# Analysis On Factors Impacting Education Test-Score Performance of 5'th and 9'th Grade Students

Module:ST4090

**UCC number:116101741** 

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Date:10/04/2020

Analysis On Factors Impacting Education Test-Score Performance of 5'th and 9'th Grade Students

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# Analysis On Factors Impacting Education Test-Score Performance of 5'th and 9'th Grade Students **Abstract:**

As discussed in the fist- step -analysis, the smart phone has a huge influence on the students' academic performance. However, the model to analysis the factors to impact the test-score performance of 5<sup>th</sup> and 9<sup>th</sup> students is not good enough. Therefore, the target of the sturdy is to find further factors that will have influences on the students' academic performance. From the extensive survey conducted within primary and middle-school students in several Chinese, attitudes, interest, classmaterelation, campus condition, satisifaction learning, strategy, subjects, manners, social morals, hard work, solidarity friendship, moral duty, sense honors ...... all total 28 factors that may have impact on students' scores.

# Analysis On Factors Impacting Education Test-Score Performance of 5'th and 9'th Grade Students 1.Introduction

In the first-step- analysis, the mobile phones were proved to have strong effect on students' academic achievement. But there are still many factors in the model we do not consider. For searching the really important factors, the author will take the method of principal component analysis, cross validation and model selections. The aim of the study is to find the best model that determine the academic performance of the 5<sup>th</sup> and 9<sup>th</sup> grade students.

# Analysis On Factors Impacting Education Test-Score Performance of 5'th and 9'th Grade Students

# 2. Methods and Data Analysis

The school survey was conducted by questionnaire within primary and middle-school students in several Chinese provinces. It focuses on two different grade students' groups (5<sup>th</sup> and 9<sup>th</sup>). We here use principal component cross-validation and stepwise model selection to find the most significant factors that influence the academic performances of 5<sup>th</sup> and 9<sup>th</sup> grade students.

# Analysis On Factors Impacting Education Test-Score Performance of 5'th and 9'th Grade Students

# 3. Results and Discussion

The Table 1 shows the principal component analysis on the independent variable of 5<sup>th</sup> students (factors that collected from the survey). Among these 28 variables, we saw that we just need the first 21 components which can explain more than 95% of variance.

**Table 1** The Principal Component Analysis of 5<sup>th</sup> students

Importance of components:						
•	PC1	PC2	PC3	PC4	Р	
C5						
Standard deviation 95	289.0136	134.8312	118.59158	108.91789	101.131	
Proportion of Variance	0.3813	0.0830	0.06421	0.05416	0.046	
Cumulative Proportion 39	0.3813	0.4643	0.52854	0.58270	0.629	
	PC6	PC7	PC8	PC9	PC10	
Standard deviation	87.65065	84.19276	82.11203	76.01038 74	4.09180	
Proportion of Variance	0.03507	0.03236	0.03078	0.02638 (	0.02506	
Cumulative Proportion	0.66446	0.69682	0.72761	0.75398 (	0.77904	
	PC11	PC12	PC13	PC14	PC15	
Standard deviation		67.25800			9.78998	
Proportion of Variance	0.02401		0.01977		0.01632	
Cumulative Proportion	0.80306	0.82371	0.84348		0.87914	
	PC16	PC17	PC18	PC19	PC20	
Standard deviation	57.92569		53.89717		8.92901	
Proportion of Variance	0.01532	0.01399	0.01326		0.01093	
Cumulative Proportion	0.89446	0.90844	0.92171		0.94418	
	PC21	PC22	PC23	PC24	PC25	
Standard deviation	48.13035	45.52968			1.52045	
Proportion of Variance	0.01058		0.00884		0.00787	
Cumulative Proportion	0.95475	0.96421	0.97305	0.98098 (	0.98885	
	PC26	PC27	PC28			
Standard deviation	37.25924		0.382			
Proportion of Variance	0.00634	0.00481	0.000			
Cumulative Proportion	0.99519	1.00000	1.000			

The Table 2 shows the principal component analysis on the independent variable of 9<sup>th</sup> students (factors that collected from the survey). Among these 28 variables, we saw that we just need the first 21 components which can explain more than 95% of

Education Test-Score Performance of 5'th and 9'th Grade Students variance.

**Table 2** The Principal Component Analysis of 9<sup>th</sup> students

```
Importance of components:
                                         PC2
                                                    PC3
                                                             PC4
                              PC1
                                                                       PC
Standard deviation
                         244.0969 130.73840 115.29660 104.3669 89.2976
                           0.3381
                                    0.09698
Proportion of Variance
                                               0.07542
                                                          0.0618 0.0452
Cumulative Proportion
                           0.3381
                                    0.43503
                                               0.51045
                                                          0.5723
                                                                   0.6174
                              PC6
                                                  PC8
                                        PC7
Standard deviation
                         81.85157 75.97027 73.78364 70.51010 67.57488
Proportion of Variance 0.03801
                                   0.03275
                                             0.03089
                                                       0.02821
                                                                 0.02591
Cumulative Proportion
                                   0.68825
                          0.65550
                                             0.71914
                                                       0.74734
                                                                 0.77325
                             PC11
                                       PC12
                                                 PC13
                                                          PC14
                         65.63317 60.99074 59.19839 57.12840 55.76189
Standard deviation
Proportion of Variance 0.02444
                                   0.02111
                                            0.01988
                                                       0.01852
                                                                 0.01764
Cumulative Proportion
                          0.79769
                                   0.81880
                                             0.83868
                                                       0.85720
                                       PC17
                                                PC18
                             PC16
Standard deviation 53.72822 52.91833 50.42785 46.52231 46.06063 Proportion of Variance 0.01638 0.01589 0.01443 0.01228 0.01204
                          0.89122
Cumulative Proportion
                                   0.90710
                                             0.92153
                                                       0.93381
                                                                 0.94585
                                      PC22
                                               PC23
                                                         PC24
                             PC21
PC26
Standard deviation
                        43.04558 40.4801 39.43025 36.38244 34.47061 3
2.22906
Proportion of Variance 0.01051 0.0093 0.00882 0.00751 0.00674
0.00589
Cumulative Proportion
                          0.95636 0.9657 0.97448 0.98199 0.98873
0.99462
                             PC27
                         30.77706 0.5302
Standard deviation
                         0.00537 0.0000
1.00000 1.0000
Proportion of Variance
Cumulative Proportion
```

The Table 3 illustrates the results of backward and cross-validation selection selected components in Table 1 to build Linear Regression for predicting English Test-Score of 5<sup>th</sup> Students. It seems that the 4 variables has the least RMSE(98.25991).

**Table 3:** Results of backward model of English Test-Score of 5<sup>th</sup> Students in PC components

	nvmax	RMSE	Rsquared	MAE	RMSESD	RsquaredSD	MAESD
1	1	103.66064	0.1475541	85.20612	6.885379	0.07571218	6.826070
2	2	102.44804	0.1804195	82.62183	8.290728	0.09767660	8.470636
3	3	98.38116	0.2488684	78.71567	7.489119	0.11519093	6.931832
4	4	98.38683	0.2421856	78.19717	7.119786	0.10473833	6.755943
5	5	97.55421	0.2656555	78.36352	9.640966	0.12204601	9.665205
6	6	98.69360	0.2438234	79.50485	8.515345	0.11051802	8.060162
7	7	99.26903	0.2389251	80.02998	8.892458	0.11388535	7.753888

```
Education Test-Score Performance of 5'th and 9'th Grade Students

8 99.42430 0.2355504 80.23107 9.434955 0.11520014 8.036141
9 99.22777 0.2381932 80.28012 9.662210 0.12000409 7.730895
10 10 99.81790 0.2268959 80.95899 9.091116 0.12017439 7.088459
11 11 99.03553 0.2369299 80.28897 8.809208 0.11996518 7.172256
12 98.54064 0.2450931 79.76120 8.579880 0.11932045 6.808899
13 13 98.55159 0.2438215 79.92042 7.981207 0.11417023 6.464402
14 98.25991 0.2472548 79.71427 8.033125 0.10717532 6.689506
15 97.79213 0.2530513 79.25268 8.575935 0.11215654 6.992857
16 97.27042 0.2602299 78.89108 8.429588 0.11531492 6.973657
17 97.33688 0.2585046 78.96429 8.377664 0.11184560 6.872161
18 97.30908 0.2587516 79.09428 8.454545 0.11138198 6.933156
19 97.20218 0.2609190 79.03426 8.458176 0.11269623 6.953179
20 97.33522 0.2591690 79.16706 8.543106 0.11313121 6.970178
21 97.35975 0.2590282 79.18118 8.559536 0.11352898 6.992859
```

The Table 4 shows the final selected components of backward selection method and its coefficients. (14 components)

**Table 4:** Coefficient of the final backward model of English Test-Score of 5<sup>th</sup> Students in PC components

```
(Intercept)
                      PC1
                                    PC2
                                                  PC3
                                                                PC4
569.97379487
               -0.13942124
                             -0.04009814
                                            0.21142705
                                                         -0.08311115
         PC5
                       PC6
                                                   PC8
                              0.04553007
-0.23031023
              -0.02603587
                                           -0.07624393
                                                          0.12641688
        PC10
                      PC11
                                    PC12
                                                  PC13
-0.18338740
                                                         -0.15855369
                0.11067562
                              0.22766629
                                           -0.13464087
        PC15
                      PC16
                                    PC17
                                                  PC18
                                                                PC21
                0.04990590
-0.09611983
                              0.14680407
                                            0.12007133
                                                         -0.07256116
```

The Table 5 illustrates the results of forward and cross-validation selection selected components in Table 1 to build Linear Regression for predicting English Test-Score of 5<sup>th</sup> Students. It seems that the 5 variables has the least RMSE (97.55032).

**Table 5:** Results of forward model of English Test-Score of 5<sup>th</sup> Students in PC components

```
nvmax RMSE Rsquared MAE RMSESD RsquaredSD MAESD
1 103.66133 0.1411858 85.15395 5.762260 0.07525440 3.456241
2 103.04216 0.1509331 83.46747 4.304889 0.05774784 2.932333
```

```
Education Test-Score Performance of 5'th and 9'th Grade Students
3 98.40772 0.2216054 78.52784 4.876523 0.08328748 4.224283
4 98.97900 0.2135179 79.10089 5.724395 0.10584972 4.351512
5 97.55032 0.2382213 78.43357 5.935305 0.12032777 5.355226
6 97.86631 0.2348027 78.85435 5.715801 0.10218525 5.239438
3 4 5 6 7 8 9 10 112 13 14 15 6 17 18 19 20 21
                      98.59299 0.2286643 79.15522
                                                                                  5.539668 0.09637373
                     98.69356 0.2303550
99.32287 0.2233862
                                                              79.62432
80.18945
                                                                                  5.980282 0.09753274
6.944773 0.10677312
                   100.02632 0.2120169 80.52684
                                                                                 7.034660 0.10720542
                      99.50697 0.2174309 80.05300 6.776950 0.10235164
                     99.16467 0.2216645
98.91781 0.2262442
                                                              79.70058 6.756945 0.09708999
79.92787 6.724407 0.09078294
                     98.55986 0.2313011 79.38848 6.438728 0.09331565 6.619720
                     98.45198 0.2332915 79.32634 6.269239 0.09248313 98.44151 0.2327251 79.49066 6.204294 0.09237554
                     98.16117 0.2362287 79.35761 6.332865 0.09287264 6.740812 98.21102 0.2354741 79.49317 6.359723 0.09056694 6.816674 97.91866 0.2388804 79.31096 6.250647 0.09018228 6.729068 98.02309 0.2379893 79.32672 6.403539 0.09328841 6.714388
                     98.05632 0.2372287 79.37235 6.321279 0.09209797 6.665890
```

The table 6 shows the final selected components of forward selection method and its coefficients.

**Table 6:** Coefficient of the final forward model of

```
(Intercept) PC1 PC3 PC5 PC10 P
C12
569.9737949 -0.1394212 0.2114271 -0.2303102 -0.1833874 0.2276
663
```

The table 7 demonstrates the results of stepwise and cross-validation selection selected components in Table 1 to build Linear Regression for predicting English Test-Score of 5<sup>th</sup> Students. The 3 variables has the smallest RMSE (98.18572).

**Table 7:** Results of stepwise model of English Test-Score of 5<sup>th</sup> Students in PC components

nvmax		RMSE RS	squared	MAE	RMSESD RS	quaredSD	MAESD
1	1	103.51798	0.1390771	85.21396	9.205258	0.05211057	8.947598
2	2	101.78069	0.1764516	82.45103	7.949162	0.06523395	7.212294
3	3	98.18572	0.2311891	78.62603	6.798652	0.08668306	5.513564
4	4	98.34358	0.2250104	78.72949	6.928802	0.06198156	6.677532
5	5	98.81557	0.2275370	79.27379	8.028963	0.08951888	8.313928
6	6	99.62974	0.2240764	79.98227	8.375940	0.08984669	8.662767
7	7	100.60179	0.2102741	80.59467	8.990805	0.07096918	9.981220
8	8	100.03024	0.2257468	79.80646	8.450699	0.08039212	9.131350
9	9	100.27242	0.2228624	80.51208	9.958317	0.09204273	10.454114
10	10	99.62329	0.2324809	80.33764	8.844298	0.08710931	9.648446

**Table 8:** Coefficient of the final stepwise model of English Test-Score of 5<sup>th</sup> Students in PC components

(Intercept) PC1 PC3 PC5
569.9737949 -0.1394212 0.2114271 -0.2303102

In conclusion, by comparing these three methods, we get th at the forward method has the smallest RMSE of cross-validation of the model. In this model, the components PC1, PC3, PC5, PC10, PC12 are needed in the model.

The table 9 shows the results of backward and cross-validation selection selected components in Table 1 to build Linear Regression for predicting Math Test-Score of 5<sup>th</sup> Students. We choose 4 max components model which has the smallest RMSE (96.15811).

**Table 9:** Results of backward model of Math Test-Score of 5<sup>th</sup> Students in PC components.

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        101.63793
        0.05624755
        80.30625
        12.099054
        0.05255154
        7.596901

        2
        98.52229
        0.12330853
        77.71261
        10.462627
        0.10910969
        7.116064

        3
        97.55361
        0.13106022
        76.16632
        10.183272
        0.11669200
        7.724318

        4
        4
        96.15811
        0.15979603
        74.65433
        9.088350
        0.12352403
        6.990549

        5
        97.31459
        0.14361667
        75.95681
        8.929836
        0.13348277
        6.583328

        6
        97.70976
        0.13233138
        76.65099
        8.027426
        0.12548296
        6.161448

        7
        98.85517
        0.11807211
        77.23557
        8.263457
        0.12057378
        6.045558

        8
        99.14480
        0.11728773
        77.21239
        7.727613
        0.12092537
        5.846592

        9
        99.66713
        0.10709479
        77.58984
        8.042480
        0.10044634
        5.747906
```

```
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10 100.03963 0.10226148 78.12987 7.905708 0.09586843 6.049791

11 99.97889 0.10613750 77.88757 7.661812 0.09627379 5.929815

12 99.90768 0.10597447 77.79233 8.124551 0.08965355 6.338267

13 99.77468 0.10560481 77.56080 8.311268 0.08985809 6.820024

14 14 99.64782 0.10661984 77.38378 8.493400 0.08688886 6.826200

15 15 99.27508 0.11075598 77.26751 8.229343 0.08986614 6.591178

16 98.84693 0.11649155 77.29090 8.744120 0.09055081 6.811313

17 98.64410 0.12185785 77.17785 8.451746 0.09372565 6.570752

18 18 98.32657 0.12628700 76.86215 8.700218 0.09595070 6.811022

19 98.00438 0.13100704 76.55189 8.945246 0.09619307 7.086440

20 97.78295 0.13410096 76.42492 9.010733 0.09802300 7.241462

21 97.55657 0.13662641 76.24876 9.139642 0.09751416 7.365583
```

Table 10 demonstrate the final selected components of backward selection method and its coefficients **Table 10:** Coefficient of the final backward model of Math Test-Score of 5<sup>th</sup> Students in PC components

```
(Intercept) PC1 PC5 PC9 PC11 559.71605128 -0.08704635 -0.21421214 0.20201382 0.24163381
```

The Table 11 shows the results of forward and cross-validation selection selected components in Table 1 to build Linear Regression for predicting Math Test-Score of 5<sup>th</sup> Students. 4 components model is the best of RMSE (96.09219)

**Table 11:** Results of forward model of Math Test-Score of 5<sup>th</sup> Students in PC components.

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        100.21841
        0.07006293
        79.10578
        8.195330
        0.05217892
        5.967139

        2
        99.02113
        0.08875416
        78.33870
        8.197846
        0.06339281
        5.559570

        3
        97.44128
        0.11793031
        76.20717
        6.992255
        0.06311165
        4.684722

        4
        4
        96.09219
        0.14907552
        74.81418
        5.787025
        0.06981308
        3.792256

        5
        97.28130
        0.12961267
        76.34853
        5.747483
        0.05800471
        3.769499

        6
        97.46429
        0.13108643
        76.89683
        5.511873
        0.06618614
        4.099125

        7
        98.21754
        0.12595414
        77.32494
        6.389539
        0.06692107
        4.179753

        8
        98.91907
        0.11580723
        77.56019
        6.577798
        0.06497193
        4.679645

        9
        98.98902
        0.11466278
        77.50506
        6.117475
        0.06720056
        5.052643

        11
        19.63851
```

**Table 13:** Results of stepwise model of Math Test-Score of 5<sup>th</sup> Students in PC components

```
x RMSE Rsquared MAE RMSESD RsquaredSD 1 100.06850 0.07869022 79.30278 11.19017 0.07472971
          nvmax
                                                                                                                                                                                                                          MAESD
                                100.068500.0786902279.3027811.190170.074729718.16338397.777480.1146501177.2917710.951210.083637998.11224696.402220.1356908975.3627910.739750.068440687.89356695.340640.1580729174.4194810.822690.090088628.79029696.160610.1415870375.6186210.197310.085673268.33924696.700540.1353367676.2098111.391760.083894119.40780297.676070.1230331077.0289211.460800.081076319.39503997.740700.1255279177.1673511.616390.087636429.30806598.185990.1203029077.2396211.511350.085050909.44586698.291460.1208492377.4362911.670900.085163519.19161498.690970.1204785277.5756811.993460.091075789.71700998.150930.1288695377.4771012.487680.0976637110.06270697.725380.1359021876.6644311.706810.101957589.80617297.731780.1357756976.9833212.537490.1013367310.25249596.288240.1552879276.7841412.585420.1038936310.461150
8.163383
                    11
12
13
                    14
15
                                                                                                      76.78414 12.58542 0.10389363
76.30609 11.76927 0.10600718
76.44116 12.44195 0.10709067
76.14088 12.18853 0.09966096
75.94117 12.01559 0.10330157
                                  96.28824 0.15528792
                                                                                                                                                                                                            10.461150
                                  96.57147 0.14759883
                                                                                                                                                                                                            10.068378
                                 96.87537 0.14844220
96.48003 0.15041375
96.38716 0.15237977
                                                                                                                                                                                                            10.465150
                                                                                                                                                                                                            10.183883
                                                                                                                                                                                                            10.021401
20
21
                                  96.27260 0.15472796 76.03420 12.04764 0.10189080 10.036254
                                  96.03794 0.15814633 75.82648 12.09046 0.10520277
```

Table 14 demonstrate the final selected components of stepwise selection method and its coefficients

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Table 14: Coefficient of the final stepwise model of

Math Test-Score of 5<sup>th</sup> Students in PC components

```
(Intercept) PC1 PC5 PC9 PC11 559.71605128 -0.08704635 -0.21421214 0.20201382 0.24163381
```

In conclusion, we choose the final forward model which has the least RMSE (95.34064) and contains 4 components PC1, PC5, PC9, PC11.

The table 15 shows the results of backward and cross-validation selection selected components in Table 2 to build Linear Regre ssion for predicting English Test-Score of 9<sup>th</sup> Students. 6 components are needed of the least of RMSE (77.76025).

Table 15: Results of backward model of English

Test-Score of 9th Students in PC components

```
Rsquared
                                                                                    MAE
                                                                                                   RMSESD RsquaredSD
                     85.28169 0.1480245 68.67041 8.268766 0.09312030 5.325685
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
                 2 81.36258 0.2187112 65.11461 9.686505 0.07565153 6.720911 3 79.17925 0.2610016 61.87381 9.949617 0.07780383 6.848879
                     79.17925 0.2610016 61.67561 9.949617 0.07760365 6.648879
79.21875 0.2614623 61.23573 8.689928 0.08814831 6.367174
78.32412 0.2833912 60.89147 8.408060 0.09281516 6.147927
77.76025 0.2942341 60.57744 8.837714 0.10673730 6.467278
77.94685 0.2943438 60.46019 8.471639 0.10960410 6.513004
78.18706 0.2908940 60.46895 8.149398 0.11043535 6.307359
                      78.56176 0.2885914 60.91781 8.307626 0.11109396 6.677555
              10 78.49018 0.2895448 60.80013 8.178019 0.11038872 6.435227 11 78.19256 0.2930042 60.65591 8.377416 0.11661968 6.670378 12 78.29851 0.2923026 60.58421 8.236996 0.11366252 6.443165 13 78.14640 0.2941156 60.23703 8.362382 0.11224854 6.663978 14 78.24323 0.2947078 60.29988 8.345027 0.11319485 6.578437 15 78.40413 0.2055791 60.10677 8.389032 0.11215507 6.607876
              15 78.19413 0.2955781 60.19677 8.389032 0.11215507 6.607876
16 78.16327 0.2969160 60.17937 8.617648 0.11565371 6.694002
17 78.12013 0.2973635 60.14938 8.560783 0.11497305 6.641787
18
19
                     78.17102 0.2964813 60.19879 8.482851 0.11432714 6.473366
               18
               19 78.23319 0.2949015 60.28956 8.481419 0.11353296 6.474378
20
21
               20 78.29399 0.2937026 60.36460 8.462719 0.11294748 6.481274
21 78.28903 0.2937634 60.35175 8.484047 0.11270726 6.478729
```

Table 16 demonstrate the final selected components of backwar d selection method and its coefficients

Table 16: Coefficient of the final backward model

of English Test-Score of 9th Students in PC

# components

```
(Intercept) PC1 PC2 PC4 PC5 P
C13
569.6981282 0.1360242 -0.1458360 -0.2442379 0.1372645 -0.2448
093
PC14
```

Education Test-Score Performance of 5'th and 9'th Grade Students 0.1810908

Table 17 shows the results of forward and cross-validation selection selected components in Table 2 to build Linear Regression for predicting English Test-Score of 9<sup>th</sup> Students. 6 components are needed in this model (RMSE 77.97222).

**Table 17:** Results of forward model of English Test-Score of 9<sup>th</sup> Students in PC components

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        85.28920
        0.1409968
        68.54569
        5.143737
        0.07823997
        3.874187

        2
        81.64255
        0.2112024
        65.08462
        5.476656
        0.05414014
        4.360349

        3
        79.64300
        0.2467383
        62.05230
        4.666330
        0.06251127
        3.234825

        4
        479.84598
        0.2459529
        62.10365
        5.053006
        0.06228841
        4.792017

        5
        78.62984
        0.2684990
        61.37811
        5.912154
        0.06834434
        4.268568

        6
        6.77.97222
        0.2812579
        60.76455
        6.130001
        0.08354894
        3.104288

        7
        78.46690
        0.2742488
        61.16246
        5.838930
        0.0893520
        3.782475

        8
        78.51582
        0.2730709
        60.81638
        5.905747
        0.07902626
        3.790873

        9
        78.94487
        0.2662659
        61.21122
        5.752218
        0.08906611
        4.170326

        10
        10.78.96078
        0.2659723</td
```

Table 18 demonstrate the final selected components of forward s election method and its coefficients

Table 19: Coefficient of the final forward model of

English Test-Score of 9th Students in PC components

```
(Intercept) PC1 PC2 PC4 PC5 P
C13
569.6981282 0.1360242 -0.1458360 -0.2442379 0.1372645 -0.2448
093
PC14
0.1810908
```

Table 20 shows the results of stepwise and cross-validation selection selected components in Table 2 to build Linear Regression for predicting English Test-Score of 9<sup>th</sup> Students. 8 components are needed

Education Test-Score Performance of 5'th and 9'th Grade Students in this model (RMSE 80.71882).

Table 20: Results of stepwise model of English

Test-Score of 9th Students in PC components

```
nvmax
                                       Rsquared
                                                                                 RMSESD RsquaredSD
              1 88.45349 0.1195927
                                                         70.98897 4.702926 0.04694936
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
                  85.53998 0.1761458 67.85792 4.195741 0.04415421 84.53518 0.1964037 66.19847 4.326775 0.04620185
                  81.97259 0.2426336 63.62408 4.229900 0.04481868 81.22778 0.2578074 62.78268 4.180097 0.05472817 81.05256 0.2590987 62.71290 4.032250 0.05068150 80.82019 0.2631758 62.49511 3.918797 0.04735428
            8 80.71882 0.2659181 62.22332 3.878313 0.04801722
9 80.86121 0.2639786 62.30322 4.051296 0.04928048
10 80.90657 0.2638732 62.48018 3.766517 0.04685998
            11 81.02113 0.2636224 62.59835
                                                                            3.557124 0.04532394
            12 81.12197 0.2626455 62.44510
                                                                            3.734041 0.04856843
                  81.31419 0.2606855 62.61493 3.804759 0.04785981
81.09441 0.2650468 62.49932 3.848097 0.04870306
81.36930 0.2605194 62.72036 3.731707 0.04866247
            13
                                                                            3.804759 0.04785981
                  81.31131 0.2614763 62.72472
                                                                            3.857385 0.04932435
17
18
19
            17 81.39839 0.2604661 62.73735 3.600256 0.04687415 18 81.28642 0.2622881 62.70896 3.557902 0.04424472 19 81.57593 0.2581671 62.91341 3.697362 0.04736706
            20 81.45852 0.2598790 62.79378 3.580937 0.04551606 2.515857 21 81.58829 0.2578504 62.89954 3.612163 0.04708022 2.551320
20
```

Table 21 demonstrate the final selected components

of stepwise selection method and its coefficients

**Table 21:** Coefficient of the final stepwise model of English Test-Score of 9<sup>th</sup> Students in PC components

```
(Intercept) PC1 PC2 PC4 PC5
569.69812821 0.13602418 -0.14583599 -0.24423790 0.13726449
PC8 PC12 PC13 PC14
-0.07578535 -0.10582892 -0.24480927 0.18109081
```

In conclusion, we choose the final backward model as it has the smallest RMSE (77.76025). The components in the model are PC1, PC2, PC4, PC5, PC13, PC14.

Table 22 shows the results of backward and cross-validation selection selected components in Table 2 to build Linear Regression for predicting Math Test-Score of 9<sup>th</sup> Students. 9 components are needed in this model (RMSE 80.35818).

Education Test-Score Performance of 5'th and 9'th Grade Students

# Table 23: Results of backward model of Math Test-

# Score of 9th Students in PC components

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        86.61905
        0.08838282
        70.16967
        8.916355
        0.08379421
        6.018933

        2
        86.05953
        0.107999999
        69.62089
        8.315134
        0.10132680
        6.179503

        3
        82.37378
        0.17656451
        66.71979
        8.449121
        0.12907457
        6.177415

        4
        4
        82.60273
        0.17328369
        66.35621
        8.802955
        0.10783052
        6.883909

        5
        81.97697
        0.18072769
        65.77462
        8.781503
        0.10337419
        6.837692

        6
        81.31255
        0.19093902
        64.79582
        8.389556
        0.08443144
        6.691995

        7
        7
        81.13567
        0.19347098
        64.57744
        8.529121
        0.09646791
        6.881678

        8
        80.51690
        0.20549483
        64.06610
        8.451665
        0.09427312
        6.644490

        9
        80.35818
        0.21052469
        64.05343
        8.032127
        0.09290158
        6.212958

        10
```

Table 24 demonstrate the final selected components

of backward selection method and its coefficients

**Table 24:** Coefficient of the final backward model of Math Test-Score of 9<sup>th</sup> Students in PC components

```
(Intercept) 570.92587179
                                      -0.12082020
                           0.06704708
              0.09737530
                                                   -0.18917357
                          PC10
-0.18692333
  0.12681604
             -0.09732012
                                      -0.33517383
                                                   -0.17984686
Table 25 shows the results of forward and cross-
validation selection selected components in Table 2
            Linear Regression for predicting Math
to build
Test-Score of 9th Students. 10 components are
needed in this model (RMSE 79.48384).
```

**Table 25:** Results of forward model of Math Test-Score of 9<sup>th</sup> Students in PC components

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        1 86.35520
        0.09014796
        70.04132
        9.214665
        0.05927938
        7.109982

        2
        2 85.67687
        0.10778112
        69.65767
        10.053312
        0.06782506
        8.011263

        3
        81.88236
        0.18370764
        66.51875
        10.372311
        0.11141956
        7.585704
```

```
ducation Test-Score Performance of 5'th and 9'th Grade Students

4 82.03329 0.18471249 66.28073 11.974610 0.13963202 8.169939

5 81.10020 0.20606573 65.00670 11.832219 0.14315724 7.781366

6 80.72247 0.21582896 64.54613 12.934825 0.14907727 9.053441

7 79.79960 0.23528412 63.90916 14.117805 0.15892611 10.092347

8 79.71411 0.23860198 63.82294 14.399842 0.16212421 10.645845

9 79.52656 0.24389127 63.79337 14.921217 0.16996146 10.878043

10 79.48384 0.24484404 63.93563 14.651943 0.16886484 10.504987

11 80.01956 0.23753581 64.30549 14.980909 0.16788803 11.026557

12 80.74227 0.22585550 64.81327 14.790117 0.16461499 10.936580

13 80.87673 0.22460330 64.71808 14.997887 0.16478747 10.581737

14 81.04304 0.22276953 64.76190 15.236947 0.16854222 10.642746

15 80.95860 0.22180425 64.60110 14.808942 0.16763329 10.266136

16 80.69522 0.22659811 64.32692 14.988909 0.17313255 10.519086

17 80.61007 0.22608548 64.26027 14.786588 0.17234502 10.328869

18 80.59294 0.22657984 64.17223 14.882774 0.17213744 10.354995

19 80.35089 0.23074334 64.02437 14.915293 0.17300357 10.363358

20 80.29797 0.23158221 64.00685 14.951378 0.17427888 10.354763

21 80.31317 0.23152958 64.04069 14.987441 0.17505432 10.348666
                                Education Test-Score Performance of 5'th and 9'th Grade Students
4
5
6
7
8
9
10
11
12
 13
14
15
16
17
  18
  \overline{19}
  20
```

Table 26 demonstrate the final selected components

of forward selection method and its coefficients

Table 26: Coefficient of the final forward model of

Math Test-Score of 9<sup>th</sup> Students in PC components

```
(Intercept) 570.92587179
                   PC1
0.09737530
                                                     PC3
-0.12082020
                                     PC2
0.06704708
                                                                                PC4
                                                                      -0.18917357
                                   PC10
-0.18692333
                                                    PC13
-0.33517383
                  PC7
-0.09732012
  0.12681604
                                                                        0.12313019
          PC15
 -0.17984686
```

Table 27 shows the results of stepwise and crossvalidation selection selected components in Table 2 Linear Regression for predicting Math to build Test-Score of 9th Students. 18 components are needed in this model (RMSE 79.78152).

Table 27: Results of stepwise model of Math Test-

Score of 9th Students in PC components

```
1 86.43205 0.08573114 70.02955
2 85.42742 0.11965138 69.93064
                                                                    8.934835 0.06713726 7.460598
9.370081 0.10684523 7.980978
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
               82.26320 0.19392887 66.83284 10.216504 0.16103730
               83.16777 0.16937173 67.15976 10.124999 0.14901429 82.07765 0.18680495 65.79757 10.313604 0.15710132 81.17960 0.19633828 64.76771 9.525427 0.14942440
                                                                                                      8.666823
               82.57161 0.16486655 65.59312
80.55391 0.20279221 63.85081
                                                                    8.614358 0.08083108
                                                                                                       7.086247
                                                                    8.497812 0.14536252
                                                                    8.378914 0.12290692 6.002085
               81.12678 0.19268630 64.52707
                                                                   9.341687 0.13422655 6.494646
9.182065 0.11996531 6.222929
          10 80.16603 0.22168738 64.02244
11 80.83249 0.20355544 64.57691
          12 80.38687 0.21005972 63.98804
                                                                    9.124550 0.11346919 6.180886
              80.30237 0.21250324 64.05834
79.93851 0.21859404 63.46475
80.41956 0.21237081 63.65593
                                                                   9.175064 0.11876128 6.405913
8.789277 0.11391868 6.520982
                                                                   9.420138 0.11576576 6.920425
```

Table 28 demonstrate the final selected components of stepwise selection method and its coefficients

Table 28: Coefficient of the final stepwise model of

# Math Test-Score of 9th Students in PC components

```
PC2
0.06704708
(Intercept) 570.92587179
                 PC1
0.09737530
                                                                     PC4
                                              -0.12082020
                                                             -0.18917357
          PC5
                                        PC8
                               -0.04339513
  0.12681604
                -0.09732012
                                              -0.03333017
                                                             -0.18692333
         PC11
                        PC12
                                       PC13
                                                      PC14
  0.04179846
                 0.08572502
                               -0.33517383
                                               0.12313019
                                                             -0.17984686
         PC17
                        PC18
                                       PC20
 -0.06458521
                                0.10570962
                 0.07227643
                                               0.12204899
```

In conclusion, we choose the final forward model which has the smallest RMSE (79.48384). st The components needed in the model are PC1, PC2, PC3, PC4, PC5, PC7, PC10, PC13, PC14, PC15

For the next step, it is reasonable to consider the real factors, then we focus on the original survey data and use above methods to seek the most important factors that influence the academic performance of students and make comparison with above PC models.

The Table 29 shows the results of backward and cross-validation selection to the survey data build Linear Regression for predicting English and Test-Score of 5<sup>th</sup> students. It seems that 8 variables are the best model of smallest RMSE (96.43758).

**Table 29:** Results of backward model of English Test-Score of 5<sup>th</sup> Students in original data

```
Education Test-Score Performance of 5'th and 9'th Grade Students
                                                                         RMSESD RsquaredSD
8.242044 0.09039469
                          RMSE
                                    Rsquared
                106.58521 0.1039808 86.87436
100.23835 0.2107657 81.06385
98.13572 0.2362969 78.91889
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
                                                                                                                 7.417611
                                                                         9.227429 0.11314422
8.405403 0.09834229
                                                                                                                7.409915
                                                                                                                 7.876471
                  98.74595 0.2284293 80.13387
98.43746 0.2339547 79.57072
98.10340 0.2406705 79.62609
                                                                         7.603703 0.08603540
                                                                                                                7.465112
                                                                                                                8.423673
                                                                         9.322027 0.11206176
                                                                       10.269334 0.12358725
                                                                                                               10.454661
                  96.88159 0.2576293 78.57878 10.020870 0.11890374
                                                                                                                9.984546
                                                                                                                9.400638
                  96.43758 0.2632854 78.41362
                                                                         9.519453 0.10988767
                  96.90991 0.2574095
97.16982 0.2533058
                                                      78.72076 9.524241 0.10908784 78.69054 10.246976 0.11765243
                                                                                                                9.565543
           10
                                                                                                               10.245334
           11
                  96.78307 0.2578848 78.51757
                                                                       10.292177 0.11944186
                                                                                                               10.117902
                  97.22296 0.2519995 78.80660 10.435047 0.12229329 97.46067 0.2503018 78.90756 10.640954 0.12503455 97.80197 0.2466426 79.44032 10.332058 0.12086584 97.51163 0.2485661 79.53833 10.405177 0.12277524 97.49860 0.2495965 79.70033 10.475061 0.12437897
                                                                                                               10.241302
                                                                                                               10.457748
                                                                                                               10.236866
                                                                                                               10.339334
           16
17
                                                                                                               10.611861
                  97.28353 0.2531286 79.56457 10.631252 0.12784588 10.877511
                  97.27596 0.2529997 79.52118 10.616188 0.12765872 97.33461 0.2524063 79.60462 10.769907 0.13009650 97.49119 0.2509441 79.57425 11.113977 0.13387351 97.90660 0.2460191 79.776508 10.949817 0.1385690
           18
19
18
19
20
21
22
23
24
25
26
                                                                                                              10.799715
                                                                                                               10.978440
           20
                                                                                                              11.106607
                                                                                                              11.026393
                  98.13650 0.2434011 79.96609 10.798086 0.12856999
                                                                                                               10.866242
                  98.41039 0.2400690 80.15245 10.803643 0.12763852 98.32588 0.2416834 80.04255 10.770348 0.12760130 98.39385 0.2409276 80.08634 10.775847 0.12765532 98.49455 0.2397761 80.16953 10.851972 0.12865248
                                                                                                              10.897287
                                                                                                               10.858942
                                                                                                               10.866819
                  98.59462 0.2386775 80.26884 10.888720 0.12904477 98.61359 0.2384379 80.30859 10.897059 0.12912645
                                                                                                              10.948998
10.953593
```

Table 30 demonstrate the final selected factors of backward selection method and its coefficients

**Table 30:** Coefficient of the final backward model of English Test-Score of 6<sup>th</sup> Students in original survey

```
(Intercept)
                                 ATTITUDE_ENG.5
                    49.8582009
                                                     0.1819962
               INTEREST_ENG.5
                                            HOMEWOK_CORR_MATH
                     0.1873185
                                                     0.3371550
SATISIFACTION_LEARNING_ENG.5
                                         STUDYINTEREST_MATH.5
                     0.1182473
                                                    -0.2147371
                                            MATH_ENG_STRESS_
    STEP_CLASSMATERELATION.5
                     8.9060675
                                                     0.2077809
                   HARD_WORK.5
                     0.\overline{1}280441
```

Table 31 shows the results of forward and cross-validation selection to the survey data build Linear Regression for predicting English and Test-Score of 5<sup>th</sup> students. It seems that 8 variables are the best model of smallest RMSE (96.77736).

**Table 31:** Results of forward model of English Test-Score of 5<sup>th</sup> Students in original data

```
Education Test-Score Performance of 5'th and 9'th Grade Students
             RMSE
106.30717
                                                          RMSESD RsquaredSD 6.927372 0.0911321
                             Rsquared
                            0.1171712
                                           86.93493
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
                                                                        0.0911321
             100.08169 0.2083530 81.39738
97.85771 0.2378998 79.26678
                                                          7.746306
                                                                        0.1240913
                                                                                       8.324279
                                                          7.904563
                                                                        0.1260353 7.083754
                                                          7.558966
              97.21636 0.2476375
                                          78.90874
                                                                        0.1129801 6.881921
              97.55525 0.2440499
97.24456 0.2480859
                                          78.86344
                                                          8.629339
                                                                        0.1171077
                                                                                       7.769884
                                                          8.476099
                                                                        0.1168628
                                                                                       6.651940
                                          78.77327
              96.91210 0.2516047
                                          79.05892
                                                          8.607947
                                                                        0.1207315
                                                                                       6.882358
              96.77736 0.2562212 78.61978
                                                          9.181956
                                                                        0.1254442
              97.07803 0.2519545
97.25485 0.2505275
                                           78.86226
                                                         9.074029
                                                                        0.1189595
                                                                                       7.269339
7.646306
         10
                                                                        0.1195899
                                           78.93747
                                                          9.321167
         11
              97.57657 0.2459504
                                                                        0.1172007
                                                                                       7.499377
                                          79.31271
                                                          9.294660
         12
13
                                                                                       7.632558
               98.30904 0.2383083
                                          79.86459
                                                          9.613623
                                                                        0.1223096
                                                                                       7.759900
              98.33550 0.2360939
                                          79.74850
                                                          9.600776
                                                                        0.1271879
              98.50140 0.2338908 79.92396
98.83388 0.2291880 80.08811
99.09289 0.2276387 80.31254
98.89793 0.2301952 80.10063
         14
15
                                                          9.581175
                                                                        0.1259255
                                                                                       7.908688
                                                          9.469823
                                                                        0.1260934
         16
17
                                                          9.804669
                                                                        0.1271221
                                                                        0.1267469
                                                          9.678079
         18
19
              99.23824 0.2265772 80.33400
99.17398 0.2272624 80.34522
18
19
20
21
22
23
24
25
26
                                                          9.952459
                                                                        0.1325702
                                                        10.016959
                                                                        0.1330442
         20
              99.38490 0.2240229 80.61422
                                                          9.568986
                                                                        0.1282752
         21
22
23
24
25
              99.62286 0.2215631 80.79415
                                                          9.568932
                                                                        0.1288395
                                                                                       7.270145
              99.62286 0.2215631 80.79415
99.48924 0.2234206 80.71797
99.69251 0.2212366 80.92967
99.67556 0.2218358 80.89863
99.72543 0.2213029 80.97170
99.77473 0.2207483 80.98516
                                                         9.519316
                                                                        0.1280629
                                                                                       7.240697
                                                         9.520207
9.598906
                                                                        0.1275483
                                                                                       7.264241
                                                                        0.1274400
                                                                                       7.335090
                                                                        0.1275898
                                                          9.604033
                                                                                       7.307681
                                                          9.583947
                                                                        0.1273151
                                                                                       7.314609
                                                                        0.1278210 7.326661
0.1278557 7.343408
              99.78450 0.2207044 80.98245
99.79782 0.2205729 80.98797
                                                         9.624207
9.631359
```

Table 32 demonstrate the final selected factors of

forward selection method and its coefficients

**Table 32:** Coefficient of the final forward model of English Test-Score of 6<sup>th</sup> Students in original survey

```
(Intercept) ATTITUDE_ENG.5
49.8582009 0.1819962
INTEREST_ENG.5 HOMEWOK_CORR_MATH
0.1873185 0.3371550
SATISIFACTION_LEARNING_ENG.5 STUDYINTEREST_MATH.5
0.1182473 -0.2147371
STEP_CLASSMATERELATION.5 MATH_ENG_STRESS_5
8.9060675 0.2077809
HARD_WORK.5
0.1280441
```

Table 33 shows the results of stepwise and cross-validation selection to the survey data build Linear Regression for predicting English and Test-Score of 5<sup>th</sup> students. It seems that 11 variables are the best model of smallest RMSE (97.35267).

**Table 33:** Results of stepwise model of English Test-Score of 5<sup>th</sup> Students in original data

```
Education Test-Score Performance of 5'th and 9'th Grade Students
                RMSE Rsquared MAE RMSESD RsquaredSD 107.31442 0.08970171 87.78679 6.421076 0.06696958 100.80395 0.19618096 81.47100 5.713018 0.09310510 99.17176 0.22712826 80.10917 6.931000 0.11455012
                                                                                                                         MAESD
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
                                                                                                                    5.348012
                                                                                                                    5.192990
                                                                                                                   6.785977
                99.06281 0.22583880 80.07863 7.387891 0.12153159 98.71517 0.23545123 79.55295 6.564105 0.12375192 99.08423 0.22403914 80.52927 5.881021 0.11509610 100.61091 0.20486279 82.79300 4.498962 0.09101214
                                                                                                                   7.892417
                                                                                                                   7.727642
                                                                                                                   7.076667
                                                                                                                   6.258348
                   98.70979 0.23854293 79.24878 7.987741 0.12350188
                   99.16862 0.23310794 80.67195 7.448768 0.11306046 97.96078 0.25025876 79.01075 6.600477 0.11084849
                                                                                                                   8.430625
            10
                                                                                                                   8.385936
           11
                   97.35267 0.25998953
                                                         78.65302 7.407283 0.12805874
                                                                                                                   9.004991
                                                                                                                   8.889582
                   97.63480 0.25827711
97.71851 0.25877942
                                                         79.23945 7.589932 0.12269442 79.58047 8.030621 0.13194950
                                                                                                                   9.791784
                  97.78083 0.26034700 79.65571 8.039742 0.13194388 98.71161 0.24632680 80.34078 8.194157 0.13090487 98.64350 0.2477804 80.29825 8.0750480 0.12691504
                                                                                                                 10.108107
                                                                                                                 10.072346
                                                                                                                 10.081598
                   97.90761 0.25253874 79.27122 6.979046 0.12379263
                                                                                                                   8.793556
                  98.80942 0.24706329 80.25638 8.846062 0.12843897 98.57317 0.24886272 79.86715 8.572390 0.12902599 98.65660 0.24838634 79.98866 8.742316 0.13344223
           18
19
18
19
20
21
22
23
24
25
26
                                                                                                                 10.763212
                                                                                                                 10.261283
           20
21
22
23
24
25
                                                                                                                 10.441710
                   99.03078 0.24338319
                                                         80.20378 8.766265 0.13143375
80.04574 8.732415 0.13091286
                                                                                                                 10.561089
                   98.72252 0.24743645
                                                                                                                 10.620652
                   99.03841 0.24209092 80.50304 8.178682 0.12864718 99.09784 0.24218270 80.53874 8.707378 0.13131835 99.18690 0.24237137 80.59237 8.836278 0.13165297
                                                                                                                   9.919866
                                                                                                                 10.595587
                                                                                                                 10.640286
                   98.98722 0.24154833 80.24436 8.124911 0.12735063
                   99.36209 0.23956911 80.58668 8.728395 0.12956643 10.700425 99.32981 0.23926315 80.51570 8.689642 0.12966466 10.671424
```

Table 34 demonstrate the final selected factors of stepwise selection method and its coefficients

**Table 34:** Coefficient of the final stepwise model of English Test-Score of 5<sup>th</sup> Students in original survey

```
(Intercept)
                           ATTITUDE_ENG.5
               56.41149441
                                               0.17516942
            INTEREST_ENG.5
                                       CAMPUS CONDITION.5
                0.19882367
                                               -0.09737558
         HOMEWOK_CORR_MATH SATISIFACTION_LEARNING_ENG.5
                0.34965731
                                               0.12199143
      STUDYINTEREST_MATH.5
                                STEP_CLASSMATERELATION.5
                                               9.74382049
                -0.18384490
                                          SOCIAL_MORALS.5
         MATH_ENG_STRESS_5
                0.20076194
                                               0.12718986
               HARD_WORK.5
                                                  AWARE.5
                                              -0.09949934
                0.13672720
```

In conclusion, we choose the final backward model which has the smallest RMSE (96.43758) e. The factors in this model are ATTITUDE\_ENG.5, INTEREST\_ENG.5, HOMEWOK\_CORR\_MATH, SATISIFACTION\_LEARNING\_ENG.5, STUDYINTEREST\_MATH.5,

Education Test-Score Performance of 5'th and 9'th Grade Students STEP CLASSMATERELATION.5,

MATH\_ENG\_STRESS\_5, HARD\_WORK.5.

Table 35 shows the results of backward and cross-validation selection to the survey data build Linear Regression for predicting English and Test-Score of 9<sup>th</sup> students. It seems that 21 variables are the best model of smallest RMSE (80.21411).

**Table 35:** Results of backward model of English Test-Score of 9<sup>th</sup> Students in original data

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        1
        83.66072
        0.1794085
        66.36241
        9.796247
        0.10192285
        6.638337

        2
        2
        84.00385
        0.1845479
        66.32792
        10.245981
        0.10056032
        7.043160

        3
        3
        82.79470
        0.2148798
        65.49425
        10.564889
        0.11787272
        6.959261

        4
        4
        82.83267
        0.2140188
        65.11660
        10.143914
        0.10661602
        6.174797

        5
        82.91717
        0.2089214
        65.02339
        9.817277
        0.10193166
        5.583376

        6
        6
        82.04321
        0.2237993
        64.20846
        9.274375
        0.10494245
        5.117426

        7
        7
        81.57647
        0.2267652
        63.93766
        8.767673
        0.09318010
        5.155877

        8
        81.19701
        0.2403731
        63.42235
        10.098583
        0.09735923
        5.924977

        9
        80.98055
        0.2421854
        63.15793
        9.826191
        0.08613078
```

Table 36 demonstrate the final selected factors of

backward selection method and its coefficients

**Table 36:** Coefficient of the final backward model of English Test-Score of 9<sup>th</sup> Students in original survey

(Intercept)

```
Education Test-Score Performance of 5'th and 9'th Grade Students
                   31.45910460
INTEREST_ENG.9
0.19943074
                                                               0.10096977
                                                   CLASSMATERELATION.9
                                                              -0.05554998
              CAMPUS_CONDITION.9
                                                  STUDYATTITUDE_MATH_9
                                                               0.1\overline{0}3911\overline{1}0
                       -0.07246136
SATISIFACTION_LEARNING_MATH.9
0.11354915
                                                         THR_MATH_NEW.9
0.04131804
              PISA_12_ST81_ENG.9
                                       SATISIFACTION_LEARNING_ENG.9
                        0.05\overline{122670}
                                                               0.08139264
                   STRATEGE_ENG.9
0.13557745
                                                    HOMEWOK_CORR_ENG.9
-0.10401341
      STEP_CLASSMATERELATION.9
                                                      MATH_ENG_STRESS_9
                       -8.61765196
                                                               0.09099346
                         MANNERS.9
                                                        SOCIAL_MORALS.9
                       -0.17728490
                                                               0.14382921
                    SENSE_HONOR.9
0.09418611
                                                             HARD_WORK.9 -0.10764102
       SOLIDARITY_FRIENDSHIP.9
                                                            MORAL_DUTY.9
                        0.06082465
                                                              -0.1\overline{3}292568
                   GRA_GEOMETRY.9
                                                      SELF_PROTECTION.9
                        0.19216913
                                                               0.28659911
```

Table 37 shows the results of forward and cross-validation selection to the survey data build Linear Regression for predicting English and Test-Score of 9<sup>th</sup> students. It seems that 26 variables are the best model of smallest RMSE (78.36493).

**Table 37:** Results of forward model of English Test-Score of 9<sup>th</sup> Students in original data

```
max RMSE Rsquared MAE RMSESD RsquaredSD 1 84.87665 0.1449221 67.60884 10.93630 0.04946970 2 83.35106 0.1716555 66.22292 11.19073 0.06904395 3 81.81599 0.2016933 64.78513 10.37354 0.07641515 4 81.68481 0.2101377 64.06949 10.53578 0.09577533 5 80.99181 0.2245732 63.13413 10.84498 0.10397591 6 80.63301 0.2310784 63.20841 10.95601 0.09248901 7 80.47836 0.2395280 63.34736 11.74061 0.10994278 8 80.38441 0.2403015 63.11657 12.84157 0.12377686 9 80.01220 0.2474213 62.58371 12.41130 0.10976454 10 80.00599 0.2491695 62.60430 12.26842 0.10788574 11 79.55687 0.2573135 62.27539 11.99599 0.10661347 12 79.11081 0.2659141 61.72775 12.30943 0.10931340 13 79.13310 0.2659344 61.94633 12.38770 0.11553588 14 79.07023 0.2680414 61.77795 12.81478 0.11979917 15 79.37241 0.2629374 62.15111 12.64110 0.11436678 16 79.13385 0.2666728 62.09189 12.82707 0.11547219 17 79.08544 0.2676876 62.01848 12.86080 0.11284603 18 79.01369 0.2683984 61.90507 12.74055 0.11337351 19 78.92952 0.2703610 61.81745 12.48284 0.11011917
                                                                                                                                                                                                                                                                                                                                                                                                          MAESD
1234567891112111119222234567
                                                                                                                                                                                                                                                                                                                                                                                      8.309408
                                                                                                                                                                                                                                                                                                                                                                                      8.021495
                                                                                                                                                                                                                                                                                                                                                                                      7.435379
8.361769
                                                                                                                                                                                                                                                                                                                                                                                      8.029456
                                                                                                                                                                                                                                                                                                                                                                                      8.418503
9.304061
                                                                                                                                                                                                                                                                                                                                                                                      9.120365
                                                                                                                                                                                                                                                                                                                                                                                      9.129555
                                                                                                                                                                                                                                                                                                                                                                                      9.102346
                                                                                                                                                                                                                                                                                                                                                                                      9.420362
                                                                                                                                                                                                                                                                                                                                                                                10.193396
                                                                                                                                                                                                                                                                                                                                                                               10.009457
                                                                                                                                                                                                                                                                                                                                                                               10.100585
                                                                                                                                                                                                                                                                                                                                                                                      9.942078
                                                                                                                                                                                                                                                                                                                                                                                      9.633711
                                     18 79.01369 0.2683984 61.90507 12.74055 0.11337351
19 78.92952 0.2703610 61.81745 12.48284 0.11011917
20 78.79081 0.2720974 61.79074 12.64931 0.11135627
21 78.65291 0.2737143 61.57654 12.72735 0.11369148
22 78.51893 0.2758123 61.45049 12.72541 0.11537376
23 78.46572 0.2769493 61.41728 12.61349 0.11394195
24 78.41849 0.2778227 61.34176 12.46344 0.11429563
25 78.51376 0.2763176 61.39025 12.53534 0.11397577
26 78.36493 0.2786878 61.23748 12.58323 0.11426675
27 78.42621 0.2777642 61.25356 12.50793 0.11310266
                                                                                                                                                                                                                                                                                                                                                                                      9.260420
                                                                                                                                                                                                                                                                                                                                                                                      9.337116
                                                                                                                                                                                                                                                                                                                                                                                     9.273431
9.233260
9.171985
                                                                                                                                                                                                                                                                                                                                                                                      9.093743
                                                                                                                                                                                                                                                                                                                                                                                      9.200404
9.139537
```

Education Test-Score Performance of 5'th and 9'th Grade Students 28 28 78.42501 0.2777337 61.27290 12.49813 0.11293132 9.123987 Table 38 demonstrate the final selected factors of forward selection method and its coefficients

**Table 38:** Coefficient of the final forward model of English Test-Score of 9<sup>th</sup> Students in original survey

```
(Intercept)
                                     ATTITUDE_ENG.9
                     53.96138580
                                                           0.10489767
                 INTEREST_ENG.9
0.20610078
                                                CLASSMATERELATION.9
                                                          -0.05703110
          STUDYINTEREST_MATH.9
                                                 CAMPUS_CONDITION.9
                     -0.04427702
          -0.0442//02
STUDYATTITUDE_MATH_9 SATISIFACTION_LEARNING_MATH.9
0.10359152 0.12533295
                                                          -0.06992796
                STRATEGY_MATH.9
                                                      THR_MATH_NEW.9
                      0.0\overline{3}798594
                                                           0.04638646
            PISA_12_ST81_ENG.9
                                                       THR_ENG_NEW.9
                      0.04566965
                                                          -0.02247754
SATISIFACTION_LEARNING_ENG.9
0.08174035
                                                      STRATEGE_ENG.9
0.12817481
            HOMEWOK_CORR_ENG.9
-0.09574697
                                          STEP_CLASSMATERELATION.9
                                                          -8.44138829
             MATH_ENG_STRESS_
                                                            MANNERS.9
                      0.09123170
                                                          -0.18712672
                SOCIAL_MORALS.9
                                                       SENSE_HONOR.9
                      0.13402812
                                                           0.09346656
                     HARD_WORK.9
                                           SOLIDARITY_FRIENDSHIP.9
                     -0.11522297
                                                           0.06090776
                   MORAL_DUTY.9 -0.14923905
                                                            THRIFTY.9
                                                           0.03512577
                                                      GRA_GEOMETRY.9
                        MP_ADD_9
                     -0.03\overline{304371}
                                                           0.19546438
             SELF_PROTECTION.9
                      0.28526181
```

Table 39 shows the results of stepwise and cross-validation selection to the survey data build Linear Regression for predicting English and Test-Score of 9<sup>th</sup> students. It seems that 21 variables are the best model of smallest RMSE (78.91380).

**Table 39:** Results of stepwise model of English Test-Score of 9<sup>th</sup> Students in original data

```
RMSE Rsquared
                                                   RMSESD RsquaredSD
nvmax
                                         MAE
            85.23346 0.1542071 67.49322
                                                     8.648361 0.07753360 6.286938
123456789
            85.10713 0.1519406 67.68731
                                                     8.632575 0.06517817
            84.33465 0.1755801 66.93217
                                                    9.217817 0.13196505
            84.21534 0.1829470 66.40881
82.73521 0.2038341 64.94619
                                                    9.362210 0.12514284
9.370806 0.11356263
            83.34975 0.1950204 65.79993
                                                     9.306528 0.10910582 7.051463
           82.08921 0.2192876 64.39764
82.23636 0.2150661 64.70252
80.68093 0.2384505 63.00174
                                                     8.547797 0.08125170 6.575521
                                                    9.551177 0.10687007 6.965613
8.058214 0.08364131 5.903869
```

Table 40 demonstrate the final selected factors of

stepwise selection method and its coefficients

**Table 40:** Coefficient of the final stepwise model of English Test-Score of 9<sup>th</sup> Students in original survey

```
(Intercept)
                                 ATTITUDE_ENG.9
                      31.45910460
                                                            0.10096977
                  INTEREST_ENG.9
0.19943074
                                                 CLASSMATERELATION.9
                                                           -0.05554998
                                                STUDYATTITUDE_MATH_9
             CAMPUS_CONDITION.9
                      -0.07246136
                                                            0.10391110
SATISIFACTION_LEARNING_MATH.9
                                                       THR_MATH_NEW.9
                       0.11354915
                                                            0.04131804
             PISA_12_ST81_ENG.9
                                      SATISIFACTION_LEARNING_ENG.9
                       0.05\overline{122670}
                                                            0.08\overline{1}39264
                  STRATEGE_ENG.9
                                                  HOMEWOK_CORR_ENG.9
                                                           -0.10\overline{401341}
                       0.13557745
                                                   MATH_ENG_STRESS_9
0.09099346
      STEP_CLASSMATERELATION.9
                      -8.61765196
                        MANNERS.9
                                                      SOCIAL_MORALS.9
                      -0.17728490
                                                            0.14382921
                   SENSE_HONOR.9
0.09418611
                                                           HARD_WORK.9
-0.10764102
       SOLIDARITY_FRIENDSHIP.9
                                                          MORAL DUTY.9
                                                           -0.1\overline{3}292568
                       0.06082465
                                                   SELF_PROTECTION.9
0.28659911
                  GRA_GEOMETRY.9
                       0.19216913
```

In conclusion, we choose the final forward model as it ha s the smallest RMSE (78.36493). The factors in this model are att itude\_eng.9, interest\_eng.9, classmaterelation.9, campus\_condition.9 studyattitude\_math\_9 satisifaction\_learning\_math.9 th r\_math\_new.9 pisa\_12\_st81\_eng.9 satisifaction\_learning\_eng.9 strat ege\_eng.9 homewok\_corr\_eng.9 step\_classmaterelation.9 math\_eng\_stress\_9 manners.9 social\_morals.9 sen se\_honor.9 hard\_work.9 solidarity\_friendship.9 gra\_geometry.9 self\_protection.9

# Analysis On Factors Impacting Education Test-Score Performance of 5'th and 9'th Grade Students

Table 41 shows the results of backward cross-validation selection to the survey data build Linear Regression for predicting Math and Test-Score of 5<sup>th</sup> students. It seems that 6 variables are the best model of smallest RMSE (97.39460).

**Table 41:** Results of backward model of Math Test-Score of 5<sup>th</sup> Students in original data

```
nvmax
                                                            RMSESD RsquaredSD
             97.84311 0.11057397 78.00083 10.444703 0.04765767
                                                                                       7.197569
1
2
3
4
5
6
7
8
9
10
             98.11514 0.10881457 78.18481
98.83029 0.09618406 78.30735
                                                       10.056523 0.04630274
10.428833 0.03470037
                                                                                       7.828095
7.964987
             97.63091 0.11549664 76.87042 10.328009 0.04001754 98.15626 0.11135593 77.72338 9.634991 0.04128930
                                          77.20906
78.04837
                                                         9.329619 0.05889646
9.728966 0.06396073
             97.39460 0.12858928
             98.76862 0.11731970
                                          78.13624
             98.85513 0.11971632
                                                         9.244026 0.06307340
             99.53307 0.11340007
                                                         9.213411 0.06727451
        10 98.71429 0.12573879 77.99611
                                                         9.108767 0.05310736 6.606173
        11 98.14475 0.13558487
12 97.90847 0.14064546
11
12
13
14
15
16
17
18
19
20
22
23
24
25
27
                                                         8.802768 0.05257514
                                                          8.983135 0.06282472
        13 97.77206 0.14606187 77.05637
                                                         9.224129 0.06913081
             97.51369 0.14998854 76.95643
                                                          9.309368 0.07352042 6.978320
            97.96107 0.14153042 77.28139
98.11947 0.13999476 77.33411
                                                         9.383429 0.06962861
                                                          9.729253 0.07139587
             98.11671 0.14207700 77.43305
                                                       9.916394 0.07424407
10.121400 0.07755527
            98.19225 0.14318964 77.48216
             98.24150 0.14310587 77.50424 10.225185 0.07873641
        20 98.12103 0.14324711 77.43616 10.199276 0.07529500 21 98.08640 0.14366128 77.48404 10.259192 0.07631502 22 98.00604 0.14507407 77.52704 10.188234 0.07812898
            97.98874 0.14556305 77.46869 10.156874 0.07907636
            97.96433 0.14657184 77.53188 10.249945 0.07921823 97.84625 0.14904226 77.44536 10.291282 0.08189763
            97.79083 0.14961190 77.35641
                                                        10.341521 0.08293871
         27 97.66617 0.15153394 77.21049 10.316422 0.08366140 7.562421 28 97.69557 0.15194422 77.25063 10.388463 0.08490681 7.651549
```

The Table 42 demonstrate the final selected factors

of backward selection method and its coefficients **Table 42:** Coefficient of the final backward model

of Math Test-Score of 5th Students in original survey

Education Test-Score Performance of 5'th and 9'th Grade Students 0.1674041 0.1143441 0.1680319

Table 43 shows the results of forward cross-validation selection to the survey data build Linear Regression for predicting Math and Test-Score of 5<sup>th</sup> students. It seems that 2 variables are the best model of smallest RMSE (97.61422).

**Table 43:** Results of forward model of Math Test-Score of 5<sup>th</sup> Students in original data

```
RMSE Rsquared MAE RMSESD RsquaredSD MAESD 1 97.83832 0.1049000 77.93062 10.264916 0.06116329 8.458077 2 97.61422 0.1141159 77.54858 10.502108 0.05497628 9.140548 3 98.25351 0.1042511 78.27758 10.262168 0.05870023 7.955360 4 98.15228 0.1161045 78.48255 10.727266 0.07124092 7.704065
       nvmax
1
2
3
4
5
6
7
8
9
10
11
12
13
                     98.91081 0.1066101 78.60514 10.778702 0.06829029 98.44168 0.1163322 78.37209 10.232613 0.07263986 98.61890 0.1156407 77.67175 9.638467 0.06975623
                                                                                             9.083901 0.07098056 7.338
8.658124 0.06973385 7.223
                 8 97.62558 0.1257011 76.47218
              9 97.95267 0.1200397 76.78740
10 98.62368 0.1138081 76.92399
11 99.02099 0.1083949 77.40641
12 98.78445 0.1129739 77.08777
                                                                                             8.639354 0.07517011
8.839886 0.07127566
              12 98.78445 0.1129739 77.08777
13 98.66266 0.1150068 77.00653
                                                                                             8.399925 0.07439665 6.783392
                                                                                             7.894852 0.07319092 6.285704
\overline{14}
              14 98.84710 0.1108773 76.97865
                                                                                             8.133782 0.06589232 6.949120
                                                                                            7.879759 0.06752656 6.542332
7.894275 0.06720565 6.594806
8.075715 0.06393143 6.650401
8.396959 0.06114397 6.987474
8.593729 0.06254538 7.248793
8.625978 0.06339578 7.080467
              15 98.80543 0.1120791 77.03701
16 98.70565 0.1131617 76.87660
15
16
17
18
19
20
21
22
23
24
25
26
              17 98.40363 0.1168254 76.72443
18 98.44458 0.1177454 76.65948
              19 98.43309 0.1177650 76.63111
20 98.46874 0.1179996 76.79040
             20 98.67435 0.1100.00

22 98.70738 0.1155386 77.08509

23 98.65482 0.1158892 76.99128

24 98.74227 0.1149323 77.09074

25 98.51679 0.1174011 76.77774

20 53713 0.1174887 76.86698
                                                                                             8.659273 0.06644836
                                                                                             8.783614 0.06774239 7.220437
                                                                                             8.877967 0.06493074 7.230532
                                                                                             8.742183 0.06278822
8.730161 0.06398288
                                                                                             8.767393 0.06247479 7.092490
              27 98.47353 0.1183745 76.80816
28 98.45024 0.1186144 76.77550
                                                                                             8.754247 0.06307105 7.021966
8.760951 0.06252087 7.065518
```

Table 44 demonstrate the final selected factors of

forward selection method and its coefficients

Table 44: Coefficient of the final forward model of

Math Test-Score of 5th Students in original survey

```
(Intercept) ATTITUDE_ENG.5 HOMEWOK_CORR_MATH 296.0711256 0.1937362 0.3078867
```

Table 45 shows the results of stepwise and cross-validation selection to the survey data build Linear

Education Test-Score Performance of 5'th and 9'th Grade Students Regression for predicting Math and Test-Score of 5<sup>th</sup> students. It seems that 27 variables are the best model of smallest RMSE (97.45196).

**Table 45:** Results of stepwise model of Math Test-Score of 5<sup>th</sup> Students in original data

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        1
        98.38140
        0.1340074
        78.27307
        11.06852
        0.12267972
        6.253139

        2
        99.31056
        0.1093756
        78.94063
        12.72111
        0.12619725
        8.196681

        3
        39.54075
        0.1093756
        79.08854
        12.21778
        0.07245265
        7.723392

        4
        4
        97.76152
        0.1419009
        78.13329
        13.20990
        0.11068534
        8.115417

        5
        5
        97.92646
        0.1189364
        78.14034
        12.92498
        0.08962180
        8.450876

        6
        6
        97.78298
        0.1324680
        77.25412
        14.52277
        0.10787949
        9.995402

        7
        797.47155
        0.1359860
        76.99488
        13.52040
        0.09966895
        9.458503

        8
        8
        8.82812
        0.1146784
        78.06529
        14.33821
        0.10308181
        9.224968

        9
        9.8.45814
        0.1252499
        77.88360
        14.57626
        0.10235987
        9.977088
```

The Table 46 demonstrate the final selected factors

of stepwise selection method and its coefficients

**Table 46:** Coefficient of the final stepwise model of Math Test-Score of 5<sup>th</sup> Students in original survey

```
(Intercept)
                                     ATTITUDE_ENG.5
                  174.859552703
                                                          0.195350924
                                                CLASSMATERELATION.5
                 INTEREST_ENG.5
                     0.033784231
                                                         -0.096217970
            CAMPUS_CONDITION.5 SATISIFACTION_LEARNING_MATH.5 -0.162006819 0.068396171
                                                      THR_MATH_NEW.5
-0.047967438
                STRATEGY_MATH.5
0.035451131
            PISA_12_ST81_ENG.5
0.009242554
                                                       THR_ENG_NEW.5
                                                         -0.165682324
             HOMEWOK_CORR_MATH
                                                      STRATEGE_ENG.5
                     0.249424201
                                                          0.045\overline{0}92019
SATISIFACTION_LEARNING_ENG.5
                                                 HOMEWOK_CORR_ENG.5
                    -0.045859473
                                                          0.143577107
          STUDYINTEREST_MATH.5
                                         STEP_CLASSMATERELATION.5
```

```
Education Test-Score Performance of 5'th and 9'th Grade Students
         -0.046776786
PISA_12_ST81_MATH.5
                                                               10.518360761
                                                       MATH_ENG_STRESS_5
0.109167839
                     0.10\overline{4}982387
                                                          SOCIAL_MORALS.5
0.189964242
                        MANNERS.5
                    -0.233720122
                                                               MP_ADD_5
-0.051183785
                     HARD_WORK.5
                     0.03\overline{4}661371
   SOLIDARITY_FRIENDSHIP.5
                                                              MORAL_DUTY.5
                                                                0.11\overline{7}125506
                     0.063084836
                     THRIFTY.5
0.057619500
                                                               AWARE.5-0.133020668
                  SENSE_HONOR.5
0.087400010
                                                            GRA_GEOMETRY.5
0.110288468
```

In conclusion, we choose the final backward model which has the smallest RMSE (97.39460). The factors in this model are attitude\_eng.5 thr\_eng\_new.5 homewok\_corr\_math homewok\_corr\_eng.5 math\_eng\_stress\_5 social\_morals.5

Table 47 shows the results of backward and cross-validation selection to the survey data build Linear Regression for predicting Math and Test-Score of 9<sup>th</sup> students. It seems that 20 variables are the best model of smallest RMSE (79.18542).

**Table 47:** Results of backward model of Math Test-Score of 9<sup>th</sup> Students in original data

Education Test-Score Performance of 5'th and 9'th Grade Students Table 48 demonstrate the final selected factors of backward selection method and its coefficients

**Table 48:** Coefficient of the final backward model of Math Test-Score of 9<sup>th</sup> Students in original survey

```
(Intercept)
                                ATTITUDE_ENG.9
                  121.98616120
                                                       0.11099561
          CLASSMATERELATION.9
                                           STUDYINTEREST_MATH.9
                                                       0.10217889
                   -0.07754025
           CAMPUS_CONDITION.9 SATISIFACTION_LEARNING_MATH.9 
-0.14748403 0.26080136
                                              PISA_12_ST81_ENG.9
                THR_MATH_NEW.9
                    0.06592582
                                                       0.13565099
SATISIFACTION_LEARNING_ENG.9
                                             HOMEWOK CORR ENG.9
                   -0.07944674
                                                      -0.10323092
            MATH_ENG_STRESS_9
                                                       MANNERS.9
                    0.03736845
                                                      -0.22820089
              SOCIAL_MORALS.9
                                                   SENSE_HONOR.9
                    0.22058516
                                                       0.15573265
                   HARD_WORK.9
                                        SOLIDARITY_FRIENDSHIP.9
                    -0.10888006
                                                       0.20032634
                  MORAL_DUTY.9
-0.22218912
                                                        THRIFTY.9
                                                       0.05902557
                      MP_ADD_9
                                                  GRA_GEOMETRY.9
                   -0.06\overline{0}40098
                                                       0.30984425
            SELF_PROTECTION.9
                    0.19963737
```

Table 49 shows the results of forward and cross-validation selection to the survey data build Linear Regression for predicting Math and Test-Score of 9<sup>th</sup> students. It seems that 17variables are the best model of smallest RMSE (80.24146).

**Table 49:** Results of forward model of Math Test-Score of 9<sup>th</sup> Students in original data

```
        nvmax
        RMSE
        Rsquared
        MAE
        RMSESD
        RsquaredSD
        MAESD

        1
        83.68883
        0.1410390
        66.06677
        6.072097
        0.06515394
        4.153679

        2
        2
        81.11783
        0.1936945
        63.69847
        5.801220
        0.09445499
        4.057824

        3
        3
        81.74043
        0.1841224
        64.56161
        6.570136
        0.12173076
        4.501733

        4
        4
        82.33877
        0.1771090
        65.32474
        6.322166
        0.11795343
        4.549133

        5
        83.41420
        0.1692773
        66.11531
        6.590467
        0.12052943
        5.138754

        6
        6
        83.70680
        0.1663289
        66.35870
        5.969662
        0.11569027
        5.533882

        7
        83.62639
        0.1712410
        66.24893
        6.532710
        0.12035323
        5.847540

        8
        83.60590
        0.1732046
        66.02055
        6.229065
        0.11785596
        5.415908

        9
        83.43834
        0.1776009
        66.06664
        6.299636
        0.12308465
        4.996483
```

```
Education Test-Score Performance of 5'th and 9'th Grade Students

15 81.28650 0.2135465 64.41304 6.286224 0.12285718 4.049777

16 80.62505 0.2242298 63.78936 6.535509 0.12284847 4.075343

17 80.24146 0.2325505 63.25677 5.805684 0.12199358 3.993002

18 80.31578 0.2323121 63.35529 6.038716 0.12232463 4.372584

19 80.44770 0.2303859 63.40173 6.144105 0.12307157 4.445353

20 80.82128 0.2249847 63.66720 6.132859 0.11932998 4.593985

21 80.64740 0.2292197 63.38965 6.457038 0.12554999 4.935972

22 80.62368 0.2296273 63.24021 6.401337 0.12524448 4.855984

23 80.77107 0.2275671 63.35758 6.270179 0.12308477 4.696474

24 80.79851 0.2264321 63.31802 6.274922 0.12152687 4.647715

25 80.87685 0.2259323 63.37706 6.349139 0.12249256 4.688714

26 80.88223 0.2253773 63.33383 6.306214 0.12146001 4.642985

27 80.88171 0.2248037 63.36470 6.226111 0.12087092 4.561523

28 80.88289 0.2249481 63.38148 6.240615 0.12086875 4.588834
```

Table 50 demonstrate the final selected factors of forward selection method and its coefficients

**Table 50:** Coefficient of the final forward model of Math Test-Score of 9<sup>th</sup> Students in original survey

```
(Intercept)
                                   ATTITUDE ENG.9
                  100.93541036
                                                        0.10772280
          CLASSMATERELATION.9
                                            STUDYINTEREST_MATH.9
                    -0.07788717
                                                        0.11337173
           CAMPUS_CONDITION.9 SATISIFACTION_LEARNING_MATH.9
                    -0.14864615
                                                        0.2\overline{5}904618
                THR_MATH_NEW.9
                                               PISA_12_ST81_ENG.9
                                                        0.14396538
                     0.06233785
SATISIFACTION_LEARNING_ENG.9
                                              HOMEWOK_CORR_ENG.9
                    -0.07\overline{6}08592
                                                       -0.10\overline{3}73583
                     MANNERS.9
                                                  SOCIAL_MORALS.9
                                                        0.24380281
                    -0.22420399
                 SENSE_HONOR.9
                                                       HARD_WORK.9
                     0.\overline{15174848}
                                                       -0.09777944
     SOLIDARITY_FRIENDSHIP.9
                                                     MORAL_DUTY.9
                                                       -0.1\overline{9}502701
                     0.20285936
                GRA_GEOMETRY.9
                                                SELF_PROTECTION.9
                     0.30641084
                                                        0.20547794
```

Table 51 shows the results of stepwise and cross-validation selection to the survey data build Linear Regression for predicting Math and Test-Score of 9<sup>th</sup> students. It seems that 20 variables are the best model of smallest RMSE (78.32629).

**Table 51:** Results of stepwise model of Math Test-Score of 9<sup>th</sup> Students in original data

```
nvmax RMSE Rsquared MAE RMSESD RsquaredSD MAESD
1 1 83.18267 0.1456005 66.05101 11.578704 0.07526664 8.400353
2 80.69206 0.2014067 63.78137 11.311542 0.08687302 8.272363
3 80.31356 0.2051515 63.88456 10.587982 0.07939790 7.564386
```

```
Education Test-Score Performance of 5'th and 9'th Grade Students

4 82.62786 0.1608288 65.44092 9.481435 0.08977031 6.543070

5 82.07441 0.1722701 64.94859 9.504673 0.06870934 6.712453

6 82.14888 0.1753129 65.31744 10.156067 0.06897840 6.539609

7 81.39503 0.1873140 64.36313 10.165821 0.07481373 6.660352

8 82.86046 0.1589582 65.23805 10.603155 0.08101522 6.928109

9 81.20002 0.1912525 64.27774 9.510666 0.07116456 6.085045

10 82.03043 0.1793196 65.26605 11.632707 0.08874771 8.476239

11 81.65800 0.1785809 64.92924 11.005737 0.09129652 7.848896

12 80.94448 0.1971828 64.54962 9.670427 0.08999739 6.473696

13 80.89273 0.1918724 64.47804 11.024049 0.08799994 7.344878

14 82.77950 0.1635994 65.97759 10.875218 0.09116375 7.867743

15 79.68167 0.2183915 63.52298 9.848480 0.09999194 6.977942

16 79.65668 0.2177780 63.96311 11.582847 0.08949741 8.578256
4
5
6
7
8
9
10
  \overline{11}
  12
  13
14
15
16
17
18
19
20
21
22
23
24
25
                                   25 79.69403 0.2171569 63.69690 9.705746 0.08271603 7.023458
26 80.90377 0.1993865 63.83857 10.764084 0.09271648 7.749028
27 79.12114 0.2261228 62.62440 10.854673 0.08525102 7.622616
28 79.30915 0.2271488 63.00905 9.860713 0.08344245 7.029540
  26
```

Table 52 demonstrate the final selected factors of

stepwise selection method and its coefficients

Table 52: Coefficient of the final stepwise model of

Math Test-Score of 9th Students in original survey

```
ATTITUDE_ENG.9
121.98616120
(Intercept)
                                                            0.11099561
                                                STUDYINTEREST_MATH.9
            CLASSMATERELATION.9
                                                            0.1\overline{0}217889
                      -0.07754025
             CAMPUS_CONDITION.9 SATISIFACTION_LEARNING_MATH.9
                      -0.14748403
                                                            0.26080136
                                                  PISA_12_ST81_ENG.9
0.13565099
                  THR_MATH_NEW.9
                       0.06\overline{5}92582
SATISIFACTION_LEARNING_ENG.9
                                                  HOMEWOK_CORR_ENG.9
                      -0.07944674
                                                           -0.10323092
              MATH_ENG_STRESS_9
0.03736845
                                                             MANNERS.9
                                                           -0.22820089
                 SOCIAL_MORALS.9
                                                        SENSE_HONOR.9
                       0.22058516
                                                            0.15573265
                      HARD_WORK.9
                                            SOLIDARITY_FRIENDSHIP.9
                      -0.10888006
                                                            0.20032634
                    MORAL_DUTY.9
-0.22218912
                                                             THRIFTY.9
                                                            0.05902557
                         MP_ADD_9
                                                       GRA_GEOMETRY.9
                      -0.06\overline{0}400\overline{9}8
                                                            0.30984425
              SELF_PROTECTION.9
0.19963737
```

In conclusion, we choose the final stepwise model which has the smallest RMSE (78.32629). The factors contained in this

```
model are ATTITUDE_ENG.9
                             CLASSMATERELATION.9
                                                           STUDYINTER
EST_MATH.9 CAMPUS_CONDITION.9 SATISIFACTION_LEARNING_MATH.9
   THR_MATH_NEW.9
                             PISA_12_ST81_ENG.9
SATISIFACTION_LEARNING_ENG.9
                                        HOMEWOK_CORR_ENG.9
                          SOCIAL_MORALS.9
  MANNERS.9
SENSE_HONOR.9
                                HARD_WORK.9
```

Education Test-Score Performance of 5'th and 9'th Grade Students SOLIDARITY\_FRIENDSHIP.9 MORAL\_DUTY.9 GRA\_GEOMETRY.9 SELF\_PROTECTION.9.

# 4. Conclusion

In the analysis of PC component, we get a model of PC1, PC3, PC5, PC10, PC12 to predict English test score of 5<sup>th</sup> students while in the analysis of the original survey data we get a model of

ATTITUDE ENG.5,

INTEREST ENG.5,

HOMEWOK CORR MATH,

SATISIFACTION\_LEARNING\_ENG.5,

STUDYINTEREST\_MATH.5, to predict which is consistent with the PC component (both has 5 variables in final model)

For the prediction of Math score of 5<sup>th</sup> students, the PC analysis preform a model of PC1, PC5, PC9, PC11. while the model of the original survey analysis is

ATTITUDE\_ENG.5

THR\_ENG\_NEW.5

HOMEWOK CORR MATH

HOMEWOK\_CORR\_ENG.5

MATH\_ENG\_STRESS\_5 SOCIAL\_MORALS.5

which is more complicated than the model got in the

PC analysis.

For the prediction of English score of 9th students,

Education Test-Score Performance of 5'th and 9'th Grade Students the PC analysis perform a model of PC1, PC2, PC4,

PC5, PC13, PC14 while the model of the original

survey analysis is ATTITUDE\_ENG.9,

INTEREST ENG.9, CLASSMATERELATION.9,

**CAMPUS CONDITION.9** 

STUDYATTITUDE\_MATH\_9

SATISIFACTION\_LEARNING MATH.9

THR MATH NEW.9 PISA 12 ST81 ENG.9

SATISIFACTION\_LEARNING\_ENG.9

STRATEGE\_ENG.9

HOMEWOK CORR ENG.9

STEP CLASSMATERELATION.9

MATH ENG STRESS 9 MANNERS.9

SOCIAL\_MORALS.9 SENSE\_HONOR.9

HARD WORK.9

SOLIDARITY\_FRIENDSHIP.9

MORAL DUTY.9

**GRA GEOMETRY.9** 

SELF\_PROTECTION.9

Which is more complicated.

For the prediction of the Math score of 9<sup>th</sup> students, the model of the PC analysis is PC1, PC2, PC3, PC4, PC5, PC7, PC10, PC13, PC14, PC15 while the variable in the original data analysis model are ATTITUDE ENG.9 CLASSMATERELATION.9

Education Test-Score Performance of 5'th and 9'th Grade Students STUDYINTEREST MATH.9

CAMPUS\_CONDITION.9

SATISIFACTION LEARNING MATH.9

THR MATH NEW.9

PISA\_12\_ST81\_ENG.9

SATISIFACTION\_LEARNING\_ENG.9

HOMEWOK CORR ENG.9

MANNERS.9

SOCIAL MORALS.9

SENSE HONOR.9

HARD\_WORK.9

SOLIDARITY\_FRIENDSHIP.9

MORAL\_DUTY.9

GRA\_GEOMETRY.9

SELF PROTECTION.9.

Which is more complicated.