

狀況報告： MURON

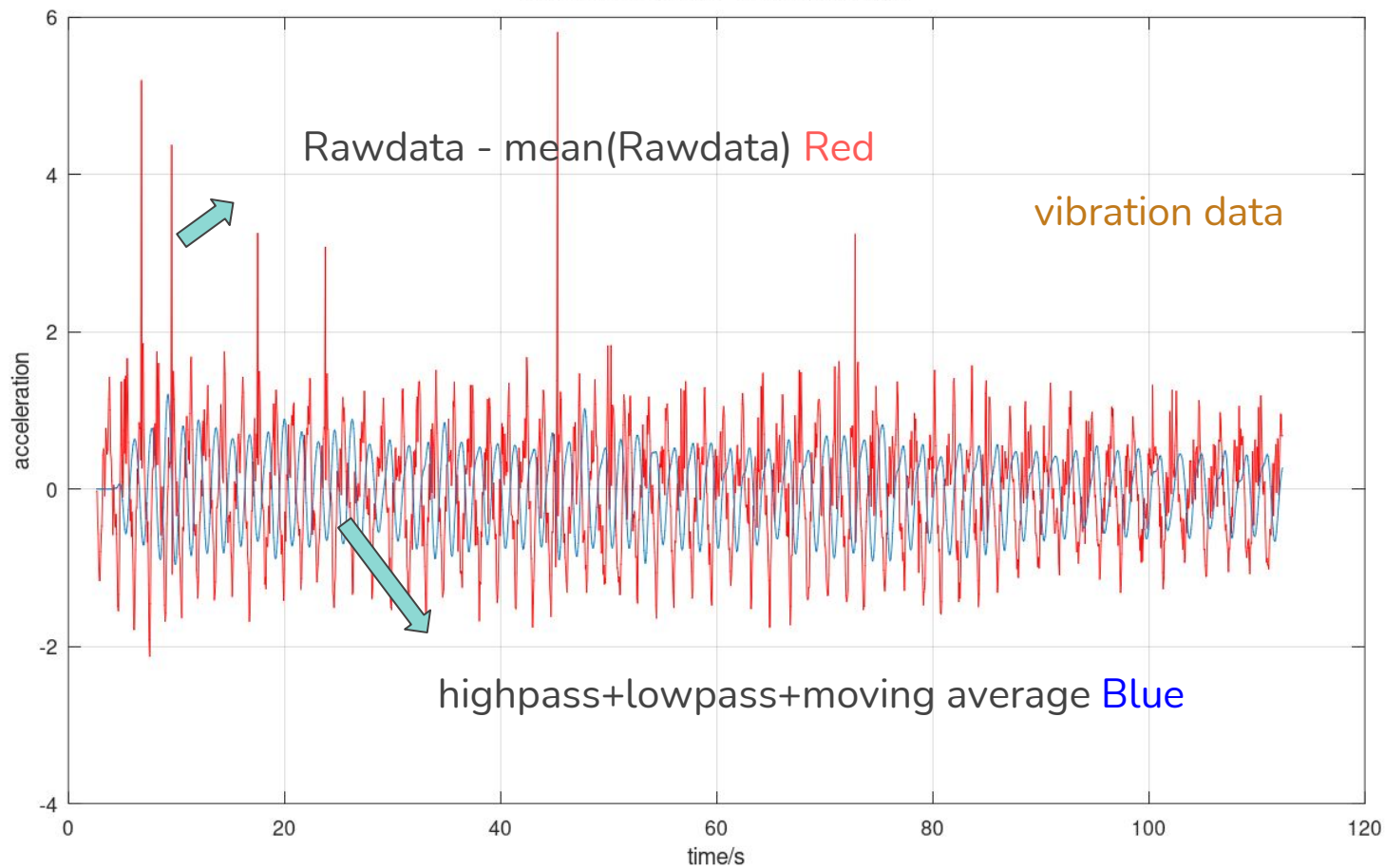
Xuanda Feng • 2021 年 9 月 10 日



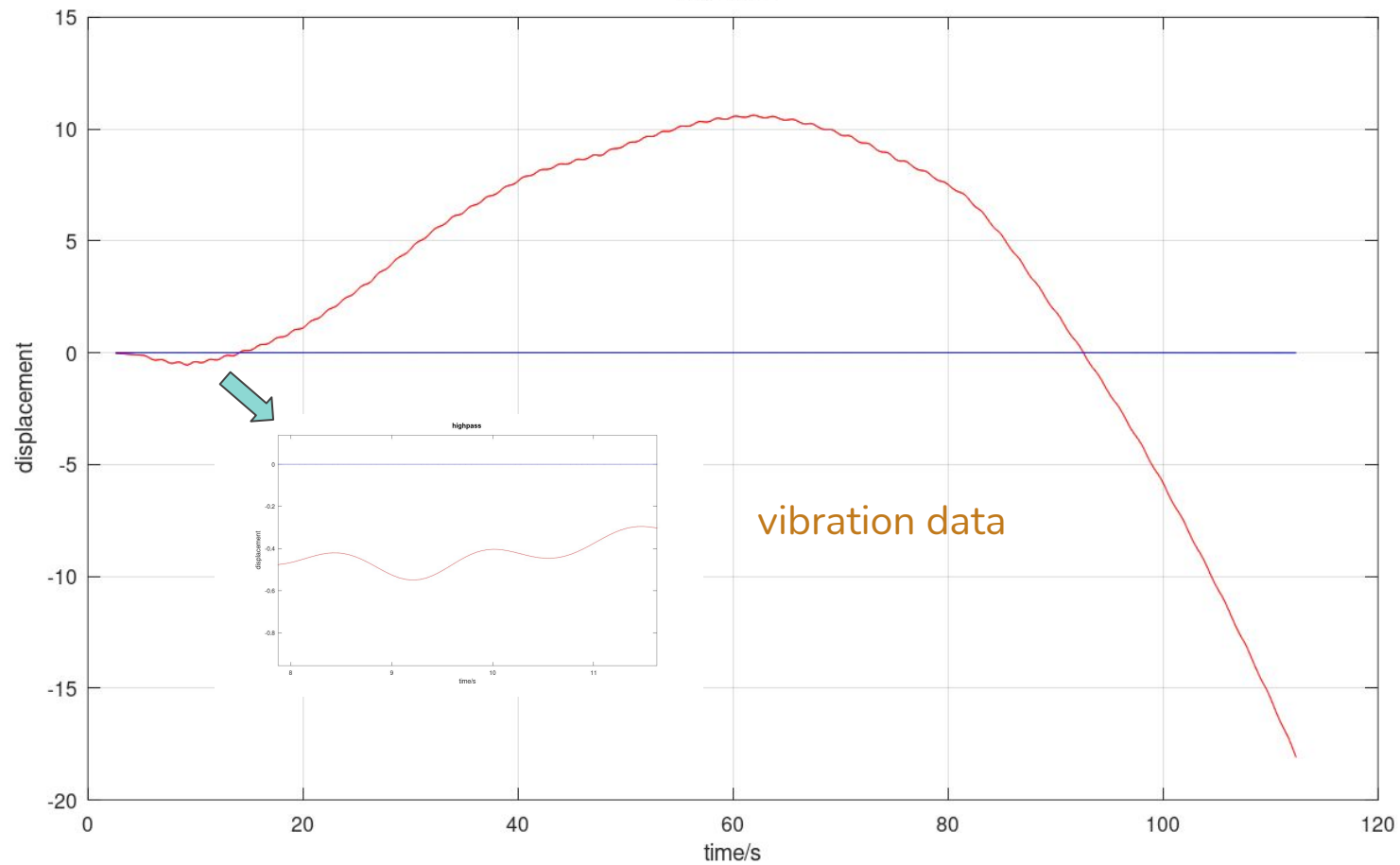


Highpass Filter

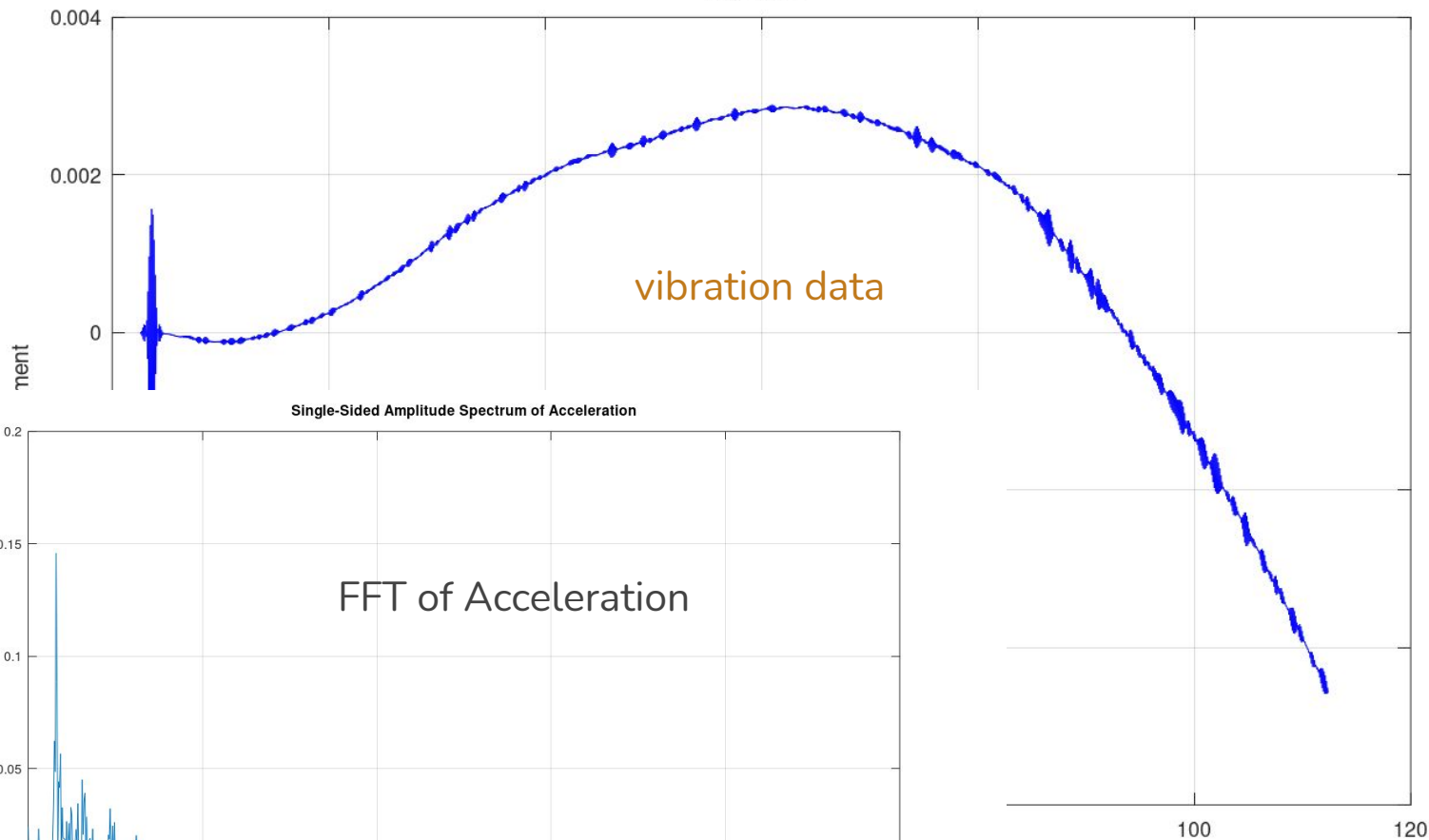
highpass-lowpass-moving average



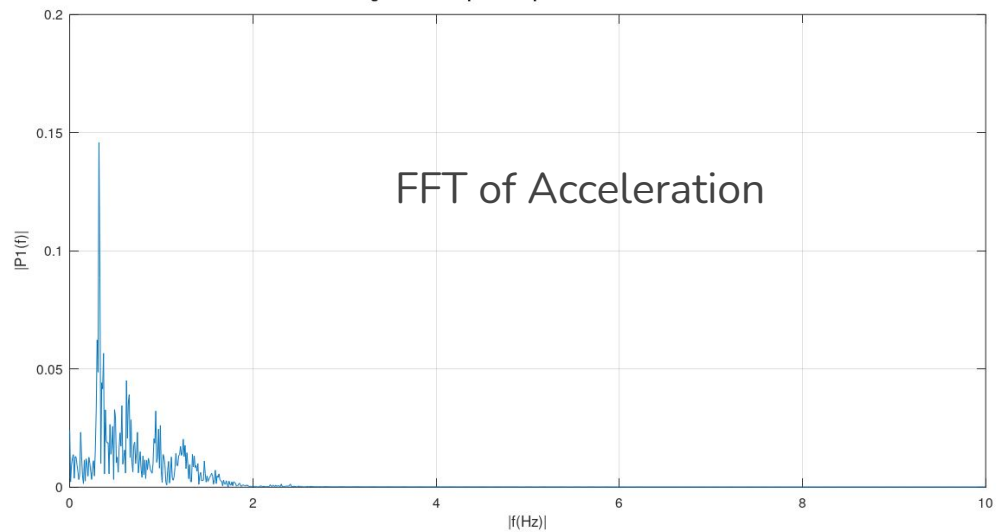
highpass



highpass



Single-Sided Amplitude Spectrum of Acceleration

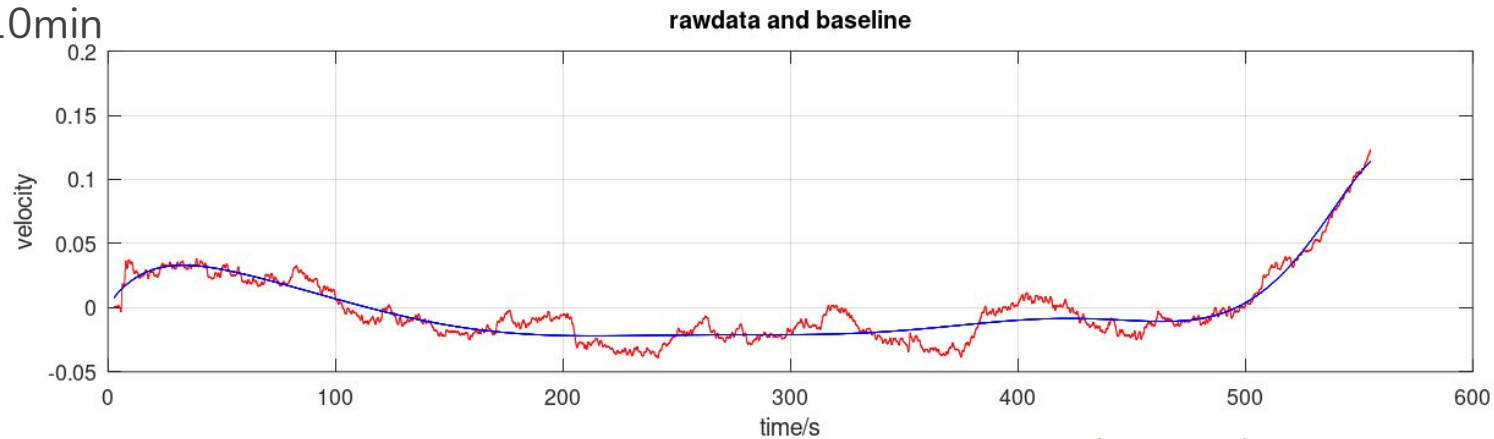




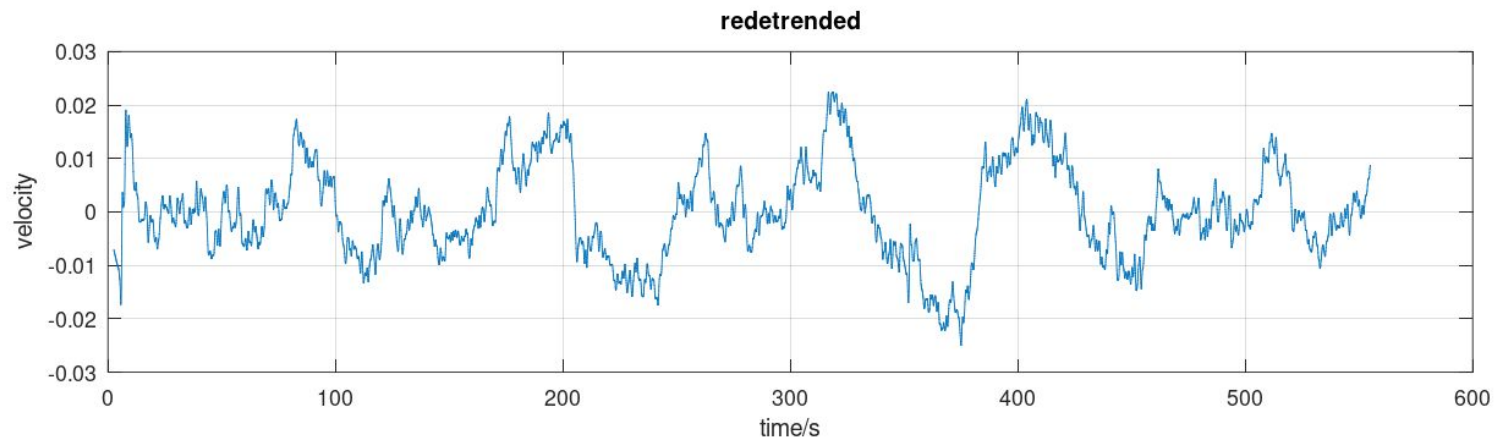
Polynomial Fitting

Number of orders: 5

Time: 10min



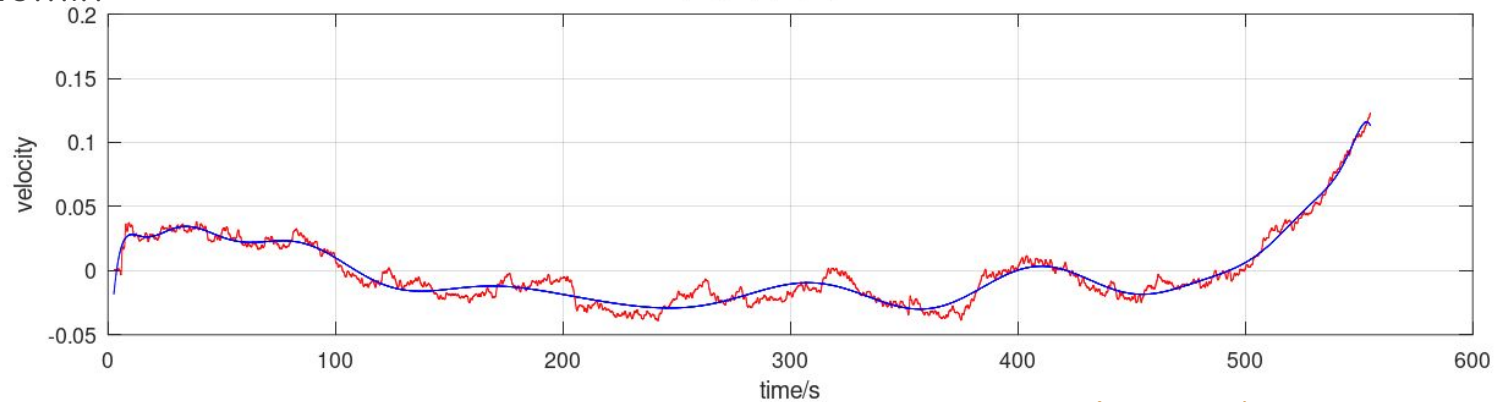
stationary data



Number of orders: 10

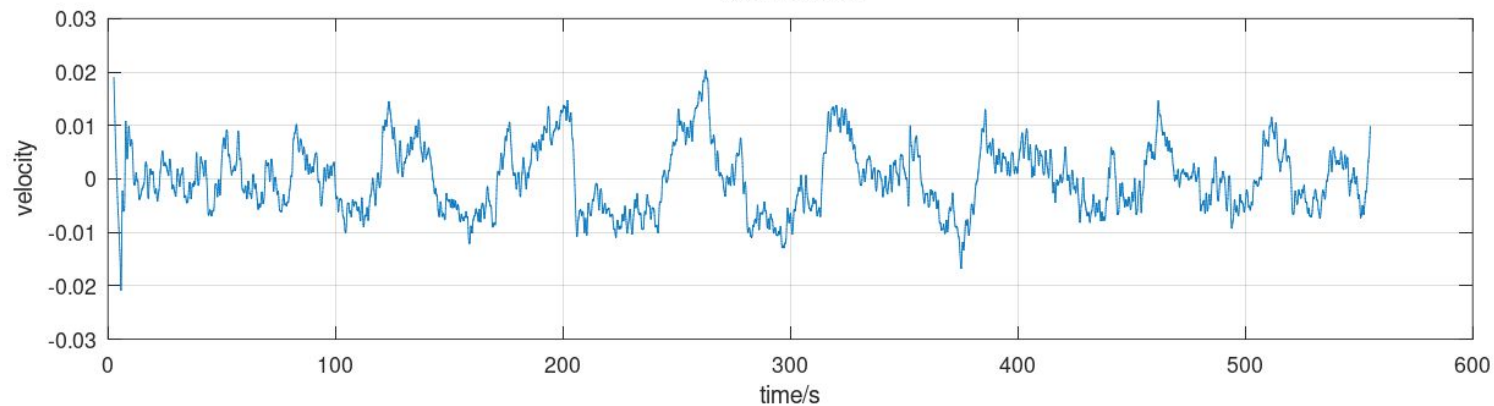
Time: 10min

rawdata and baseline



stationary data

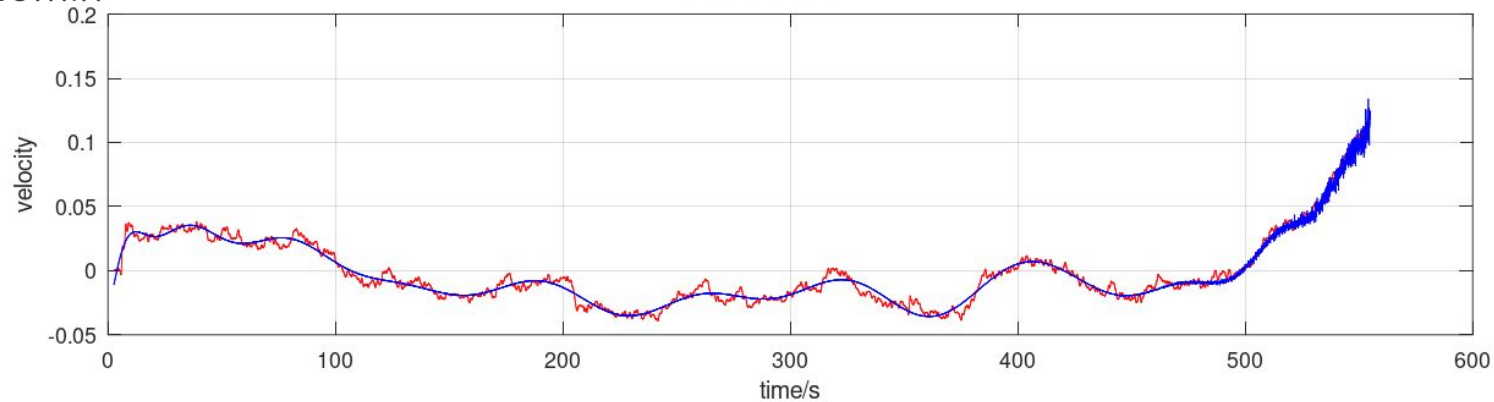
redetrended



Number of orders: 20

Time: 10min

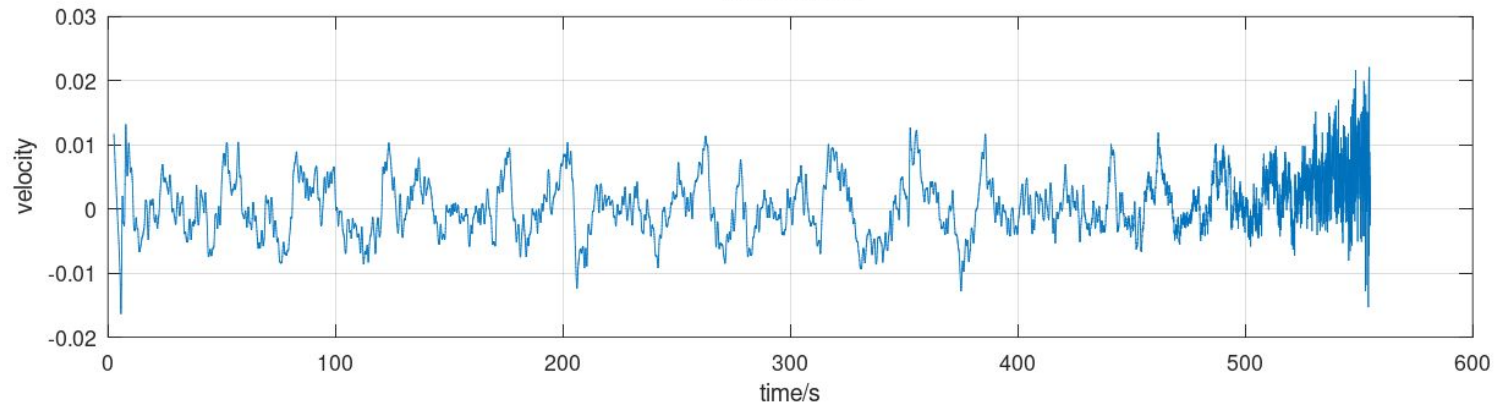
rawdata and baseline



stationary data

Overfitting

redetrended



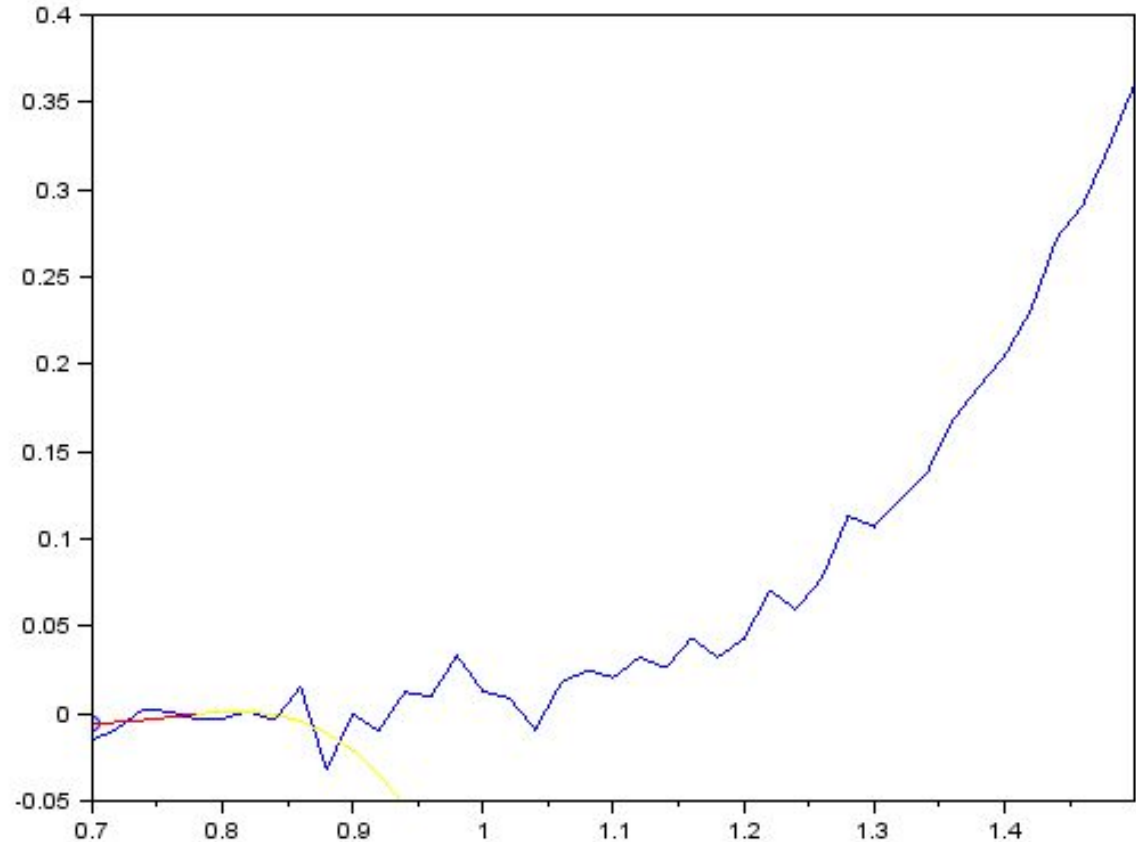
Savitzky-Golay Filter

Moving Average + Polynomial Fitting (Least Square Method)

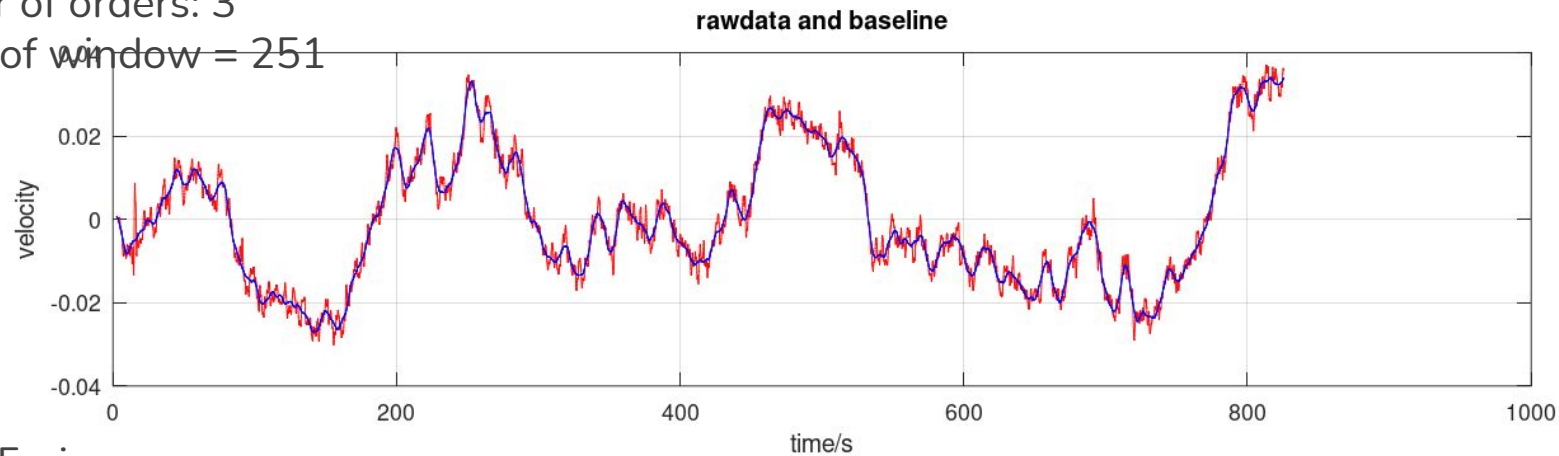


Tunable parameter:

1. length of fitting(**red**)
2. number of orders of polynomial(**red** + **yellow**)

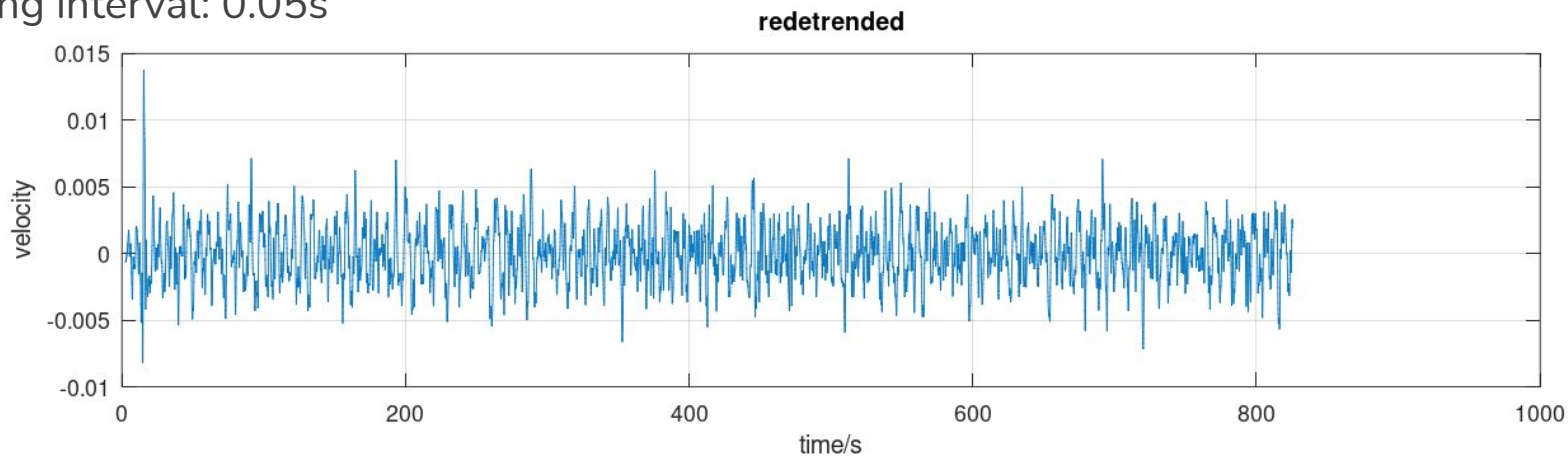


Number of orders: 3
Length of window = 251



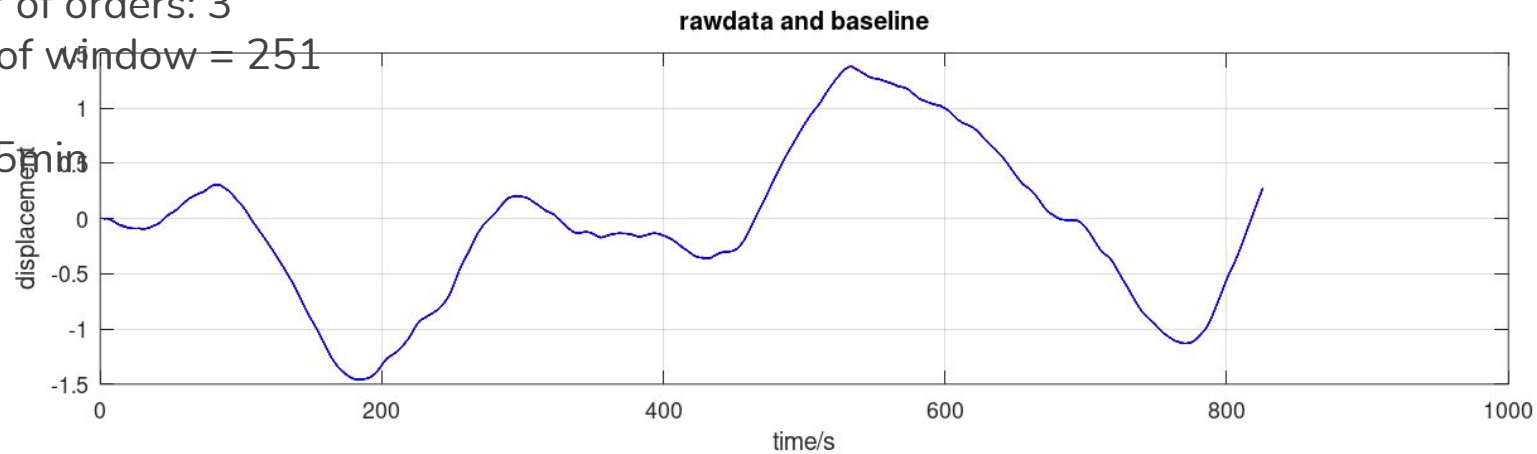
Time: 15min
Sampling interval: 0.05s

stationary data

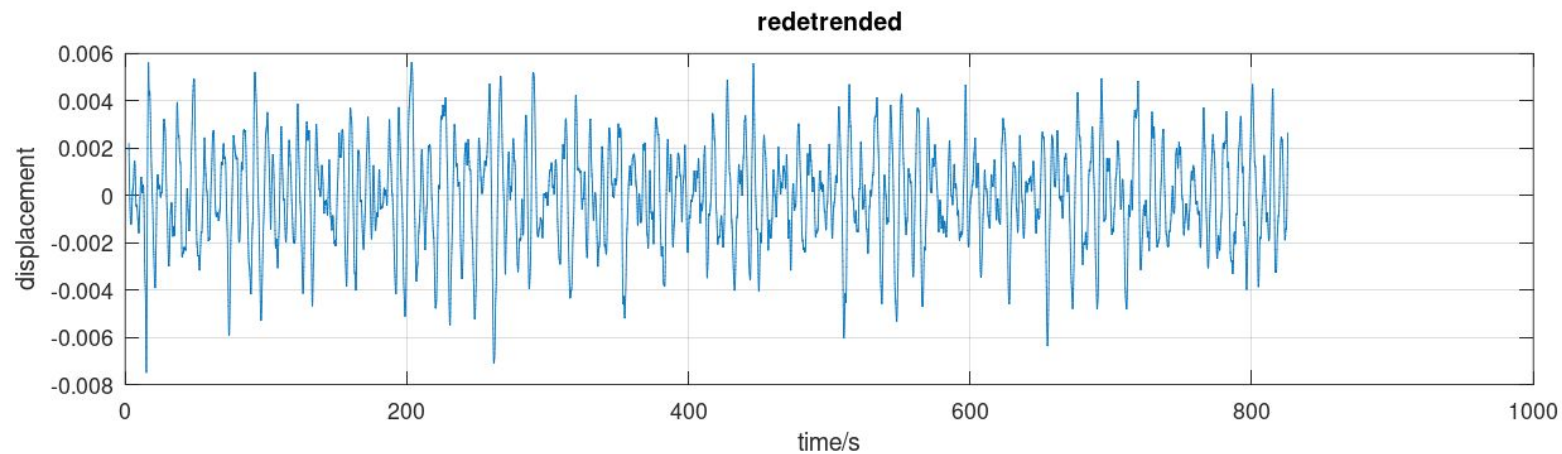


Number of orders: 3
Length of window = 251

Time: 15 min

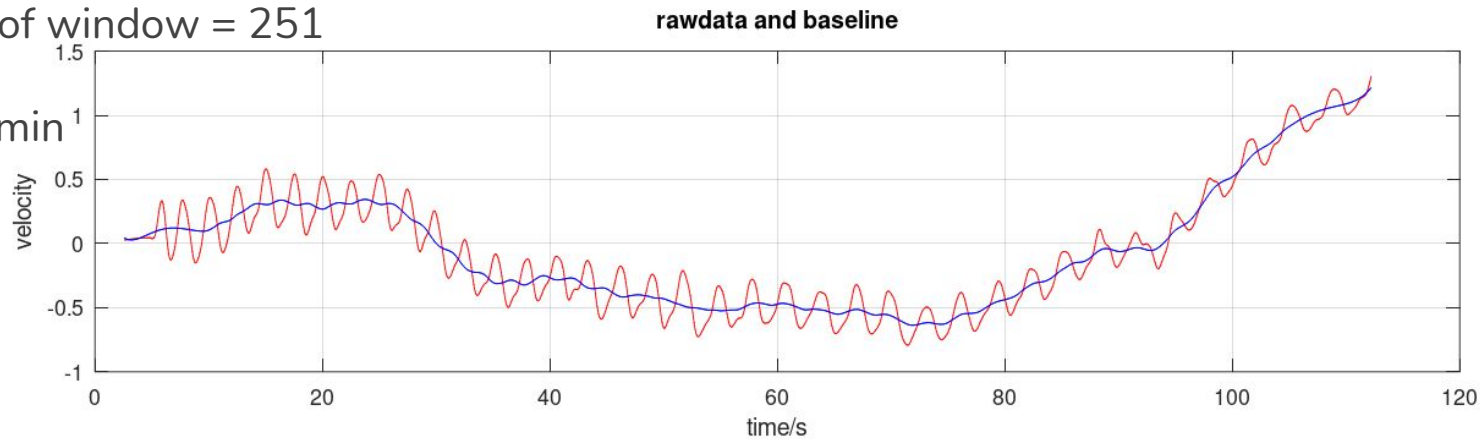


stationary data

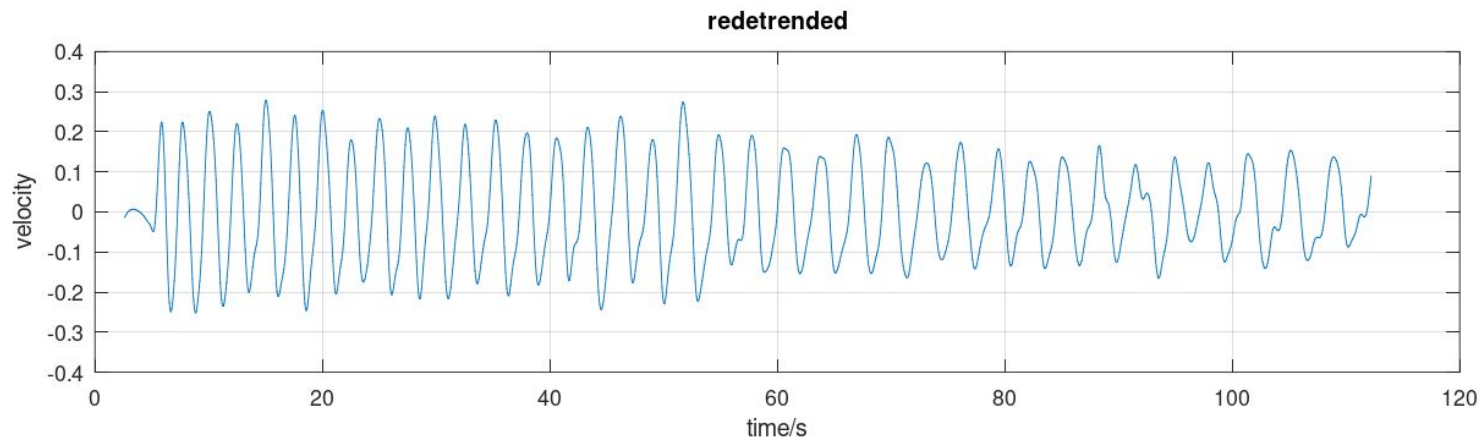


Number of orders: 2
Length of window = 251

Time: 2min

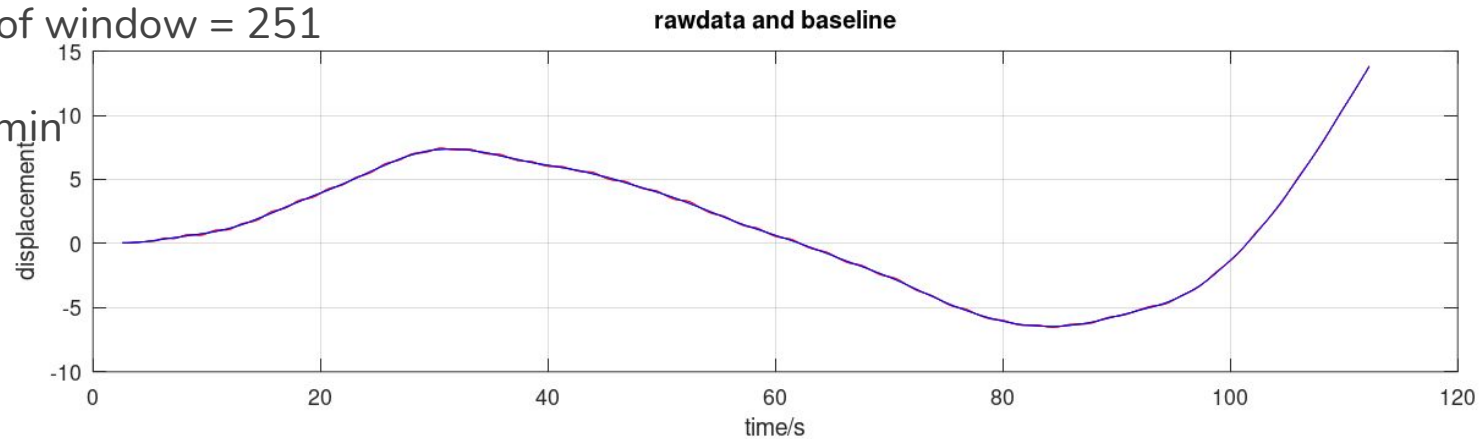


vibration data

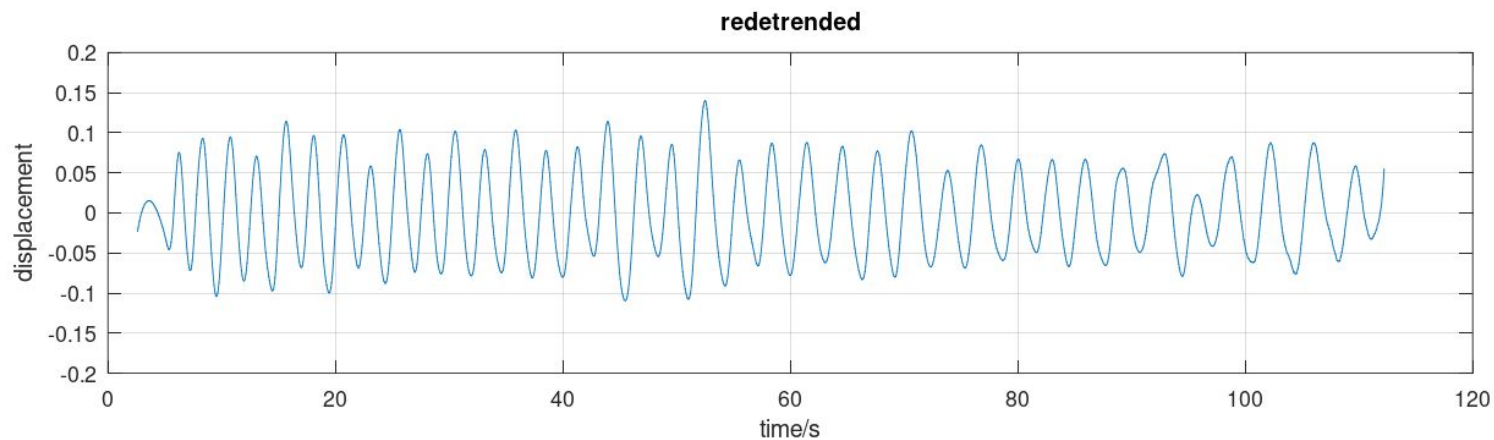


Number of orders: 2
Length of window = 251

Time: 2min

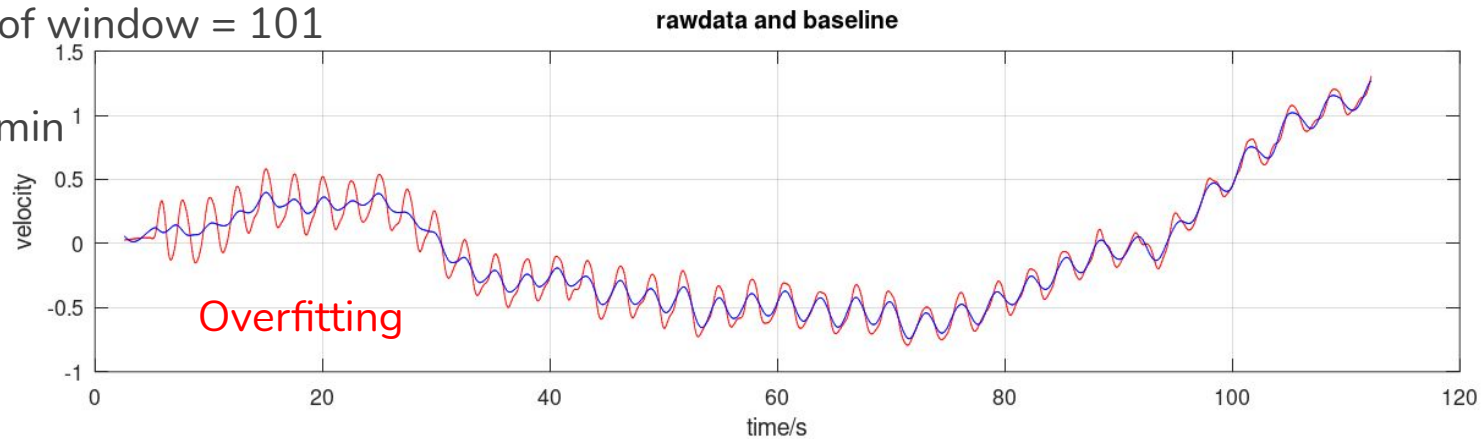


vibration data

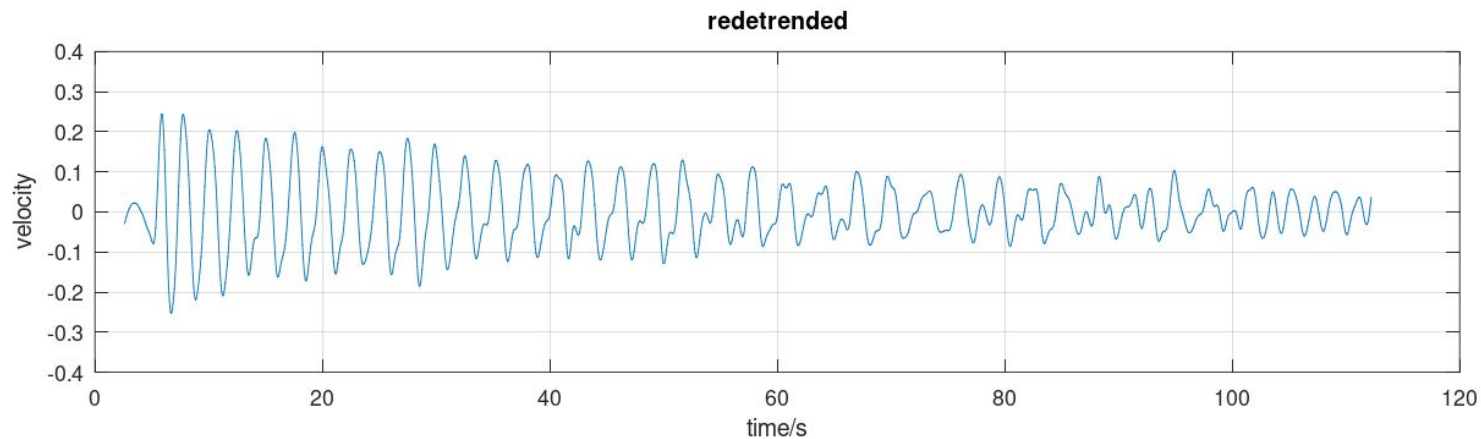


Number of orders: 2
Length of window = 101

Time: 2min



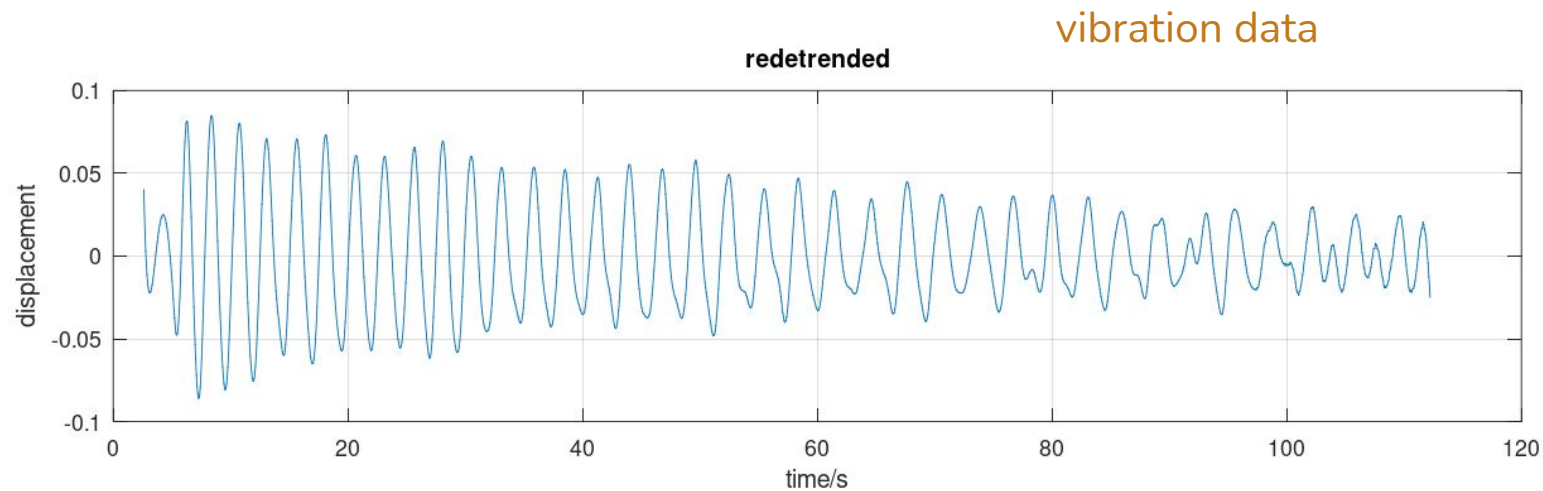
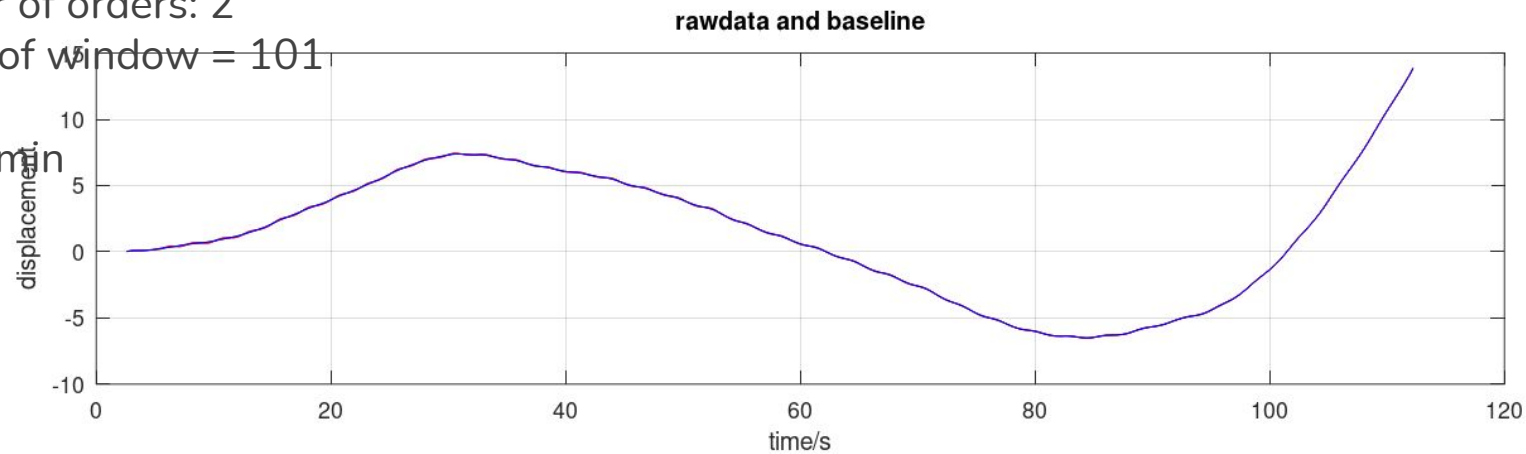
vibration data



Number of orders: 2

Length of window = 101

Time: 2min





Wavelet Decomposition

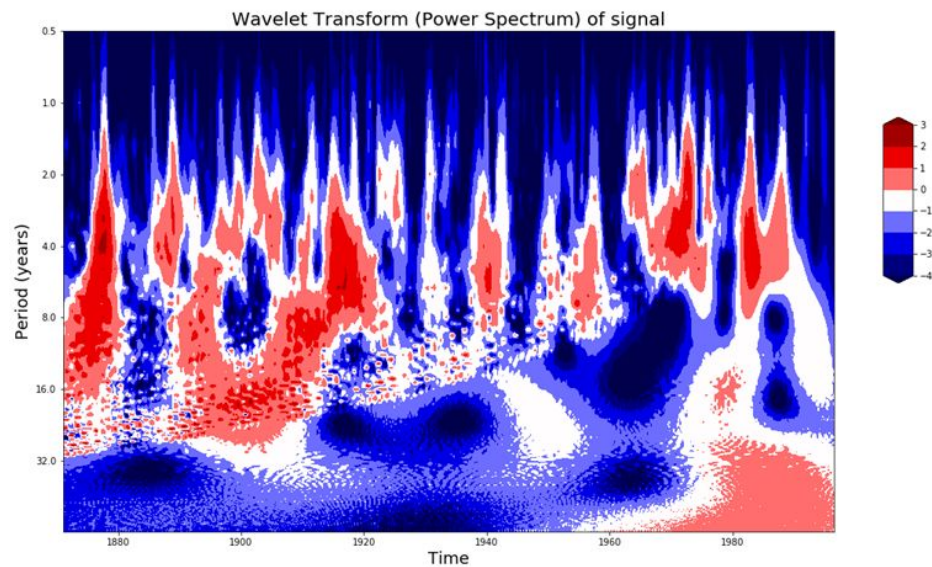
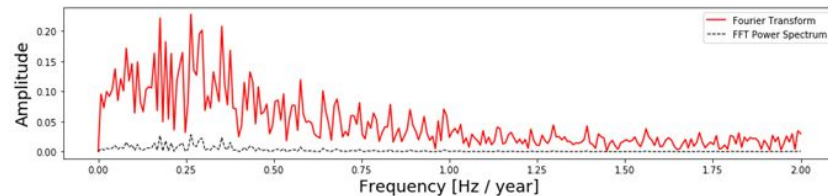
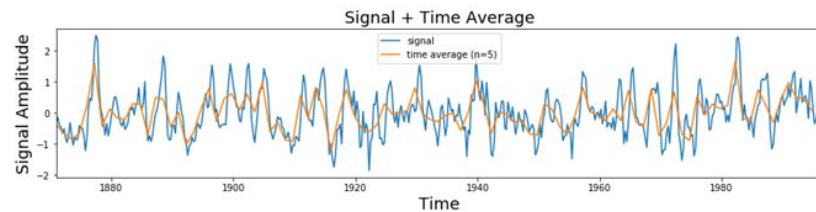




Signal

Fourier
Transformation

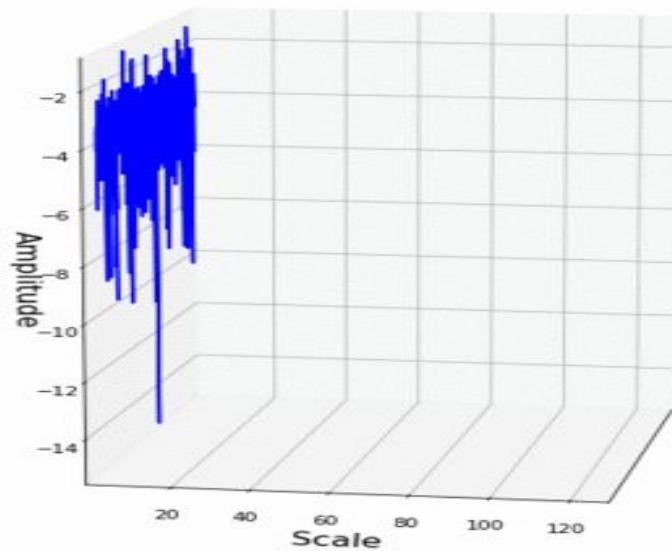
Wavelet
Transformation



$$\text{Signal (S)} * \text{Scaled Wavelet (SW)} = \text{Convolution(S, SW)}$$


The diagram illustrates the convolution process. On the left, a noisy blue line represents the 'Signal (S)'. This is followed by an asterisk (*) and a blue triangular line representing the 'Scaled Wavelet (SW)'. An equals sign (=) follows, leading to the final result, a noisy blue line representing 'Convolution(S, SW)'.

3D plot of Wavelet Transform

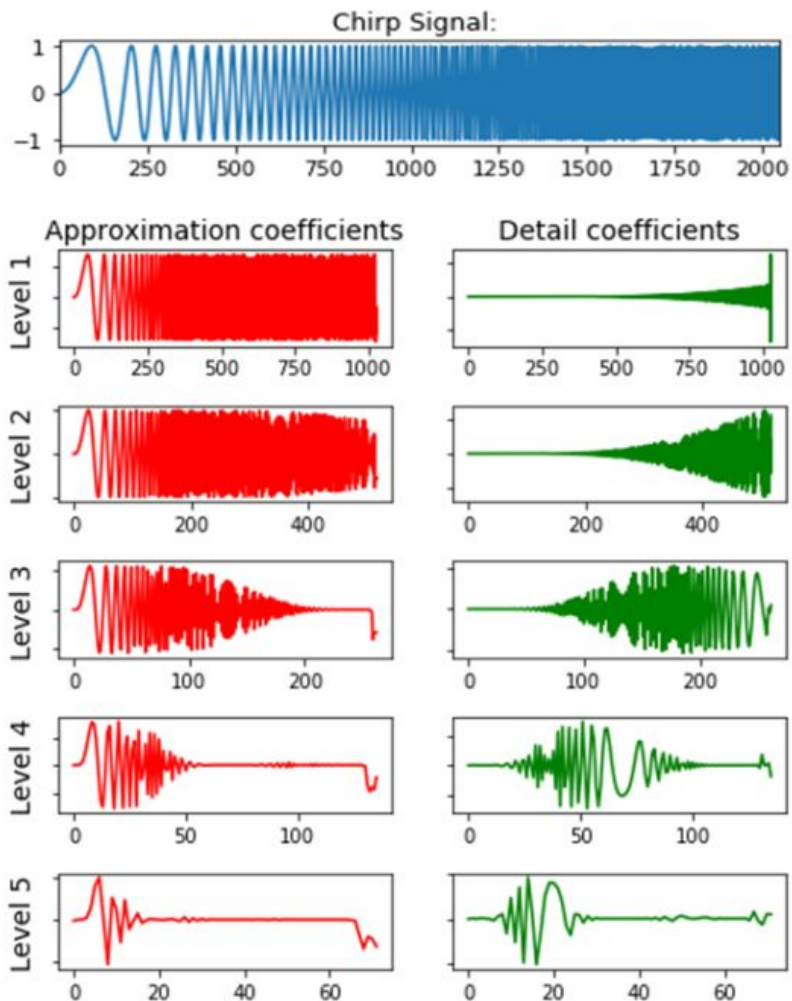
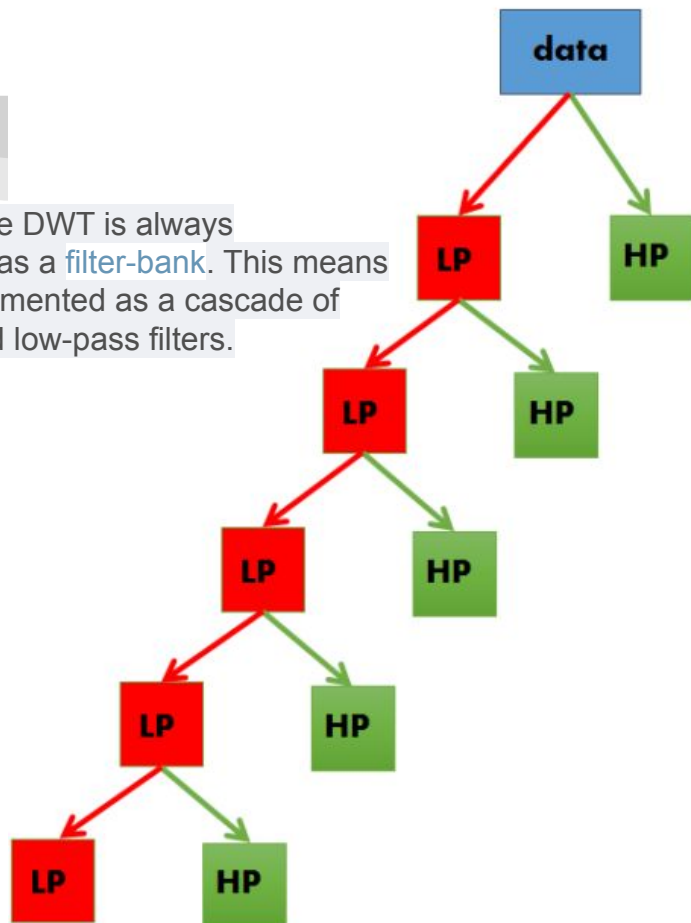


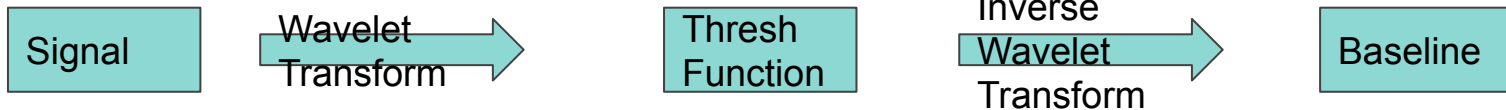
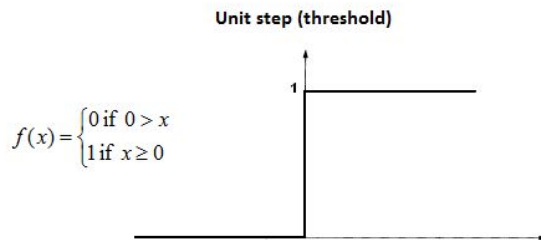
2D plot of Wavelet Transform



source: ataspinar.com

In practice, the DWT is always implemented as a [filter-bank](#). This means that it is implemented as a cascade of high-pass and low-pass filters.



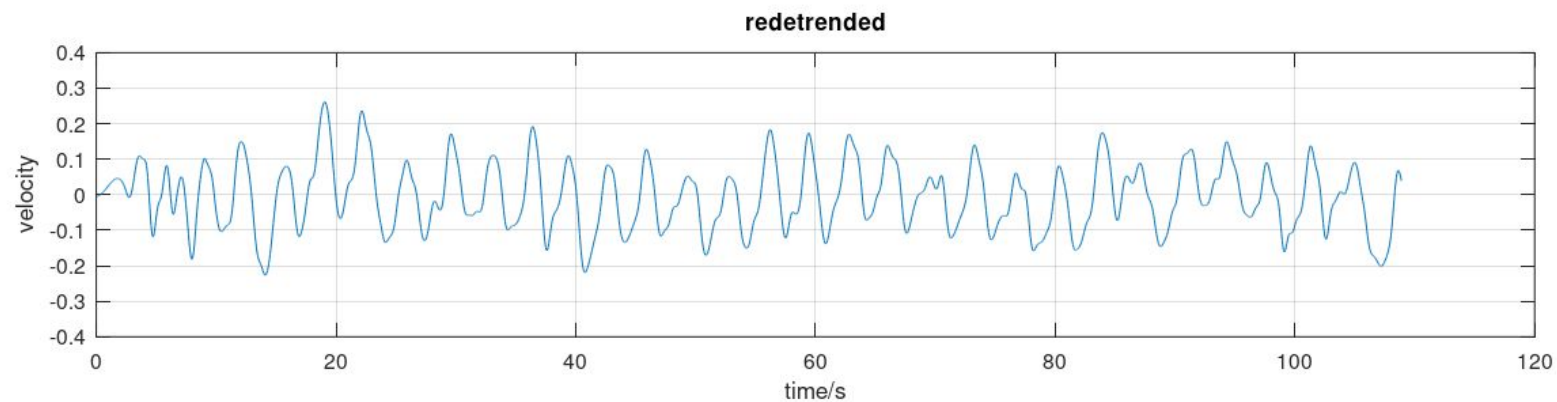
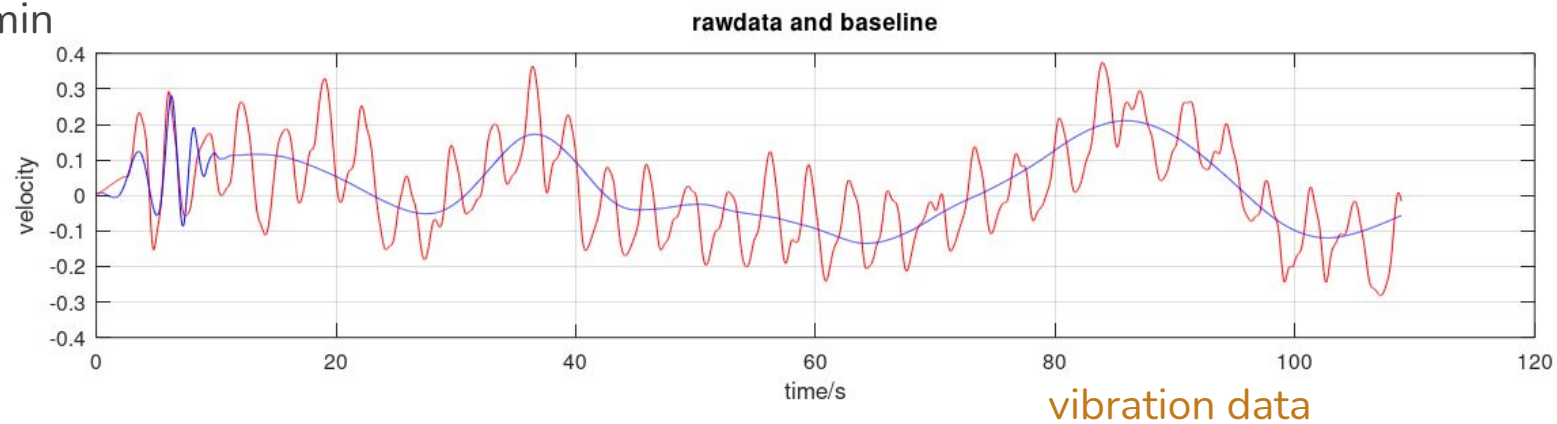


Tunable parameter:

1. wavelet type
2. order of filter_bank
3. threshold value

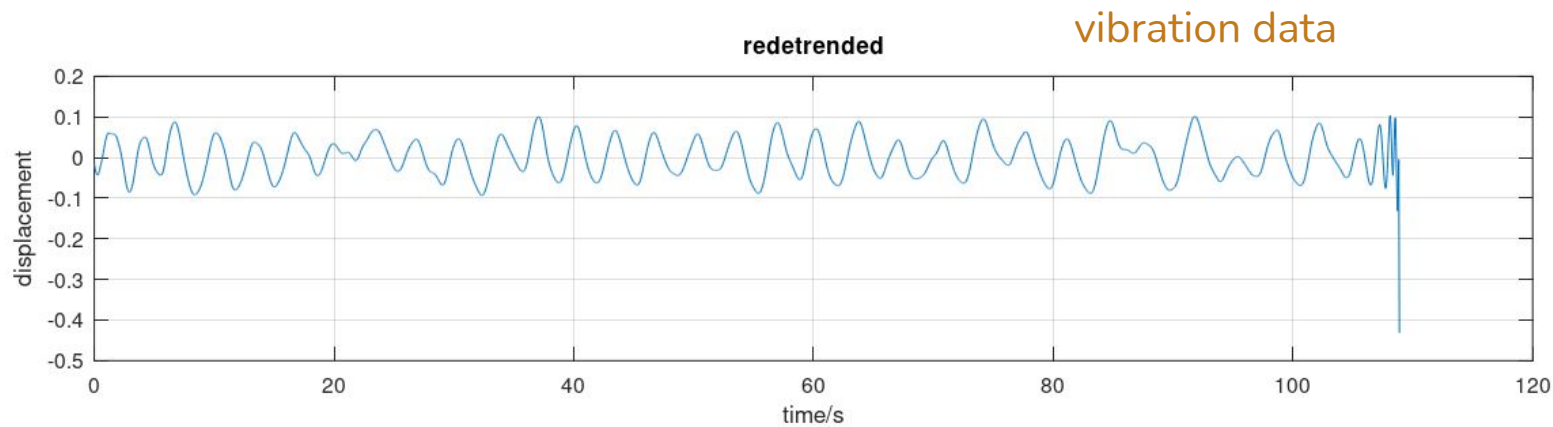
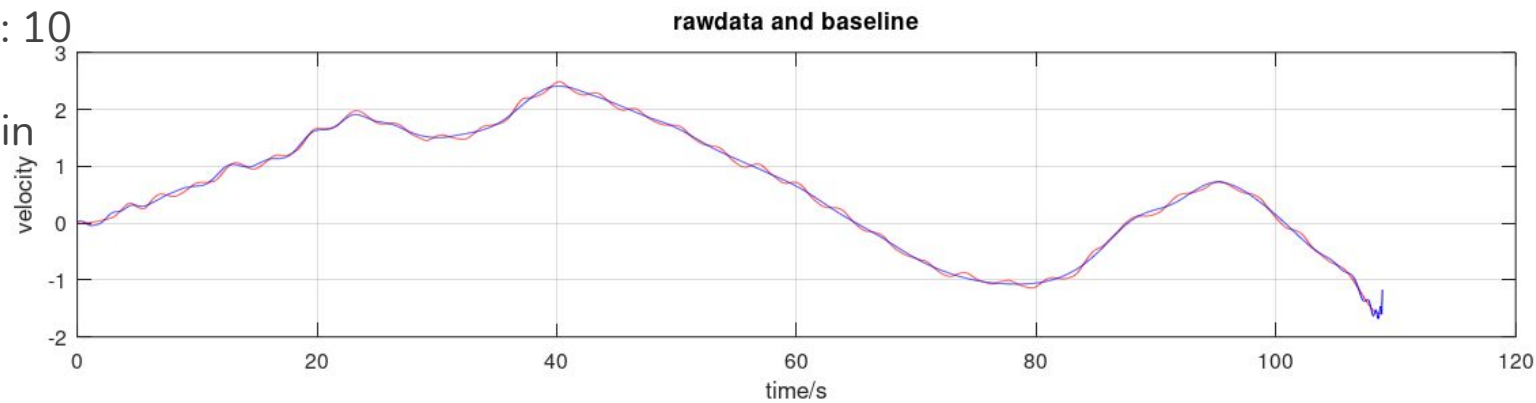
wavelet: db8
iterations: 10

Time: 2min

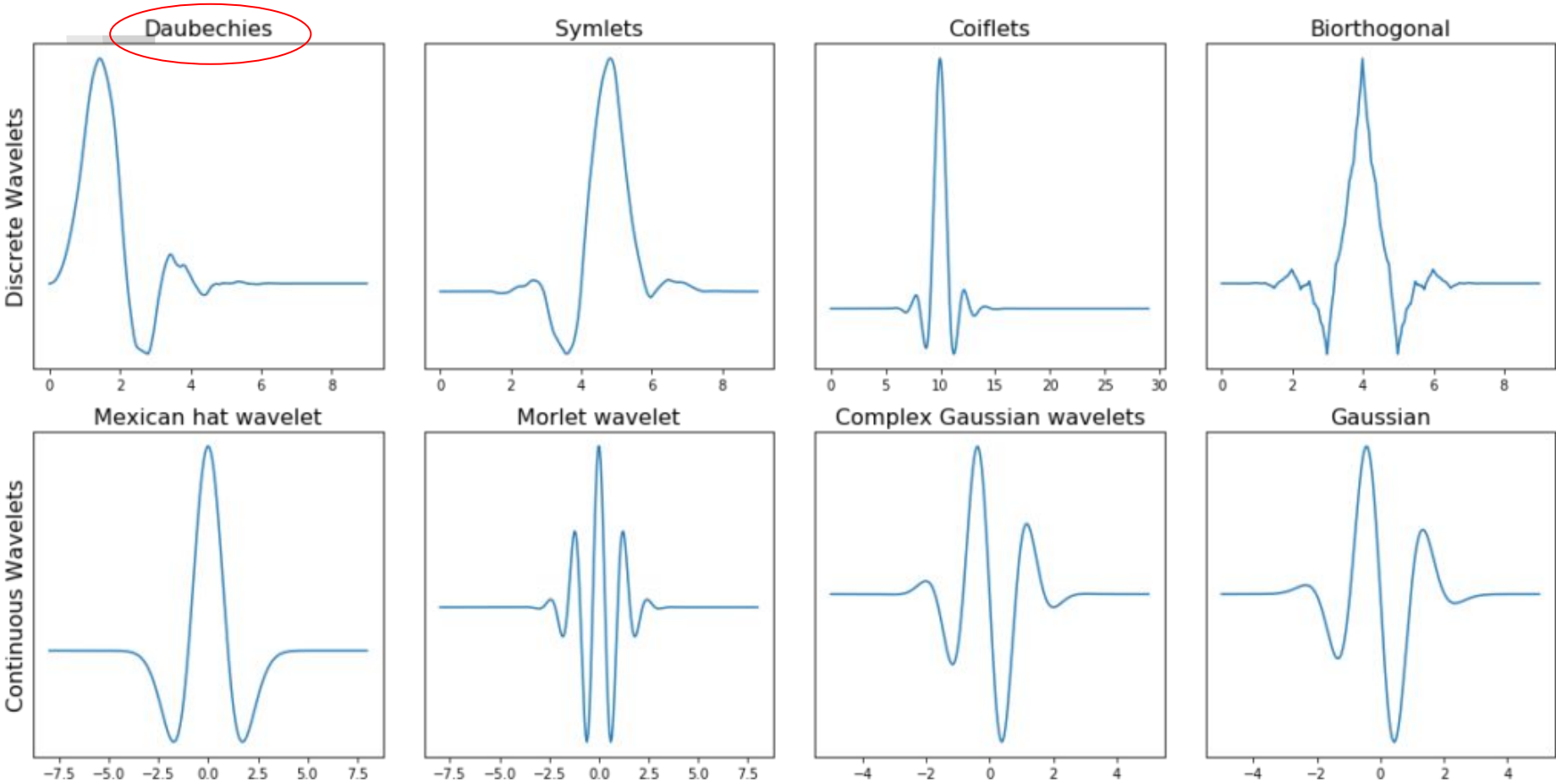


wavelet: db8
iterations: 10

Time: 2min

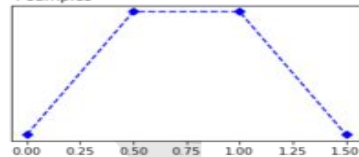


Wavelets Families

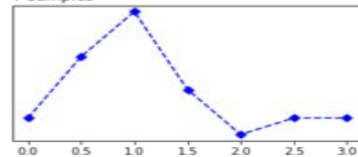


Daubechies family of wavelets

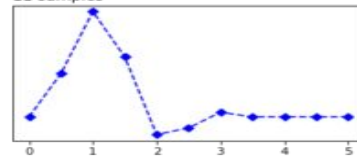
db1 - level 1
1 vanishing moments
4 samples



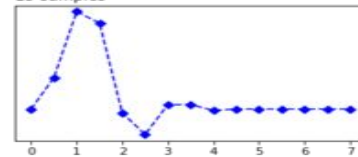
db2 - level 1
2 vanishing moments
7 samples



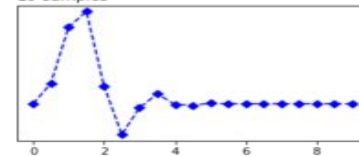
db3 - level 1
3 vanishing moments
11 samples



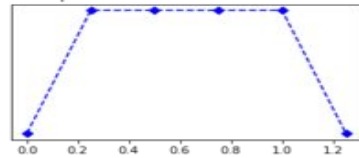
db4 - level 1
4 vanishing moments
15 samples



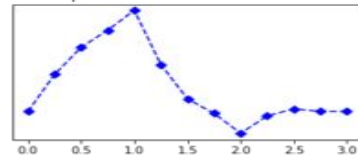
db5 - level 1
5 vanishing moments
19 samples



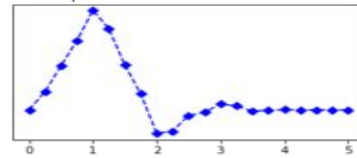
db1 - level 2
1 vanishing moments
6 samples



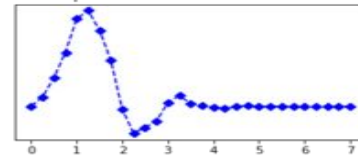
db2 - level 2
2 vanishing moments
13 samples



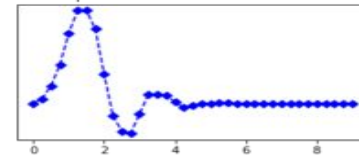
db3 - level 2
3 vanishing moments
21 samples



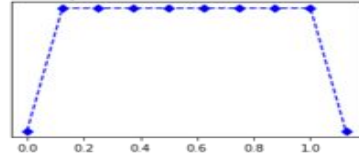
db4 - level 2
4 vanishing moments
29 samples



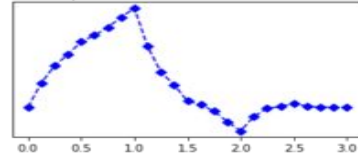
db5 - level 2
5 vanishing moments
37 samples



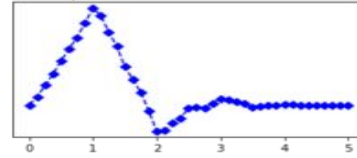
db1 - level 3
1 vanishing moments
10 samples



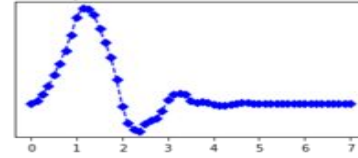
db2 - level 3
2 vanishing moments
25 samples



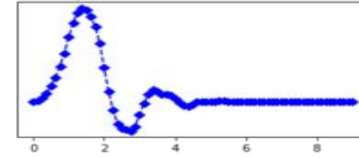
db3 - level 3
3 vanishing moments
41 samples



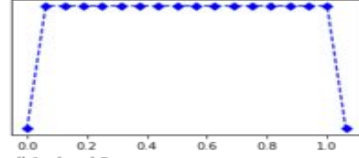
db4 - level 3
4 vanishing moments
57 samples



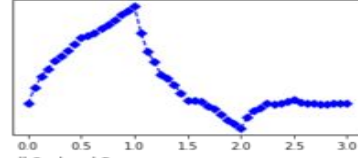
db5 - level 3
5 vanishing moments
73 samples



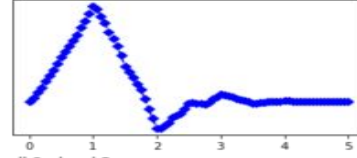
db1 - level 4
1 vanishing moments
18 samples



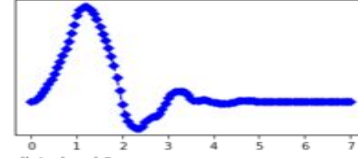
db2 - level 4
2 vanishing moments
49 samples



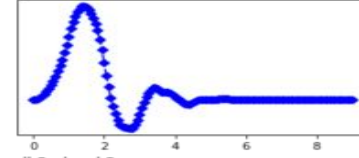
db3 - level 4
3 vanishing moments
81 samples



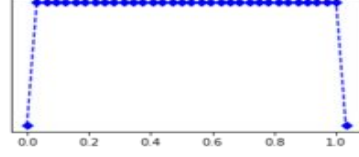
db4 - level 4
4 vanishing moments
113 samples



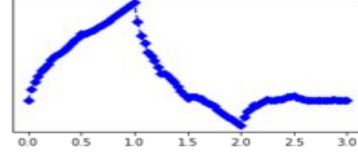
db5 - level 4
5 vanishing moments
145 samples



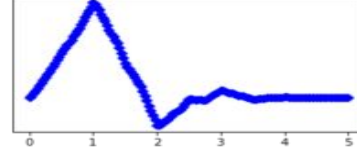
db1 - level 5
1 vanishing moments
34 samples



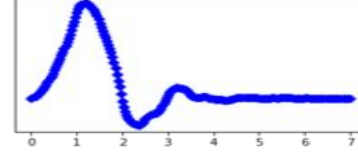
db2 - level 5
2 vanishing moments
97 samples



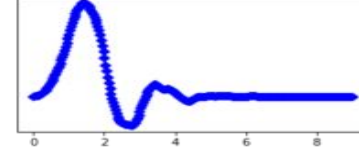
db3 - level 5
3 vanishing moments
161 samples



db4 - level 5
4 vanishing moments
225 samples



db5 - level 5
5 vanishing moments
289 samples



Octave: `[c,info] = fwt(...);`

`c`: Amplitude Coefficient (1-d vector)



Selection of Threshold Value

Syntax

```
THR = thselect(X,TPTR)
```

Description

`THR = thselect(X,TPTR)` returns the threshold value adapted to the 1-D signal `X` using the selection rule specified by `TPTR`. Available selection rules are:

- 'rigrsure' — Adaptive threshold selection using the principle of Stein's Unbiased Risk Estimate (SURE).
- 'sqtwolog' — Fixed-form threshold is $\sqrt{2 \cdot \log(\text{length}(X))}$.
- 'heursure' — Heuristic variant of 'rigrsure' and 'sqtwolog'.
- 'minimaxi' — Minimax thresholding.

Rule of Threshold Value

'hard'	Perform hard thresholding. This is the default.
'wiener'	Perform empirical Wiener shrinkage. This is in between soft and hard thresholding.
'soft'	Perform soft thresholding.



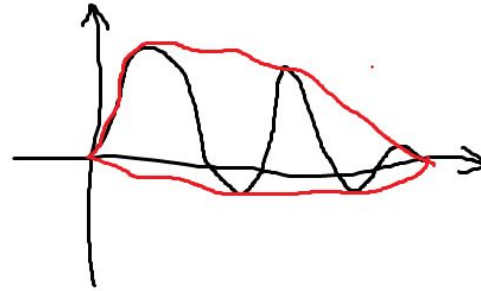
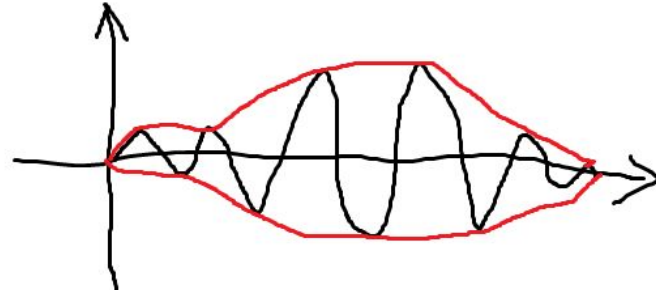
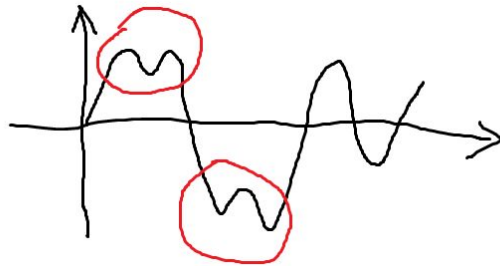
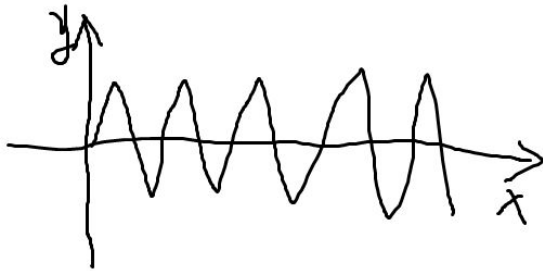
So why should you use the DWT instead? The advantage of the DWT again comes from the many wavelet shapes there are available. You can choose a wavelet which will have a shape characteristic to the phenomena you expect to see. In this way, less of the phenomena you expect to see will be smoothed out.

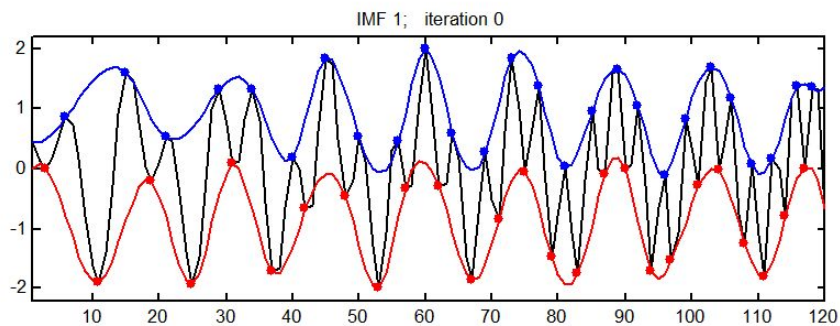


Empirical Mode Decomposition (EMD)

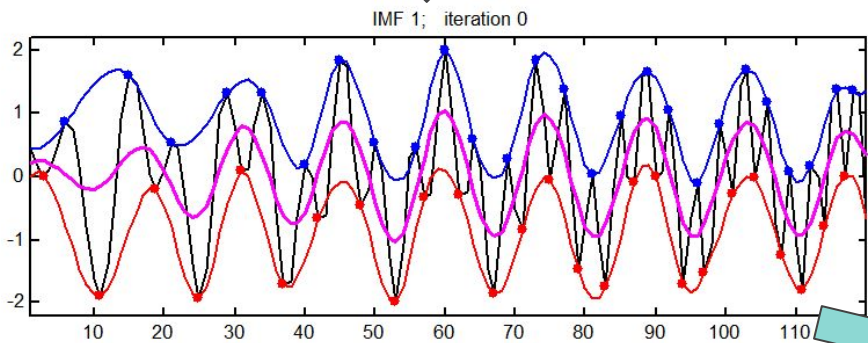
Intrinsic Mode Functions, IMF

1. In the whole data set, the number of **extrema** and the number of zero-crossings must either be equal or differ at most by one.
2. At any point, the mean value of the envelope defined by the local **maxima** and the envelope defined by the local **minima** is zero.

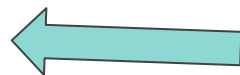




Cubic Spline Interpolation
MATLAB spline()



subtract this IMF from raw signal



IMF

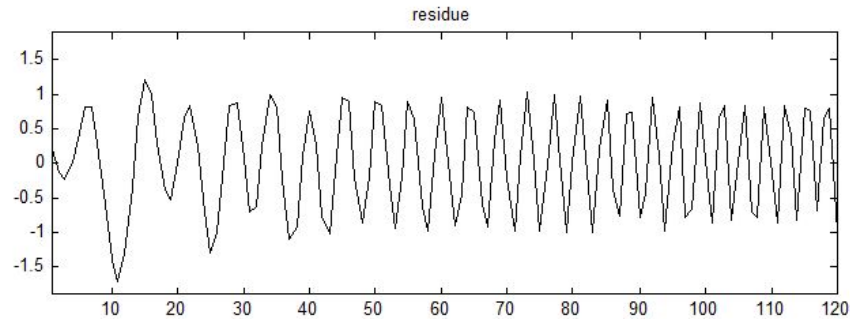


satisfied

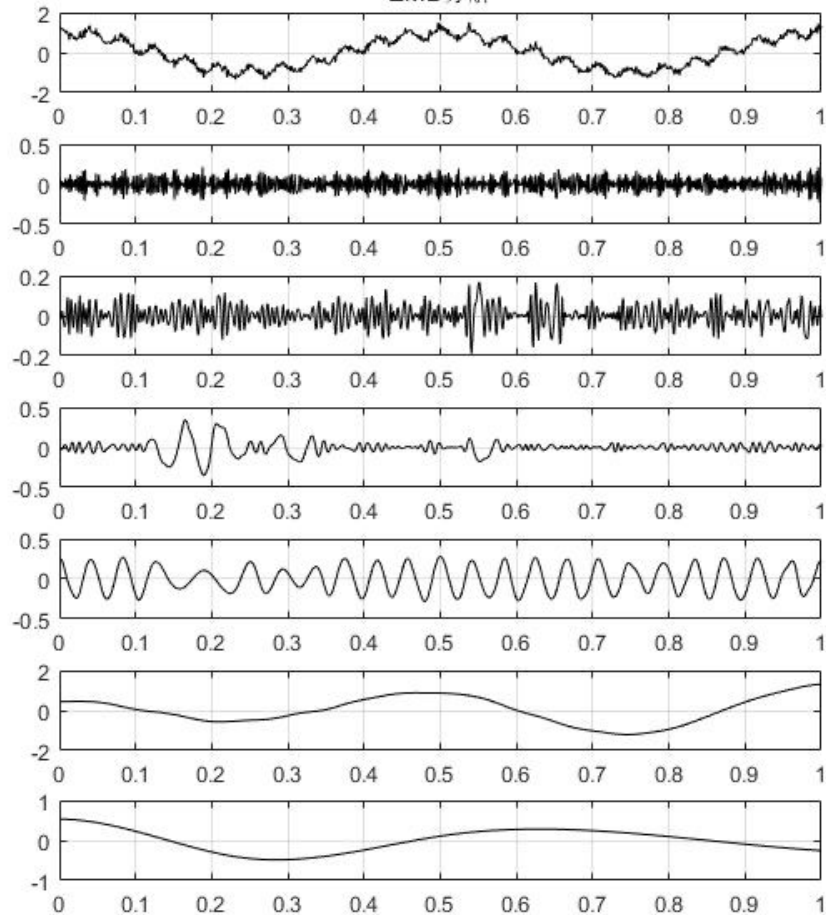
not satisfied



Limitation 1 and
2



EMD分解



Vibration components

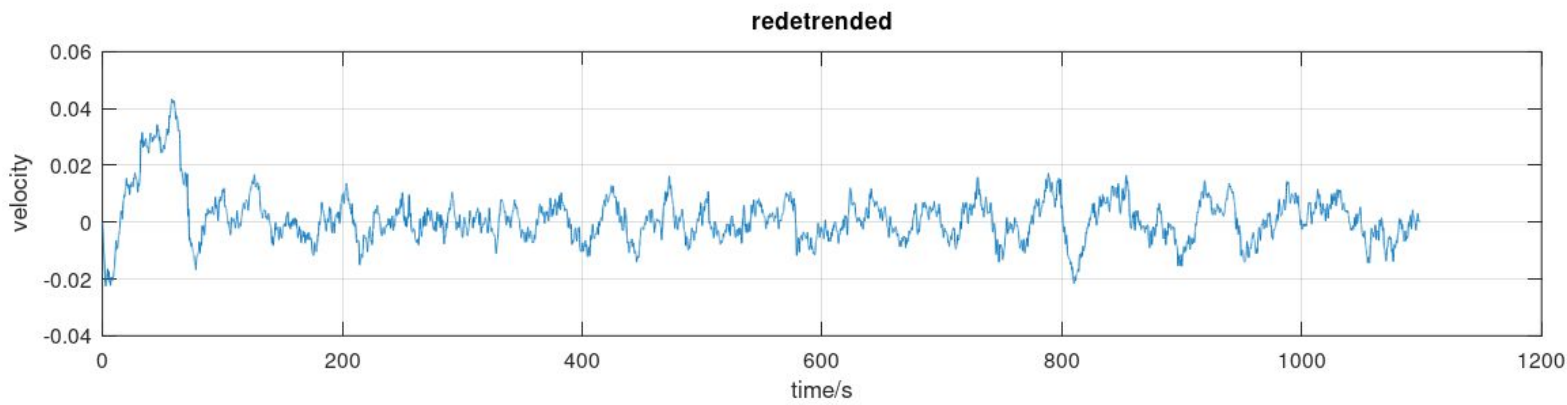
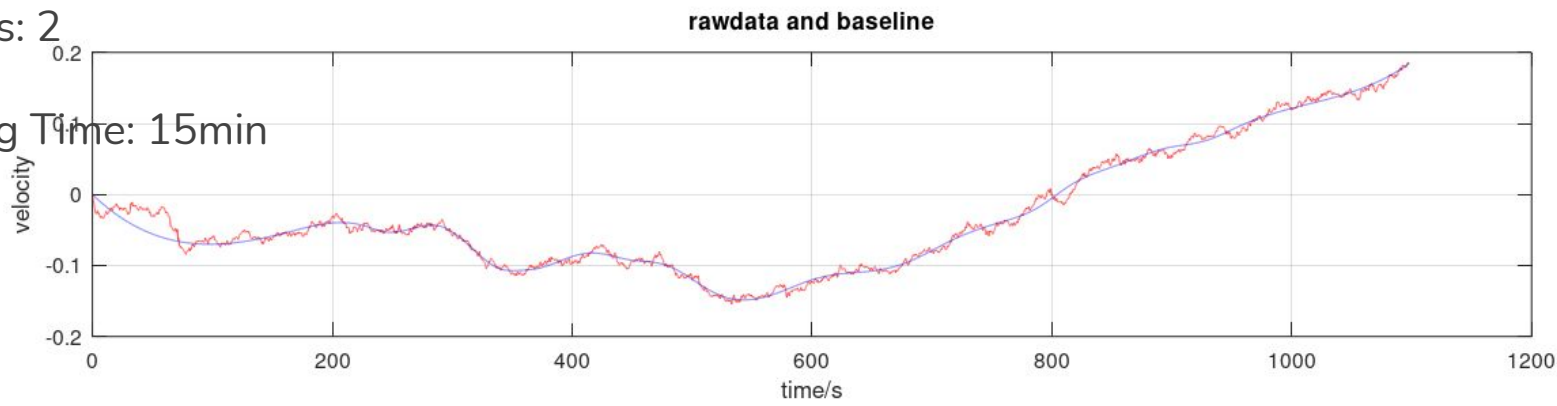
Stop Condition:

1. residue error
2. number of poles

Random Walk

Residue error: 0.03
iterations: 2

Sampling Time: 15min

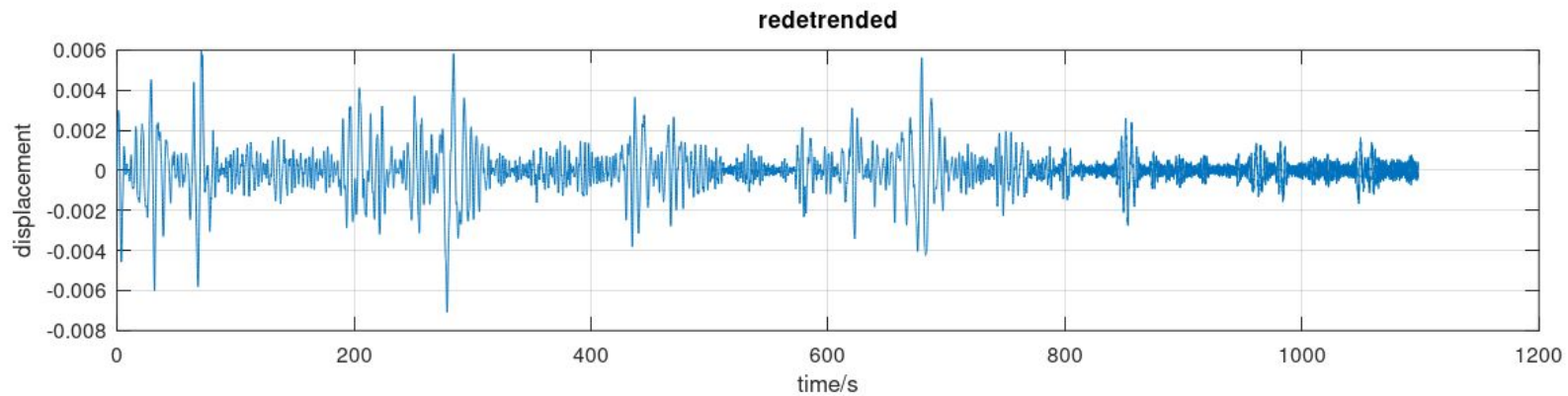
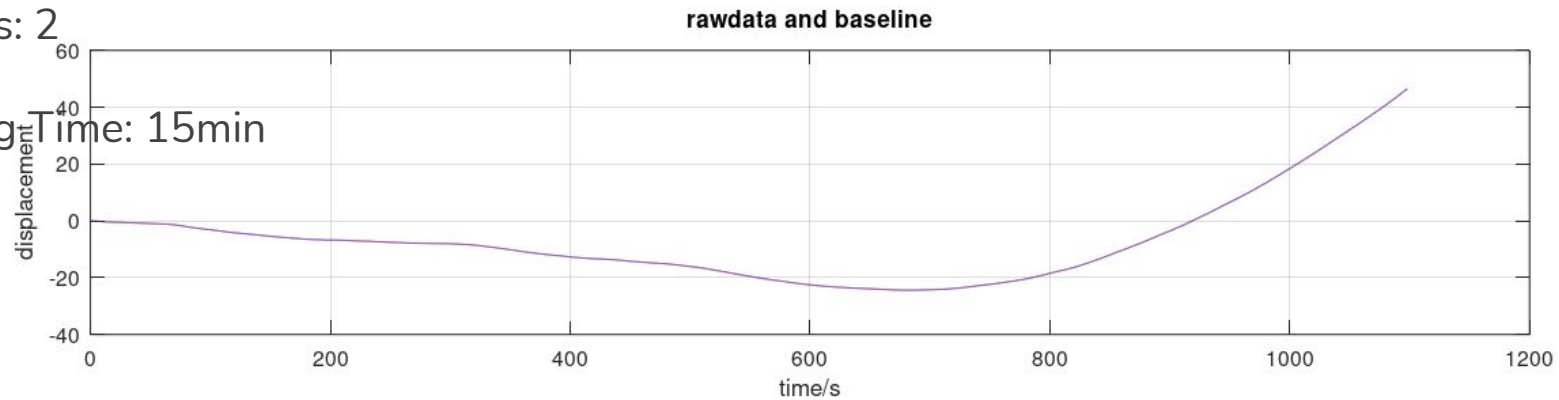


Calculation Time: 1h

Residue error: 0.3

iterations: 2

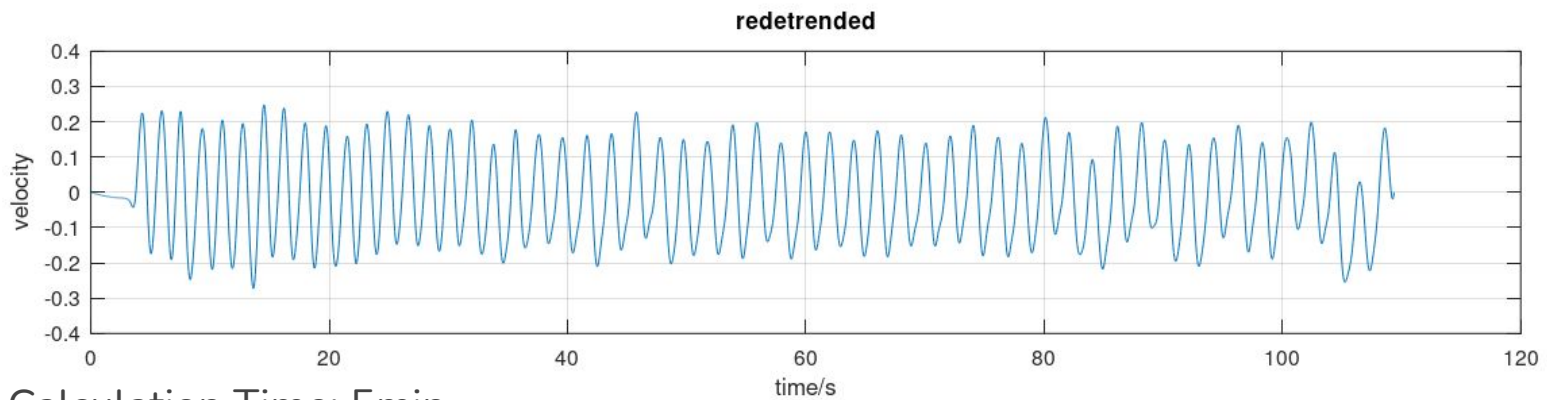
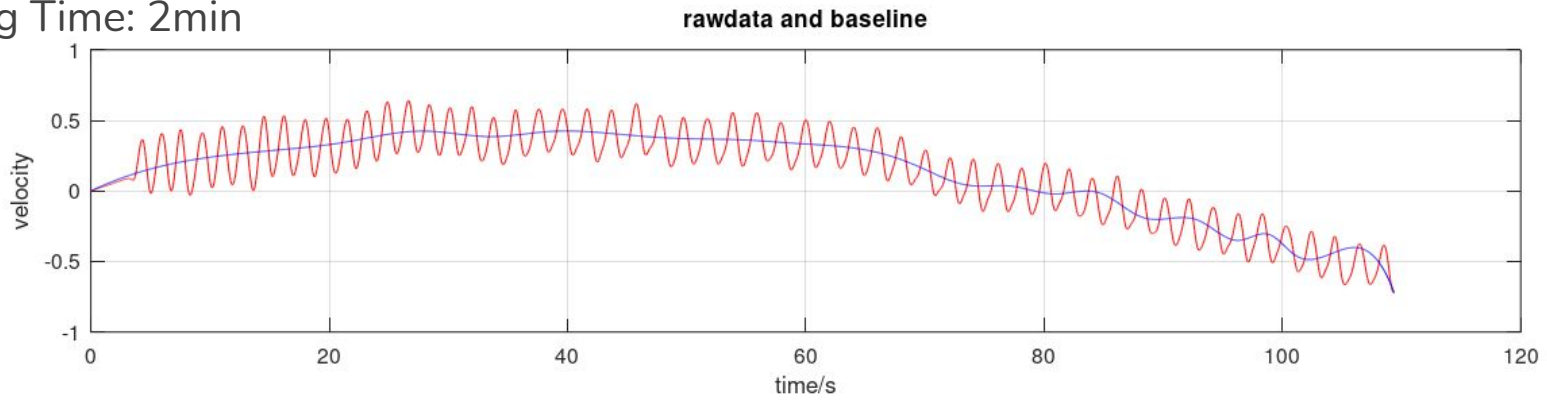
Sampling Time: 15min



Calculation Time: 1h

Residue error: 0.03
iterations: 15

Sampling Time: 2min

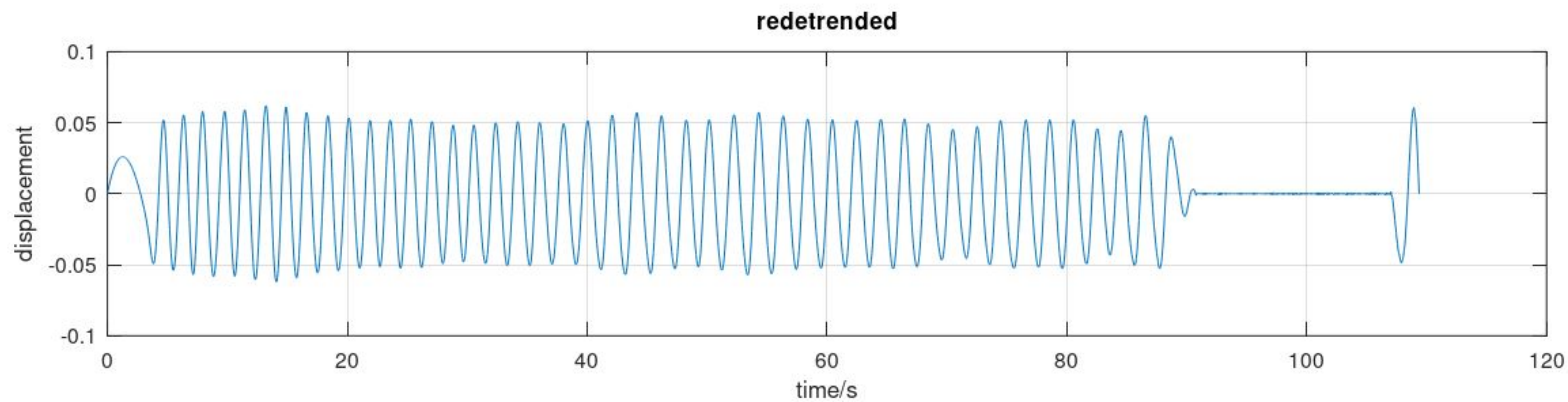
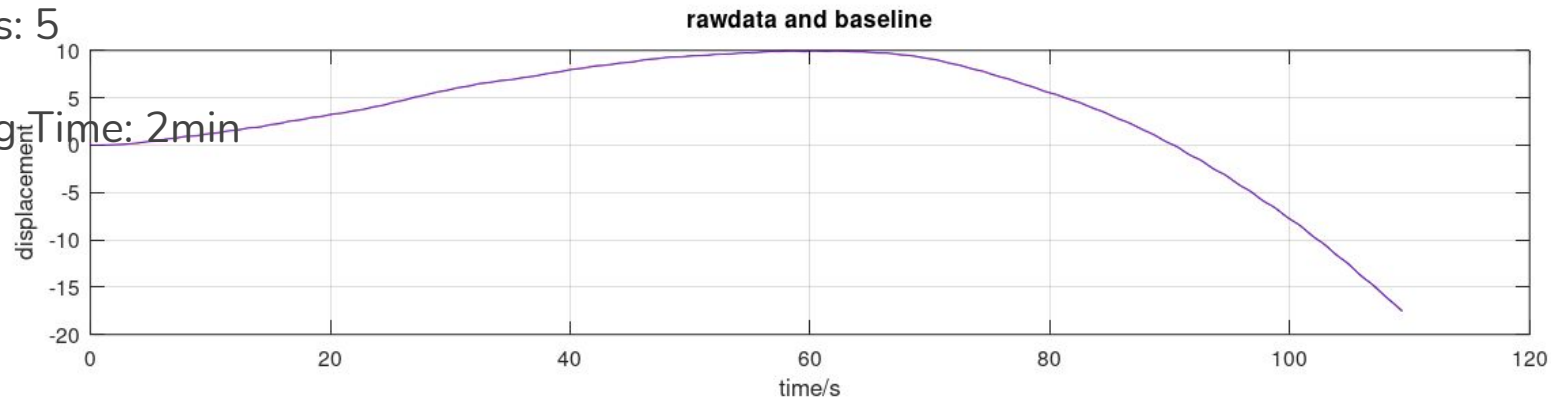


Calculation Time: 5min

Residue error: 0.03

iterations: 5

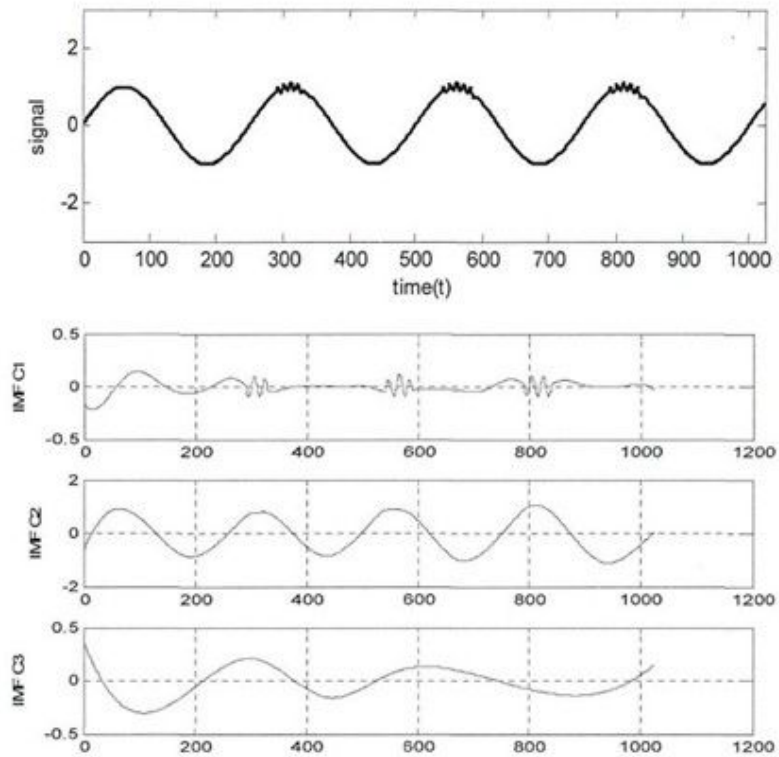
Sampling Time: 2min



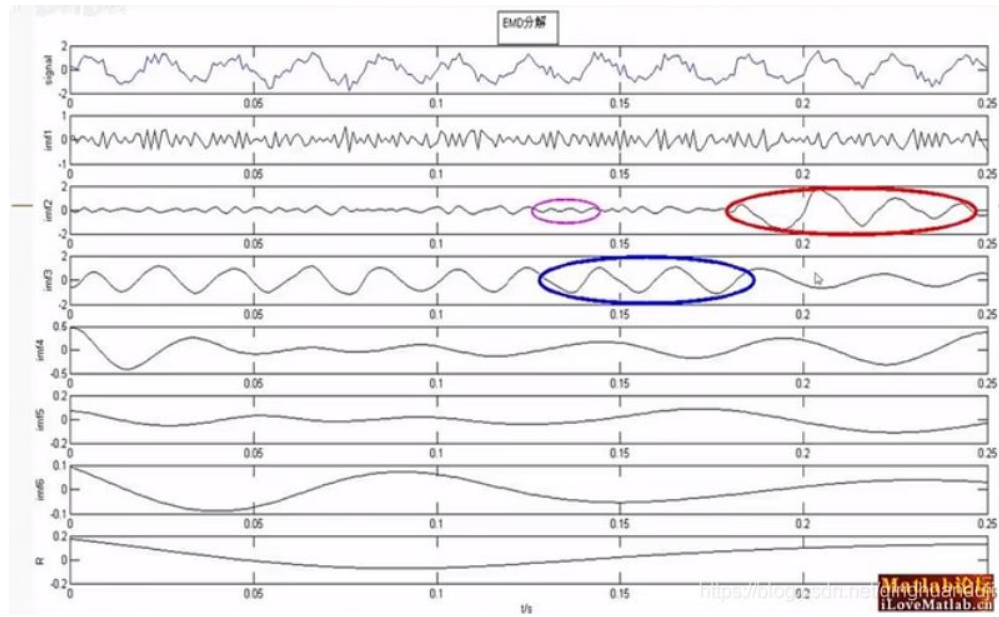
Calculation Time: 5min

Some Problems in EMD

Modal Mixing Problem



Endpoint Effect



Stop Conditions

Summary



	Savitzky-Golay Filter	Wavelet Decomposition	Empirical Mode Decomposition
Performance	Good	configure depended	Excellent
Computation Load	Good	Good	Bad
Adapativity	Good	Bad	ExceleInt

Other methods

Chromatogram baseline estimation and denoising using sparsity (BEADS) (OPT, convex optimization problem)

Smoothness Priors Approach Parameter Identification , Regularized Least Squares Solution

variational mode decomposition



Thank you for listening