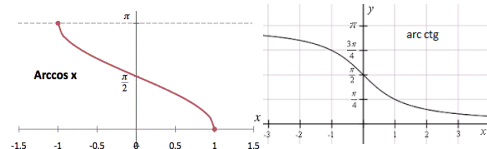


$$X=(-1,1) \quad Y=(\pi/2,-\pi/2)$$

$$X=(-1,1) \quad Y=(\pi,0)$$



$$X=R \quad Y=(\pi/2,-\pi/2)$$

$$X=R \quad Y=(0,\pi)$$

$$\begin{aligned} \sin 2x + \cos 2x &= 1 \\ \operatorname{tg} x \cdot \operatorname{ctg} x &= 1 \\ \operatorname{tg} x &= \sin x / \cos x \\ \operatorname{ctg} x &= \cos x / \sin x \\ \sin(2x) &= 2 \sin x \cdot \cos x \\ \cos(2x) &= \cos^2 x - \sin^2 x \\ 2 \sin x \cos x &= \sin 2x \end{aligned}$$

0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0
0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$	—
—	$\sqrt{3}$	1	$\frac{\sqrt{3}}{3}$	0

$$\begin{aligned} \log_a x + \log_a y &= \log_a (x \cdot y) & \ln 0 &\rightarrow -\infty & \ln 1 &= 0 & \ln e &= 1 & \ln \infty &\rightarrow \infty \\ \log_a x - \log_a y &= \log_a (x/y) & a/\infty &= 0, & a/0 &= \infty \\ n \cdot \log_a x &= \log_a x^n & 1/\operatorname{tg} &= \operatorname{ctg} \\ \log_a x &= \log_a x / \log_a a & (a-b)^3 &= a^3 - 3a^2b + 3ab^2 - b^3 \end{aligned}$$

#### LINIOWE RÓWNANIE RÓŻNICZKOWE:

- lewa = 0 R, C ∈ R, A > 0 2. wynik = RORJ, potem dopisać A(x)
- po pochodną wyniku pkt 2, uzupełnić pierwszy wzór o y' i y = prawa całka całości, wyliczyć A(x), podstawić A(x) do RORJ tj. pkt 2 = RSRN
- stworzyć RORN (y = ...) = RORJ + RSRN

**POLE OBSZARU** całka dół z lewej x, góra w prawo [f góra - f dół]

przy wyliczaniu najpierw postawienie góry całki - dół całki

**CAŁKA NIEOZN.WIELOM:** dla -del, licz.to wiel.1st = dopasować dla -del, licznik to liczba  $ax^2+bx+c = a[(x+b/2a)^2 - \Delta/4a^2]$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$f(x)^{g(x)'} = e^{g(x) \cdot \ln f(x)}$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

$$\frac{1}{x^n} = x^{-n}$$

$$x^n = nx^{n-1}$$

$$\frac{1}{x^2} = x^{-2} = -2x^{-3}$$

$$\frac{a}{x} = -\frac{a}{x^2}$$

$$\pi = 1$$

$$(x^a)' = a \cdot x^{a-1}$$

$$(a^x)' = a^x \ln a$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(\sin x)' = \cos x$$

$$(\cos x)' = -\sin x$$

$$(\operatorname{tg} x)' = \frac{1}{\cos^2 x}$$

$$(\operatorname{ctg} x)' = -\frac{1}{\sin^2 x}$$

$$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$

$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$$

$$(\operatorname{arctg} x)' = \frac{1}{1+x^2}$$

$$(\operatorname{arcctg} x)' = -\frac{1}{1+x^2}$$

-----calki-----

$$\sqrt[n]{n^a} = x^{\frac{a}{n}} // \frac{1}{x^a} = x^{-a}$$

$$2. x^n = \frac{1}{n+1} x^{n+1} + C$$

$$3. x = \frac{1}{2} x^2 + C$$

$$4. \frac{1}{x} = \ln |x| + C$$

$$4a. \frac{1}{x^2} = -\frac{1}{x} + C$$

$$5. a^x = \frac{a^x}{\ln a} + C$$

$$6. e^{ax} = \frac{1}{a} e^{ax} + C$$

$$7. \sin x = -\cos x + C$$

$$7a. \sin ax = -\frac{1}{a} \cos ax + C$$

$$8. \cos x = \sin x + C$$

$$8a. \cos ax = \frac{1}{a} \sin ax + C$$

$$9. \operatorname{tg} x = -\ln |\cos x| + C$$

$$10. \operatorname{ctg} x = \ln |\sin x| + C$$

$$11. \frac{dx}{\cos^2 x} = \operatorname{tg} x + C$$

$$12. \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C$$

$$13. \frac{dx}{x^2 + a^2} = \frac{1}{a} \operatorname{arctg} \frac{x}{a} + C$$

$$14. \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x-a}{x+a} \right| + C$$

$$15. \frac{dx}{\sqrt{a^2 - x^2}} = \operatorname{arcsin} \frac{x}{a} + C$$

$$16. \frac{dx}{\sqrt{x^2 + q}} = \ln |x + \sqrt{x^2 + q}| + C$$

$$17. -\frac{1}{1+x^2} = \operatorname{arcctg} x + C$$

$$18. \frac{-1}{\sqrt{1-x^2}} = \arccos x + C$$

$$19. \arcsin x = \sqrt{1-x^2} + x \cdot \arcsin x + C$$

$$\text{POCHLOG: } f'(x)/f(x) = \ln (f(x)) + C$$