

In a lot having defective $p = 2\% = 0.02$ $n = 89$ find the probability of acceptance upto the acceptance number

$$P_a = \sum_{d=0}^c \frac{n!}{d!(n-d)!} \times p^d (1-p)^{n-d}$$

$$= \frac{89!}{0!89!} \times (0.02)^0 \times (1-0.02)^{89-0} = 0.16$$

$$P_1(1) = \frac{89!}{1!(89-1)!} \times 0.02^1 \times (1-0.02)^{89-1} = 0.2849$$

$$P_2(2) = \frac{89!}{2!(89-2)!} \times 0.02^2 \times (1-0.02)^{89-2} = 0.26$$

$$P_a = 0.731$$

In a double sampling plan

$$N = 1000 \quad n_1 = 35 \quad c_1 = 0 \quad n_2 = 30 \quad c_2 = 1$$

Find probability if 1% defective is the total probability

- ① If zero defective in first sample
- ② Exactly one defective in first sample
- ③ Zero defective in second sample

For 1st sample

$$n_1 p' = 35 \times 0.01 = 0.35$$

$$\therefore n_1 p' = 0.35 \quad c_1 = 0$$

$$P_a = 0.705$$

② Exactly one defect $n_1 p' = 0.35$

$$c_1 = 1$$

$$P_a = 0.951$$

Exactly defective $P_1 - P_0$

$$= 951 - 705 = P_{a1} = 246$$

2nd Sample

$$n_2 = 30 \quad p' = 0.01 \quad n_2 p' = 0.30 \quad c_2 = 0$$

$$\therefore P_a = 0.741$$

$$\text{Total Prob} = P_1(0) + P_1(1) \times P_2(0)$$

$$= 0.705 + 0.2467 \times 0.791$$

$$P_a = 0.1872$$

3) In a single sampling plan $N=100$ $n=71$ $C=1$

$AQL=0.005$ $LTPD:RAI=0.05$ determine producer risk & consumer risk & draw OC curve.

When $n=71$ $AQL=p'=0.005$ $C=1$ (max 1 or less defective)

P_a

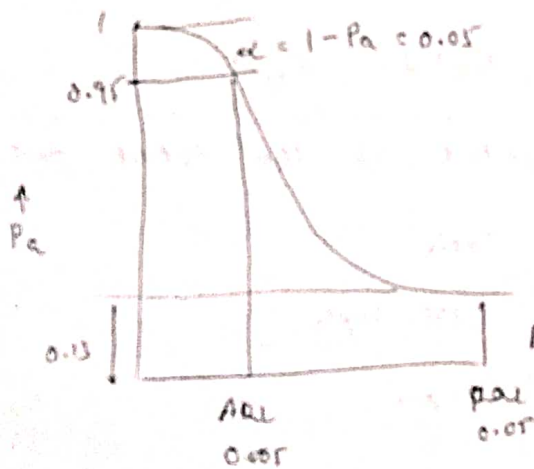
$$np' = 71 \times 0.005 = 0.355$$

$$\text{for } np' = 0.355 \text{ \& } C=1$$

$$\text{from table } P_c = 0.95$$

producer risk $1 - P_a =$

$$1 - 0.95 = 0.05$$



Consumer risk

$$n=71 \quad AQL=p'=0.005$$

$$np' = 71 \times 0.005 = 3.55$$

$$C=1$$

$$P_c = 0.1307 \text{ from table}$$

$$P_a = 13.07\%$$

Consumer risk

$$\text{Final } P_1(1) = 0.736 - 0.368 = \boxed{0.368}$$

$$\text{No of defect} = 4910 \frac{\%}{10} = 49$$

$$\text{no. of non defective} = 4910 - 49 = 4859$$

$$\eta_2 p = 100\% = 1 \quad C_2 = 0$$

$C_2 = 0$ because C_2' given in Q4 combined result from first & 2nd type both

$$\eta_1' = \eta_1 + \eta_2$$

$$P_2(0) = \boxed{0.368}$$

$$\begin{aligned} \text{total probability of acceptance } P_a &= P_1(0) + P_1(1) \times P_2(0) \\ &= 0.368 + 0.368 \times 0.368 \\ &= 0.5038 \end{aligned}$$

$$N = 5000 \quad n = 120 \quad C = 2$$

$$0.0907 \quad \lambda^0$$

P_0'	$100P_0'$	n	nP_0'	P_a
0.10	1	120	1.2	0.87
.12	2	1	2.4	0.86
.13	3	1	3.6	0.30
.14	4	1	4.8	0.14
.15	5	1	6.0	0.06
.16	6	1	7.2	0.015
.17	7	1	8.4	0.010
.18	8	1	9.6	0.003
.19	9	1	10.8	0.001
.1	10	1	12	0.0002

$$n = \frac{1}{p(1-p)} = \frac{1}{0.02(1-0.02)} = \frac{1}{0.0196} \approx 51.02$$

A shipment of 2000 units is inspected if $n=120$ $P_1' = AQL = 0.02$

$$c = 1.3$$

$$P_2' = RQL = 2707 = 0.07$$

Construct OC curve & find out α & β

Selected Values of defectives	np'	P_a
0.01	1.2	0.966
0.02	2.4	0.779
0.3	3.6	0.515
0.4	4.8	0.294
0.5	6.0	0.151
0.6	7.2	0.072
0.7	8.4	0.032
0.8	9.6	0.014

$$np' = 120 \times 0.02 = 1.2$$

To find out α

$$\text{Wkt } AQL = 0.02 \text{ \& } P_a = 0.779$$

$$\therefore \alpha = 1 - P_a$$

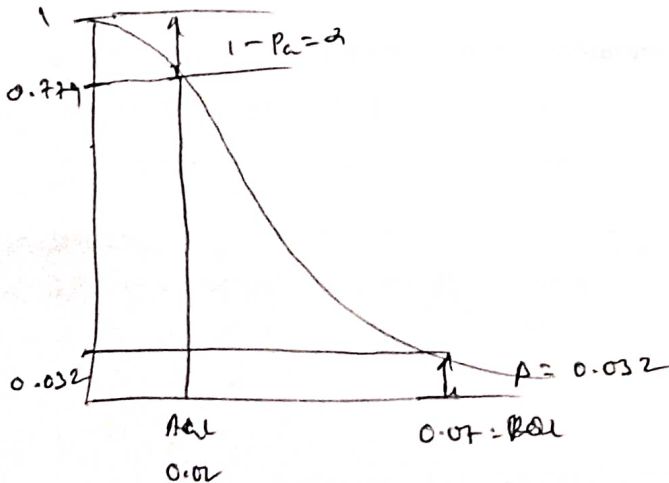
$$= 1 - 0.779$$

$$\boxed{\alpha = 0.221} = 22.1\%$$

To find Curve risk β

$$RQL = 0.07 \text{ \& } P_a = 0.032$$

$$\beta =$$



$$= \frac{100}{100 \times 9.8150} = 1.02$$

$$P_c = M_{10}^2$$