

# CS 145 Midterm Review

The Best Of Collection (Master Tracks), Vol. 1



= requested on piazza (@585)

# Announcements

- Thanks for doing the surveys!
- Updates from online survey in (@696)
- **Highlights:**
  - Longer activities (spotted by the Stephanie and Alex),
  - more feedback on HWs (we can do better!)
  - SCPD accessibility
- See Piazza post @728 to vote on topics to cover (in real time!!!)

# High-Level: Lecture 2

- Basic terminology:
  - relation / table (+ “instance of”), row / tuple, column / attribute, multiset
- Table schemas in SQL
- Single-table queries:
  - SFW (selection + projection)
  - Basic SQL operators: LIKE, DISTINCT, ORDER BY
- Multi-table queries:
  - Foreign keys
  - JOINS:
    - Basic SQL syntax & semantics of

# Tables in SQL

**Product**

PName	Price	Manufacturer
Gizmo	\$19.99	GizmoWorks
Powergizmo	\$29.99	GizmoWorks
SingleTouch	\$149.99	Canon
MultiTouch	\$203.99	Hitachi

A tuple or row is a single entry in the table having the attributes specified by the schema

An attribute (or column) is a typed data entry present in each tuple in the relation

A relation or table is a multiset of tuples having the attributes specified by the schema

A multiset is an unordered list (or: a set with multiple duplicate instances allowed)

# Table Schemas

- The **schema** of a table is the table name, its attributes, and their types:

```
Product(Pname: string, Price: float, Category:  
string, Manufacturer: string)
```

- A **key** is an attribute whose values are unique; we underline a key

```
Product(Pname: string, Price: float, Category:  
string, Manufacturer: string)
```

# SQL Query

- Basic form (there are many many more bells and whistles)

```
SELECT <attributes>
FROM   <one or more relations>
WHERE  <conditions>
```

Call this a SFW query.

# LIKE: Simple String Pattern Matching

```
SELECT *  
FROM Products  
WHERE PName LIKE '%gizmo%'
```

# DISTINCT: Eliminating Duplicates

```
SELECT DISTINCT Category  
FROM Product
```

# ORDER BY: Sorting the Results

```
SELECT PName, Price  
FROM Product  
WHERE Category='gizmo'  
ORDER BY Price, PName
```

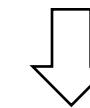
# Joins

## Product

PName	Price	Category	Manuf
Gizmo	\$19	Gadgets	GWorks
Powergizmo	\$29	Gadgets	GWorks
SingleTouch	\$149	Photography	Canon
MultiTouch	\$203	Household	Hitachi

## Company

Cname	Stock	Country
GWorks	25	USA
Canon	65	Japan
Hitachi	15	Japan

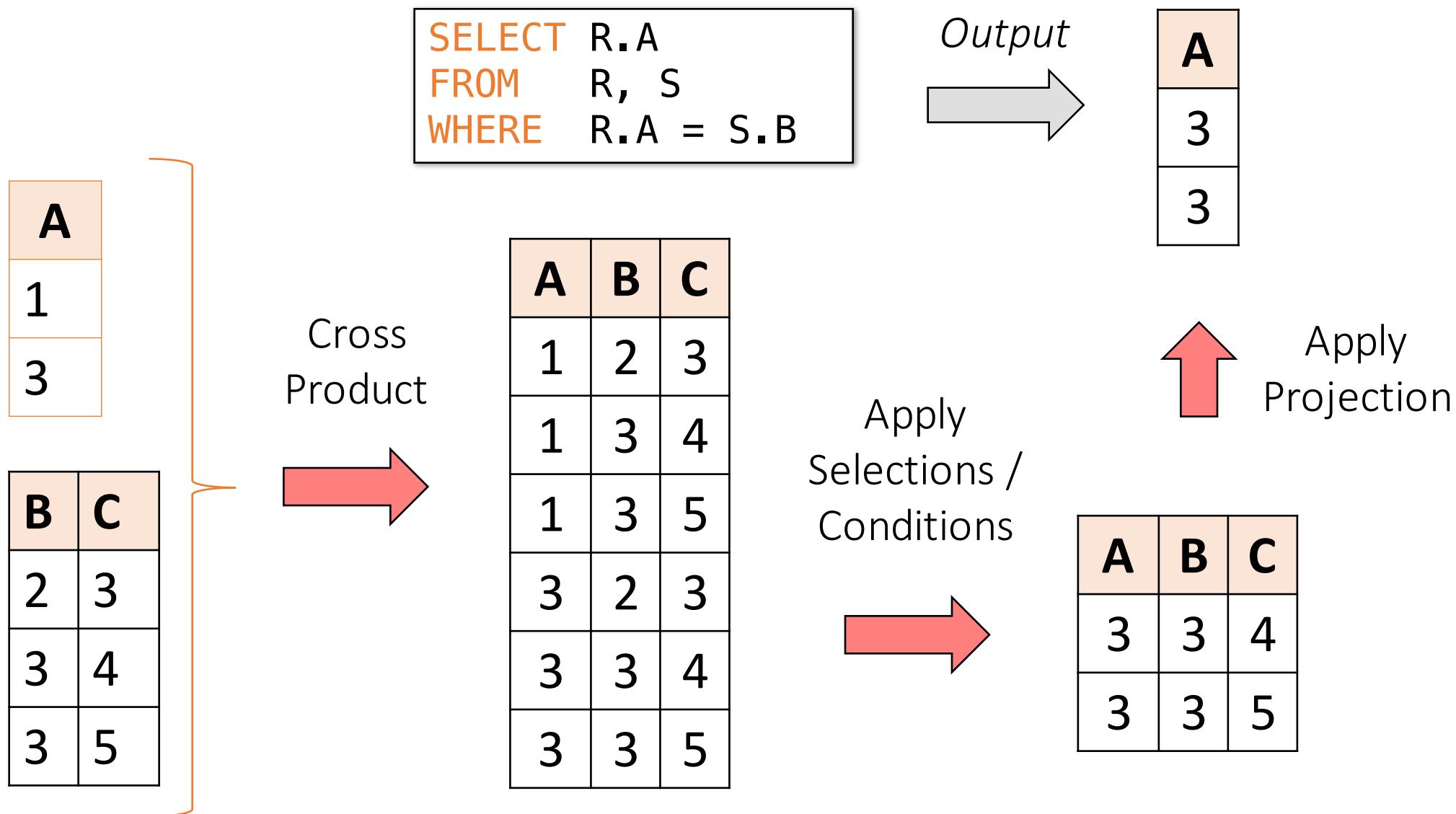


```

SELECT PName, Price
FROM Product, Company
WHERE Manufacturer = CName
AND Country='Japan'
AND Price <= 200
    
```

PName	Price
SingleTouch	\$149.99

# An example of SQL semantics

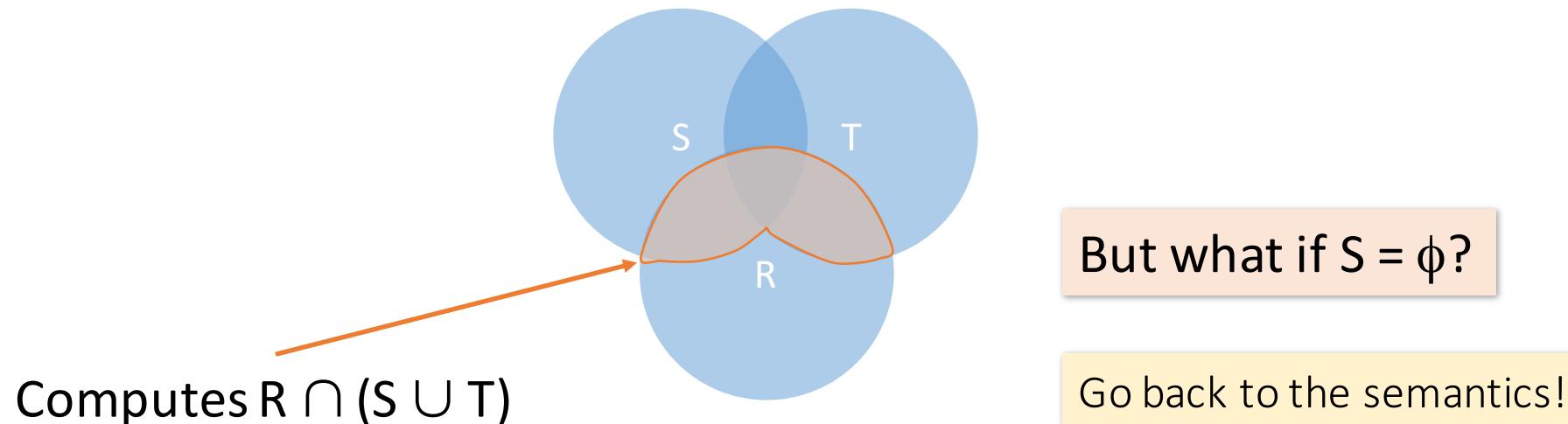


# High-Level: Lecture 3

- Set operators
  - INTERSECT, UNION, EXCEPT, [ALL]
  - Subtleties of multiset operations
- Nested queries
  - IN, ANY, ALL, EXISTS
  - Correlated queries
- Aggregation
  - AVG, SUM, COUNT, MIN, MAX, ...
- GROUP BY
- NULLs & Outer Joins

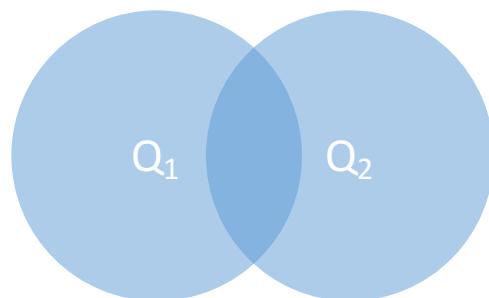
# An Unintuitive Query

```
SELECT DISTINCT R.A  
FROM   R, S, T  
WHERE  R.A=S.A OR R.A=T.A
```



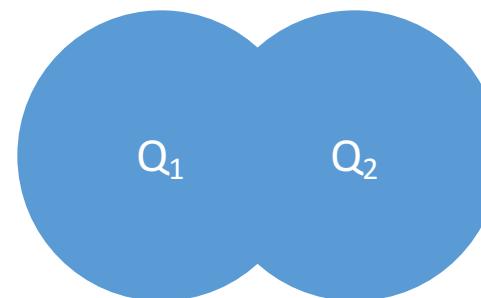
# INTERSECT

```
SELECT R.A  
FROM R, S  
WHERE R.A=S.A  
INTERSECT  
SELECT R.A  
FROM R, T  
WHERE R.A=T.A
```



# UNION

```
SELECT R.A  
FROM R, S  
WHERE R.A=S.A  
UNION  
SELECT R.A  
FROM R, T  
WHERE R.A=T.A
```



# EXCEPT

```
SELECT R.A  
FROM R, S  
WHERE R.A=S.A  
EXCEPT  
SELECT R.A  
FROM R, T  
WHERE R.A=T.A
```



# Nested queries: Sub-queries Returning Relations

```
Company(name, city)
Product(name, maker)
Purchase(id, product, buyer)
```

```
SELECT c.city
FROM Company c
WHERE c.name IN (
    SELECT pr.maker
    FROM Purchase p, Product pr
    WHERE p.product = pr.name
    AND p.buyer = 'Joe Blow')
```

“Cities where one can find companies that manufacture products bought by Joe Blow”

# Nested Queries: Operator Semantics

**Product(name, price, category, maker)**

ALL

```
SELECT name
FROM Product
WHERE price > ALL(
    SELECT price
    FROM Product
    WHERE maker = 'G')
```

ANY

```
SELECT name
FROM Product
WHERE price > ANY(
    SELECT price
    FROM Product
    WHERE maker = 'G')
```

EXISTS

```
SELECT name
FROM Product p1
WHERE EXISTS (
    SELECT *
    FROM Product p2
    WHERE p2.maker = 'G'
    AND p1.price =
        p2.price)
```

Find products that are more expensive than *all products* produced by “G”

Find products that are more expensive than *any one product* produced by “G”

Find products where *there exists some* product with the same price produced by “G”

# Nested Queries: Operator Semantics

Product(name, price, category, maker)

ALL

```
SELECT name  
FROM Product  
WHERE price > ALL(X)
```

ANY

```
SELECT name  
FROM Product  
WHERE price > ANY(X)
```

EXISTS

```
SELECT name  
FROM Product p1  
WHERE EXISTS (X)
```

Price must be  $>$  *all* entries  
in multiset X

Price must be  $>$  *at least one* entry in multiset X

X must be non-empty

\*Note that p1 can be  
referenced in X (correlated  
query!)

# Correlated Queries

Movie(title, year, director, length)

```
SELECT DISTINCT title
FROM Movie AS m
WHERE year <> ANY(
    SELECT year
    FROM Movie
    WHERE title = m.title)
```

Find movies whose title appears more than once.

Note the scoping of the variables!

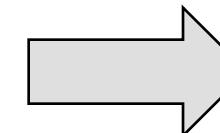
*Note also: this can still be expressed as single SFW query...*

# Simple Aggregations

## Purchase

Product	Date	Price	Quantity
bagel	10/21	1	20
banana	10/3	0.5	10
banana	10/10	1	10
bagel	10/25	1.50	20

```
SELECT SUM(price * quantity)
FROM Purchase
WHERE product = 'bagel'
```



50 (= 1\*20 + 1.50\*20)

# Grouping & Aggregations: GROUP BY

```
SELECT      product, SUM(price*quantity)
FROM        Purchase
WHERE       date > '10/1/2005'
GROUP BY    product
HAVING     SUM(quantity) > 10
```

Find total sales after 10/1/2005, only for products that have more than 10 total units sold

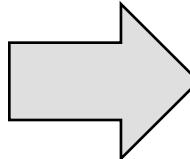
HAVING clauses contains conditions on **aggregates**

Whereas WHERE clauses condition on *individual tuples*...

# GROUP BY: (1) Compute FROM-WHERE

```
SELECT product, SUM(price*quantity) AS TotalSales  
FROM Purchase  
WHERE date > '10/1/2005'  
GROUP BY product  
HAVING SUM(quantity) > 10
```

FROM  
WHERE



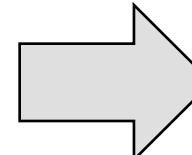
Product	Date	Price	Quantity
Bagel	10/21	1	20
Bagel	10/25	1.50	20
Banana	10/3	0.5	10
Banana	10/10	1	10
Craisins	11/1	2	5
Craisins	11/3	2.5	3

# GROUP BY: (2) Aggregate by the GROUP BY

```
SELECT product, SUM(price*quantity) AS TotalSales  
FROM Purchase  
WHERE date > '10/1/2005'  
GROUP BY product  
HAVING SUM(quantity) > 10
```

Product	Date	Price	Quantity
Bagel	10/21	1	20
Bagel	10/25	1.50	20
Banana	10/3	0.5	10
Banana	10/10	1	10
Craisins	11/1	2	5
Craisins	11/3	2.5	3

GROUP BY



Product	Date	Price	Quantity
Bagel	10/21	1	20
	10/25	1.50	20
Banana	10/3	0.5	10
	10/10	1	10
Craisins	11/1	2	5
	11/3	2.5	3

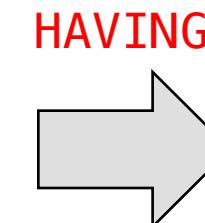
# GROUP BY: (3) Filter by the HAVING clause

```

SELECT product, SUM(price*quantity) AS TotalSales
FROM Purchase
WHERE date > '10/1/2005'
GROUP BY product
HAVING SUM(quantity) > 30

```

Product	Date	Price	Quantity
Bagel	10/21	1	20
	10/25	1.50	20
Banana	10/3	0.5	10
	10/10	1	10
Craisins	11/1	2	5
	11/3	2.5	3

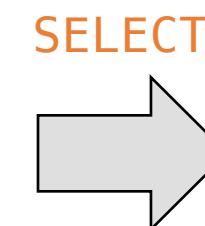


Product	Date	Price	Quantity
Bagel	10/21	1	20
	10/25	1.50	20
Banana	10/3	0.5	10
	10/10	1	10

# GROUP BY: (3) SELECT clause

```
SELECT product, SUM(price*quantity) AS TotalSales  
FROM Purchase  
WHERE date > '10/1/2005'  
GROUP BY product  
HAVING SUM(quantity) > 100
```

Product	Date	Price	Quantity
Bagel	10/21	1	20
	10/25	1.50	20
Banana	10/3	0.5	10
	10/10	1	10



Product	TotalSales
Bagel	50
Banana	15

# General form of Grouping and Aggregation

<b>SELECT</b>	S
<b>FROM</b>	$R_1, \dots, R_n$
<b>WHERE</b>	$C_1$
<b>GROUP BY</b>	$a_1, \dots, a_k$
<b>HAVING</b>	$C_2$

Evaluation steps:

1. Evaluate **FROM-WHERE**: apply condition  $C_1$  on the attributes in  $R_1, \dots, R_n$
2. **GROUP BY** the attributes  $a_1, \dots, a_k$
3. **Apply HAVING condition  $C_2$  to each group (may have aggregates)**
4. Compute aggregates in **SELECT**, S, and return the result

# Null Values



- *For numerical operations*,  $\text{NULL} \rightarrow \text{NULL}$ :
  - If  $x = \text{NULL}$  then  $4*(3-x)/7$  is still  $\text{NULL}$
- *For boolean operations*, in SQL there are three values:

**FALSE**        =        0

**UNKNOWN**   =        0.5

**TRUE**          =        1

- If  $x = \text{NULL}$  then  $x = \text{"Joe"}$  is UNKNOWN

# Null Values



- $C1 \text{ AND } C2 = \min(C1, C2)$
- $C1 \text{ OR } C2 = \max(C1, C2)$
- $\text{NOT } C1 = 1 - C1$

```
SELECT *
FROM Person
WHERE (age < 25)
    AND (height > 6 AND weight > 190)
```

Won't return e.g.  
(age=20  
height=NULL  
weight=200)!

Rule in SQL: include only tuples that yield TRUE / 1.0

# Null Values



Unexpected behavior:

```
SELECT *  
FROM Person  
WHERE age < 25  
OR age >= 25
```



```
SELECT *  
FROM Person  
WHERE age < 25  
OR age >= 25  
OR age IS NULL
```

Some Persons are not included !

Now it includes all Persons!

Can test for NULL explicitly:

- x IS NULL
- x IS NOT NULL

# RECAP: Inner Joins



By default, joins in SQL are “**inner joins**”:

```
Product(name, category)  
Purchase(prodName, store)
```

```
SELECT Product.name, Purchase.store  
FROM Product  
JOIN Purchase ON Product.name = Purchase.prodName
```

```
SELECT Product.name, Purchase.store  
FROM Product, Purchase  
WHERE Product.name = Purchase.prodName
```

Both equivalent:  
Both INNER JOINS!



# INNER JOIN:

**Product**

name	category
Gizmo	gadget
Camera	Photo
OneClick	Photo

**Purchase**

prodName	store
Gizmo	Wiz
Camera	Ritz
Camera	Wiz

```
SELECT Product.name, Purchase.store
FROM Product
INNER JOIN Purchase
ON Product.name = Purchase.prodName
```



name	store
Gizmo	Wiz
Camera	Ritz
Camera	Wiz

Note: another equivalent way to write an  
INNER JOIN!

# LEFT OUTER JOIN:

**Product**

name	category
Gizmo	gadget
Camera	Photo
OneClick	Photo

**Purchase**

prodName	store
Gizmo	Wiz
Camera	Ritz
Camera	Wiz

```
SELECT Product.name, Purchase.store
FROM Product
LEFT OUTER JOIN Purchase
ON Product.name = Purchase.prodName
```



name	store
Gizmo	Wiz
Camera	Ritz
Camera	Wiz
OneClick	NULL

# General clarification: Sets vs. Multisets



- In theory, and in any more formal material, by definition all relations are ***sets of tuples***
- In SQL, relations (i.e. tables) are **multisets**, meaning you can have duplicate tuples
  - We need this because intermediate results in SQL don't eliminate duplicates
- If you get confused: just state your assumptions & we'll be forgiving!

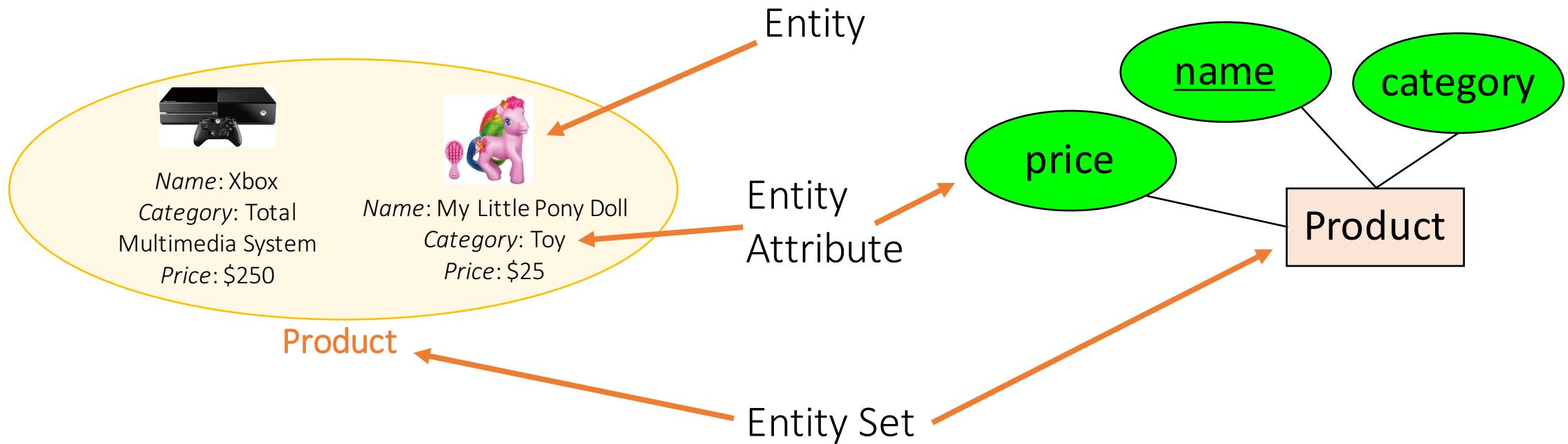
# High-Level: Lecture 4

- ER diagrams!
  - Entities (vs. Entity Sets)
  - Relationships
  - Multiplicity
  - Constraints: Keys, single-value, referential, participation, etc...

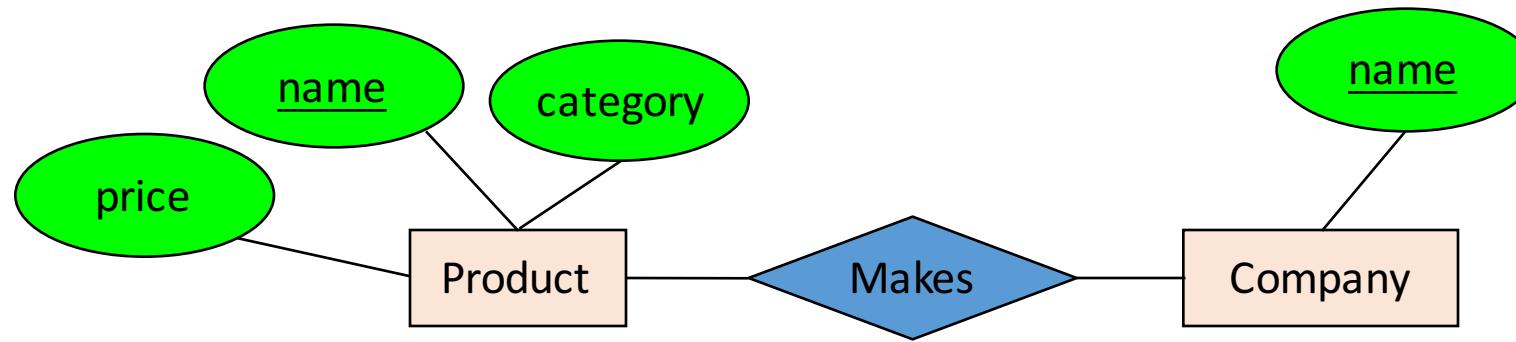
# Entities vs. Entity Sets

*Example:*

Entities are not explicitly represented in E/R diagrams!



# What is a Relationship?



A relationship between entity sets  $P$  and  $C$  is a *subset of all possible pairs of entities in  $P$  and  $C$ ,* with tuples uniquely identified by  $P$  and  $C$ 's keys

# What is a Relationship?

**Company**

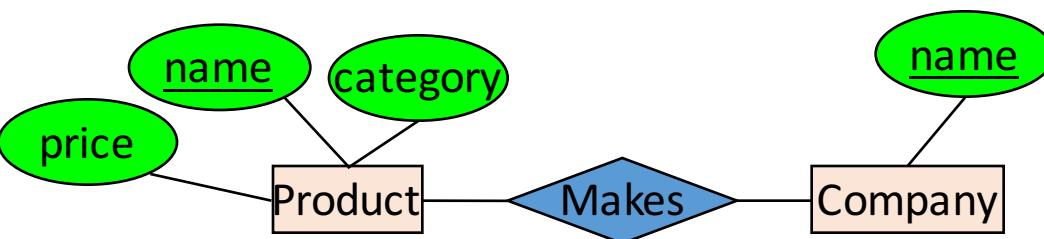
<u>name</u>
GizmoWorks
GadgetCorp

**Product**

<u>name</u>	<u>category</u>	<u>price</u>
Gizmo	Electronics	\$9.99
GizmoLite	Electronics	\$7.50
Gadget	Toys	\$5.50

**Company C × Product P**

<u>C.name</u>	<u>P.name</u>	<u>P.category</u>	<u>P.price</u>
GizmoWorks	Gizmo	Electronics	\$9.99
GizmoWorks	GizmoLite	Electronics	\$7.50
GizmoWorks	Gadget	Toys	\$5.50
GadgetCorp	Gizmo	Electronics	\$9.99
GadgetCorp	GizmoLite	Electronics	\$7.50
GadgetCorp	Gadget	Toys	\$5.50



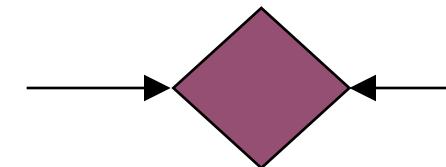
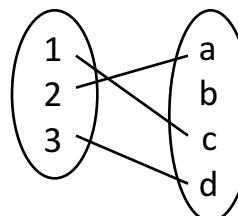
↓  
**Makes**

A relationship between entity sets P and C is a *subset of all possible pairs of entities in P and C*, with tuples uniquely identified by P and C's keys

<u>C.name</u>	<u>P.name</u>
GizmoWorks	Gizmo
GizmoWorks	GizmoLite
GadgetCorp	Gadget

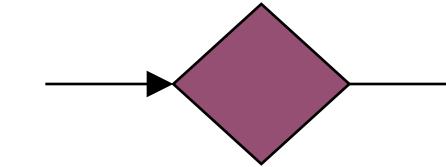
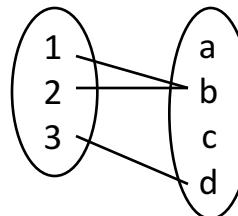
# Multiplicity of E/R Relationships

One-to-one:

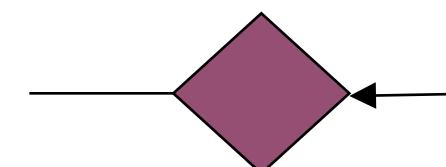
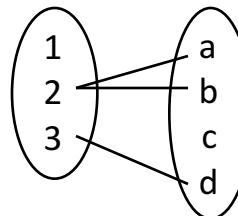


Indicated using  
arrows

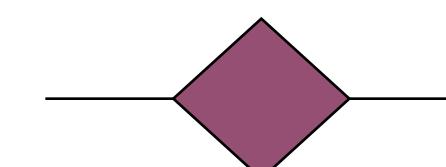
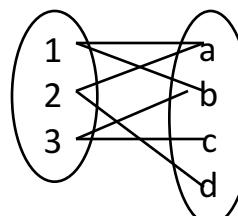
Many-to-one:



One-to-many:



Many-to-many:

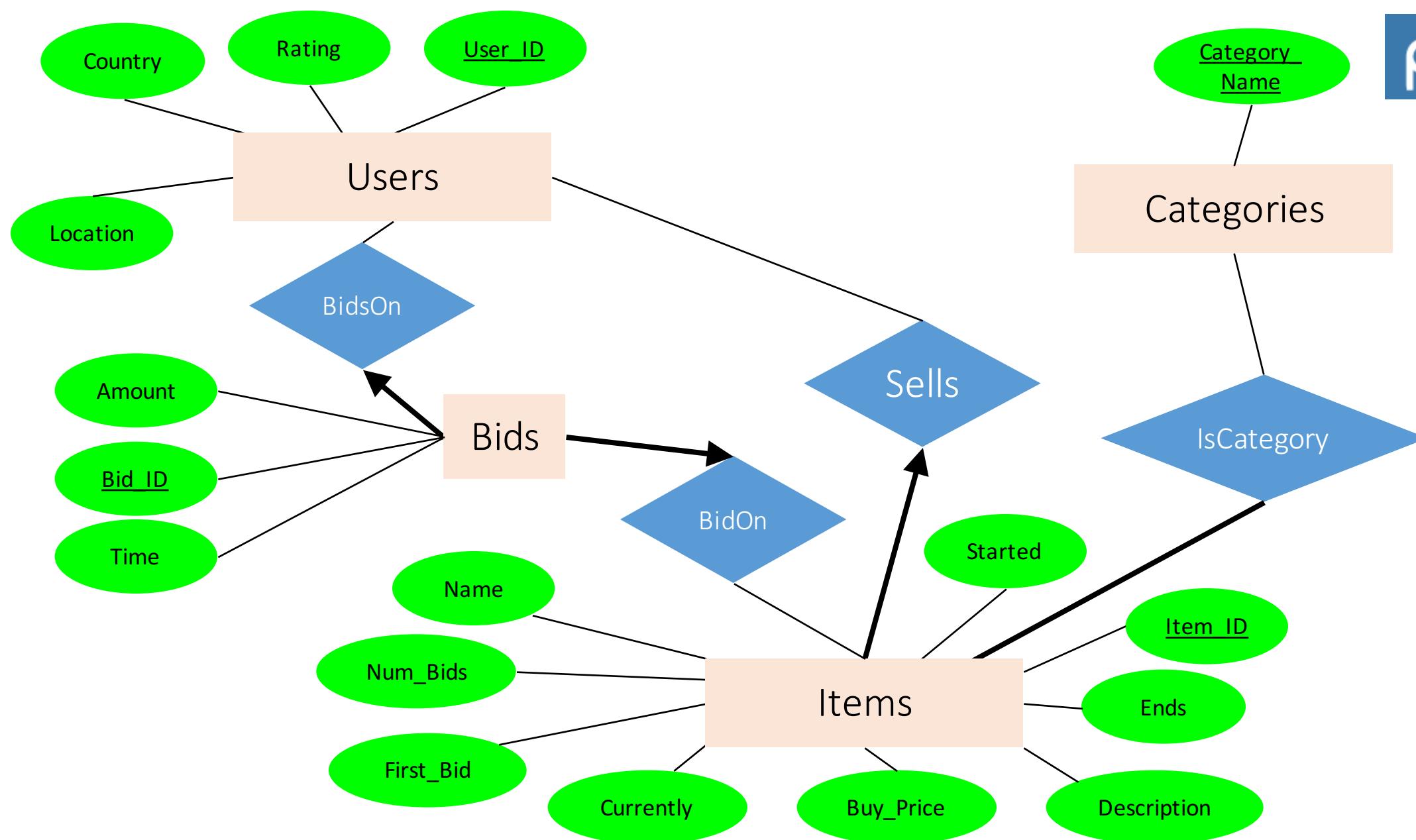


X → Y means  
there exists a  
function mapping  
from X to Y (recall  
the definition of a  
function)

# Constraints in E/R Diagrams

- Finding constraints is part of the E/R modeling process. Commonly used constraints are:
  - Keys: Implicit constraints on uniqueness of entities
    - *Ex: An SSN uniquely identifies a person*
  - Single-value constraints:
    - *Ex: a person can have only one father*
  - Referential integrity constraints: Referenced entities must exist
    - *Ex: if you work for a company, it must exist in the database*
  - Other constraints:
    - *Ex: peoples' ages are between 0 and 150*

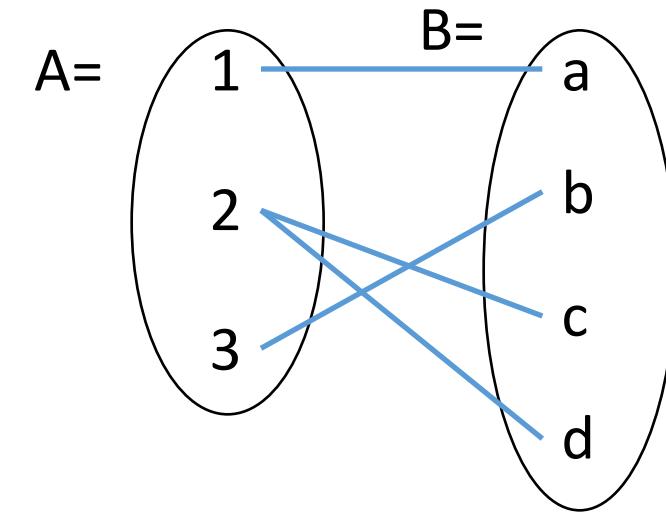
Recall  
FOREIGN  
KEYs!



# RECALL: Mathematical def. of Relationship

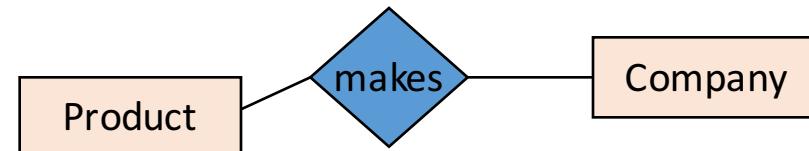
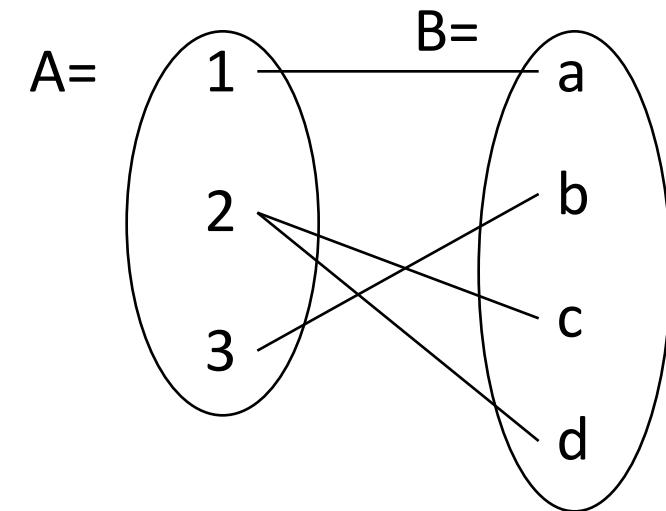
- **A *mathematical definition*:**

- Let A, B be sets
  - $A=\{1,2,3\}$ ,  $B=\{a,b,c,d\}$ ,
  - $A \times B$  (the ***cross-product***) is the set of all pairs (a,b)
    - $A \times B = \{(1,a), (1,b), (1,c), (1,d), (2,a), (2,b), (2,c), (2,d), (3,a), (3,b), (3,c), (3,d)\}$
  - We define a **relationship** to be a subset of  $A \times B$ 
    - $R = \{(1,a), (2,c), (2,d), (3,b)\}$



# RECALL: Mathematical def. of Relationship

- **A mathematical definition:**
  - Let A, B be sets
  - $A \times B$  (the **cross-product**) is the set of all pairs
  - A relationship is a subset of  $A \times B$
- **Makes** is relationship- it is a **subset** of **Product  $\times$  Company**:

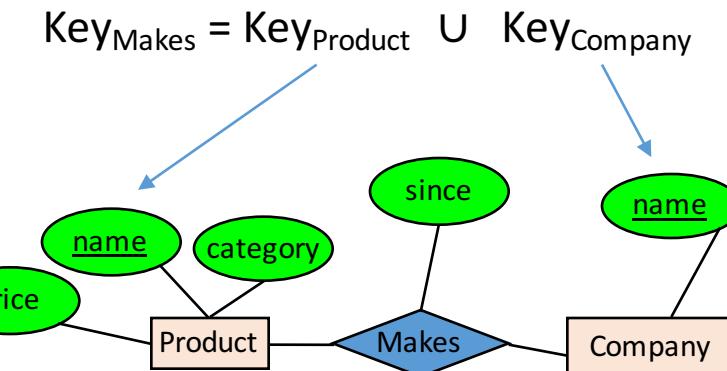


# RECALL: Mathematical def. of Relationship

- There can only be **one relationship for every unique combination of entities**
- This also means that **the relationship is uniquely determined by the keys of its entities**

This follows from our mathematical definition of a relationship- it's a SET!

- *Example: the key for Makes (to right) is {Product.name, Company.name}*



Why does this make sense?

# High-Level: Lecture 5

- Redundancy & data anomalies
- Functional dependencies
  - For database schema design
  - Given set of FDs, find others implied- using Armstrong's rules
- Closures
  - Basic algorithm
  - To find all FDs
- Keys & Superkeys

# Constraints Prevent (some) Anomalies in the Data

A poorly designed database causes *anomalies*:

Similarly, we can't reserve a room without students = an *insert* anomaly

...	CS229	C12
-----	-------	-----



Student	Course	Room
Mary	CS145	B01
Joe	CS145	B01
Sam	CS145	B01
..	..	..

If everyone drops the class, we lose what room the class is in! = a *delete* anomaly

If every course is in only one room, contains *redundant* information!

If we update the room number for one tuple, we get inconsistent data = an *update* anomaly

# Constraints Prevent (some) Anomalies in the Data

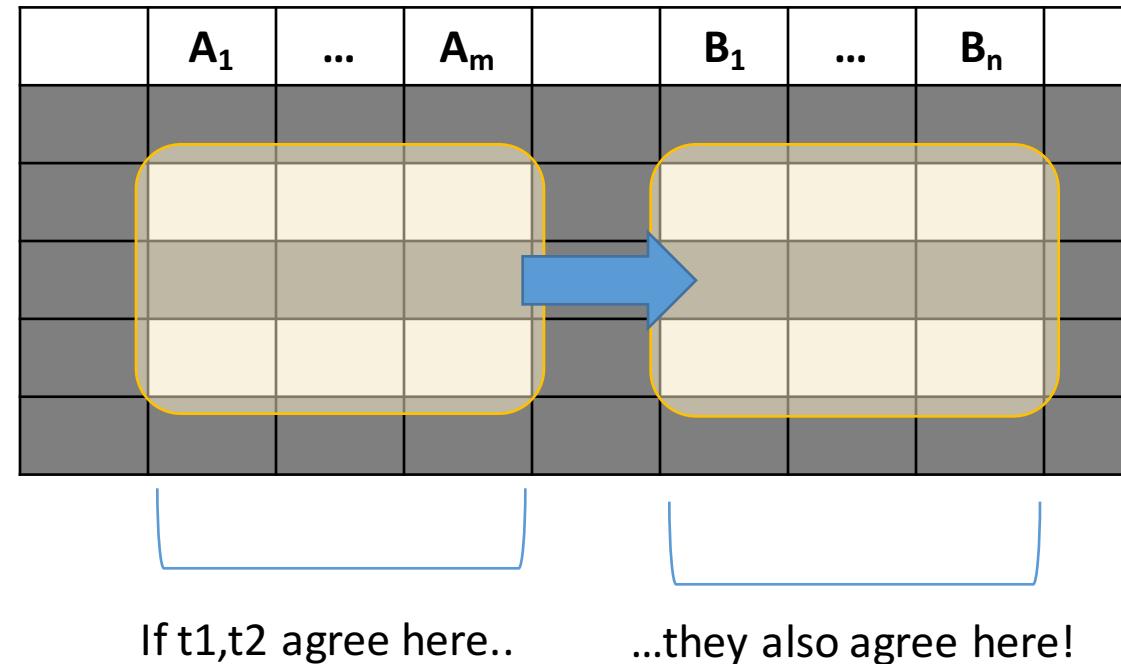
<b>Student</b>	<b>Course</b>
Mary	CS145
Joe	CS145
Sam	CS145
..	..

<b>Course</b>	<b>Room</b>
CS145	B01
CS229	C12

Is this form better?

- Redundancy?
- Update anomaly?
- Delete anomaly?
- Insert anomaly?

# A Picture Of FDs



Defn (again):

Given attribute sets  $A = \{A_1, \dots, A_m\}$  and  $B = \{B_1, \dots, B_n\}$  in  $R$ ,

The *functional dependency*  $A \rightarrow B$  on  $R$  holds if for *any*  $t_i, t_j$  in  $R$ :

if  $t_i[A_1] = t_j[A_1]$  AND  $t_i[A_2] = t_j[A_2]$  AND ... AND  $t_i[A_m] = t_j[A_m]$

then  $t_i[B_1] = t_j[B_1]$  AND  $t_i[B_2] = t_j[B_2]$  AND ... AND  $t_i[B_n] = t_j[B_n]$

# FDs for Relational Schema Design

- High-level idea: **why do we care about FDs?**

1. Start with some relational *schema*
2. Find out its *functional dependencies (FDs)*
3. Use these to *design a better schema*
  1. One which minimizes possibility of anomalies

*This part can be tricky!*

# Finding Functional Dependencies

Equivalent to asking: Given a set of FDs,  $F = \{f_1, \dots, f_n\}$ , does an FD  $g$  hold?

**Inference problem:** How do we decide?

Answer: Three simple rules called **Armstrong's Rules**.

1. Split/Combine,
2. Reduction, and
3. Transitivity... *ideas by picture*

# Closure of a set of Attributes

Given a set of attributes  $A_1, \dots, A_n$  and a set of FDs  $F$ :

Then the closure,  $\{A_1, \dots, A_n\}^+$  is the set of attributes  $B$  s.t.  $\{A_1, \dots, A_n\} \rightarrow B$

Example:  $F =$

$$\begin{aligned}\{name\} &\rightarrow \{color\} \\ \{category\} &\rightarrow \{department\} \\ \{color, category\} &\rightarrow \{price\}\end{aligned}$$

*Example  
Closures:*

$$\begin{aligned}\{name\}^+ &= \{name, color\} \\ \{name, category\}^+ &= \\ \{name, category, color, dept, price\} & \\ \{color\}^+ &= \{color\}\end{aligned}$$

# Closure Algorithm

Start with  $X = \{A_1, \dots, A_n\}$ , FDs  $F$ .

**Repeat until**  $X$  doesn't change; **do**:

**if**  $\{B_1, \dots, B_n\} \rightarrow C$  is in  $F$  **and**  $\{B_1, \dots, B_n\} \subseteq X$ :  
**then** add  $C$  to  $X$ .

**Return**  $X$  as  $X^+$

$F =$

$\{name\} \rightarrow \{color\}$

$\{category\} \rightarrow \{dept\}$

$\{color, category\} \rightarrow \{price\}$

$\{name, category\}^+ =$   
 $\{name, category\}$

$\{name, category\}^+ =$   
 $\{name, category, color\}$

$\{name, category\}^+ =$   
 $\{name, category, color, dept\}$

$\{name, category\}^+ =$   
 $\{name, category, color, dept, price\}$

# Keys and Superkeys

A superkey is a set of attributes  $A_1, \dots, A_n$  s.t.  
for *any other* attribute  $B$  in  $R$ ,  
we have  $\{A_1, \dots, A_n\} \rightarrow B$

i.e. all attributes are  
*functionally determined*  
by a superkey

A key is a *minimal* superkey

Meaning that no subset of  
a key is also a superkey

# CALCULATING Keys and Superkeys



- **Superkey?**

- Compute the closure of A
- See if it = the full set of attributes

Let A be a set of attributes, R set of all attributes, F set of FDs:

```
IsSuperkey(A, R, F):
    A+ = ComputeClosure(A, F)
    Return (A+==R)?
```

- **Key?**

- Confirm that A is superkey
- Make sure that no subset of A is a superkey
  - *Only need to check one 'level' down!*

Also see Lecture-5.ipynb!!!

```
IsKey(A, R, F):
    If not IsSuperkey(A, R, F):
        return False
    For B in SubsetsOf(A, size=len(A)-1):
        if IsSuperkey(B, R, F):
            return False
    return True
```

# High-Level: Lecture 7

- Conceptual design
- Boyce-Codd Normal Form (BCNF)
  - Definition
  - Algorithm
- Decompositions
  - Lossless vs. Lossy
  - A problem with BCNF
- MVDs
  - *In slightly greater depth since we skipped in lecture...*

# Back to Conceptual Design

Now that we know how to find FDs, it's a straight-forward process:

1. Search for “bad” FDs
2. If there are any, then *keep decomposing the table into sub-tables* until no more bad FDs
3. When done, the database schema is *normalized*

Recall: there are several normal forms...

# Boyce-Codd Normal Form



BCNF is a simple condition for removing anomalies from relations:

A relation R is in BCNF if:

if  $\{A_1, \dots, A_n\} \rightarrow B$  is a *non-trivial* FD in R

then  $\{A_1, \dots, A_n\}$  is a superkey for R

Equivalently:  $\forall$  sets of attributes X, either  $(X^+ = X)$  or  $(X^+ = \text{all attributes})$

In other words: there are no “bad” FDs

# Example



Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

$\{SSN\} \rightarrow \{Name, City\}$

This FD is *bad*  
because it is not a  
superkey

$\Rightarrow$  Not in BCNF

What is the key?  
 $\{SSN, PhoneNumber\}$

# Example

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Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Madison

$$\{\text{SSN}\} \rightarrow \{\text{Name}, \text{City}\}$$

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

This FD is now  
*good* because it is  
the key

Let's check anomalies:

- Redundancy ?
- Update ?
- Delete ?

Now in BCNF!

# BCNF Decomposition Algorithm



BCNFDekomp(R):

# BCNF Decomposition Algorithm



BCNFD**e**comp( $R$ ):

Find a *set of attributes*  $X$  s.t.:  $X^+ \neq X$  and  $X^+ \neq$   
[all attributes]

Find a set of attributes  $X$  which has non-trivial “bad” FDs, i.e. is not a superkey, using closures

# BCNF Decomposition Algorithm



BCNFD**e**comp( $R$ ):

Find a *set of attributes*  $X$  s.t.:  $X^+ \neq X$  and  $X^+ \neq [$ all attributes $]$

**if** (not found) **then Return**  $R$

If no “bad” FDs found, in BCNF!

# BCNF Decomposition Algorithm



BCNFDekomp(R):

Find a *set of attributes*  $X$  s.t.:  $X^+ \neq X$  and  $X^+ \neq [all\ attributes]$

if (not found) then Return R

let  $Y = X^+ - X$ ,  $Z = (X^+)^C$

Let  $Y$  be the attributes that  $X$  *functionally determines* (+ that are not in  $X$ )

And let  $Z$  be the other attributes that it *doesn't*

# BCNF Decomposition Algorithm



BCNFDcomp( $R$ ):

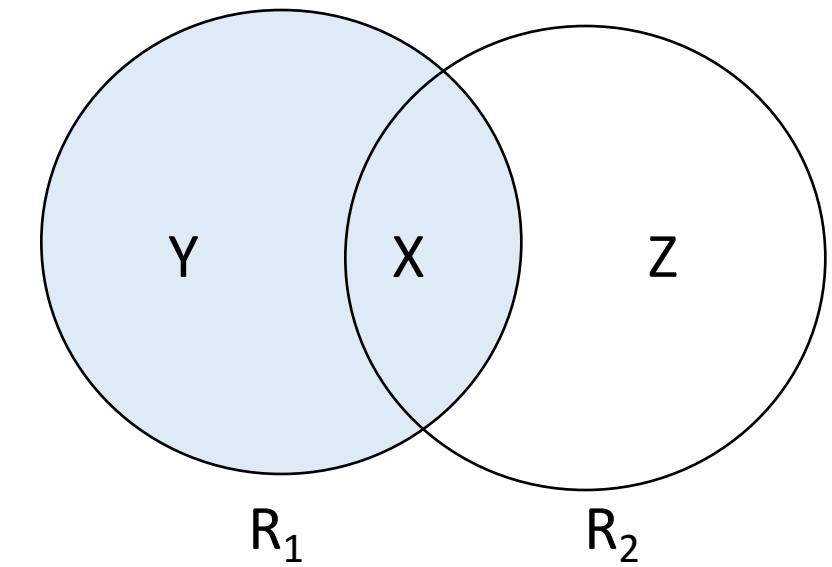
Find a *set of attributes*  $X$  s.t.:  $X^+ \neq X$  and  $X^+ \neq$   
[all attributes]

if (not found) then Return  $R$

let  $Y = X^+ - X$ ,  $Z = (X^+)^C$

**decompose  $R$  into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$**

Split into one relation (table)  
with  $X$  plus the attributes  
that  $X$  determines ( $Y$ )...



# BCNF Decomposition Algorithm



BCNFDcomp( $R$ ):

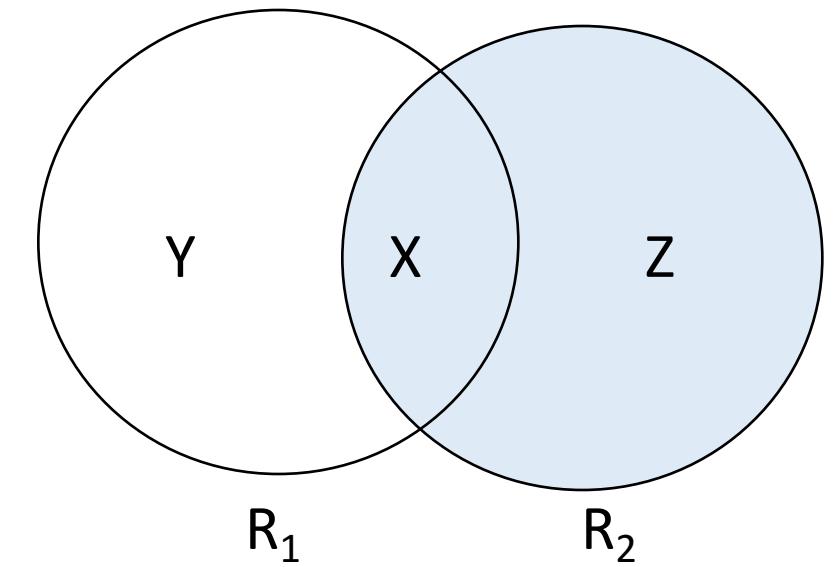
Find a set of attributes  $X$  s.t.:  $X^+ \neq X$  and  $X^+ \neq$   
[all attributes]

if (not found) then Return  $R$

let  $Y = X^+ - X$ ,  $Z = (X^+)^C$

**decompose  $R$  into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$**

And one relation with  $X$  plus  
the attributes it *does not*  
determine ( $Z$ )



# BCNF Decomposition Algorithm



BCNFD**e**comp( $R$ ):

Find a *set of attributes*  $X$  s.t.:  $X^+ \neq X$  and  $X^+ \neq [$ all attributes $]$

if (not found) then Return  $R$

let  $Y = X^+ - X$ ,  $Z = (X^+)^C$

decompose  $R$  into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$

**Return** BCNFD**e**comp( $R_1$ ), BCNFD**e**comp( $R_2$ )

Proceed recursively until no more “bad” FDs!

# Example



BCNFDecomp( $R$ ):

Find a set of attributes  $X$  s.t.:  $X^+ \neq X$  and  $X^+ \neq$   
[all attributes]

if (not found) then Return  $R$

let  $Y = X^+ - X$ ,  $Z = (X^+)^C$

decompose  $R$  into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$

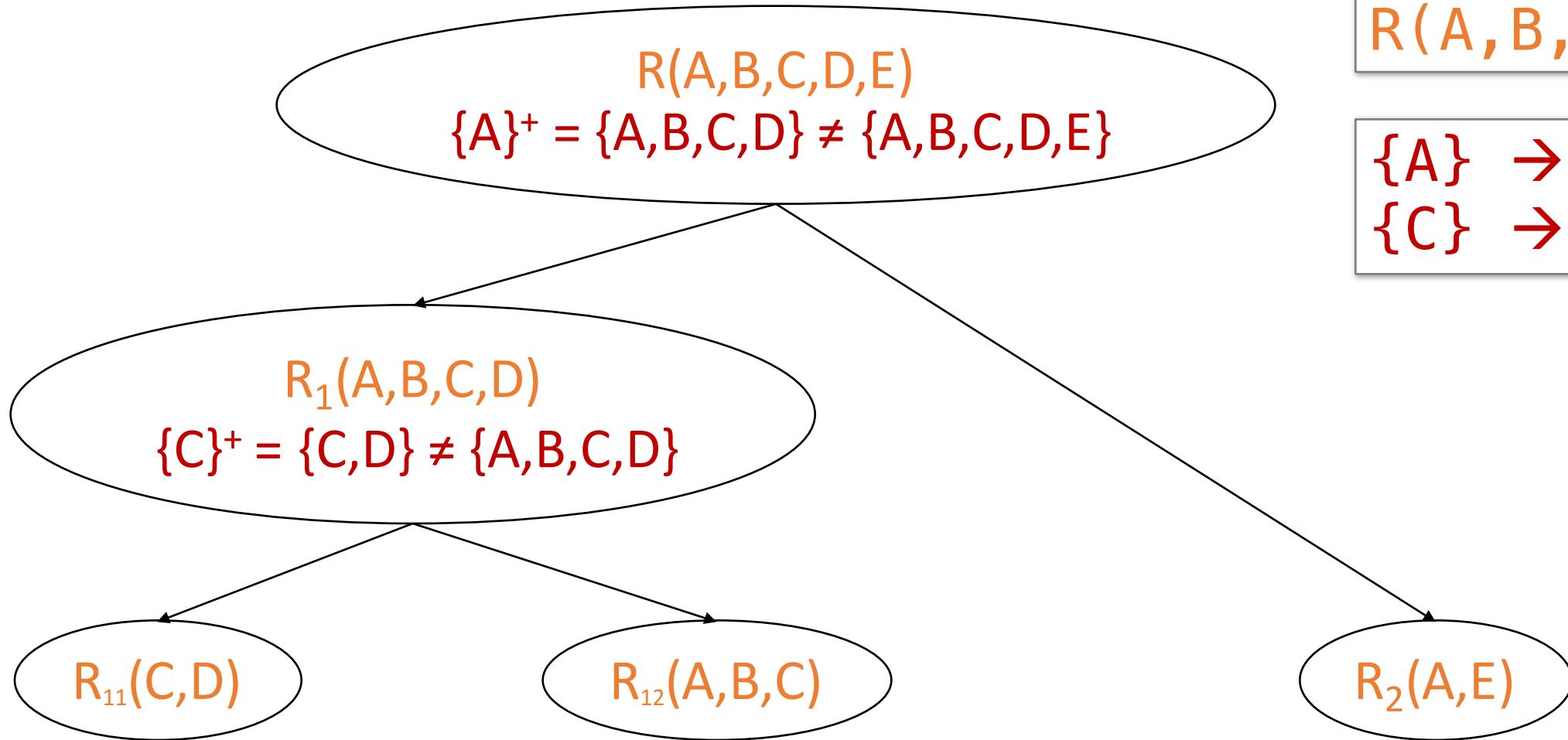
Return BCNFDecomp( $R_1$ ), BCNFDecomp( $R_2$ )

$R(A, B, C, D, E)$

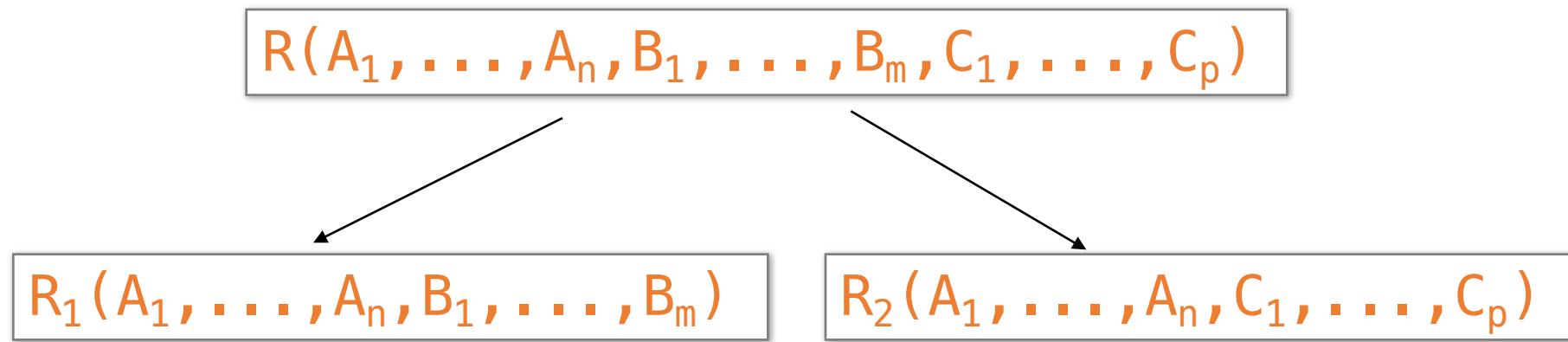
$\{A\} \rightarrow \{B, C\}$   
 $\{C\} \rightarrow \{D\}$

# Example

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# Lossless Decompositions



If  $\{A_1, \dots, A_n\} \rightarrow \{B_1, \dots, B_m\}$   
Then the decomposition is lossless

Note: don't need  
 $\{A_1, \dots, A_n\} \rightarrow \{C_1, \dots, C_p\}$

BCNF decomposition is always lossless. Why?

# A Problem with BCNF

Unit	Company	Product
...	...	...

$\{Unit\} \rightarrow \{Company\}$   
 $\{Company, Product\} \rightarrow \{Unit\}$

Unit	Company
...	...

Unit	Product
...	...

$\{Unit\} \rightarrow \{Company\}$

We do a BCNF decomposition  
on a “bad” FD:  
 $\{Unit\}^+ = \{Unit, Company\}$

We lose the FD  $\{Company, Product\} \rightarrow \{Unit\}!!$

# Multiple Value Dependencies (MVDs)



Many of you asked, “what do these mean in real life?”



*Grad student CA thinks:*  
“Hmm... what is real life??  
Watching a movie over the  
weekend?”

# MVDs: Movie Theatre Example



Movie_theater	film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

Are there any functional dependencies that might hold here?

No...

And yet it seems like there is some pattern / dependency...

# MVDs: Movie Theatre Example



Movie_theater	film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

For a given movie theatre...

# MVDs: Movie Theatre Example



Movie_theater	film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

For a given movie theatre...

Given a set of movies and snacks...

# MVDs: Movie Theatre Example

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Movie_theater	film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

For a given movie theatre...

Given a set of movies and snacks...

Any movie / snack combination is possible!

# MVDs: Movie Theatre Example



	<b>Movie_theater (A)</b>	<b>film_name (B)</b>	<b>Snack (C)</b>
$t_1$	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
	Rains 216	Star Trek: The Wrath of Kahn	Burrito
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
$t_2$	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write  $\{A\} \twoheadrightarrow \{B\}$  if for any tuples  $t_1, t_2$  s.t.  $t_1[A] = t_2[A]$

# MVDs: Movie Theatre Example



	Movie_theater (A)	film_name (B)	Snack (C)
t <sub>1</sub>	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
t <sub>3</sub>	Rains 216	Star Trek: The Wrath of Kahn	Burrito
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
t <sub>2</sub>	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write  $\{A\} \twoheadrightarrow \{B\}$  if for any tuples  $t_1, t_2$  s.t.  $t_1[A] = t_2[A]$  there is a tuple  $t_3$  s.t.

- $T_3[A] = t_1[A]$

# MVDs: Movie Theatre Example



	Movie_theater (A)	film_name (B)	Snack (C)
$t_1$	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
$t_3$	Rains 216	Star Trek: The Wrath of Kahn	Burrito
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
$t_2$	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write  $\{A\} \twoheadrightarrow \{B\}$  if for any tuples  $t_1, t_2$  s.t.  $t_1[A] = t_2[A]$  there is a tuple  $t_3$  s.t.

- $t_3[A] = t_1[A]$
- $t_3[B] = t_1[B]$

# MVDs: Movie Theatre Example

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	Movie_theater (A)	film_name (B)	Snack (C)
$t_1$	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
$t_3$	Rains 216	Star Trek: The Wrath of Kahn	Burrito
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
$t_2$	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write  $\{A\} \twoheadrightarrow \{B\}$  if for any tuples  $t_1, t_2$  s.t.  $t_1[A] = t_2[A]$  there is a tuple  $t_3$  s.t.

- $t_3[A] = t_1[A]$
- $t_3[B] = t_1[B]$
- and  $t_3[R \setminus B] = t_2[R \setminus B]$

Where  $R \setminus B$  is “R minus B” i.e. the attributes of R not in B

# MVDs: Movie Theatre Example



	Movie_theater (A)	film_name (B)	Snack (C)
t <sub>2</sub>	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
	Rains 216	Star Trek: The Wrath of Kahn	Burrito
t <sub>3</sub>	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
t <sub>1</sub>	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

Note this also works!

Remember, an MVD holds over a *relation or an instance*, so defn. must hold for every applicable pair...

# MVDs: Movie Theatre Example

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	Movie_theater (A)	film_name (B)	Snack (C)
$t_2$	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
	Rains 216	Star Trek: The Wrath of Kahn	Burrito
$t_3$	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
$t_1$	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

This expresses a sort of dependency (= data redundancy) that we *can't* express with FDs

\*Actually, it expresses conditional independence (between film and snack given movie theatre)!

MVDs...

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Think you can't understand them?

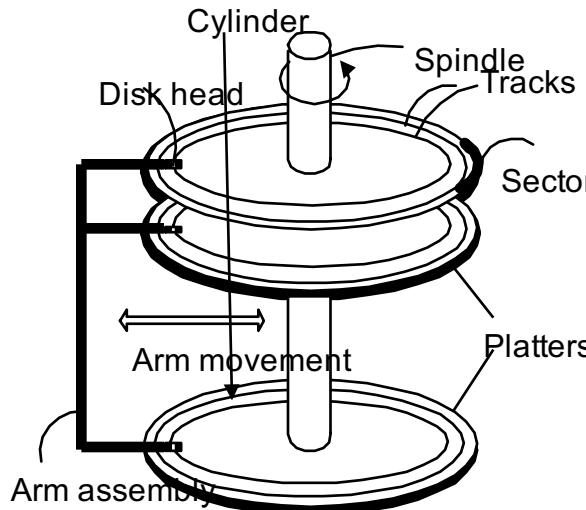
YES YOU



# High-Level: Lecture 8

- Our model of the computer: Disk vs. RAM, local vs. global
- Transactions (TXNs)
- ACID
- Logging for Atomicity & Durability
  - Write-ahead logging (WAL)

# High-level: Disk vs. Main Memory



## Disk:

- **Slow:** Sequential access
  - (although fast sequential reads)
- **Durable:** We will assume that once on disk, data is safe!
- **Cheap**

## Random Access Memory (RAM) or Main Memory:

- **Fast:** Random access, byte addressable
  - ~10x faster for sequential access
  - ~100,000x faster for random access!
- **Volatile:** Data can be lost if e.g. crash occurs, power goes out, etc!
- **Expensive:** For \$100, get 16GB of RAM vs. 2TB of disk!

# Our model: Three Types of Regions of Memory

1. **Local:** In our model each process in a DBMS has its own local memory, where it stores values that only it “sees”
2. **Global:** Each process can read from / write to shared data in main memory
3. **Disk:** Global memory can read from / flush to disk
4. **Log:** Assume on stable disk storage- spans both main memory and disk...

	Local	Global
Main Memory (RAM)	1	2 4
Disk	3	

Log is a *sequence* from main memory -> disk

“Flushing to disk” = writing to disk + erasing (“evicting”) from main memory

# Transactions: Basic Definition

A transaction (“TXN”) is a sequence of one or more *operations* (reads or writes) which reflects *a single real-world transition*.

In the real world, a TXN either happened completely or not at all

```
START TRANSACTION  
    UPDATE Product  
        SET Price = Price - 1.99  
        WHERE pname = 'Gizmo'  
    COMMIT
```

# Transaction Properties: ACID

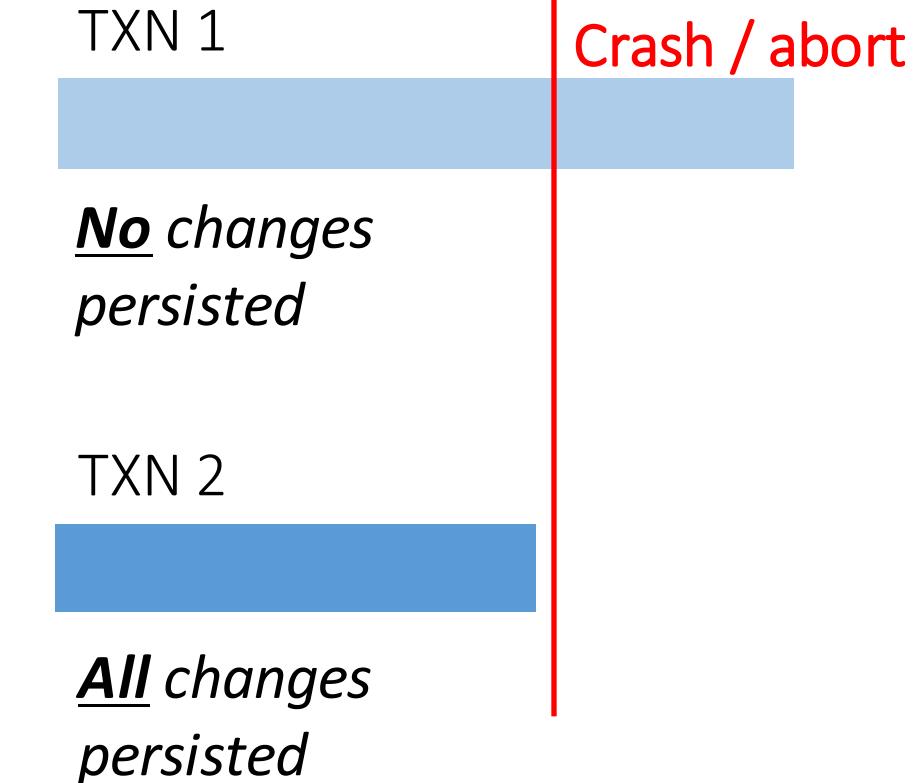
- **A**tomic
  - State shows either all the effects of txn, or none of them
- **C**onsistent
  - Txn moves from a state where integrity holds, to another where integrity holds
- **I**solated
  - Effect of txns is the same as txns running one after another (ie looks like batch mode)
- **D**urable
  - Once a txn has committed, its effects remain in the database

ACID is/was source of great debate!

# Goal of LOGGING: Ensuring Atomicity & Durability

ACID

- Atomicity:
  - TXNs should either happen completely or not at all
  - If abort / crash during TXN, *no* effects should be seen
- Durability:
  - If DBMS stops running, changes due to completed TXNs should all persist
  - *Just store on stable disk*



# Basic Idea: (Physical) Logging

- Record UNDO information for every update!
  - Sequential writes to log
  - Minimal info (diff) written to log
- The **log** consists of an ordered list of actions
  - Log record contains:  
**<XID, location, old data, new data>**

This is sufficient to UNDO any transaction!

# Write-ahead Logging (WAL) Commit Protocol

T: R(A), W(A)



This time, let's try committing after we've written log to disk but before we've written data to disk... this is WAL!

**OK, Commit!**

If we crash now, is T durable?

# Write-ahead Logging (WAL) Commit Protocol

T: R(A), W(A)

T →



A: 0 → 1



This time, let's try committing after we've written log to disk but before we've written data to disk... this is WAL!

**OK, Commit!**

If we crash now, is T durable?

**USE THE LOG!**

# Write-Ahead Logging (WAL)

- DB uses **Write-Ahead Logging (WAL)** Protocol:

Each update is logged! Why not reads?

1. Must *force log record* for an update *before* the corresponding data page goes to storage

→ Atomicity

2. Must *write all log records* for a TX *before commit*

→ Durability

# High-Level: Lecture 9

- Motivation: Concurrency with Isolation & consistency
  - Using TXNs...
- Scheduling
- Serializability
- Conflict types & classic anomalies

# Concurrency: Isolation & Consistency

- The DBMS must handle concurrency such that...

1. **Isolation** is maintained: Users must be able to execute each TXN as if they were the only user
  - DBMS handles the details of *interleaving* various TXNs

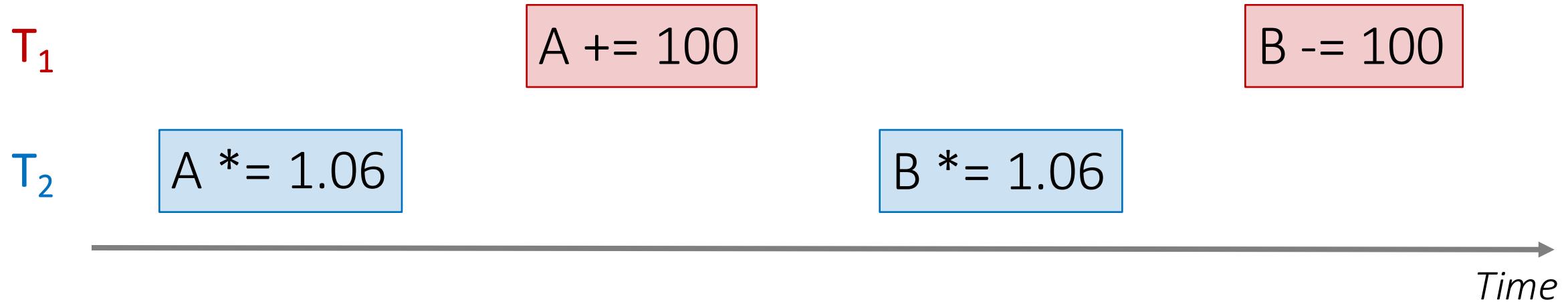
ACID

2. **Consistency** is maintained: TXNs must leave the DB in a **consistent state**
  - DBMS handles the details of enforcing integrity constraints

ACID

Example- consider two TXNs:

The DBMS can also **interleave** the TXNs



What goes / could go wrong here??

# Scheduling examples

*Starting  
Balance*

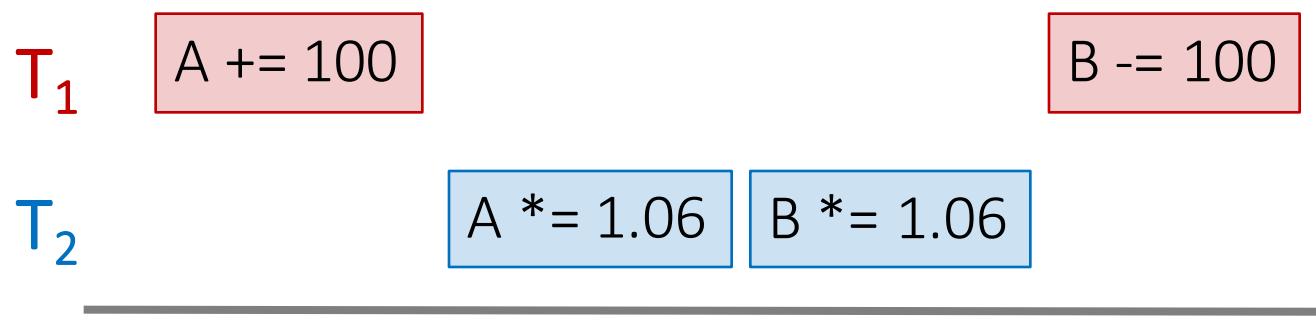
A	B
\$50	\$200

Serial schedule  $T_1 \rightarrow T_2$ :



A	B
\$159	\$106

Interleaved schedule B:



A	B
\$159	\$112

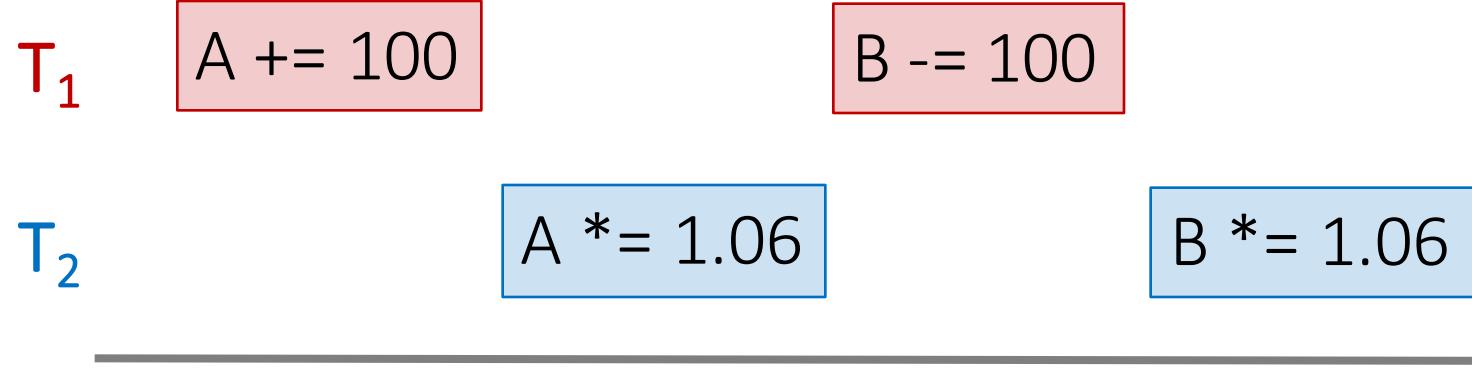
Different result than serial  $T_1 \rightarrow T_2$ !

# Scheduling Definitions

- A **serial schedule** is one that does not interleave the actions of different transactions
- A and B are **equivalent schedules** if, *for any database state*, the effect on DB of executing A is **identical** to the effect of executing B
- A **serializable schedule** is a schedule that is equivalent to **some** serial execution of the transactions.

The word “**some**” makes this def powerful and tricky!

# Serializable?



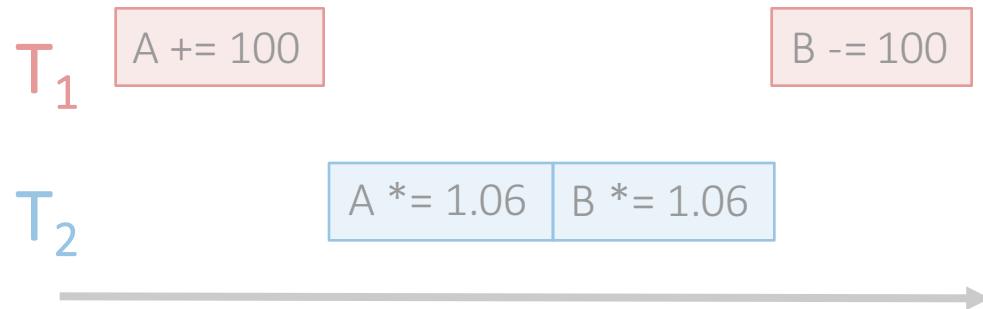
Serial schedules:

	A	B
$T_1 \rightarrow T_2$	$1.06*(A+100)$	$1.06*(B-100)$
$T_2 \rightarrow T_1$	$1.06*A + 100$	$1.06*B - 100$

A	B
1.06*(A+100)	1.06*(B-100)

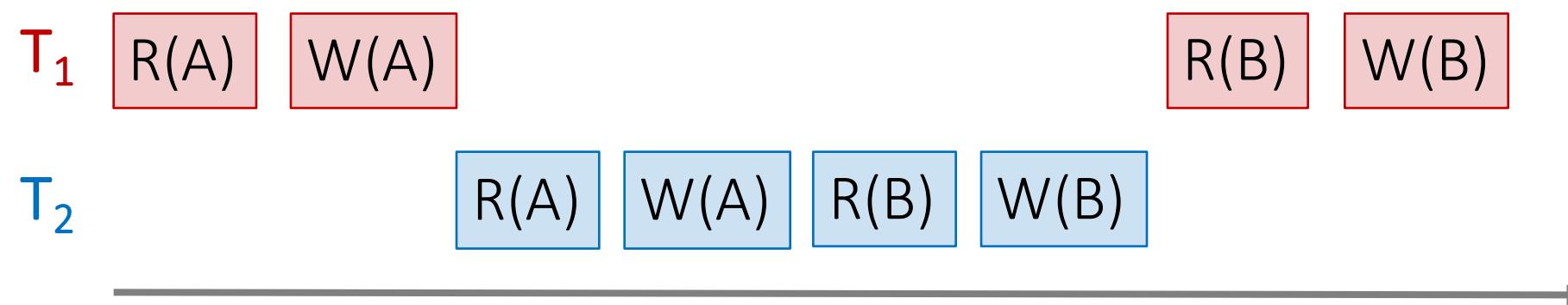
Same as a serial schedule  
*for all possible values of A, B = Serializable*

# The DBMS's view of the schedule



Each action in the TXNs *reads a value from global memory and then writes one back to it*

Scheduling order matters!



# Conflict Types

Two actions **conflict** if they are part of different TXNs, involve the same variable, and at least one of them is a write

- Thus, there are three types of conflicts:

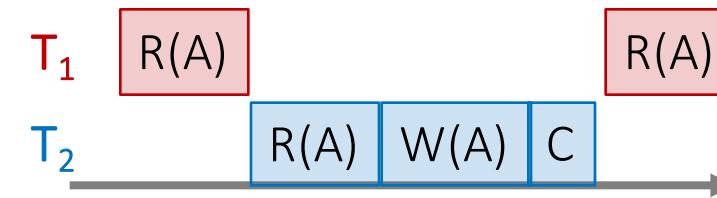
- Read-Write conflicts (RW)
- Write-Read conflicts (WR)
- Write-Write conflicts (WW)

Why no “RR Conflict”?

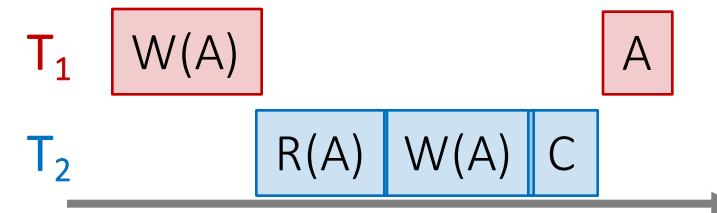
Interleaving anomalies occur with / because of these conflicts between TXNs (*but these conflicts can occur without causing anomalies!*)

# Classic Anomalies with Interleaved Execution

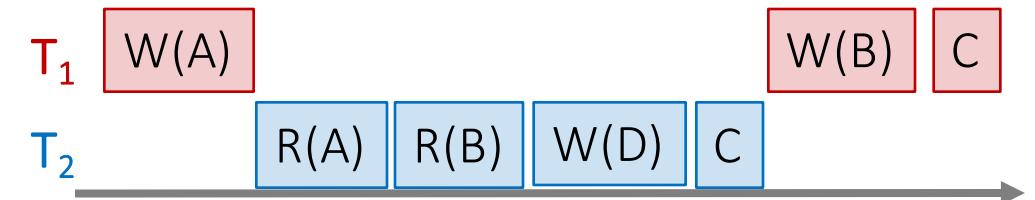
“Unrepeatable read”:



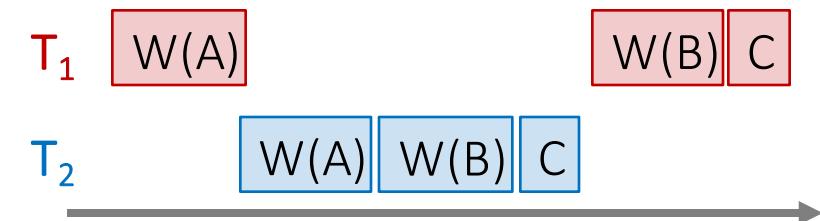
“Dirty read” / Reading uncommitted data:



“Inconsistent read” / Reading partial commits:



Partially-lost update:

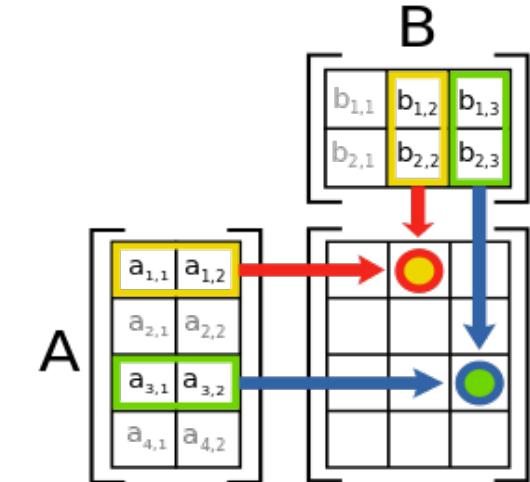


# Notes

- Locking & etc. (all content in lecture 9 after activity 9-1) will not be covered
- PS1 review slides included as appendix (after this...)
- PS2 & additional content covered in extra review session on Sunday, in Gates 104

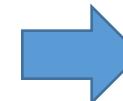
# Linear Algebra, Declaratively

- Matrix multiplication & other operations = just **joins!**
- The shift from **procedural** to **declarative** programming



$$C_{ij} = \sum_{k=1}^m A_{ik}B_{kj}$$

```
C = [[0]*p for i in range(n)]
for i in range(n):
    for j in range(p):
        for k in range(m):
            C[i][j] += A[i][k] * B[k][j]
```



```
SELECT A.i, B.j, SUM(A.x * B.x)
FROM A, B
WHERE A.j = B.i
GROUP BY A.i, B.j;
```

*Proceed through a series of instructions*

*Declare a desired output set*

# Common SQL Query Paradigms

GROUP BY / HAVING + Aggregators + Nested queries

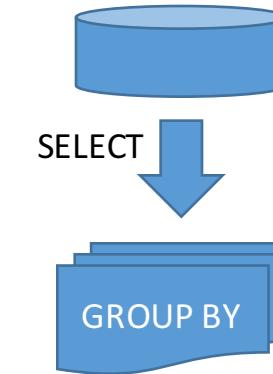
```
SELECT station_id,  
       COUNT(day) AS nbd  
FROM precipitation,  
     (SELECT day, MAX(precip)  
      FROM precipitation  
     GROUP BY day) AS m  
WHERE day = m.day AND precip = m.precip  
GROUP BY station_id  
HAVING COUNT(day) > 1  
ORDER BY nbd DESC;
```

Think about **order\***!

*\*of the semantics, not the actual execution*

# Common SQL Query Paradigms

GROUP BY / HAVING + Aggregators + Nested queries



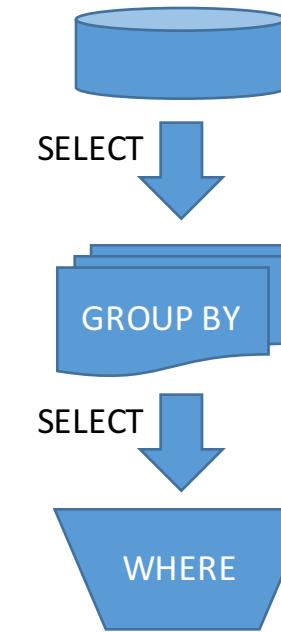
Get the max precipitation **by day**

```
SELECT station_id,  
       COUNT(day) AS nbd  
FROM precipitation,  
     (SELECT day, MAX(precip)  
      FROM precipitation  
     GROUP BY day) AS m  
WHERE day = m.day AND precip = m.precip  
GROUP BY station_id  
HAVING COUNT(day) > 1  
ORDER BY nbd DESC;
```

# Common SQL Query Paradigms

GROUP BY / HAVING + Aggregators + Nested queries

```
SELECT station_id,  
       COUNT(day) AS nbd  
FROM precipitation,  
     (SELECT day, MAX(precip)  
      FROM precipitation  
     GROUP BY day) AS m  
WHERE day = m.day AND precip = m.precip  
GROUP BY station_id  
HAVING COUNT(day) > 1  
ORDER BY nbd DESC;
```



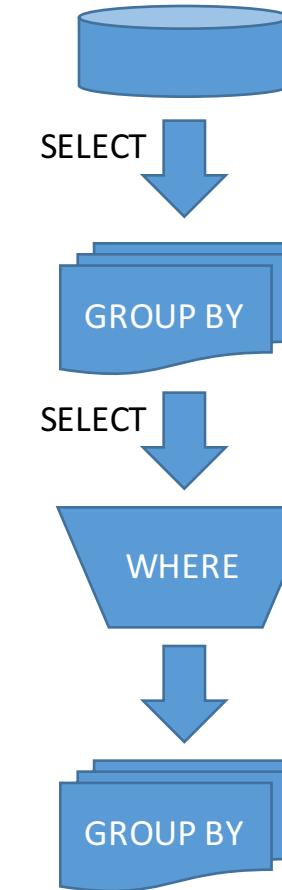
Get the max precipitation **by day**

Get the station, day pairs where / when this happened

# Common SQL Query Paradigms

GROUP BY / HAVING + Aggregators + Nested queries

```
SELECT station_id,  
       COUNT(day) AS nbd  
FROM precipitation,  
     (SELECT day, MAX(precip)  
      FROM precipitation  
     GROUP BY day) AS m  
WHERE day = m.day AND precip = m.precip  
GROUP BY station_id  
HAVING COUNT(day) > 1  
ORDER BY nbd DESC;
```



Get the max precipitation **by day**

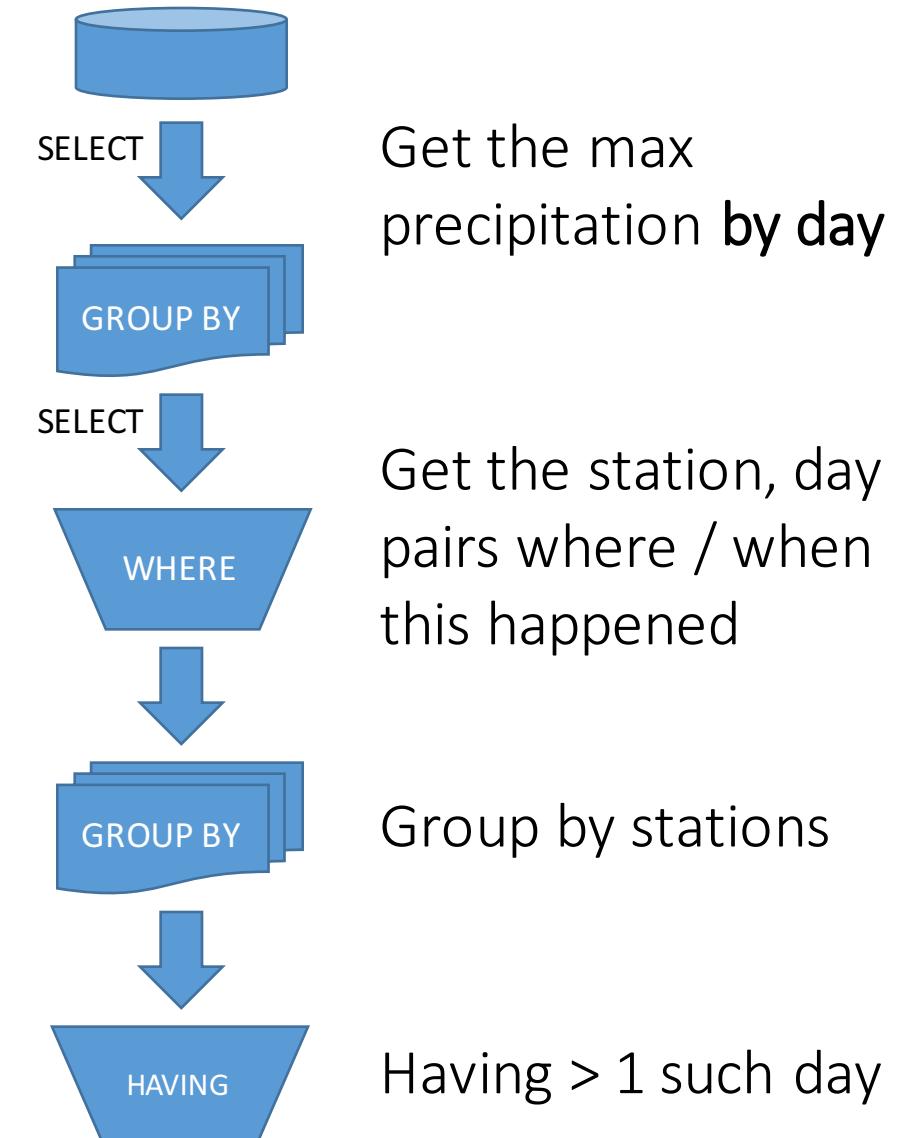
Get the station, day pairs where / when this happened

Group by stations

# Common SQL Query Paradigms

GROUP BY / HAVING + Aggregators + Nested queries

```
SELECT station_id,  
       COUNT(day) AS nbd  
FROM precipitation,  
     (SELECT day, MAX(precip)  
      FROM precipitation  
     GROUP BY day) AS m  
WHERE day = m.day AND precip = m.precip  
GROUP BY station_id  
HAVING COUNT(day) > 1  
ORDER BY nbd DESC;
```



# Common SQL Query Paradigms

## Complex correlated queries

```
SELECT x1.p AS median
FROM x AS x1
WHERE
  (SELECT COUNT(*)
   FROM X AS x2
   WHERE x2.p > x1.p)
  =
  (SELECT COUNT(*)
   FROM X AS x2
   WHERE x2.p < x1.p);
```

This was a tricky problem- but good practice in thinking about things declaratively

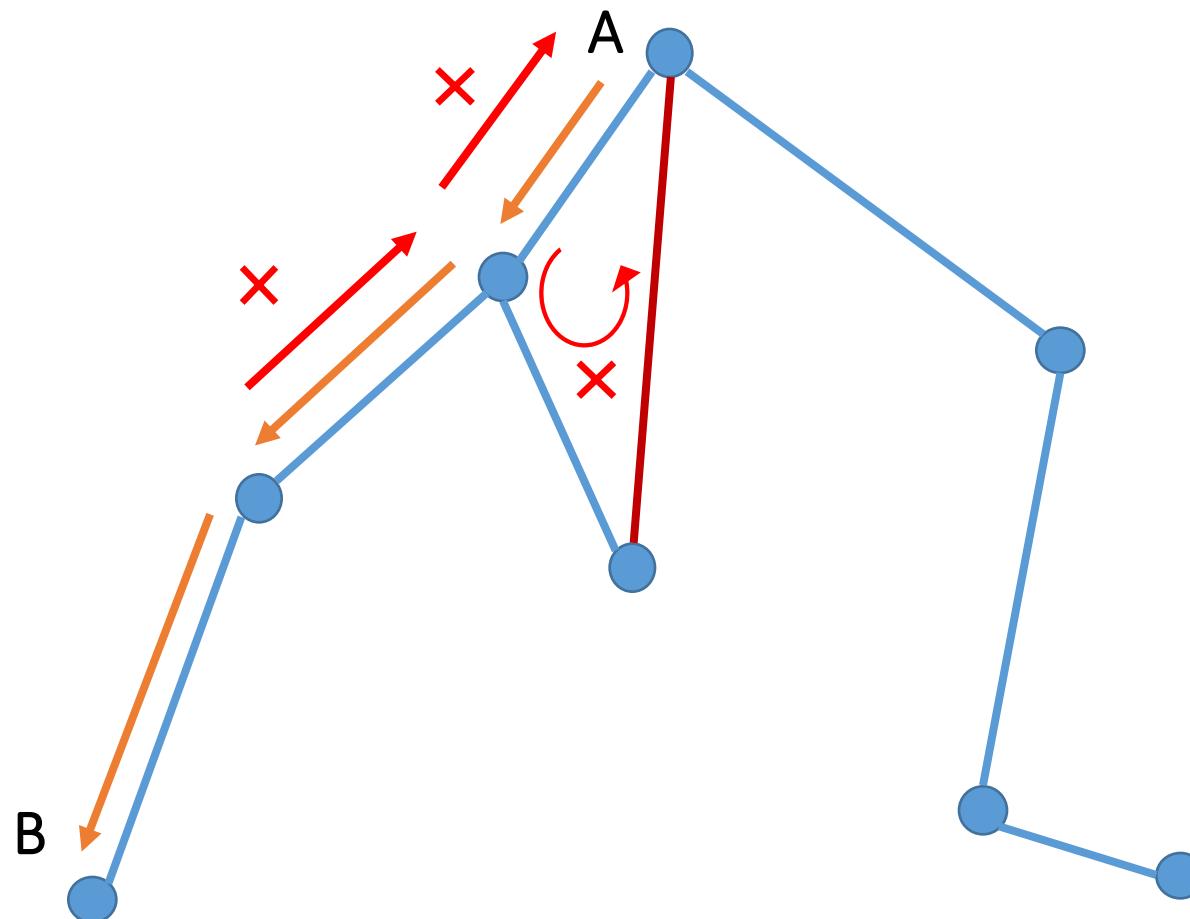
# Common SQL Query Paradigms

## Nesting + EXISTS / ANY / ALL

```
SELECT sid, p3.precip
FROM (
    SELECT sid, precip
    FROM precipitation AS p1
    WHERE precip > 0 AND NOT EXISTS (
        SELECT p2.precip
        FROM precipitation AS p2
        WHERE p2.sid = p1.sid
            AND p2.precip > 0
            AND p2.precip < p1.precip)) AS p3
WHERE NOT EXISTS (
    SELECT p4.precip
    FROM precipitation AS p4
    WHERE p4.precip - 400 > p3.precip);
```

More complex,  
but again just  
think about  
order!

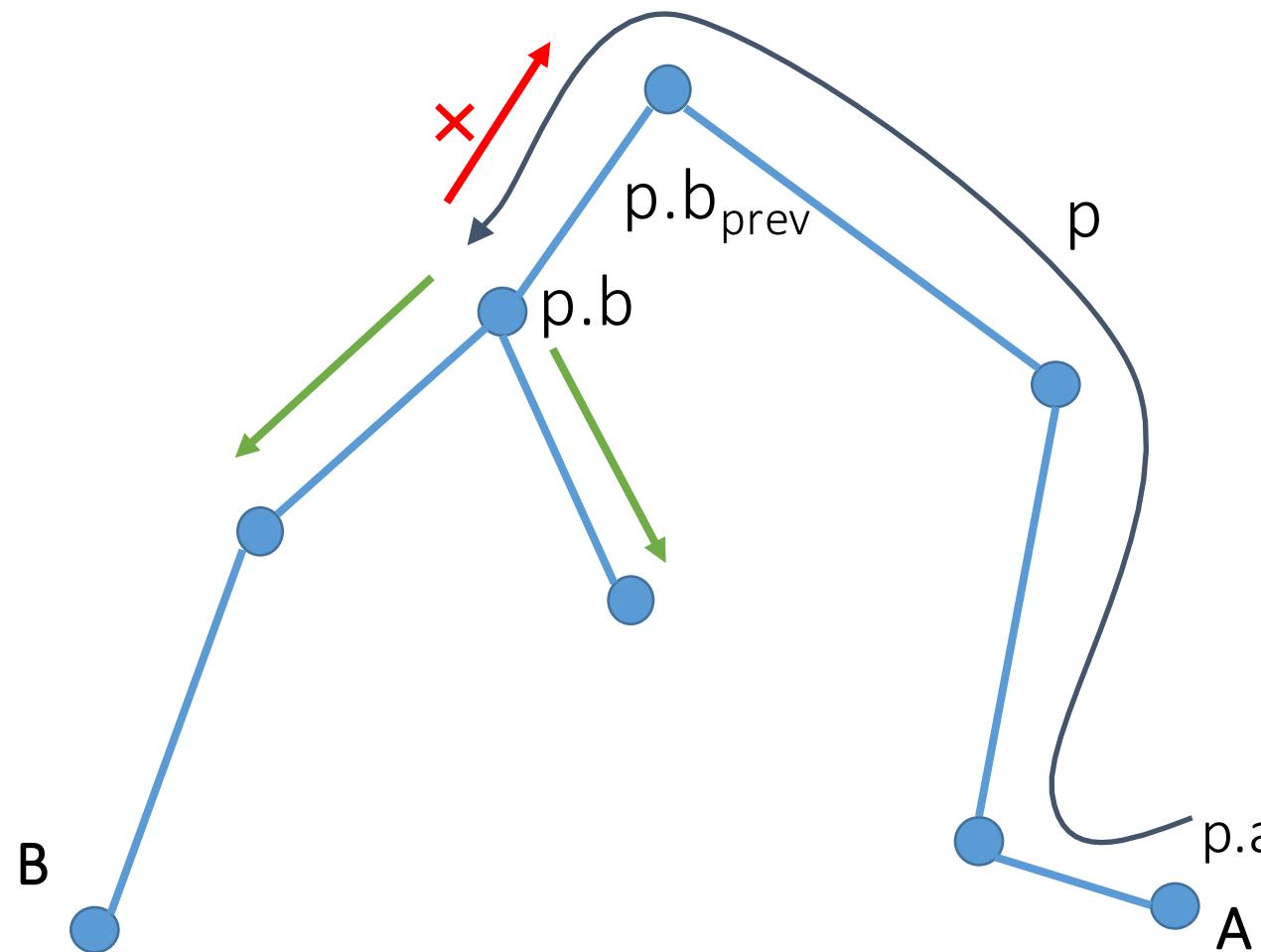
# Graph traversal & recursion



## For fixed-length paths

```
SELECT A, B, d
FROM edges
UNION
SELECT e1.A, e2.B,
       e1.d + e2.d AS d
FROM edges e1, edges e2
WHERE e1.B = e2.A
      AND e2.B <> e1.A
UNION
SELECT e1.A, e3.B,
       e1.d + e2.d + e3.d AS d
FROM edges e1, edges e2, edges e3
WHERE e1.B = e2.A
      AND e2.B = e3.A
      AND e2.B <> e1.A
      AND e3.B <> e2.A
      AND e3.B <> e1.A
```

# Graph traversal & recursion



For variable-length paths on trees

```

WITH RECURSIVE
paths(a, b, b_prev, d) AS (
    SELECT A, B, A
    FROM edges
    UNION
    SELECT p.a, e.B, e.A,
           p.d + e.d
    FROM paths p, edges e
    WHERE p.b = e.A
          AND e.B <> p.b_prev)
SELECT a, b, MAX(d)
FROM paths;
  
```