Normal Vector

For a triangle ABC, $N = (B-A) \times (C-A)$ (Select 2 edges counter-clockwise, and normalize)

Vector Distance

For two points $P = (x_1, y_1, z_1), Q = (x_2, y_2, z_2),$

$$\|\overrightarrow{PQ}\| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}.$$

For $\mathbf{u}, \mathbf{v} \in \mathbb{R}^3$, $\mathbf{u} \cdot \mathbf{v} = u_x v_x + u_y v_y + u_z v_z = \|\mathbf{u}\| \|\mathbf{v}\| \cos \theta$. **Use:** angle between vectors, projection, parallelism.

$$\mathbf{u} \times \mathbf{v} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ u_x & u_y & u_z \\ v_x & v_y & v_z \end{vmatrix} = \begin{bmatrix} u_y v_z - u_z v_y \\ u_z v_x - u_x v_z \\ u_x v_y - u_y v_x \end{bmatrix}$$

gives a vector orthogonal to both \mathbf{u}, \mathbf{v} . Use: normal computation, orientation.

Common Transformation Matrices

Translation: glTranslatef (t_x, t_y, t_z) ; Scaling by (s_x, s_y, s_z) :

$$T = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} S = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Rotation about x, y, z axis: $glRotatef(\theta, x?, y?, z?)$

$$R_x(\theta) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta & 0 \\ 0 & \sin\theta & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} R_y(\theta) = \begin{bmatrix} \cos\theta & 0 & \sin\theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta & 0 & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$R_z(\theta) = \begin{bmatrix} \cos\theta & -\sin\theta & 0 & 0 \\ \sin\theta & \cos\theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Perspective (simple form): \rightsquigarrow Initialize \rightarrow register callback functions \rightarrow enter glutMainLoop() \rightarrow wait for events \rightarrow call corresponding callbacks \rightarrow program exits when closed.

Primitive Drawing

• glBegin(mode) ...glEnd() Define a sequence of vertices for drawing. mode = GL_POINTS, GL_LINES, GL_TRIANGLES, GL_QUADS, etc. Note: only draw convex, planar polygons.

```
glBegin(GL_TRIANGLES);
    glColor3f(1,0,0); glVertex3f(0,0,0);
    glColor3f(0,1,0); glVertex3f(1,0,0);
    glColor3f(0,0,1); glVertex3f(0,1,0);
glEnd();
```

- **glColor3f(r,g,b)** Set current drawing color (RGB, 0-1).
- glVertex2f(x,y), glVertex3f(x,y,z) Specify a vertex in 2D or 3D.

State Management

- **glLoadIdentity()** Reset current matrix to identity (no transform).
- glClear(mask) Clear buffers. Common: GL COLOR BUFFER BIT | GL DEPTH BUFFER BIT.
- glFlush() Force execution of all issued OpenGL commands (mainly for single-buffered mode).

Window / Display Setup

- glutInit(&argc, argv) Initialize GLUT.
- glutInitDisplayMode(flags) Select display mode, e.g. GLUT_RGB | GLUT_DOUBLE | GLUT_DEPTH.
- glutDisplayFunc(func) Register display callback (called whenever window redraws).
- **glutMainLoop()** Enter GLUT event loop (program stays here).

Shading

• glShadeModel(mode) GL_FLAT = uniform color per primitive, GL_SMOOTH = interpolated colors.

Matrices & Viewing

- glMatrixMode(mode) Select current matrix stack: GL MODELVIEW or GL PROJECTION.
- **GL_MODELVIEW** Holds modeling + viewing transforms.
- GL_PROJECTION Holds projection (camera lens) transforms.
- **gluOrtho2D(left,right,bottom,top)** 2D orthographic projection.
- glOrtho(l,r,b,t,n,f) 3D orthographic projection volume.
- glFrustum(l,r,b,t,n,f) Perspective frustum volume.
- gluPerspective(fov,aspect,n,f) Perspective projection with vertical field-of-view.
- gluLookAt(eye,center,up) Set camera at eye, looking at center, with up direction.

Depth & Culling

- glEnable(cap) Turn on a feature. E.g. GL_DEPTH_TEST, GL_CULL_FACE.
- glDepthMask(flag) Enable/disable writing to depth buffer.
 Useful for transparency.
- glCullFace(mode) Choose which faces to cull: GL_BACK, GL_FRONT, GL_FRONT_AND_BACK.
- GL_DEPTH_TEST Feature that discards fragments hidden behind others in depth.

1 Model-View and 3D Representation (Algorithms & Data Structures)

Model-View: Frames, Matrices, and Hierarchies

- Model–View matrix M: concatenates object–to–world (model) and world–to–camera (view) transforms. Typical composition (right-multiplied): $M \leftarrow MT(\mathbf{t}) R(\theta, \hat{\mathbf{a}}) S(s_x, s_y, s_z)$. Order matters (non-commutative).
- Matrix stack: use glPushMatrix/glPopMatrix to delimit local frames. Transform state between pushes affects all descendants; popping restores the parent frame.
- Hierarchical transforms: model parts as a tree (e.g., torso
 → arm → forearm → hand). Each node stores a local transform; the global pose is the product along the path from root to the node. Animations vary local parameters over time.
- Orientation/winding: triangle order encodes front face (right-hand rule). Choose CCW or CW consistently; configure the API (e.g., glfrontFace(GL_CCW)) and optional back-face culling.

3D Object Representations

- Independent faces: each face stores three vertex (x, y, z). *Pros*: simplest. *Cons*: duplicated vertices; no explicit adjacency/topology.
- Indexed face set (triangle list): a vertex array of unique points plus a face array of integer triplets (indices). Pros: shared vertices, compact, GPU-friendly. Cons: still lacks explicit edge/face adjacency.
- Adjacency-enriched meshes: store connectivity to enable fast traversal and editing.
 - Per-vertex/face adjacency lists: neighbors of a vertex; neighboring faces of a face.
 - Half-edge / winged-edge (canonical for robust geometry):
 each directed edge stores pointers to its origin vertex,
 twin, next/prev in the face, and incident face. Pros: O(1)
 local traversal; supports topology edits. Cons: higher memory, more bookkeeping.

• Other representations (for context): parametric patches, CSG, spatial subdivision (voxels), implicit surfaces.

Core Algorithms on Meshes

- Vertex deduplication (build indexed mesh): hash (x, y, z) (with epsilon tolerance) to map repeated coordinates to one index; emit faces as index triplets.
- Face normals: for triangle $v_0, v_1, v_2,$

$$\mathbf{n}_f = \frac{(v_1 - v_0) \times (v_2 - v_0)}{\|(v_1 - v_0) \times (v_2 - v_0)\|}.$$

- Vertex normals (smooth shading): area- or angle-weighted average of incident face normals, then renormalize.
- Topology checks: manifoldness (each edge has at most two incident faces), consistent winding, boundary detection (edges with one incident face), connected components (DFS/BFS over adjacency).
- Rendering paths:
 - Indexed draw calls (e.g., glDrawElements) for an indexed face set.
 - Depth buffering for visibility (preferred) vs. painter's algorithm (order-dependent).
 - Optional back-face culling to skip backfacing triangles.

Practical Tips

- Keep geometry (vertex positions) separate from topology (indices/connectivity); this avoids numeric drift and reduces memory.
- Use the matrix stack to isolate local edits: push, apply local T/R/S, draw child, pop.
- Be consistent with triangle winding across the asset pipeline; fix mismatches at import.

Hidden Surface Removal (HSR) + 3D BSP Cheatsheet

Context

After modeling, viewing, and perspective transforms, we must ensure polygons are drawn in correct visibility order to avoid "wrong drawing order." Two broad families exist: *object-precision* (control draw order) and *image-precision* (decide per-pixel overwrite).

Object-precision (orderly).

Depth sort with splitting (e.g., Weiler–Atherton) and **BSP trees** produce a back-to-front order for any viewpoint. Handles transparency but can be expensive to build or split polygons.

Image-precision (non-orderly).

Z-buffer keeps a depth value per pixel; simple and hardware-friendly, robust for interpenetrating geometry, but suffers from precision issues (Z-fighting) and limited transparency.

Binary Space Partitioning (BSP) in 3D

Goal: Preprocess a static polygon set into a tree so that, for any camera point p, an in-order traversal yields a correct back-to-front drawing order. Standard in classic FPS engines.

Definitions

Each node stores:

- A splitting plane Π : $\mathbf{n} \cdot \mathbf{x} + d = 0$ coincident with a polygon P (node's polygon).
- Two child subspaces: $Back (\mathbf{n} \cdot \mathbf{x} + d < 0)$ and Front (> 0).
- Polygons in the node's plane; polygons crossing Π are split into coplanar parts for the two sides.

Note: In practice, any polygon can be chosen to define the split; repeated recursively until leaves contain simple geometry. :contentReference[oaicite:4]index=4

Construction (static scene)

- 1. If set S of polygons is empty: return null.
- 2. Choose a polygon $A \in S$ and define its plane Π_A .

- 3. Partition every $Q \in S \setminus \{A\}$ against Π_A :
 - If entirely in back/front half-space, send to that child set.
 - If straddling Π_A , split Q into Q_{back} and Q_{front} .
 - If coplanar with Π_A , attach to the node (commonly to a coplanar list).
- Recurse on back set to build node->back; recurse on front set for node->front.

This preprocessing is view-independent and reused for all camera positions. :contentReference[oaicite:5]index=5

Rendering (any viewpoint p)

For a node with plane $\Pi : \mathbf{n} \cdot \mathbf{x} + d = 0$:

- 1. Compute $s = \mathbf{n} \cdot p + d$.
- 2. If s>0 (camera in front half-space): draw(node->back) \rightarrow draw(node->coplanar) \rightarrow draw(node->front)
- 3. If s < 0 (camera in back half-space): draw(node->front) \rightarrow draw(node->back) \rightarrow draw(node->back)

This is exactly a view-dependent in-order traversal that yields back-to-front order. Transparency becomes straightforward (alpha-blend as you go). :contentReference[oaicite:6]index=6 Build BSP:

- 1. Choose A as root; split B and C against Π_A . They are not straddling (z=0), so both go fully to either front (z>0) or back (z<0) depending on their extents. Suppose both lie in front (z>0) for illustration \Rightarrow root->back = null, root->front contains $\{B,C\}$.
- 2. Recurse on front: choose B next, partition C by Π_B into C_{front} (x > 0) and C_{back} (x < 0).
- 3. Continue until sets become simple leaves.

Render for a viewpoint. Let p = (2, 2, 2):

 $\mathbf{n}_A \cdot p + d_A = 2 > 0 \Rightarrow \text{at root, draw Back, then } A, \text{ then Front.}$

Since Back is empty: draw A (the z=0 polygon). Descend to Front (node B). With p:

 $\mathbf{n}_B \cdot p + d_B = 2 > 0 \Rightarrow \text{draw Back subtree of } B$, then B, then Front su

Those subtrees contain the parts of C (C_{back} at x < 0 and C_{front} at x > 0). The emitted sequence is a correct backto-front order for this p. If we move to p', the traversal order flips accordingly—without rebuilding the tree. :contentReference[oaicite:7]index=7

Pros / Cons (at a glance)

- **Pros:** Single precomputation supports *all* viewpoints; good for transparency ordering; widely used in classic game engines (static maps). :contentReference[oaicite:8]index=8
- Cons: Expensive splits; not ideal for dynamic/moving geometry; preprocessing time and potential growth in polygon count. :contentReference[oaicite:9]index=9

OpenGL Hooks (use with BSP or Z-buffer)

- Depth buffer: glEnable(GL_DEPTH_TEST); glClear(GL_COLOR_GL_DEPTH_BUFFER_BIT); glDepthMask(GL_TRUE); (clear each frame). :contentReference[oaicite:10]index=10
- Back-face culling: glEnable(GL_CULL_FACE); glCullFace(GL_F Use consistent winding (glFrontFace(GL_CCW)). Test via $\mathbf{V} \cdot \mathbf{N} > 0$. :contentReference[oaicite:11]index=11

This emits a back-to-front order; swap the order to front-to-back if you prefer early-Z culling with an opaque Z-buffer pass. :contentReference[oaicite:12]index=12

2 Projection

Families of Projections

• Orthographic (parallel): Projectors are parallel; depth is discarded (e.g., take (x, y)). Preserves sizes along projector direction; good for CAD/engineering drawings; less realistic.

• **Perspective**: Projectors meet at a center of projection; distant objects appear smaller (foreshortening).

Perspective Basics

- Canonical setup: camera at (0,0,-f) looking along +z; image plane at z=0.
- Mapping: $x' = \frac{f}{z} x$, $y' = \frac{f}{z} y$.
- Homogeneous form: use a perspective projection matrix to map to clip space; after division by w you obtain normalized device coordinates (NDC).

$$P = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & \frac{1}{f} & 1 \end{bmatrix} \text{ homogenous coord: } \begin{bmatrix} x \\ y \\ z \\ \frac{z+f}{f} \end{bmatrix} = \begin{bmatrix} \frac{fx}{z+f} \\ \frac{yf}{z+f} \\ \frac{zf}{z+f} \end{bmatrix}$$

2.1 Model-View Matrix and Transform State

Where a vertex goes. Whenever you submit a vertex p (e.g., with glVertex), OpenGL draws it at

$$p' = M p, p'' = PMp$$

Set Projection when the window resizes or the "lens" changes. Set Model–View every frame (camera), and per object (model transforms).

```
void reshape(int w,int h){
 glViewport(0,0,w,h);
  glMatrixMode(GL_PROJECTION);
  glLoadIdentity();
  gluPerspective(40.0, (float)w/h, 1.0, 80.0); // or glOrtho(...)
  glMatrixMode(GL_MODELVIEW);
                                                  // back to MV for
    drawing
void display(){
  glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT);
  glMatrixMode(GL_MODELVIEW);
  glLoadIdentity();
  gluLookAt(0,0,6, 0,0,0, 0,1,0);
                                                  // View part of MV
  glPushMatrix();
                                                   // Model part
    for object A
    glTranslatef(...); glRotatef(...); glScalef(...);
    drawA();
  glPopMatrix();
  glPushMatrix();
                                                   // Object B
    glTranslatef(...);
    drawB();
 glPopMatrix();
```

Changing the transformation matrix M.

- glMatrixMode(GL_MODELVIEW) select the Model-View matrix stack.
 - Other choices: GL_PROJECTION, GL_TEXTURE, GL_COLOR.
- glLoadIdentity() set $M \leftarrow I$ (identity).
- glTranslatef(tx,ty,tz) postmultiply: $M \leftarrow MT$.
- glRotatef(angle,x,y,z) postmultiply: $M \leftarrow MR$.

Camera (View) Transform

- Build a camera frame with position \mathbf{t} , forward \mathbf{w} , up \mathbf{u} , and left $\mathbf{v} = \mathbf{u} \times \mathbf{w}$.
- Transform world points to this camera frame (*view* transform) before applying projection.

OpenGL Fixed-Function Pipeline Cheatsheet

- Order: $\mathbf{Model} \to \mathbf{View} \to \mathbf{Projection} \to \mathbf{Viewport}$.
- View (camera):

```
• Perspective (viewing frustum and clipping):
```

```
glMatrixMode(GL_PROJECTION);
glLoadIdentity();
gluPerspective(fovy, aspect, near, far); // or glFru
```

Orthographic:

```
glMatrixMode(GL_PROJECTION);
glLoadIdentity();
glOrtho(left,right,bottom,top,near,far); // 2D: gluC
```

• Objects outside the frustum are clipped; default window after projection and division is $[-1,1]^3$ in NDC.

Extras

- Stereoscopic/3D: render two slightly offset views (delivery via anaglyph, polarization, shutter glasses, etc.).
- Other projections (e.g., stereographic) exist for special purposes.

3 Colors

Light and Color Basics

- Visible light is a band of electromagnetic (EM) waves; what we perceive as a color is a *mixture* of EM frequencies (e.g., red $\sim 4.3 \times 10^{14}$ Hz, violet $\sim 7.5 \times 10^{14}$ Hz). White is the most "impure" (broad-mixture) color.
- A color's spectrum can be sketched by an energy-frequency curve: dominant frequency (peak), brightness (area under the curve), and purity (how concentrated the energy is around the dominant frequency).

Color Models (Tri-stimulus Theory)

- A **color model** chooses three descriptors (axes) to specify colors, echoing the three cone types in the human eye.
- We use three common models: **RGB** (displays), **CMY** (printing), and **HSV** (artist/user-oriented control).

RGB (Additive)

- Colors are 3D vectors $(r, g, b) \in [0, 1]^3$; adding colors is vector addition. The full set of colors forms a unit cube.
- Additive system: adding primaries makes the result brighter; complementary pairs (e.g., red-cyan, green-magenta, blue-yellow) sum to white.

CMY (Subtractive)

- Uses cyan, magenta, yellow as primaries (ink/filters).
- Subtractive system: stacking pigments removes light—adding primaries makes the result darker.

HSV (Hue-Saturation-Value)

- Constructed as a *hexcone*: project the RGB cube onto a hexagon and stack layers by brightness.
- $V = \max(R, G, B)$ (brightness), S = distance from the gray axis to the color normalized by the hexagon radius (pureness), H = angle around the axis (red 0°, green 120°, blue 240°).
- Pure hue at V = 1, S = 1; when S = 0 the hue is undefined (grays).

Color Gamut and Devices

- No device or primary set reproduces *all* perceivable colors; the **gamut** is the subset achievable by a system.
- Different devices (and even extended-primary systems like RGBY or RGBCMY) have different gamuts.

Additive vs. Subtractive (Summary)

- Additive (RGB): emit light; more primaries ⇒ brighter (white at full).
- Subtractive (CMY): filter/absorb light; more inks \Rightarrow

Illumination and Shading

Phong Illumination: $I_{phong} = I_a K_a + f_{att} I_p K_d(N \cdot L) + f_{att} I_p K_s (R \cdot V)^n$

$$\begin{bmatrix} i_r \\ i_g \\ i_b \end{bmatrix} = \begin{bmatrix} i_{ar}k_{ar} \\ i_{ag}k_{ag} \\ i_{ab}k_{ab} \end{bmatrix} \text{ (Ambient)} + f_{att}I_pK_d(N \cdot L) \text{ (Diffuse)} + f_{att}I_pK_s(R \cdot V)^n \text{ (Speembar)} \text{ (GL_DEPTH_TEST)};$$

- I_a luminance in ambient term: $\begin{bmatrix} i_{ar} & i_{ag} & i_{ab} \end{bmatrix}^T$: uniform lighting on every surface in the scene
- K_a material property: $[k_{ar} \quad k_{ag} \quad k_{ab}]^T$
- K_a diffuse material property: $\begin{bmatrix} k_{dr} & k_{dg} & k_{db} \end{bmatrix}^T$
- K_s specular mat. prop: $\begin{bmatrix} k_{sr} & k_{sg} & k_{sb} \end{bmatrix}^T$ all material properties $\in [0, 1]$
- f_{att} distance attenuation factor (of point light source)
- I_p point light source vector
- $N \cdot L$ diffuse reflection $\propto \cos(\theta)$, N is surface normal, L is light vector
- $R \cdot V$ reflection vector, V is viewpoint vector, R is reflection vector.

$$R = 2(N \cdot L)N - L$$

• n shininess coefficient: higher $n \to \text{smaller}$ and sharper highlights $\in [1, 500]$

Multiple lightings:

$$I_{phong} = I_a K_a + \sum_i f_{att,i} I_{p,i} [K_d(N \cdot L) + K_s (R \cdot V)^n]$$

```
// Call once after you create the GL context/window
static void setupPhongExample(bool highlight = false) {
       // ----- Material (object) terms
       // K_a: ambient reflectance (RGBA)
GLfloat K_a[4] = { 0.20f, 0.20f, 0.20f, 1.0f };
        // K_d: diffuse/albedo reflectance (RGBA)
       GLfloat K_d[4] = { 0.70f, 0.70f, 0.75f, 1.0f }; // slightly
       // K_s: specular reflectance (RGBA) - white when highlight is on
       GLfloat K_s[4] = { 0.20f, 0.20f, 0.20f, 1.0f };
       if (highlight) { K_s[0] = K_s[1] = K_s[2] = 1.0f; } // strong
        white specular
       // n: shininess exponent (0..128 in fixed-function OpenGL)
       GLfloat shininess = highlight ? 100.0f : 16.0f;
       glMaterialfv(GL_FRONT_AND_BACK, GL_AMBIENT,
       glMaterialfv(GL_FRONT_AND_BACK, GL_DIFFUSE,
                                                                                              K_d);
       glMaterialfv(GL_FRONT_AND_BACK, GL_SPECULAR, K_s);
       glMaterialf (GL_FRONT_AND_BACK, GL_SHININESS, shininess); // n
            ----- Global ambient light (scene ambient)
        // I_a: global ambient intensity (RGBA)
       GLfloat I_a[4] = \{ 0.15f, 0.15f, 0.15f, 1.0f \};
       glLightModelfv(GL_LIGHT_MODEL_AMBIENT, I_a); // contributes
        K_a \times I_a
       // Optional: two-sided lighting if you render both faces
       // glLightModeli(GL_LIGHT_MODEL_TWO_SIDE, GL_TRUE);
                  ---- One positional light (Light 0) ----
       //I_l: light intensities (ambient/diffuse/specular) for this
       GLfloat L_ambient [4] = { 0.10f, 0.10f, 0.10f, 1.0f }; GLfloat L_diffuse [4] = { 1.00f, 1.
       GLfloat L_specular[4] = { 1.00f, 1.00f, 1.00f, 1.0f };
       glLightfv(GL_LIGHTO, GL_AMBIENT, L_ambient); // I_l (ambient) glLightfv(GL_LIGHTO, GL_DIFFUSE, L_diffuse); // I_l (diffuse)
       glLightfv(GL_LIGHTO, GL_SPECULAR, L_specular); // I_l (specular)
           Position (w=1 for point light, w=0 for directional/infinite)
       GLfloat lightPos[4] = { -3.0f, 4.0f, 6.0f, 1.0f }; // (x,y,z,1) glLightfv(GL_LIGHTO, GL_POSITION, lightPos);
       // ----- Distance attenuation f_{att}(d) = 1/(k_c + k_l d + k_q d^2)
       // Defaults are kc=1, kl=kq=0 (no falloff). Set your own:
                                              // constant term
       GLfloat k_c = 1.0f;
       GLfloat k_1 = 0.06f; // linear term
       GLfloat k_q = 0.02f; // quadratic term (most physically
        plausible
       glLightf(GL_LIGHTO, GL_CONSTANT_ATTENUATION,
       glLightf(GL_LIGHTO, GL_LINEAR_ATTENUATION,
```

```
glLightf(GL_LIGHTO, GL_QUADRATIC_ATTENUATION, k_q);
// ----- Pipeline toggles -----
glEnable(GL_LIGHTO);
glEnable(GL_LIGHTING);
glShadeModel(GL_SMOOTH); // Gouraud shading
glEnable(GL_NORMALIZE); // keep normals unit-length after
scaling
(SptEndare)(GL_DEPTH_TEST); // needed for proper 3D visibility
```

Spotlight: $\phi = \cos^{-1}(s \cdot v)$ where v is spotlight direction, s is vector from light source to the surface. both are unit vectors.

light intensity of spotlight at s: $I_p' = I_p(\cos \phi)^n = I_p(s \cdot v_s)^n$

Shadings

- Flat shading: glShadeModel(GL_FLAT);
- Gouraud shading: use vertex normal (avg of all surfaces sharing the vertex), pixels in the polygon has interpolated color from all vertices. glShadeModel(GL_SMOOTH)
- Phong Shading: Compute vertex normal, interpolate normal vectors on each pixels
- Toon shading: phong shading but use $N \cdot L$ and $R \cdot V$ with discrete range

Problems with Interpolated Shading with Polygonal Models

- Non-global effects
- No shadow
- Polygonal silhouette
- Orientation dependence
- Shared vertices
- Misleading vertex normals

Global vs Non-global Illumination

- Global (Ray Tracing)
 - More photorealistic/complex
 - Computes many types of physical light interactions
 - Slow
 - e.g., CG movies

• Non-global (e.g., Phong Shading)

- Only considers the light source, the surface point, and the viewer directly
- Faster but less realistic
- e.g., no shadow/reflection
- e.g., real-time 3D games

Fractal drawings

```
void drawRecursiveSquares(int n) {
 glPushMatrix();
  if(n==0) return;
  for(int i=0;i<4;i++) {</pre>
    glPushMatrix();glPushMatrix();
    glRotatef(90*i,0,0,1);
    glTranslatef(1,1,0);
    glScalef(0 5 0 5 0 5);glScalef(0.5,0.5,0.5);
    drawRecursiveSquares(n-1);
    glPopMatrix();
 drawUnitTwoSquare();
  glPopMatrix();
void drawHive(int n) {
  if (n == 1) {
    drawHexagon();
    return;
 glPushMatrix();
  for (int i = 0; i < 6; i++) {
    glRotated(60, 0, 0, 1);
    glPushMatrix();
    glTranslated(0, sqrt(3), 0);
    drawHives(n - 1);
    glPopMatrix();
 glPopMatrix();
```