

Based on:

https://www.researchgate.net/publication/276493313_RSSI-based_Algorithm_for_Indoor_Localization

Distance between p_i and device:

$$d_i^2 = (x_i - x_0)^2 + (y_i - y_0)^2 + (z_i - z_0)^2$$

$$\Rightarrow d_i^2 = x_i^2 + y_i^2 + z_i^2 - 2x_i x_0 - 2y_i y_0 - 2z_i z_0 + x_0^2 + y_0^2 + z_0^2$$

Where x_i , y_i , and z_i are coordinate of p_i number i

x_0 , y_0 and z_0 are coordinate of the device

Suppose distances between the device and 3 pis are known:

$$d_1^2 = x_1^2 + y_1^2 + z_1^2 - 2x_1 x_0 - 2y_1 y_0 - 2z_1 z_0 + x_0^2 + y_0^2 + z_0^2 \quad (1)$$

$$d_2^2 = x_2^2 + y_2^2 + z_2^2 - 2x_2 x_0 - 2y_2 y_0 - 2z_2 z_0 + x_0^2 + y_0^2 + z_0^2 \quad (2)$$

$$d_3^2 = x_3^2 + y_3^2 + z_3^2 - 2x_3 x_0 - 2y_3 y_0 - 2z_3 z_0 + x_0^2 + y_0^2 + z_0^2 \quad (3)$$

Subtract (2) from (1):

$$d_1^2 - d_2^2 = x_1^2 + y_1^2 + z_1^2 - x_2^2 - y_2^2 - z_2^2 - 2(x_1 - x_2)x_0 - 2(y_1 - y_2)y_0 - 2(z_1 - z_2)z_0$$

$$\Rightarrow 2(x_1 - x_2)x_0 + 2(y_1 - y_2)y_0 + 2(z_1 - z_2)z_0 = x_1^2 + y_1^2 + z_1^2 - x_2^2 - y_2^2 - z_2^2 - d_1^2 + d_2^2$$

Let $a_{12} = 2(x_1 - x_2)$

$$b_{12} = 2(y_1 - y_2)$$

$$c_{12} = 2(z_1 - z_2)$$

$$e_{12} = x_1^2 + y_1^2 + z_1^2 - x_2^2 - y_2^2 - z_2^2 - d_1^2 + d_2^2$$

$$\Rightarrow a_{12}x_0 + b_{12}y_0 + c_{12}z_0 = e_{12} \quad (4)$$

Similarly, subtract (3) from (2):

$$a_{23}x_0 + b_{23}y_0 + c_{23}z_0 = e_{23} \quad (5)$$

subtract (1) from (3):

$$a_{31}x_0 + b_{31}y_0 + c_{31}z_0 = e_{31} \quad (6)$$

The coordinate of device can be solved using Cramer's Rule on (4), (5) and (6)