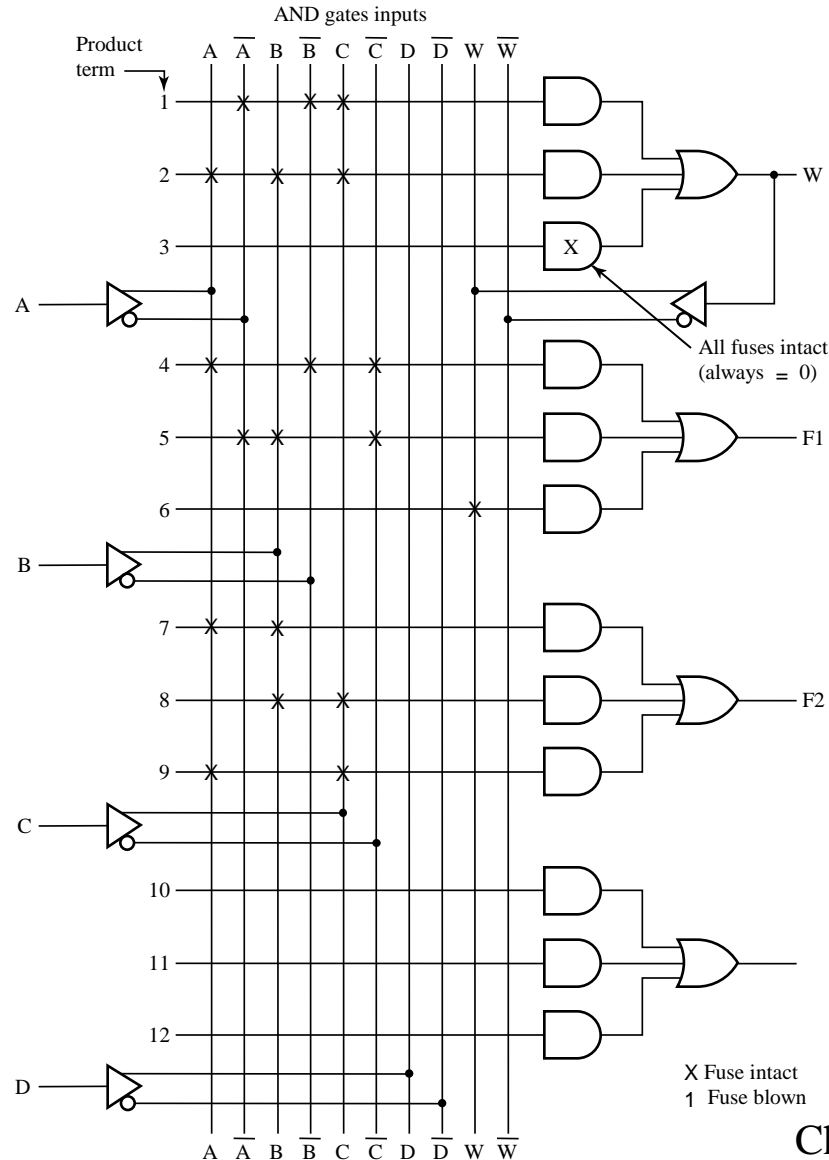


Programmable Array Logic Example

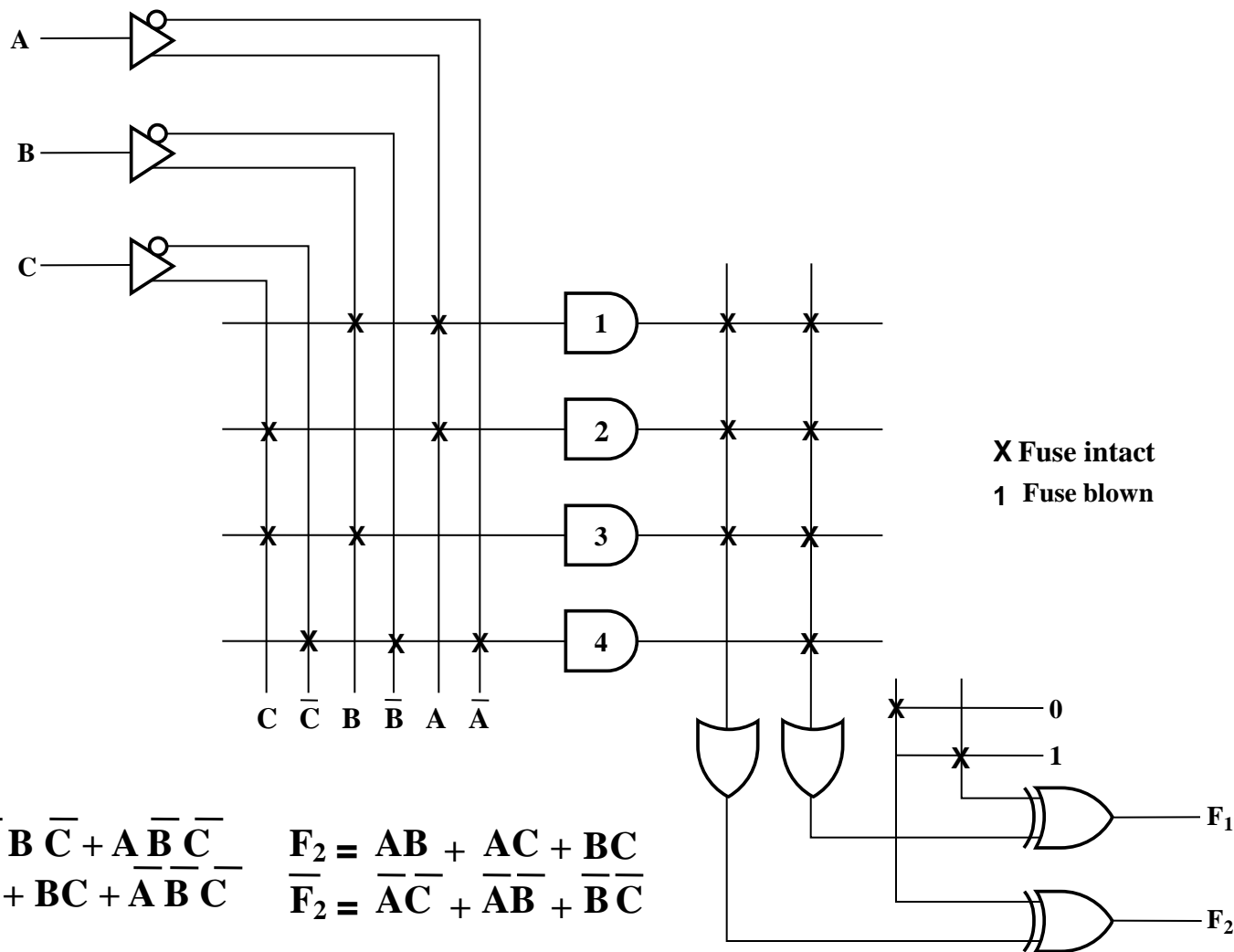
$$W = \overline{\overline{A}}\overline{\overline{B}}\overline{\overline{C}} + \overline{\overline{A}}\overline{\overline{B}}\overline{\overline{C}}$$

$$F1 = X = \overline{\overline{A}}\overline{\overline{B}}\overline{\overline{C}} + \overline{\overline{A}}\overline{\overline{B}}\overline{\overline{C}} + W$$

$$F2 = Y = \overline{\overline{A}}\overline{\overline{B}}\overline{\overline{C}} + \overline{\overline{A}}\overline{\overline{B}}\overline{\overline{C}} + \overline{\overline{A}}\overline{\overline{B}}\overline{\overline{C}}$$

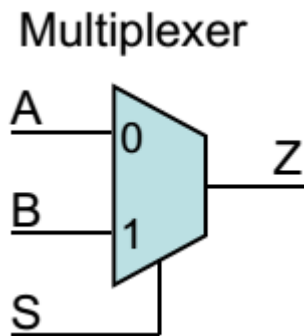


Programmable Logic Array Example

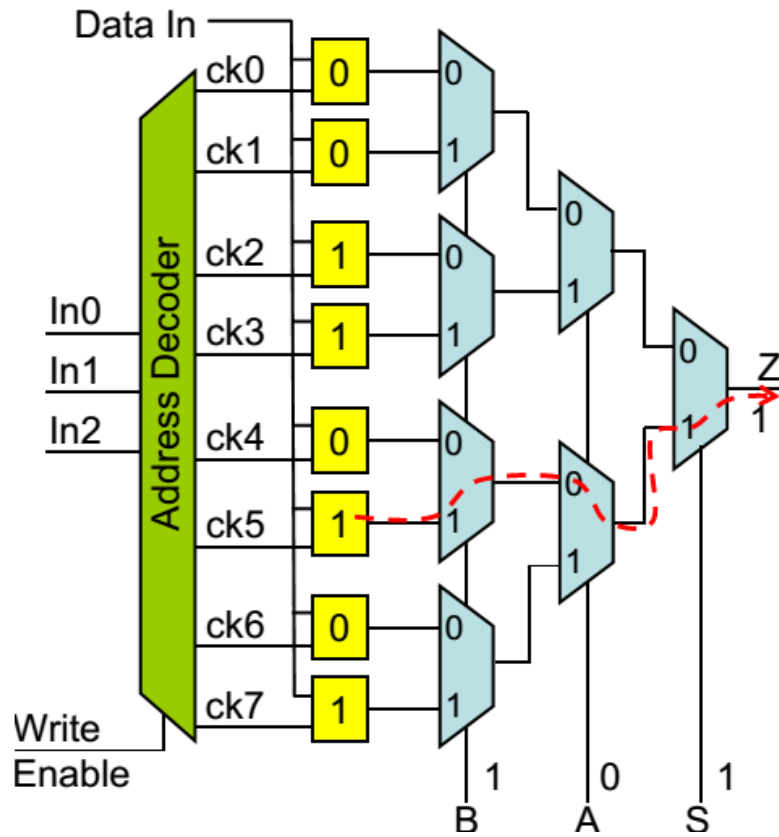


Lookup Tables

- Lookup tables (LUTs) are used for implementing logic in Field-Programmable Gate Arrays (FPGAs) and Complex Logic Devices (CPLDs)
- Lookup tables implement truth table in small memories (usually SRAM).



Truth table			
S	A	B	Z
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1



Assignments

Reading

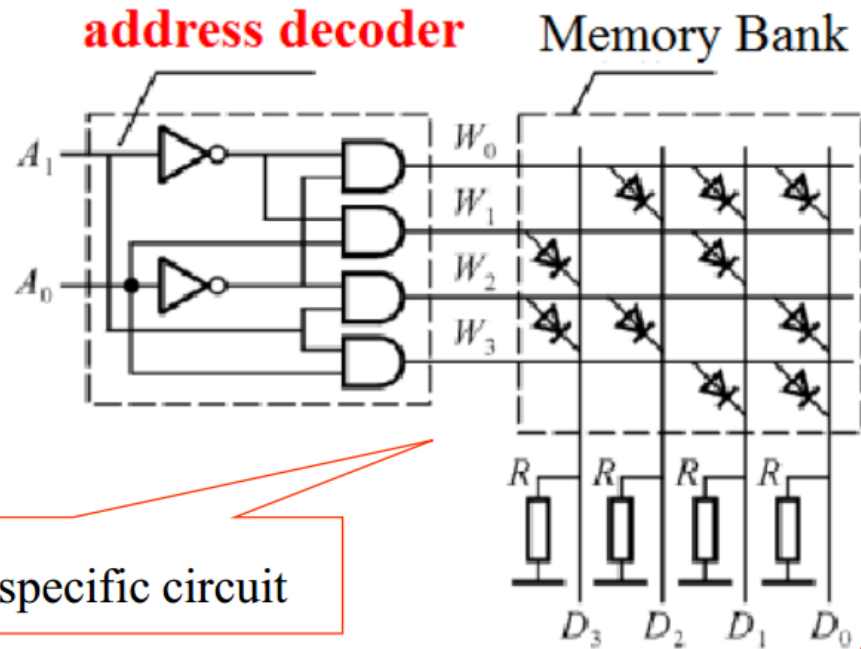
- 5.2

Problem assignment

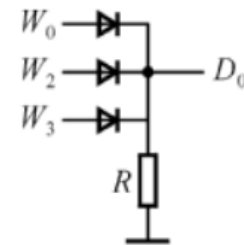
- 5-4, 5-12

Appendix A: The general structure of ROM

- The **address decoder** is a completely minterms (Full decoder) circuit, that is a non-programmable “AND” array and the memory bank is a “OR” array.



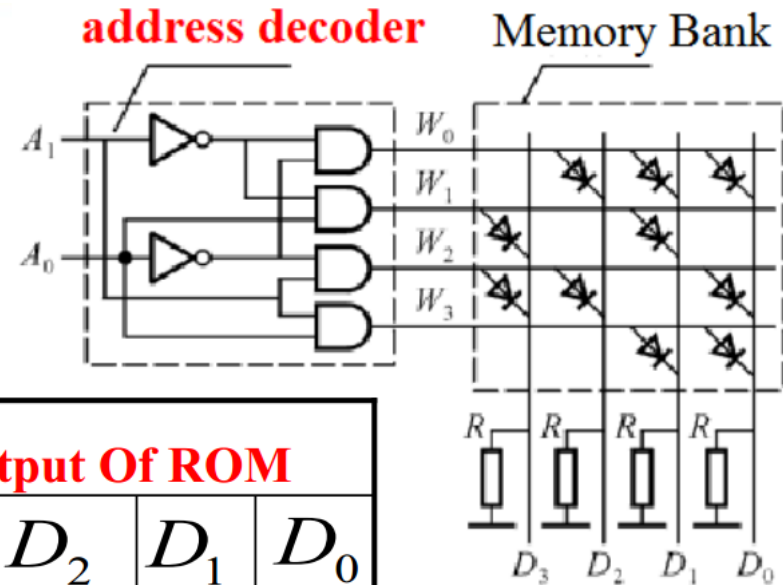
4 × 4 ROM specific circuit



"D₀" bit wire "OR" gate structure

The general structure of ROM (continued)

- Output information of ROM:
- ROM size = $2^2 \times 4 = 16\text{bit}$



address		Word select wire	Output Of ROM			
A_1	A_0	W	D_3	D_2	D_1	D_0
0	0	W_0	0	1	1	1
0	1	W_1	1	0	1	0
1	0	W_2	1	1	0	1
1	1	W_3	0	0	1	1