

HW1: A non-linear pendulum system is described by the following equation:

- a) Find the equilibrium points of the system.
- b) Linearize the system around the equilibrium points.
- c) Analyze the stability of the equilibrium points using the linearized system.

(Analysis using MATLAB tools)

$$\begin{aligned} \text{(1)} \quad \dot{x}_1 &= x_2 \\ \dot{x}_2 &= -x_1 + \frac{x_1^3}{6} - x_2 \end{aligned}$$

$$\begin{aligned} \text{(2)} \quad \dot{x}_1 &= -x_1 + x_2 \\ \dot{x}_2 &= 0.1x_1 - 2x_2 - x_1^2 - 0.1x_1^3 \end{aligned}$$