Supplementary material: Quantifying early marine diagenesis in shallow-water carbonate sediments

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1. Geological setting

- 2 Carbonate sediments from the Bahamas platform and associated slope pro-
- vide a modern analog to the carbonate rocks that comprise the ancient geological
- 4 record. In this study, we used previously published geochemical measurements
- ⁵ (Higgins et al., 2018; Blättler et al., 2015) from various sites to constrain and
- 6 validate a numerical model of carbonate recrystallization, neomorphism, and
- 7 dolomitization.
- The Great Bahamas Bank (GBB) is a modern example of a low-angle pro-
- 9 grading carbonate platform and consists almost entirely of a mixture of sedi-
- ments sourced from the platform top (aragonite) and pelagic sediments from the
- open ocean (low-Mg calcite) (Swart and Eberli, 2005). The variable abundance
- of platform and pelagic carbonate have been linked to changes in eustatic sea
- level with pelagic carbonate dominating during periods of low sea-level and plat-
- 14 form exposure (Eberli et al., 1997; Swart and Eberli, 2005; Swart, 2008). These
- sediments offer the opportunity to study the marine diagenetic alterations as-
- 16 sociated with large volumes of fluid flow during sea level changes. Detailed
- descriptions of the geochemistry, sedimentology, and stratigraphy of each site

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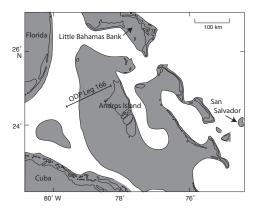


Figure 1: Map of the Bahamas (modified from Eberli et al., 1997) showing the location of ODP Leg 166 (Sites 1003 and 1007), the Little Bahamas Bank (LBB), and San Salvador Island (gray shaded regions are shelf/bank-top environments).

- 18 from the GBB has been published elsewhere and are only briefly reviewed here
- 19 (e.g. Eberli et al., 1997; Ginsburg, 2001; Supko, 1977; Swart and Eberli, 2005;
- ²⁰ Swart et al., 1987; Vahrenkamp et al., 1988, 1991).

21 1.1. The Bahamas bank: Clino and Unda

- During the initial phase of the Bahamas drilling project, two cores Clino
- 23 and *Unda* were collected from the shallow platform sediments of the GBB,
- ²⁴ west of Andros Island (Eberli et al., 1997; Ginsburg, 2001; Swart and Eberli,
- $_{25}$ 2005). Unda is located most proximal to Andros Island, situated 8.5 km east
- of Clino, and consists of shallow-water platform sands and reefal deposits that
- 27 alternate with intervals of deeper skeletal and peloidal platform margin deposits.
- ²⁸ Subaerial exposure surfaces and intervals of pervasive dolomitization indicate
- that the sediments in Unda have seen a wide range of diagenetic conditions.
- The samples used in this study are from a \sim 70 m thick dolomitized interval,
- between 350-250 mbsf, containing shallow-water deposits that grade upwards
- into skeletal packstone and coral. Pore-fluid profiles indicate that there is a
- 33 significant influx of modern seawater throughout the bank top sediments (Swart
- et al., 2001).

Clino is located at the modern platform margin and is composed of three 35 major lithologic units: an upper platform section (0–100 mbsf) containing reefal deposits and several subaerial exposure surfaces, a middle reefal unit with upward progression from deep reef to back reef, and slope sediments (> 200 mbsf) consisting mainly of monotonous intervals of skeletal and non-skeletal grains. The mineralogy of the sediments varies widely with depth. The upper part of 40 the core is dominated by low-Mg calcite (<150 mbsf), whereas between 150-367 mbsf aragonite is abundant. Below 367 m dolomite is prevalent as a minor fraction of the sediment. The measurements used in this study are from the deeper interval below 200 mbsf, below the well studied upper part of the core that is significantly influenced by meteoric diagenesis (Ginsburg, 2001; Swart 45 and Eberli, 2005; Swart, 2015). In order to study the isolated dolomitic component in the deeper interval, a subset of the $\delta^{44/40}$ Ca and δ^{26} Mg measurements are from leached samples (Higgins et al., 2018).

49 1.2. ODP Leg 166: Sites 1003 and 1007

ODP Leg 166 collected cores from the prograding western margin of the GBB along a transect from the platform margin into the Straits of Florida 51 (Eberli et al., 1997). Site 1003 is located at \sim 483 m water depth on the middle 52 slope of the western margin, approximately 4 km from the platform edge and 53 12.6 km from the borehole Clino (Eberli et al., 1997). The core consists of a ~1300 m thick Neogene section with a series of mixed pelagic and bank-derived carbonate sediments. Sedimentation rates from the lowermost Pleistocene to the lowermost Miocene seem to be controlled by changes in sea level. The 57 Pleistocene to upper Pliocene interval is significantly condensed indicating slow 58 sedimentation rate and decreased input from the bank top. The lower Pliocene section, on the other hand, is protracted. During this period, the platform produced a lot of material that was shed onto the upper slope. The early Miocene section of the core is characterized by pelagic sedimentation rates. The carbonate mineralogy is dominated by aragonite with lesser amounts of high-Mg calcite (HMC) and dolomite throughout the upper ~ 100 mbsf. Below this depth, corresponding with the Pliocene/Pleistocene boundary, aragonite decreases markedly, HMC disappears, and low-Mg calcite becomes dominant with a minor dolomitic component (Eberli et al., 1997).

Site 1007 is located on the toe of the slope in 647 m water depth and penetrates the entire Neogene and upper Oligocene interval to \sim 1235 mbsf (Eberli et al., 1997). The sediments alternate between platform-derived material and 70 thinner intervals with pelagic-derived material. The input of pelagic derived material is interpreted to coincide with sea-level lowstands when the platform is exposed. In the upper Pliocene (<200 mbsf), there is an increase in more platform-derived material (highstands) with biowackestone, aragonite needles, and peloids. The Miocene sequences in the deeper part of the core, on the other 75 hand, contain mostly pelagic background sediments and skeletal debris (lowstands). It is likely that the transition from a carbonate ramp in the Miocene to a steep-sided platform in the Pliocene contributed to a turnover from skeletalto aragonite needle-dominated redeposited sediments (Eberli et al., 1997; Swart and Eberli, 2005). 80

81 1.3. Little Bahamas Bank

The Little Bahamas Bank (LBB) is the northernmost carbonate platform 82 of the Bahamian Archipelago and hosts an extensive dolomite body in Neogene 83 sediments at shallow depths (20–100 mbsf). We use measurements from four wells drilled along a N-S transect across Walkers Cay Island (WCI), Sales Cay Island (SCI) and Grand Bahama Island (GB1, GB2) (Vahrenkamp et al., 1988, 1991: Williams, 1985). Two main dolomitic units are recognized in these cores: 87 A lower coarse-crystalline Middle Miocene unit and an overlying Pliocene cream-88 white unit that has been significantly recrystallized. These two dolomitic intervals are separated by an unconformity following subaerial exposure (Vahrenkamp et al., 1991). All the measurements presented in this study are from the upper Pliocene dolomite unit between 43–87 mbsf. Previous studies on the petrography and geochemistry of these dolomites indicate that the dolomitization occurred early after sediment deposition by a fluid that was essentially unaltered seawater (Vahrenkamp et al., 1991; Williams, 1985).

96 1.4. San Salvador Island

A 168 m deep well on the north coast of San Salvador Island consists almost entirely of Neogene dolomites. The dolomites can be subdivided into two dis-98 tinct types: stratal and massive. The massive dolomites make up most of the 99 core and are largely replacements of supratidal backreef, coralgal and lagoonal 100 facies. The stratal dolomites are thinly bedded and laminated, contain a poor 10 fauna, and have occasional intraclasts and bird's-eye structures (Supko, 1977). 102 The basal rocks in the core are late Miocene in age and show a striking litho-103 logical similarity with the Miocene strata from LBB (Vahrenkamp et al., 1991). 104 Compared to LBB, however, at least two additional dolomitization episodes have been identified (Swart et al., 1987; Vahrenkamp et al., 1991). Several samples 106 (62 m and 78 m) have Sr isotope ratios close to or even higher than modern day 107 ⁸⁷Sr/⁸⁶Sr (Vahrenkamp et al., 1991; Swart et al., 1987). This Sr isotope signa-108 ture has been related to eustatic sea-level fluctuations during glaciations, which 109 induced higher isotopic ratios than those of today during parts of the Pleis-110 tocene. For these dolomites an age of between 100-200 Ka is independently 111 confirmed by U/Th dates (Swart et al., 1987). 112

1.5. The Monterey Formation

The deep marine Monterey Formation is from the middle Miocene and is 114 exposed along the central Californian coastal area. The hemipelagic to pelagic 115 sediments are rich in organic matter, carbonate, phosphate, and biosilica and 116 act as productive oil source rocks serving the Elwood offshore oil field, a few 117 kilometers off the coast in the Santa Barbara Basin (Bartlett, 1998). All measurements used in this study are from drill-core recovered from Platform Holly in 119 the South Elwood oil field (Miller, 1995). Carbonates occur in discrete intervals 120 throughout the core as authigenic beds and nodules formed as early diagenetic 121 concretionary phases prior to sediment compaction (Bramlette, 1946). Carbonate precipitation and dolomitization within the sediment was likely driven by 123

remineralization of organic matter through bacterial sulfate reduction, which would decrease dolomite-inhibiting sulfate and increase carbonate alkalinity in pore fluids (Compton, 1988). In this study, we explore the limits of the numerical model by simulating authigenic dolomitization in the siliciclastic Monterey Formation and comparing the results to published geochemical measurements (Blättler et al., 2015). Two sets of measurements are used: one set is from carbonates that have been treated to isolate the dolomite fraction (leached), and another set is from the bulk carbonate samples (Blättler et al., 2015).

132 2. Analytical methods

The majority of the isotopic and elemental measurements used to validate 133 the model predictions are previously published with thorough descriptions of 134 the analytical procedures including sample preparation, ion chromatography, 135 and mass spectrometry (Blättler et al., 2015; Higgins et al., 2018). Additionally, 136 a subset of new measurements from San Salvador is included in this dataset. These samples have been analyzed for $\delta^{44/40}$ Ca values, δ^{26} Mg values, and major-138 minor elements using identical procedures outlined in Higgins et al. (2018). For 139 a full description of the methods we refer to Higgins et al. (2018), but here 140 present a short summary.

At Princeton University, samples for isotope analyses were processed us-142 ing an automated high-pressure ion chromatography system (IC, Dionex UCS-143 5000+) to isolate either Ca or Mg. The purified samples were analyzed for 144 $\delta^{44/40}$ Ca and δ^{26} Mg on a Thermo Scientific Neptune Plus MC-ICP-MS. Mea-145 surements were carried out at low resolution for Mg and medium resolution for Ca to avoid ArHH⁺ interferences. All data are reported in delta notation 147 relative to a known standard. For Ca isotopes the measured $\delta^{44/42}$ Ca values are converted to $\delta^{44/40}$ Ca values relative to seawater assuming mass dependent 149 fractionation with a slope of 2.05. Long-term external reproducibility for each isotopic system is determined based on the difference between two known standards taken through the full chemical procedure with each batch of samples. 152

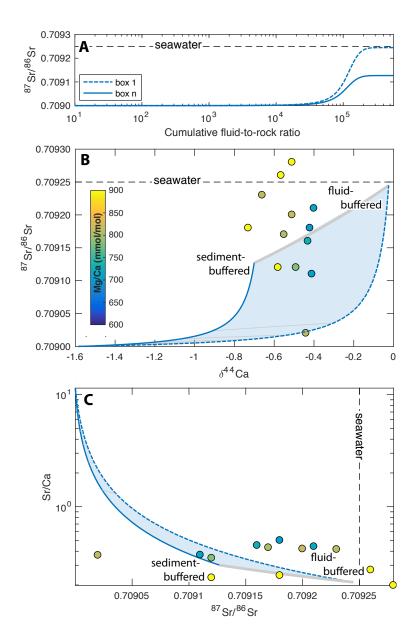


Figure 2: Model results for $^{87}{\rm Sr}/^{86}{\rm Sr}$ demonstrating dolomitization of primary aragonite $(^{87}{\rm Sr}/^{86}{\rm Sr}_{primary}=0.70900)$ in modern seawater (A) Change in composition over time with increasing cumulative fluid-to-rock ratio, (B) Model phase space for $^{87}{\rm Sr}/^{86}{\rm Sr}$ versus $\delta^{44/40}{\rm Ca}$ values from box 1 (fluid-buffered) to box N (sediment-buffered), (C) Model phase space for Sr/Ca versus $^{87}{\rm Sr}/^{86}{\rm Sr}$ ratios. Samples are $^{87}{\rm Sr}/^{86}{\rm Sr}$ measurements on dolomites from the San Salvador core (Swart et al., 1987, since we do not have measurements from exact samples, the data has been extrapolated to match our equivalent $\delta^{44/40}{\rm Ca}$ and Sr/Ca measurements)

For Ca isotopes the external reproducibility for SRM915b relative to modern seawater is $-1.18 \pm 0.16\%$ (2 σ , N=125). $\delta^{44/40}$ Ca_{Seawater} is $\pm 1.92\%$ on the 154 SRM-915a scale and $\pm 0.98\%$ on the bulk silicate bulk Earth scale. For Mg, the long-term external reproducibility of our measurements is estimated by com-156 paring the Mg standard Cambridge-1 and modern seawater against Dead Sea 157 Metal (DSM-3). The measured δ^{26} Mg values for Cambridge-1 and seawater are 158 $-2.56 \pm 0.09\%$ (2 σ , N=76) and $-0.83 \pm 0.08\%$ (2 σ , N=99), respectively. 159 The Sr/Ca and Mg/Ca ratios were measured on aliquots of dissolved powders 160 analyzed for $\delta^{44/40}\mathrm{Ca}$ and $\delta^{26}\mathrm{Mg}$ isotopes using a ThermoFinnegan Element-2 161 Inductively Coupled Plasma Mass Spectrometer (ICP-MS). The metal to cal-162 cium ratios were determined using a set of matrix-matched in-house standards 163 spanning the sample range. The external reproducibility of the ratios are es-164 timated at $\pm 5 - 7\%$ from replicate measurements of SRM-88b, a dolomitic limestone. 166

3. Modeling Sr isotopes

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In order to compare model results to the original work of Banner and Han-168 son (1990), we here include a summary of model predictions for the covariation 169 between $^{87}\mathrm{Sr}/^{86}\mathrm{Sr}$ ratios, $\delta^{44/40}\mathrm{Ca}$ values, and Sr/Ca ratios. Fig. 2 illustrates 170 model cross-plots of ${}^{87}\mathrm{Sr}/{}^{86}\mathrm{Sr}$ against both $\delta^{44/40}\mathrm{Ca}$ and Sr/Ca ratios. During 17 dolomitization along a fluid to sediment-buffered trajectory the model predicts 172 linear covariation between ${}^{87}\mathrm{Sr}/{}^{86}\mathrm{Sr}$ and $\delta^{44/40}\mathrm{Ca}$ values (grey line, Fig. 2). In 173 addition, due to the high concentrations of Sr in primary aragonite, the bulk 174 sediment remains sediment-buffered with respect to Sr at higher fluid-to-rock 175 ratios than for Ca (i.e. J-curve in Fig. 2B). However, the model results also 176 demonstrate a number of complications for using ⁸⁷Sr/⁸⁶Sr ratios in studying 177 early marine diagenesis: First, recrystallized calcite/dolomite have small con-178 centrations of Sr, which makes the isotopic ratio sensitivity to input from other 179 non-marine sources (e.g. deeper basin fluids or in situ ⁸⁷Rb decay to ⁸⁷Sr). For example, dolomite samples from San Salvador have ${}^{87}\mathrm{Sr}/{}^{86}\mathrm{Sr}$ ratios that 181

are more radiogenic than modern seawater (Swart et al., 1987, Fig. 2). Second, the sensitivity to other non-marine sources is further increased by the fact that the range of ⁸⁷Sr/⁸⁶Sr values in modern to late Miocene sediments is small (0.70925–0.70910, DePaolo, 1986). Third, it is highly likely that these sediments have been dolomitized or neomorphosed at different points in time ranging from the Pleistocene to the Miocene (Swart et al., 1987), making it difficult to fit a model trajectory for a single primary end-member ⁸⁷Sr/⁸⁶Sr ratio.

¹⁸⁹ 4. Sensitivity test of model parameters

The most important factors governing the modeled isotopic trajectories are: 190 1) The mineralogy of the primary and diagenetic sediments, 2) the advection and 191 reaction rates, 3) the elemental partitioning, and 4) the mass of the fluid. The 192 model is sensitive to these parameters because they each to some extent influence 193 the abundance of elements in the fluid relative to the sediment along the fluid 194 flow path. In the following section, we test the model sensitivity to changes in these parameters as demonstrated by the shape of the isotopic cross-plot area 196 carved out by the model trajectories. By testing the sensitivity of the model 197 to changes in these boundary conditions, we can isolate the major uncertainties 198 and evaluate their importance and implications for the final predictions.

200 4.1. Percent alteration

The fraction of diagenetic versus primary minerals in the bulk sediment can be used to infer the percentage (%) of the bulk sediment that has been recrystallized during early diagenesis. The rate of change in the mass of primary minerals is directly proportional to the reaction constant (R) and follows exponential decay:

$$\frac{\partial M_{primary}}{\partial t} = -R \times M_{primary} \tag{1}$$

$$M_{primary}(t) = M_{primary}(0)e^{-R \times t}$$
 (2)

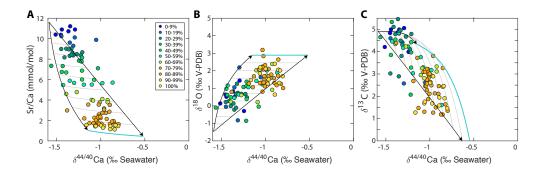


Figure 3: Percentage of the bulk rock that has been diagenetically altered. The modeled trajectories are compared to limestones in the upper part (0–400 mbsf) of core sediments from the Bahamas Transect (Sites 1003, 1007, Clino). The data points are binned into percentages based on correlation between the observed Sr/Ca ratios and the modeled phase space **A** and the binned data are then compared to δ^{18} O (**B**), and δ^{13} C (**C**) vs. $\delta^{44/40}$ Ca values

where t is time in years and $M_{primary}$ is the mass of primary minerals.

The model makes specific predictions for each geochemical proxy based on the fraction of primary vs. diagenetic minerals. By comparing the model to limestones from the younger part of the Bahamian dataset (where the initial boundary conditions are best constrained), it is possible to evaluate whether the distribution of data follows the model prediction for percentage alteration across all proxies (Fig. 3). Broadly, the model predictions are in agreement with the measured δ^{13} C vs. $\delta^{44/40}$ Ca values and δ^{18} O vs. $\delta^{44/40}$ Ca values, following a consistent increasing trend from 0 to 100%, although with variable offsets from the specific model trajectories (Fig. 3A-C). This inconsistency is most likely related to variability in the boundary conditions of the Bahamian dataset as the choice of both initial conditions and the specific diagenetic mineral (low-Mg calcite vs. dolomite) will affect the modeled trajectories.

4.2. Mineralogy

The primary mineral. The model is sensitive to mineralogy because the stoichiometry of the bulk sediment directly controls the ratio of elemental abundance in the sediment relative to the fluid. This sediment-fluid ratio (together with the advection/reaction ratio) sets the length scale of the flow path over

Parameter	Baseline	Sensitivity tests	Figure
Length	50 m	-	-
scale (N)			
$lpha_{Ca}$	1.000	-	-
$lpha_{Mg}$	0.998	-	-
$lpha_C$	1.001	-	-
α_O	1.0330	-	-
K_{Sr}	0.05	0.05 vs. 0.1	Fig. 9
$R \text{ myr}^{-1}$	10%	100% vs. $1%$	Fig. 7
u cm/yr	10	100 vs. 1	Fig. 8
Diagenetic	dolomite	low-Mg calcite	Fig. 4
mineralogy		vs. dolomite	
Primary	aragonite	low-Mg calcite	Fig. 5
mineralogy		vs. aragonite	
M_f (Ca ²⁺	10.6	106 vs. 1.6	Fig. 10–11
$\mathrm{mmol/kg})$			
M_f (Mg ²⁺	52.8	2.5 vs. 1.3	Fig. 11
$\mathrm{mmol/kg})$			
$\delta_f~(\%_0)$	$\delta^{44/40}$ Ca: 0% δ^{26} Mg: -0.8% δ^{13} C: -2% δ^{18} O: -29.5%	-	-

Table 1: Summary and model boundary conditions for each sensitivity test. N is the length scale (i.e. number of boxes), α is the element-specific fractionation factor, K_{Sr} is the partitioning coefficient for Sr, R is the reaction constant, u is advection rate, M_f is the elemental mass in the diagenetic fluid, δ_f is the isotopic composition of the diagenetic fluid. The symbol '-' indicates that the parameter was kept constant in all scenarios. $\delta^{44/40}\mathrm{Ca}$ is stated relative to seawater, $\delta^{26}\mathrm{Mg}$ relative to DSM-3, $\delta^{13}\mathrm{C}$ relative to V-PDB, and $\delta^{18}\mathrm{O}$ relative to V-PDB.

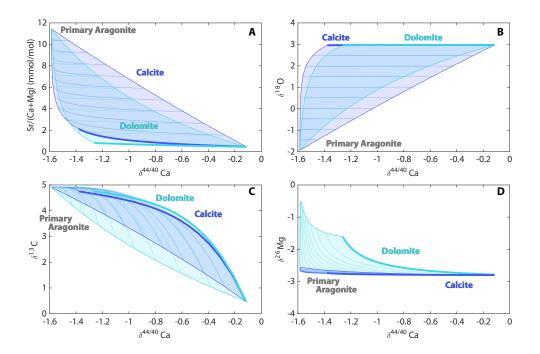


Figure 4: Neomorphism of primary aragonite to low-Mg calcite (dark blue) vs. dolomite (light blue). The model results predict that the shape of the isotopic trajectory from box 1 to N changes based on the mineralogy/stoichiometry of the diagenetic mineral. Here, 50 boxes are included in the model to illustrate the spread of isotopic trajectories from the top to the bottom of the sediment column (box 1-N).

which the fluid becomes sediment-buffered. For example, during neomorphism of aragonite (low concentrations of Mg) the fluid needs to pass through several boxes (long flow path), dissolving a large volume of sediment, in order to become sediment buffered with respect to Mg. On the other hand, the dissolution flux of Mg from high-Mg calcite would be significantly larger and the fluid would become sediment-buffered over a much smaller length scale (fewer boxes).

The concentration of Mg in the primary mineral will also affect the modeled cross-plot phase space of $\delta^{26} \rm Mg$ vs. $\delta^{44/40} \rm Ca$ values. In comparison to calcite recrystallization, neomorphism of aragonite (with lower concentration of Mg than calcite) will results in a larger degree of Rayleigh-type distillation of the

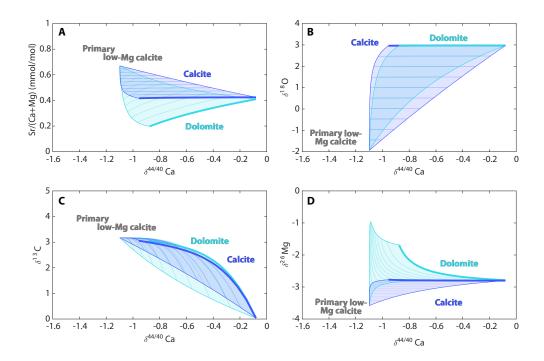


Figure 5: Recrystallization of primary low-Mg calcite (dark blue) vs. dolomitization (light blue). The model results predict that the shape of the isotopic trajectory from box 1 to N changes based on the mineralogy/stoichiometry of the diagenetic mineral (similar to Fig. 4, but with different initial mineralogy)

fluid along the flow path, producing more enriched δ^{26} Mg values in the sedimentbuffered end-member (Fig. 4–5).

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Similarly, primary aragonite generally has larger concentrations of Sr than calcite. The modeled phase-space of Sr/Ca versus $\delta^{44/40}$ Ca for neomorphism of aragonite is therefore offset from the modeled phase-space for recrystallization of calcite (Fig. 4–5). This offset is set by the initial higher Sr/Ca ratios and depleted $\delta^{44/40}$ Ca values in primary aragonite relative to calcite (-1.6% vs. -1.1%, respectively Blättler et al. 2012; Tang et al. 2008; Gussone et al. 2005).

The diagenetic mineral. The mineralogy of the diagenetic mineral controls the partitioning, and thus precipitation rate, of each individual element into the

solid. As the elemental abundance of the pore-fluid is directly related to the 244 precipitation rate, the mineralogy/stoichiometry of the diagenetic mineral also 245 controls the length scale of the flow path over which the fluid becomes sedimentbuffered. For example, due to the differences in stoichiometry between diage-247 netic calcite and dolomite, the concentration of Ca²⁺ in the pore-fluid increases 248 along the flow path during dolomitization while the concentration of Mg²⁺ de-249 creases. In constrast, this phenomenon is not expected during calcite recrys-250 tallization or aragonite neomorphism. This process is especially important for 25 the modeled isotopic trajectories of $\delta^{44/40}\mathrm{Ca},~\delta^{26}\mathrm{Mg},$ and the concentration of 252 Sr/Ca in the bulk rock (Fig. 6). 253

The model predicts that for the same set of initial conditions, the incorporation of Sr²⁺ into the diagenetic mineral is lower during dolomitization than during both neomorphism of aragonite or recrystallization of calcite. This difference is due to the increase of Ca²⁺ in the pore-fluids with depth during dolomitization, which blocks the structural sites in the mineral lattice and inhibits Sr incorporation. As a result, for a constant partition coefficient ($K_d = 0.05$), more Sr will be incorporated into low-Mg calcite than dolomite (Fig. 4–5).

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The model further predicts that during dolomitization (as opposed to aragonite neomorphism), $\delta^{44/40}$ Ca values become more enriched in the 100% altered 262 sediment in box N (Fig. 6). This difference is controlled by the increase in Ca²⁺ along the flow path during dolomitization leading to Ca²⁺ from infiltrating seawater, with enriched $\delta^{44/40}$ Ca values, penetrating farther along the flow path.

Dolomitization also differs from aragonite neomorphism in distinctive ways within each individual box. This difference is evident in the modeled cross-plot space of δ^{13} C vs. $\delta^{44/40}$ Ca and δ^{18} O vs. $\delta^{44/40}$ Ca (Fig. 4–5): During aragonite neomorphism, the isotopic trajectory in box 1 (from 0 to 100%) follows a simple linear binary mixing relationship between the primary and diagenetic sediment. In contrast, during dolomitization the concentration of Ca decreases in the bulk sediment over time (from 0 to 100%) and the modeled trajectory in box 1 instead follows a concave mixing pathway.

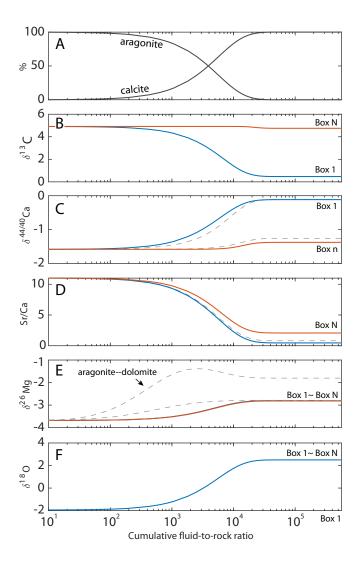


Figure 6: Aragonite neomorphism (**A**) vs. dolomitization (gray dashed line) in box 1 (blue) to box N (red) with increasing cumulative fluid-to-rock ratio over time. The modeled trajectories for δ^{13} C values (**B**) and δ^{18} O values (**F**) are similar for aragonite neomorphism and dolomitization. The differences in the modeled trajectories for $\delta^{44/40}$ Ca values (**D**), δ^{26} Mg values (**E**), and Sr/Ca ratios (**E**) between aragonite neomorphism and dolomitization is governed by the elemental abundance in the diagenetic mineral as defined by the mineral stoichiometry.

The difference between aragonite neomorphism, calcite recrystallization, and 275 dolomitization is also apparent in the modeled phase space between $\delta^{26}{\rm Mg}$ and 276 $\delta^{44/40}$ Ca values. The δ^{26} Mg values of the bulk sediment are especially sensitive to the mineralogical difference: Enrichment of ²⁶Mg values due to Rayleigh-type 278 distillation of the fluid is significantly more pronounced during dolomitization, 279 whereas recrystallization/neomorphism does not change the downstream pore-280 fluid concentration of Mg²⁺ and therefore produces little to no isotopic enrichment (Fig. 4). The modeled cross-plot space of $\delta^{26} \mathrm{Mg}$ vs. $\delta^{44/40} \mathrm{Ca}$ values illustrates the effect of these differences (Fig. 4–5): the $\delta^{26}{\rm Mg}$ values are com-283 pletely reset to the original fluid value during calcite recrystallization whereas 284 δ^{26} Mg values are significantly enriched during dolomitization. In both case, 285 however, the primary δ^{26} Mg value of the sediment is completely altered.

287 4.3. Reaction rate

The reaction rate (R) imposes a strong control on the length scale of the 288 flow path over which the fluid becomes sediment-buffered (i.e. over how many 289 boxes). The model carves out an area in cross-plot space that covers this length 290 scale from box 1 to box N. Changing the reaction rate will change the isotopic 291 trajectories (from 0 to 100% recrystallization) in each specific box: Increasing 292 the reaction rate will drive the pore-fluid towards system more sediment-buffered 293 conditions over a shorter length scale (fewer boxes). In contrast, decreasing the reaction rate will drive the pore-fluid towards more fluid-buffered conditions and a longer length scale of the flow path is needed to reach the sediment-buffered 296 end-member (Fig. 7). However, independent of the reaction rate, the model 297 will always converge towards fully sediment-buffered conditions at some point 298 along an infinitely long flow path (box N). In cross-plot space, the size of the 299 integrated area from box 1 to box N is thus not dependent on the reaction rate when the modeled area covers the entire spectrum from fully fluid-buffered to 301 fully sediment-buffered. The reaction rate remains an important factor when 302 considering the stratigraphic expression of diagenesis, although the modeled 303 cross-plot space is unaffected because the number of boxes can be adjusted to capture the sediment-buffered end-member (Fig. 7). As a result, the model has little capability for constraining diagenetic reaction rates (or advection rates, see below).

308 4.4. Advection rate

The sensitivity of the model to advection rates is similar, though in an op-309 posite sense, to the sensitivity to reaction rates. A 10-fold increase in advection rates produces the same response as a 10-fold decrease in reaction rates and 31 vice versa (Fig. 7-8). Similarly to the sensitivity for reaction rates, the model 312 cross-plot space is unaffected by changing advection rates as long as the length 313 scale/number of boxes is adjusted to capture the entire range from fully fluid-314 buffered to sediment-buffered conditions. Advection and reaction rates are thus only important for considering the stratigraphic expression of diagenesis. In the 316 model, the main impact of both advection and reaction rates is on the extent 317 to which the top of the sediment column is fully fluid-buffered, since for a low 318 advection/reaction rate ratio, even box 1 will tend to be partially sediment-319 buffered (Fig. 7-8). This phenomenon can easily be eliminated by adding a re-dissolution flux of the diagenetic minerals to the model, thereby infinitely 321 dissolving the bulk sediment and eventually alway reaching the fluid-buffered 322 end-member giving enough time. 323

324 4.5. Partition coefficient for strontium

In the model, the behavior of strontium is entirely determined by its partitioning into various minerals, where strontium generally is partitioned more strongly into the primary mineral than the diagenetic mineral. This behavior leads to an increase in pore-fluid Sr^{2+} along the flow path accompanied by a relative increase in the Sr/Ca ratio of the diagenetic mineral from box 1 to box N. By increasing the partition coefficient (K_d) that prescribes the relationship between the concentration of Sr^{2+} in the pore-fluid and the diagenetic mineral, a larger amount of Sr will be incorporated into the diagenetic mineral for a given pore-fluid concentration (Fig. 9). In contrast, a lower partition coefficient will

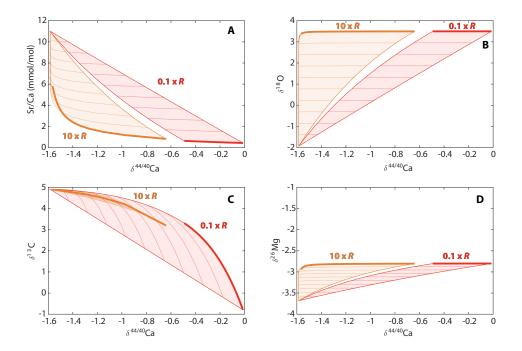


Figure 7: The sensitivity of the model trajectories to changes in reaction rate (R). In the scenario, the model carves out an area in cross-plot space that covers a length scale of 50 m (from box 1 to box 50). Increasing the reaction rate (orange) will drive the pore-fluid system towards more sediment-buffered conditions across all boxes. In contrast, decreasing the reaction rate (red) will drive the pore-fluid system towards more fluid-buffered conditions across all boxes. However, the change in reaction rate can be balanced by changing the length scale of the flow path (i.e. by adding or removing boxes) in order to capture the full range of fluid- to sediment-buffered conditions

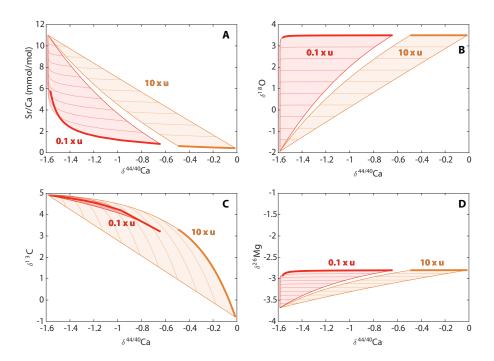


Figure 8: The sensitivity of the model trajectories to changes in advection rate (u). In this scenario, the model carves out an area in cross-plot space that covers a length scale of 50 m (from box 1 to box 50). Increasing the advection rate (orange) will drive the pore-fluid system towards more fluid-buffered conditions whereas, decreasing the reaction rate (red) will drive the pore-fluid system towards more sediment-buffered conditions across all boxes. However, the change in advection rate can be balanced by changing the length scale of the flow path (i.e. by adding or removing boxes) in order to capture the full range of fluid to sediment-buffered conditions (similarly to Fig. 7).

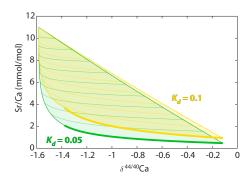


Figure 9: The sensitivity of the model results to the partitioning coefficient of strontium. By increasing the partition coefficient (K_d) , a larger amount of Sr will be incorporated into the diagenetic mineral for a similar pore-fluid concentration (yellow). In contrast, a lower partition coefficient will decrease the amount of strontium incorporated into the diagenetic mineral across all boxes (box 1–50, green).

decrease the amount of Sr incorporated into the diagenetic mineral (Fig. 9).

In addition to the empirically defined partition coefficient and the Sr^{2+} concentration of the fluid, the incorporation of strontium into the diagenetic mineral is also affected by the concentration of Ca^{2+} in the fluid. A higher concentration of Ca^{2+} in the fluid will decrease the partitioning of strontium into the diagenetic mineral phases, as Ca^{2+} blocks the available structural sites in the mineral lattice. This behavior is demonstrated when modeling dolomitization where pore-fluid Ca^{2+} increases along the flow path (Fig. 4).

4.6. Fluid composition

The concentration of various elements in the fluid – a direct lever on the relative mass ratio between fluid and solid – has a strong control on the shape of the modeled isotopic trajectories. For example, the concentration of Ca^{2+} in the fluid controls the degree to which $\delta^{44/40}\operatorname{Ca}$ values are reset and covary with other proxies during diagenesis. High Ca^{2+} concentrations in the infiltrating fluid will result in pore-fluids that are more fluid-buffered over a greater length scale. As a result, bulk sediment $\delta^{44/40}\operatorname{Ca}$ values will be more reset towards the

initial fluid value across all 50 boxes (Fig. 10). In contrast, a lower concentration of $\mathrm{Ca^{2+}}$ in the initial diagenetic fluid will result in pore-fluids that are more sediment-buffered, and bulk sediment $\delta^{44/40}\mathrm{Ca}$ values will be less reset across a similar length scale (Fig. 10).

The model demonstrates that the relative concentrations of solutes in the 354 pore-fluid has a direct effect on the area carved out by the model in cross-plot 355 space. For example, relatively higher Ca²⁺ concentrations in the diagenetic fluid will shift the covariation between $\delta^{13}\mathrm{C}$ and $\delta^{44/40}\mathrm{Ca}$ in the bulk sediment 357 towards generally heavier $\delta^{44/40}\mathrm{Ca}$ values over a similar range in $\delta^{13}\mathrm{C}$ (Fig. 358 10). Similarly, the covariation between $\delta^{26} \text{Mg}$ vs. $\delta^{44/40} \text{Ca}$ values in the bulk 359 sediment changes depending on the relative concentrations of Ca²⁺ and Mg²⁺ 360 in the fluid (Fig. 11): During dolomitization, the model predicts that a higher initial Ca²⁺ concentration in the fluid will increase the slope of the isotopic trajectory (100% recrystallization from box 1-N), reflecting the more enriched 363 $\delta^{44/40}$ Ca values of the diagenetic fluid (i.e. more influence from seawater). Low-364 ering the Mg²⁺ concentration in the fluid will produce a similar response in the 365 modeled trajectories because $\delta^{26} \text{Mg}$ will be less sensitive to resetting relative to $\delta^{44/40}$ Ca (Fig. 11). As a result, modern seawater (which contains higher 367 concentrations of Mg²⁺ than Ca²⁺) will produce a concave and less steep fluid-368 to sediment-buffered isotopic trajectory between δ^{26} Mg and $\delta^{44/40}$ Ca from box 369 1-N. In contrast, the model results predict that lower seawater $\mathrm{Mg}^{2+}/\mathrm{Ca}^{2+}$ ra-370 tios will produce an increase in the slope between $\delta^{26} \mathrm{Mg}$ and $\delta^{44/40} \mathrm{Ca}$ values of the diagenetic sediment during early marine diagenesis (Fig. 11). Due to 372 distillation of the fluid during dolomitization, the slope of this modeled trajec-373 tory can never become positive as δ^{26} Mg always will be more enriched in box N 374 than box 1. However, the model predicts that during aragonite neomorphism, 375 a tipping point exists at very low fluid Mg/Ca ratios ($\sim < 0.02$) where $\delta^{44/40}$ Ca 376 values of the bulk sediment become more sensitive to diagenesis than δ^{26} Mg. As a result, the $\delta^{44/40}$ Ca values are reset before (lower box number) the δ^{26} Mg 378 values thereby producing and inverted isotopic trajectory (Fig. 11).

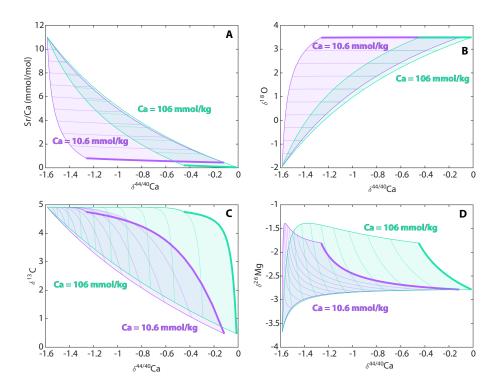


Figure 10: Model sensitivity to $\mathrm{Ca^{2+}}$ concentrations in the infiltrating fluid. For a higher $\mathrm{Ca^{2+}}$ concentration (orange) the pore-fluids are more fluid-buffered over a greater length scale. For a lower $\mathrm{Ca^{2+}}$ concentration (purple) the pore-fluids are more sediment-buffered and bulk sediment $\delta^{44/40}\mathrm{Ca}$ values will be less reset across a similar length scale.

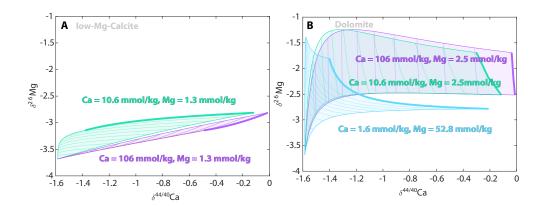


Figure 11: Model sensitivity to the concentration of Ca^{2+} and Mg^{2+} in the infiltrating fluid. The covariation between $\delta^{26}\operatorname{Mg}$ and $\delta^{44/40}\operatorname{Ca}$ values in the diagenetic sediment (diagenetic end-member indicated by thicker line) is directly determined by the $\operatorname{Mg}/\operatorname{Ca}$ ratio of the diagenetic fluid. **A.** During aragonite neomorphism, a tipping point exists at very low fluid $\operatorname{Mg}/\operatorname{Ca}$ ratios where $\delta^{44/40}\operatorname{Ca}$ values of the bulk sediment become more sensitive to diagenetic alteration than $\delta^{26}\operatorname{Mg}$ values. **B.** In contrast, due to distillation of the fluid during dolomitization, the slope of the $\delta^{26}\operatorname{Mg}$ vs. $\delta^{44/40}\operatorname{Ca}$ modeled trajectory can never be become positive as $\delta^{26}\operatorname{Mg}$ are always more enriched in box N than box 1 and as $\delta^{44/40}\operatorname{Ca}$ values are always more enriched in box 1 than box N.

5. δ^{18} O values in bulk sediment from the Bahamas

The isotopic fractionation between $\delta^{18}O$ values in carbonate minerals and 381 pore-fluids can be used as a proxy for temperature during diagenesis (e.g. Böhm 382 et al., 2000; Kim and O'Neil, 1997). The sensitivity of δ^{18} O value to temperature is reflected in the limestones from the deeper part of the Bahamian cores (400– 1200 mbsf), where sediments are recrystallized during later burial diagenesis 385 (Murray and Swart, 2017; Swart and Eberli, 2005; Swart, 2015). Pore-fluids in 386 these older sediments are sediment-buffered with respect to carbon and calcium, 387 but in response to the higher temperatures at depth, the δ^{18} O values of the bulk sediment decrease (from +2 to -2\%). If assuming no change in fluid δ^{18} O values with depth, the observed change in δ^{18} O values can be estimated to reflect an 390 increase in temperature from 10 to 30°C (Kim and O'Neil, 1997). This estimate 391 broadly agrees with calculations of the local geothermal gradient in a well north of Andros Island (~1.3°C per 100 m; Epstein and Clark 2009).

Oxygen isotopes are also sensitivity to early marine diagenesis. In cores 394 from the Bahamas Transect, aragonite neomorphism is indirectly reflected in progressively increasing δ^{18} O values with depth (from 0-400 mbsf): Primary aragonite that precipitates in warm surface waters ($\sim 27^{\circ}$ C) is isotopically de-397 pleted (-1.5%), while diagenetic low-Mg calcite that precipitates in the cooler 398 deeper waters on the slope ($\sim 10^{\circ}$ C, Eberli et al. 1997) is isotopically enriched (+3%). The stratigraphic trend in δ^{18} O values from 0 to 400 mbsf thus broadly reflects increasing mixing between primary aragonite and diagenetic calcite with 401 depth (see Fig. 5 main text). However, the temperature difference between sur-402 face and deeper water masses cannot solely explain the measured range in δ^{18} O 403 values from the Bahamas Transect (using estimates of α from Böhm et al., 2000; 404 Kim and O'Neil, 1997), suggesting that the deeper water masses and/or porefluids are isotopically enriched in comparison with surface waters masses (-30.5 406 vs. -29\% V-PDB, respectively, equivalent to -0.5-1\% SMOW, Coplen et al. 407 1983). 408

Pore-fluid profiles from across the Bahamas demonstrate that $\delta^{18}{\rm O}$ values 409 generally increase with depth (Swart et al., 2000; Kramer et al., 2000; Murray 410 and Swart, 2017; Winkelstern and Lohmann, 2016). These isotopically enriched 411 fluids may be remnants of Pleistocene seawater from the last glacial period 412 (Adkins and Schrag, 2003; Schrag et al., 1996) or they may reflect mixing be-413 tween reflux brines and normal seawater (Murray and Swart, 2017). Swart et al. (2000) attributed the pore-water δ^{18} O profile to carbonate recrystallization dur-415 ing burial where the dissolution of aragonite (δ^{18} O-enriched) and the subsequent 416 precipitation of calcite at higher temperature (δ^{18} O-depleted) would drive an 417 increase in pore-water δ^{18} O values with depth. However, our model cannot re-418 produce the observed trends in pore-fluid chemistry, suggesting that this type 419 of enrichment of fluid δ^{18} O values can only occur during extreme closed-system 420 conditions that require high reaction rates in combination with very little fluid 421 flow: For example, using reaction rates of 10% per Ma, flow rates of 0.5 cm/yr, 422 and a fractionation factor of 1.0289 yields an enrichment of 0.09\% in pore-fluid δ^{18} O values along a 50 m flow path.

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