

段母定一生强项音选的担当。 就集不管世事。也有光芒。







The Second Course

List





Lists

- * A <u>list</u> is a finite, ordered sequence of data items called <u>elements</u>.
- Each list element has a data type.
- The <u>empty</u> list contains no elements.
- The <u>length</u> of the list is the number of elements currently stored.
- The beginning of the list is called the <u>head</u>, the end of the list is called the <u>tail</u>.





Lists

- Sorted lists have their elements positioned in ascending order of value
- <u>unsorted lists</u> have no necessary relationship between element values and positions.
- * Notation: $(a_0, a_1, ..., a_{n-1})$



What operations should we implement?





Operations

- <u>Construct</u> the list, leaving it empty
- Determine whether the list is <u>empty</u> or not
- * Determine whether the list is full or not
- Find the <u>size</u> of the list
- Clear the list to make it empty
- Insert an entry at a specified position of the list





Operations

- Remove an entry from a specified position in the list
- * <u>Retrieve</u> the entry from a specified position in the list
- Replace the entry at a specified position in the list
- Traverse the list, performing a given operation on each entry





Position Number in a List

To find an entry in a list, we use an integer that gives its position within the list.

• We shall number the positions in a list so that the first entry in the list has position 0, the second position 1, and so on.

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Position Number in a List

- Locating an entry of a list by its position is superficially like indexing an array, but there are important differences.
- If we <u>insert</u> an entry at a particular position, then the position numbers of all later entries increase by 1.
- If we <u>remove</u> an entry, then the positions of all following entries decrease by 1.





Position Number in a List

- The position number for a list is defined without regard to the implementation.
- For a contiguous list, implemented in an array, the position will indeed be the index of the entry within the array.
- But we will also use the position to find an entry within linked implementations of a list, where no indices or arrays are used at all.





```
class List {
                                         // List class ADT
  public:
    List(int =LIST_SIZE);
                                         // Constructor
    ~List();
                                         // Destructor
    void clear();
                                         // Remove all
    void insert(const Elem);
                                     // Insert Elem at curr
    void append(const Elem);
                                     // Insert Elem at tail
    Elem remove();
                                // Remove and return Elem
    void setFirst();
                                     // Set curr to first pos
```



Lists ADT(1)

```
void prev();
                             // Move curr to prev pos
void next();
                             // Move curr to next pos
int length() const;
                             // Return current length
void setPos(int);
                             // Set curr to position
void setValue(const Elem);// Set current value
Elem currValue() const;
                             // Return current value
bool isEmpty() const;
                             // TRUE if list is empty
bool isInList() const;
                             // TRUE if curr in list
bool find(int);
                              // Find value
```

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- List::List();
 - The List has been created and is initialized to be empty
- void List::clear();
 - All List entries have been removed; the List is empty
- int List::size() const;
 - The function returns the number of entries in the List





- bool List ::empty() const;
 - The function returns true or false according to whether the List is empty or not.
- bool List::full() const;
 - The function returns true or false according to whether the List is full or not





- Error_code List::insert(int position, const List_entry &x);
 - * If the List is not full and 0 ≤ position≤ n, where n is the number of entries in the List, the function succeeds: Any entry formerly at position and all later entries have their position numbers increased by 1, and x is inserted at position in the List

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- Error_code List::remove(int position, List_entry &x);
 - If 0 ≤ position< n, where n is the number of entries in the List, the function succeeds: The entry at position is removed from the List, and all later entries have their position numbers decreased by 1. The parameter x records a copy of the entry formerly at position

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- Error_code List::retrieve(int position, List_entry &x) const;
 - If 0 ≤ position < n, where n is the number of entries in the List, the function succeeds: The entry at position is copied to x; all List entries remain unchanged
 </p>
 - Else: The function fails with a diagnostic error code





- Error_code List::replace(int position, const List_entry &x);
 - If 0 ≤ position < n, where n is the number of entries in the List, the function succeeds: The entry at position is replaced by x; all other entries remain unchanged
 - Else: The function fails with a diagnostic error code





- void List::traverse(void (*visit)(List_entry &));
 - The action specified by function *visit has been performed on every entry of the List, beginning at position 0 and doing each in turn





List ADT Examples

List: (13; 12; 20; 8; 3)

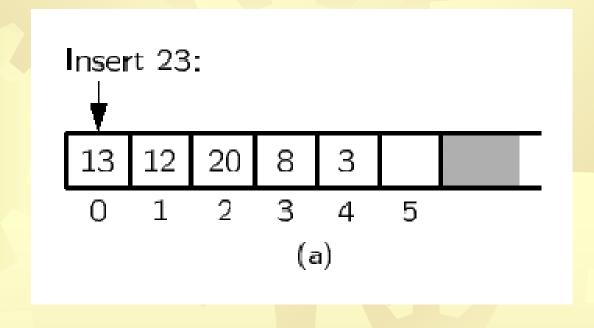
- List: MyList
- MyList.insert(23);
- Assume MyPos has 13 as current element

Put 23 before current element, yielding (23; 13; 12; 20; 8; 3)



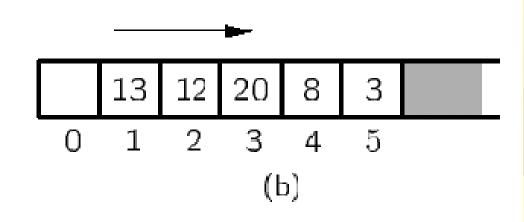


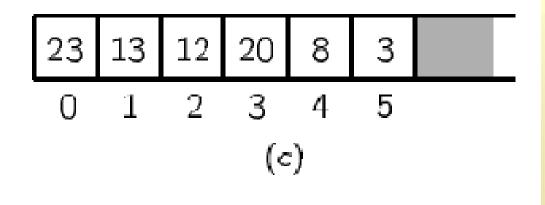
Array-Based List Insert





Array-Based List Insert



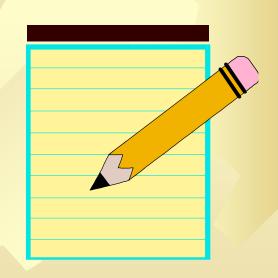






Questions?







- * A C++ template construction allows us to write code, usually code to implement a class, that uses objects of an arbitrary, generic type.
- In template code we utilize a parameter enclosed in angle brackets < >to denote the generic type.
- template <<pre><<pre>template <<pre>< template name>

 { <template body>

 }:





- Later, when a client uses our code, the client can substitute an actual type for the template parameter. The client can thus obtain several actual pieces of code from our template, using different actual types in place of the template parameter.
- <template name><<actual type>>





Example: We shall implement a template class List that depends on one generic type parameter. A client can then use our template to declare several lists with different types of entries with declarations of the following form:

```
template <class List_entry> class List {};
List<int> first_list;
List<char> second_list;
```





- Templates provide a new mechanism for creating generic data structures, one that allows many different specializations of a given data structure template in a single application.
- The added generality that we get by using templates comes at the price of slightly more complicated class specifications and implementations.





Implementation of List

- contiguous implementations using arrays
- linked implementations using pointers
 - Simple linked implementation
 - Doubly linked list
 - * Circular list





Contiguous Memory

* LOC(i) = LOC(i-1) + l = a + i * l,

LOC: Memory Addr, l: size of element

$$LOC(i) = \begin{cases} a, & i = 0 \\ LOC(i-1)+l = a+i*l, & i > 0 \end{cases}$$



```
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```

```
template < class List_entry>
class List {
public:
    methods of the List ADT
  List();
  int size() const;
  bool full() const;
  bool empty() const;
  void clear();
  void traverse(void (*visit)(List_entry &));
  Error_code retrieve(int position, List_entry &x) const;
  Error_code replace(int position, const List_entry &x);
  Error_code remove(int position, List_entry &x);
  Error_code insert(int position, const List_entry &x);
```



Number of entries

```
protected.
// data members for a contiguous list implementation
  int count;
  List_entry entry [max_list];
};
```

Storage



Function Templates

Many of the methods depend on the template parameter, and so must be implemented as templates too.

template <<parameter list>> <function definition>;

Function definition: <return type><function name>(<parameter list>) {<function body>};



List Size

```
template <class List_entry>
int List<List_entry>::size() const

/* Post: The function returns the number of entries in the List. */

{
    return count;
}
```



Insertion

template < class List_entry>

Error_code List<List_entry>::insert(int position, const List_entry &x)

I* Post: If the List is not full and $0 \le position \le n$, where n is the number of entries in the List, the function succeeds: Any entry formerly at position and all later entries have their position numbers increased by 1 and x is inserted at position of the List.

Else: The function fails with a diagnostic error code. */

```
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```

```
if (full())
  return overflow;
if (position < 0 || position > count)
  return range_error;
for (int i = count -1; i >= position; i--)
  entry [i + 1] = entry [i];
entry[position] = x;
count++;
return success;
```

Insert

$$AMN = \frac{1}{n+1} \sum_{i=0}^{n} (n-i) = \frac{1}{n+1} (n+\dots+1+0)$$
$$= \frac{1}{(n+1)} \frac{n(n+1)}{2} = \frac{n}{2}$$

Traversal



Delete

entry

$$AMN = \frac{1}{n} \sum_{i=0}^{n-1} (n-i-1) = \frac{1}{n} \frac{(n-1)n}{2} = \frac{n-1}{2}$$



Performance of Methods

- In processing a contiguous list with n entries:
 - insert and remove operate in time approximately proportional to n.
 - List, clear, empty, full, size, replace, and retrieve operate in constant time.







Simple linked implementation

Node declaration:

```
template <class Node_entry>
struct Node {
// data members
   Node_entry entry;
   Node<Node_entry> *next;
// constructors
   Node();
   Node(Node_entry, Node<Node_entry> *link = NULL);
};
```

entry

next

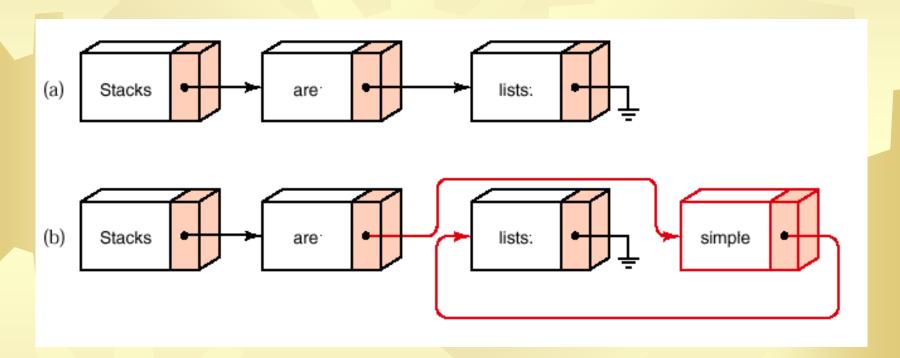




List declaration:

```
template < class List_entry>
class List {
public:
    Specifications for the methods of the list ADT go here.
II
    The following methods replace compiler-generated defaults.
   \simList();
  List(const List<List_entry> &copy);
  void operator = (const List<List_entry> &copy);
protected:
    Data members for the linked list implementation now follow.
  int count;
  Node<List_entry> *head;
    The following auxiliary function is used to locate list positions
  Node<List_entry> *set_position(int position) const;
};
```

Actions on a Linked List

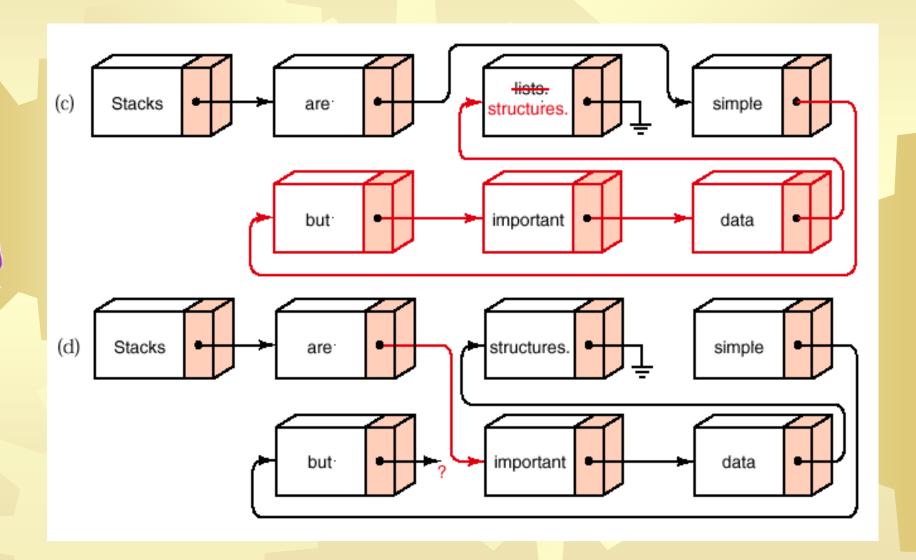


first
$$a_1$$
 a_2 a_3 a_4 a_5



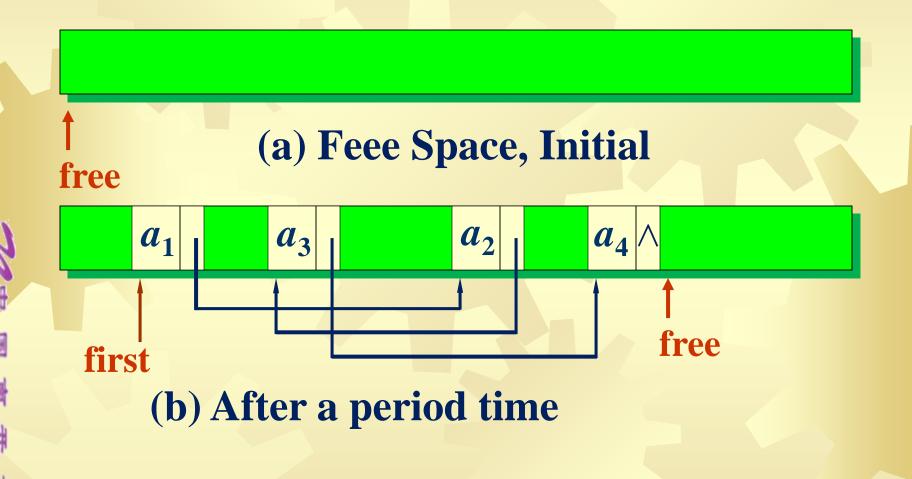


Actions on a Linked List



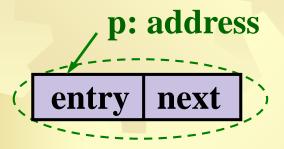


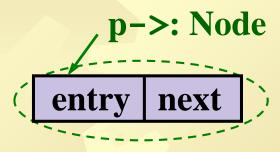
Memory Map

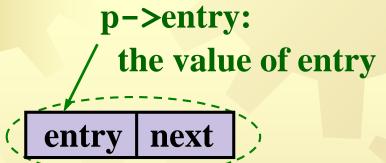


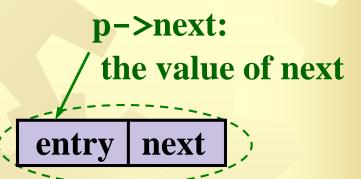


Pointer











Finding a List Position

- * Function set_position takes an integer parameter position and returns a pointer to the corresponding node of the list.
- Declare the visibility of set_position as protected, since set_position returns a pointer to, and therefore gives access to, a Node in the List.



Finding a List Position

- * To construct set_position, we start at the beginning of the List and traverse it until we reach the desired node.
- If all nodes are equally likely, then, on average, the set position function must move halfway through the List to find a given position.
- On average, its time requirement is approximately proportional to n, the size of the List.



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Implementation of set_position

```
template < class List_entry>
Node<List_entry> *List<List_entry>::set_position(int position) const
I* Pre: position is a valid position in the List; 0 \le position < count.
  Post: Returns a pointer to the Node in position. */
  Node<List_entry> *q = head;
  for (int i = 0; i < position; i++) q = q->next;
  return q;
```



Questions

- Why declare the visibility of set_position as protected?
- If we need a methof of getPosition(anEntry), how to do?
 - Task: Gets the position of the first or only occurrence of anEntry.
 - Input: anEntry is the object to be found.
 - Output: Returns the position of anEntry if it occurs in the list.
 Otherwise, returns the position where anEntry would occur in the list, but as a negative integer.
 - If a list L is a empty list, call L.getPosition(anEntry), what is the return value?
- How about to sorted list?
 - replace method?





Insertion

template < class List_entry>

Error_code List<List_entry>::insert(int position, const List_entry &x)

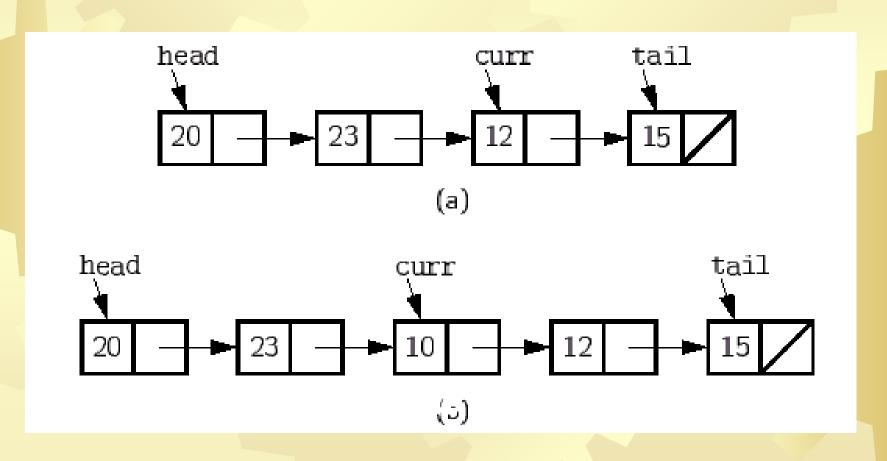
I* **Post:** If the List is not full and $0 \le \text{position} \le n$, where n is the number of entries in the List, the function succeeds: Any entry formerly at position and all later entries have their position numbers increased by 1 and x is inserted at position of the List.

Else: The function fails with a diagnostic error code. */

```
{
 if (position < 0 || position > count)
    return range_error;
 Node<List_entry> *new_node, *previous, *following;
 if (position > 0) {
    previous = set_position(position - 1);
    following = previous->next;
 else following = head;
 new_node = new Node<List_entry>(x, following);
 if (new_node == NULL)
    return overflow;
 if (position == 0)
    head = new_node;
 else
    previous->next = new_node;
 count++;
 return success;
```

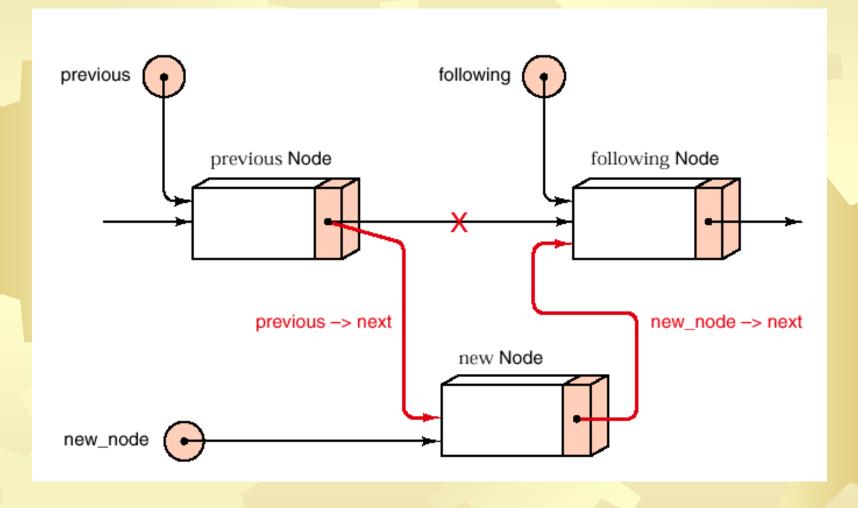


Example of Insert



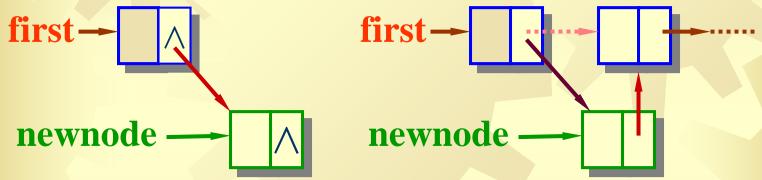


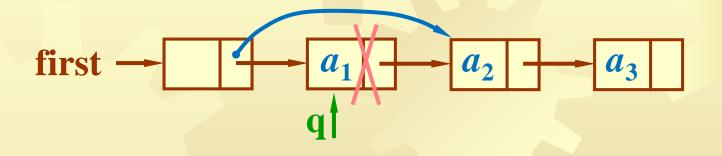
Insertion into a Linked List











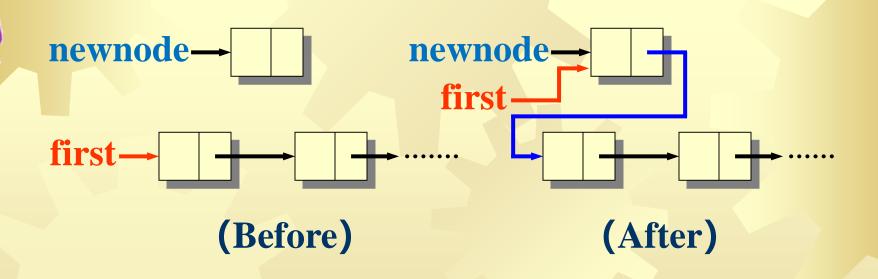


Insertion

* Before the first node:

```
newnode->next = first;
```

first = newnode; //change the head pointer

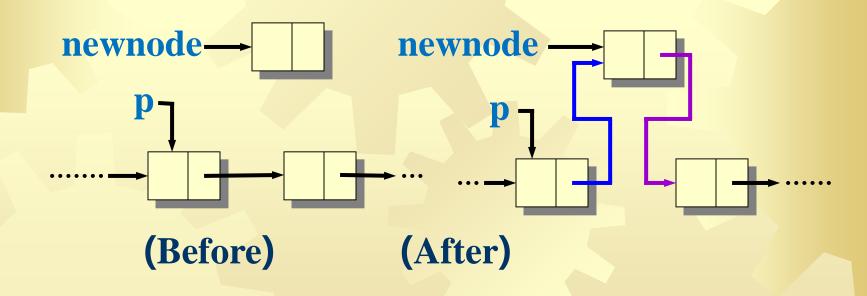




Insertion

Middle in the list:

```
newnode->next = p->next;
p->next = newnode;
```

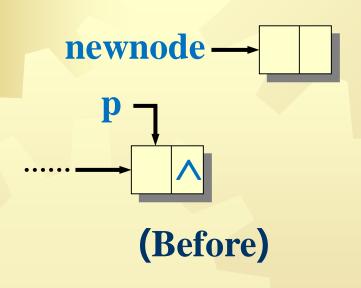


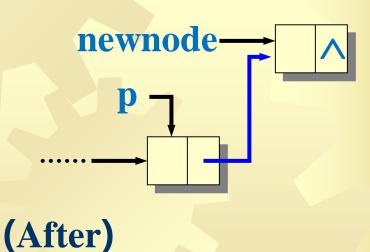




After the last node:

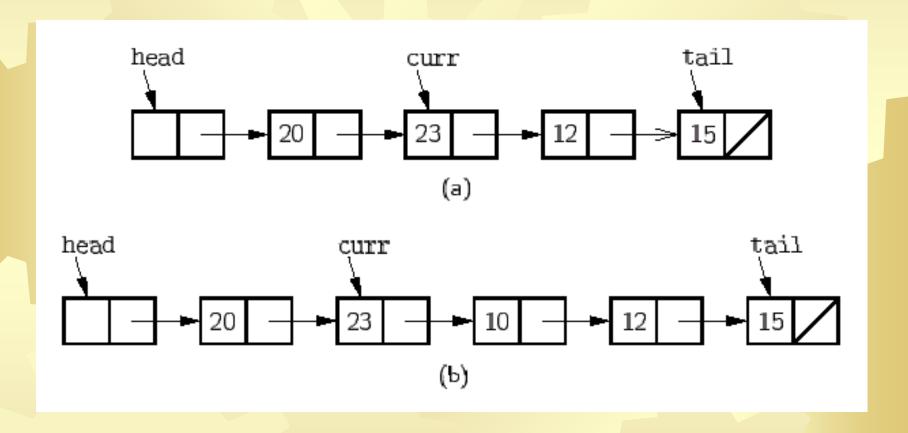
newnode->next = p->next;
p->next = newnode;

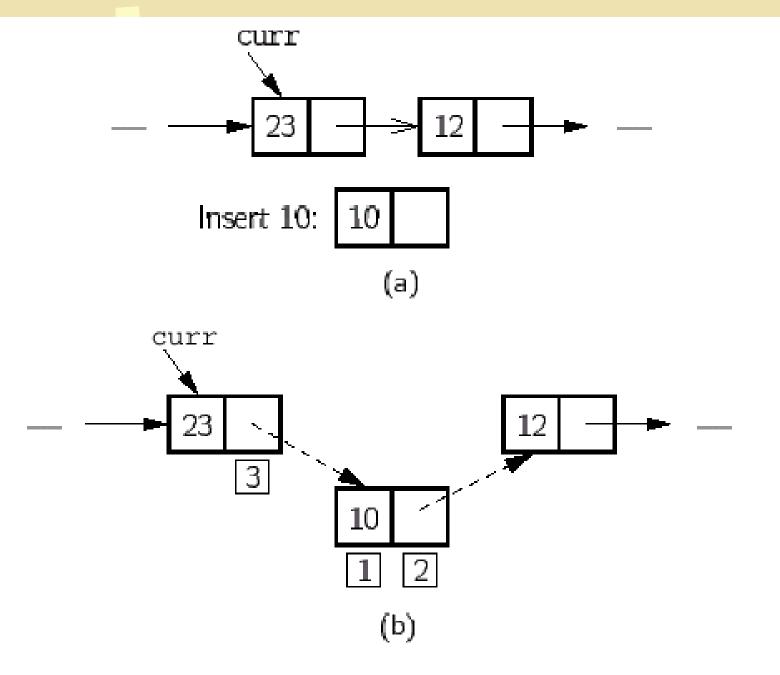






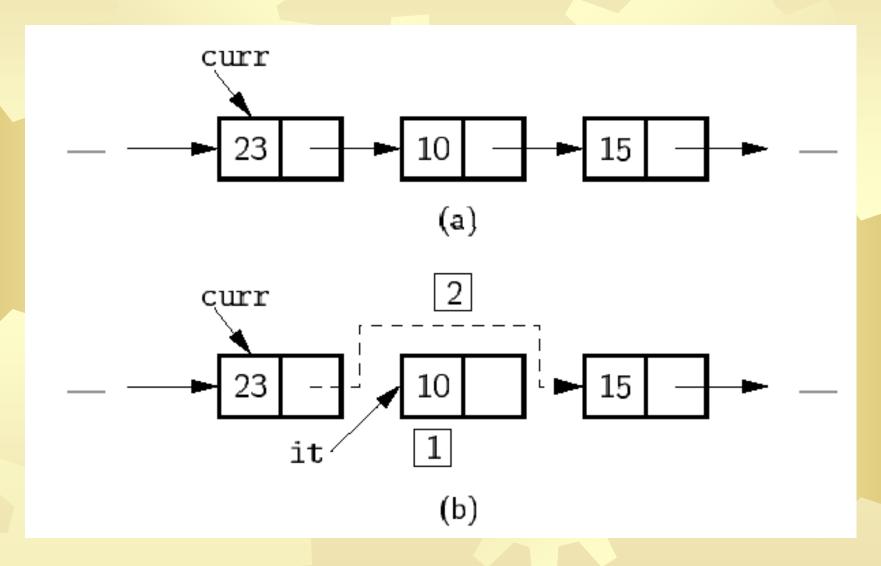
Example of Insert







Example of Remove







Performance of Methods

- In processing a linked List with n entries
 - * clear, insert, remove, retrieve, and replace require time approximately proportional to n.
 - List, empty, full, and size operate in constant time.





The cost

The cost of a list is the extra space required in each Node for a link

- E: Space for data value
- P: Space for pointer
- D: Number of elements in array
- n: Count of List





Keeping the Current Position

- Suppose an application processes list entries in order or refers to the same entry several times before processing another entry.
- Remember the last-used position in the list and, if the next operation refers to the same or a later position, start tracing through the list from this last-used position.

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```
template < class List_entry>
    class List {
     public:
    Add specifications for the methods of the list ADT.
    Add methods to replace the compiler-generated defaults.
protected:
    Data members for the linked-list implementation with
    current position follow:
  int count:
  mutable int current_position;
  Node<List_entry> *head;
  mutable Node<List_entry> *current;
    Auxiliary function to locate list positions follows:
  void set_position(int position) const;
};
```

* The current_position is now a member of the class List, so there is no longer a need for set position to return a pointer; instead, the function simply resets the pointer current directly within the List.

Implementation of set_position

```
template < class List_entry>
void List<List_entry>::set_position(int position) const
/* Pre: position is a valid position in the List: 0 \le position < count.
  Post: The current Node pointer references the Node at position. */
  if (position < current_position) { // must start over at head of list
    current_position = 0;
    current = head;
  for (; current_position != position; current_position++)
    current = current->next;
```



Performance of Methods

For repeated references to the same position, neither the body of the if statement nor the body of the for statement will be executed, and hence the function will take almost no time.





Performance of Methods

- If we move forward only one position, the body of the for statement will be executed only once, so again the function will be very fast.
- If it is necessary to move backwards through the List, then the function operates in almost the same way as the version of set position used in the previous implementation.

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Questions

- LList is the type of a list, SortedList is the type of sorted list, then SortedList and LList have a has-a relationship.
- as follows:
 - public class SortedList<T extends Comparable<? super T>> extends LList<T> implements SortedListInterface<T>
 - Is OK?
 - This implementation contains a pitfall that is the direct result of using inheritance.
 - SortedList inherits two methods that a client can use to destroy the order of a sorted list, add and replace.



Possible ways to avoid the pitfall

- Implement the list's add and replace methods within the class SortedList and have them throw an exception when invoked.
- For example, add could appear as follows:

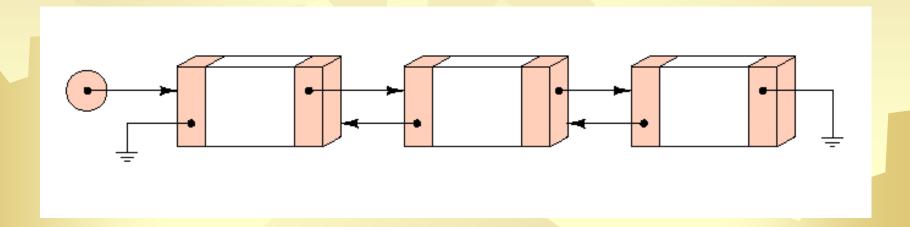
```
public void add(int newPosition, T newEntry) {
   throw new UnsupportedOperationException(
        "Illegal attempt to add " +
        "at a specified position within a sorted list.");
   } // end add
```

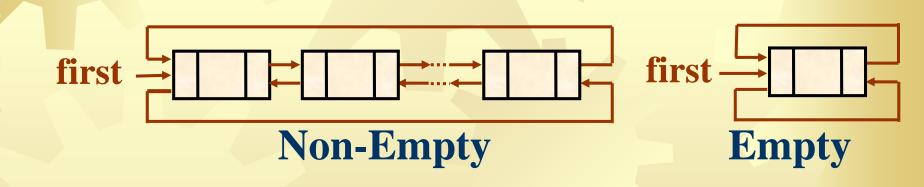
* This version of add also overrides the version that LList implements. If the client invokes this method, an exception occurs. This approach is a common practice, and it is the one we prefer.





Doubly Linked Lists







Node definition

To Precursor \leftarrow

```
template < class Node_entry>
struct Node {
   data members
  Node_entry entry;
  Node<Node_entry> *next;
  Node<Node_entry> *back;
   constructors
  Node();
  Node(Node_entry, Node<Node_entry> *link_back = NULL,
                    Node<Node_entry> *link_next = NULL);
};
             back
                       entry
                                 next
```

→ to Subsequent



List definition

```
template < class List_entry>
class List {
public:
    Add specifications for methods of the list ADT.
    Add methods to replace compiler generated defaults.
protected:
    Data members for the doubly-linked list implementation follow:
  int count;
  mutable int current_position;
  mutable Node<List_entry> *current;
11
     The auxiliary function to locate list positions follows:
  void set_position(int position) const;
};
```

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Doubly Linked Lists

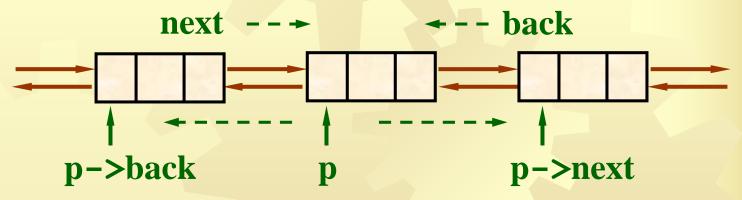
- * We can move either direction through the List while keeping only one pointer, current, into the List.
- We do not need pointers to the head or the tail of the List, since they can be found by tracing back or forth from any given node.

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Doubly Linked Lists

To find any position in the doubly linked list, we first decide whether to move forward or backward from the current position, and then we do a partial traversal of the list until we reach the desired position.



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Implementation of set_position

```
template <class List_entry>
void List<List_entry>::set_position(int position) const
        position is a valid position in the List: 0 \le position < count.
  Post: The current Node pointer references the Node at position. */
  if (current_position <= position)</pre>
    for ( ; current_position != position; current_position++)
       current = current->next;
  else
    for ( ; current_position != position; current_position --)
       current = current->back;
```

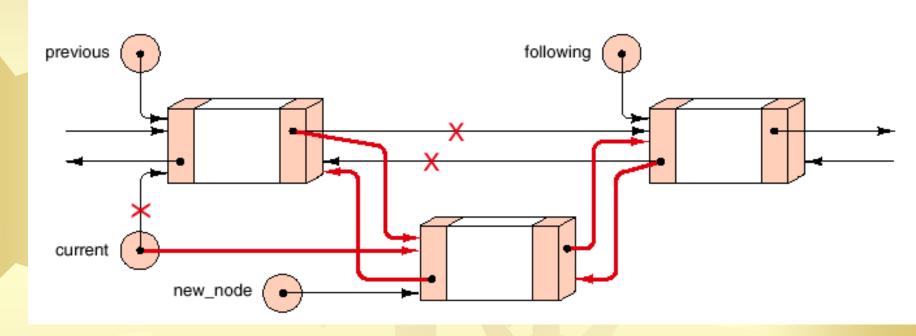


The cost

The cost of a doubly linked list is the extra space required in each Node for a second link, usually trivial in comparison to the space for the information member entry.



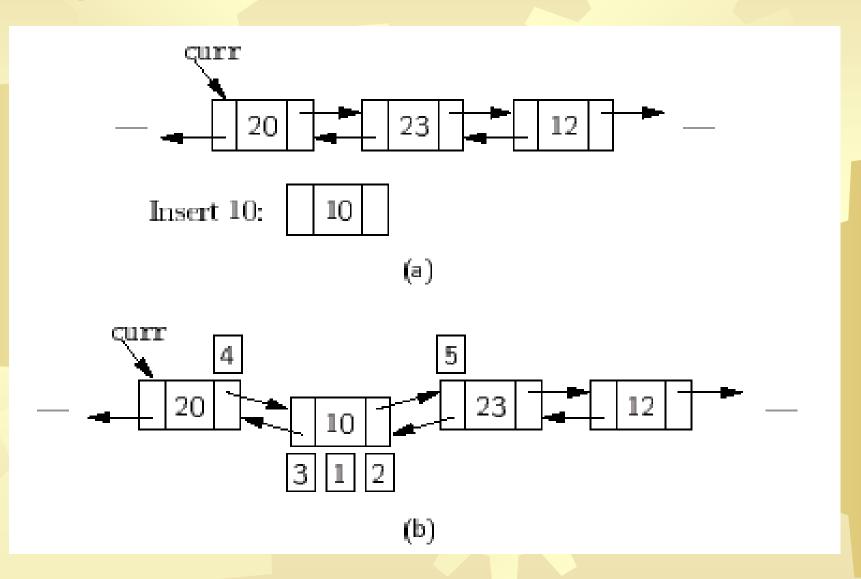








Steps of Insert



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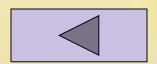
```
template < class List_entry>
Error_code List<List_entry>::insert(int position, const List_entry &x)
/* Post: If the List is not full and 0 \le position \le n, where n is the number of
         entries in the List, the function succeeds: Any entry formerly at position and
         all later entries have their position numbers increased by 1 and x is inserted at
         position of the List.
         Else: the function fails with a diagnostic error code. */
  Node<List_entry> *new_node, *following, *preceding;
  if (position < 0 || position > count) return range_error;
```



```
if (position == 0) {
  if (count == 0) following = NULL;
  else {
    set_position(0);
    following = current;
  preceding = NULL;
else {
  set_position(position - 1);
  preceding = current;
  following = preceding->next;
new_node = new Node<List_entry>(x, preceding, following);
```

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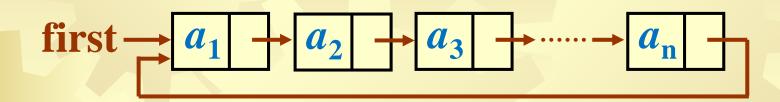
```
if (new_node == NULL) return overflow;
if (preceding != NULL) preceding->next = new_node;
if (following != NULL) following->back = new_node;
current = new_node;
current_position = position;
count++;
return success;
}
```

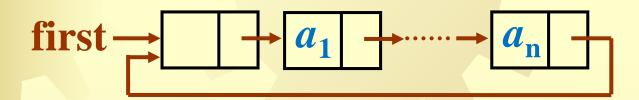






Circular List





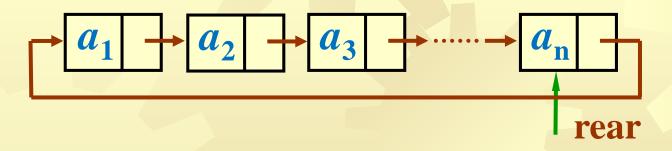






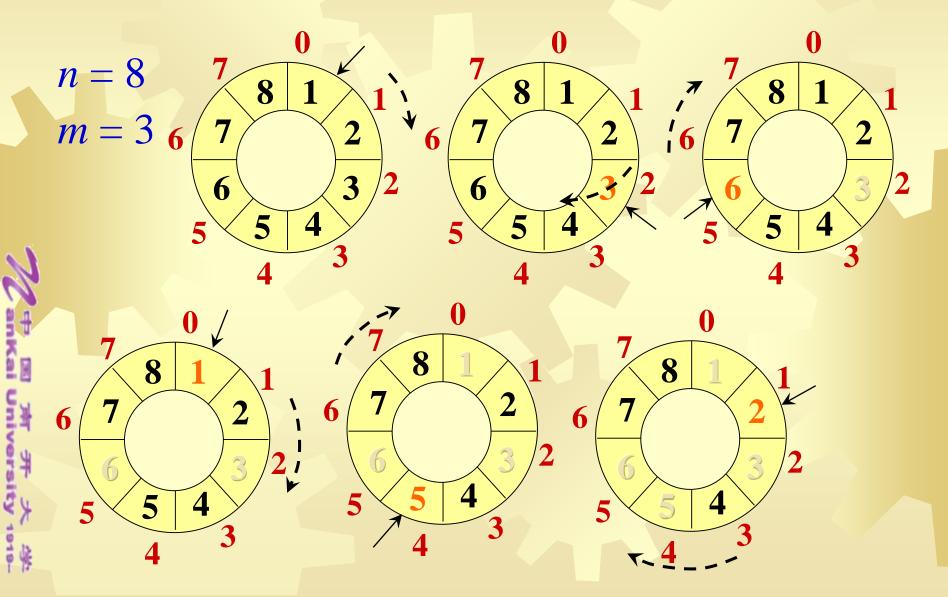
- ** Is-Empty: first->next == first。
- For every node:

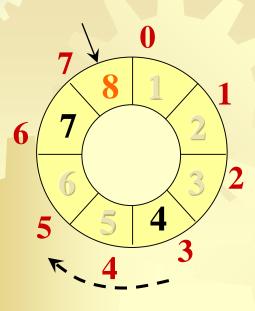
- * No node has a NULL in its next field.
- With a tail pointer:

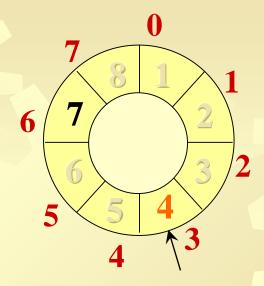


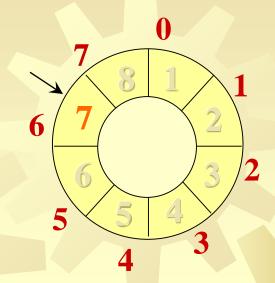


Josephus













Comparison of Implementations

- Contiguous storage is generally preferable
 - when the entries are individually very small;
 - when the size of the list is known when the program is written;
 - * when few insertions or deletions need to be made except at the end of the list; and
 - * when random access is important.





Comparison of Implementations

- Linked storage proves superior
 - when the entries are large;
 - * when the size of the list is not known in advance; and
 - * when flexibility is needed in inserting, deleting, and rearranging the entries.





How to choose

- Which of the operations will actually be performed on the list and which of these are the most important?
- Is there locality of reference? That is, if one entry is accessed, is it likely that it will next be accessed again?

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How to choose

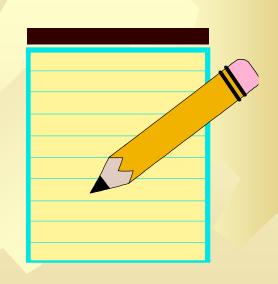
- Are the entries processed in sequential order? If so, then it may be worthwhile to maintain the last-used position as part of the list structure.
- Is it necessary to move both directions through the list? If so, then doubly linked lists may prove advantageous.

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Questions?







Linked Lists in Arrays

- Applications where linked lists in arrays may prove preferable are those where
 - * the number of entries in a list is known in advance,
 - * the links are frequently rearranged, but relatively few additions or deletions are made, or
 - * the same data are sometimes best treated as a linked list and other times as a contiguous list.



$$first \rightarrow 25 \rightarrow 49 \rightarrow 92 \rightarrow 57 \rightarrow 11 \rightarrow 36 \rightarrow 78 \land$$

data -1 next

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CS

プロ オ チ 大 は anKai University 191	0	Clark, F.	70	50
	1	Smith, A.	75	92
	2			
	3	Garcia, T.	83	90
	4	Hall, W.	50	55
	5	Evans, B.	92	85
	6			
	7			
	8	Arthur, E.	40	60
	9			
± d≥				

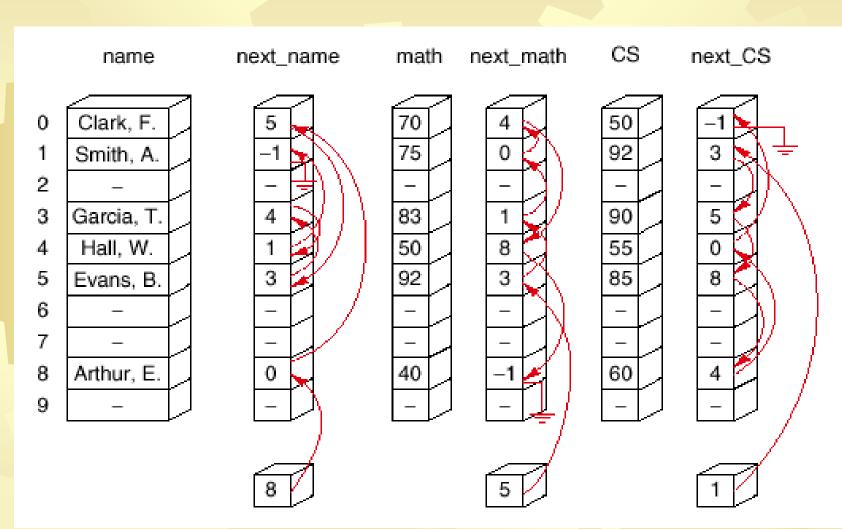
name

math



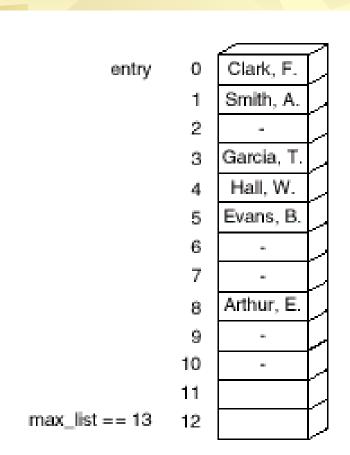


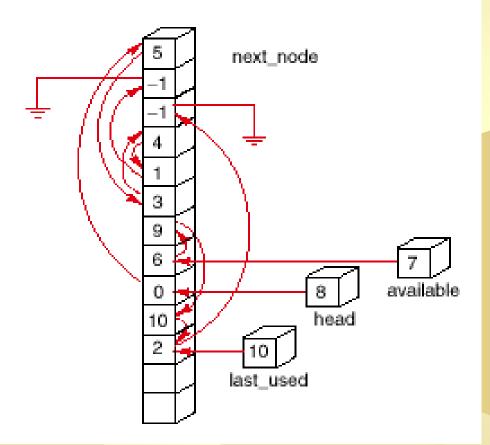
Linked Lists in Arrays





Linked Lists in Arrays







Class Declaration

```
template < class List_entry>
class Node {
public:
   List_entry entry;
   index next;
};
```





Class Declaration

```
template < class List_entry>
class List {
public:
    Methods of the list ADT
  List();
  int size() const;
  bool full() const;
  bool empty() const;
  void clear();
  void traverse(void (*visit)(List_entry &));
  Error_code retrieve(int position, List_entry &x) const;
  Error_code replace(int position, const List_entry &x);
  Error_code remove(int position, List_entry &x);
  Error_code insert(int position, const List_entry &x);
```





Class Declaration

```
protected:
    Data members
  Node<List_entry> workspace [max_list];
  index available, last_used, head;
  int count;
    Auxiliary member functions
  index new_node();
  void delete_node(index n);
  int current_position(index n) const;
  index set_position(int position) const;
};
```





New

```
template < class List_entry>
index List<List_entry>::new_node()
/* Post: The index of the first available Node in workspace is returned; the data
        members available, last_used, and workspace are updated as necessary.
        If the workspace is already full, -1 is returned. */
  index new_index;
  if (available !=-1) {
    new_index = available;
    available = workspace[available].next;
  } else if (last_used < max_list — 1) {</pre>
    new\_index = ++last\_used;
  } else return — 1;
  workspace [new_index].next = -1;
  return new_index;
```

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Delete

```
template < class List_entry>
void List<List_entry>::delete_node(index old_index)
/* Pre: The List has a Node stored at index old_index.
  Post: The List index old_index is pushed onto the linked stack of available space;
        available, last_used, and workspace are updated as necessary. */
  index previous;
  if (old_index == head) head = workspace[old_index].next;
  else {
    previous = set_position(current_position(old_index) - 1);
    workspace[previous].next = workspace[old_index].next;
  workspace[old_index].next = available;
  available = old_index;
```

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Other Operations

- index List<List entry> ::set_position(int position) const;
- int List<List entry> ::current_position(index n) const;
- void List<List entry> ::traverse(void (*visit)(List entry &))
- Error_code List<List entry> ::insert(int position, const List entry &x)





FreeList

System new and delete are slow

