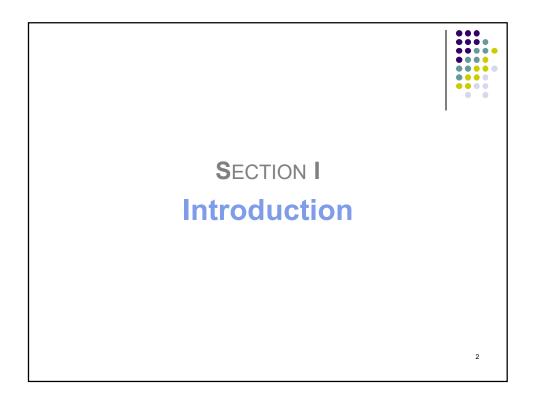
Determining Genome Sequences from Experimental Data Using Evolutionary Computation



Introduction



- Bioinformatics
 - Analyze and exploit the information in DNA sequences
- How to generate accurate sequence data?
 - Challenging, important, and time-consuming
- In this chapter
 - Determination of DNA sequences
 - Advanced optimization techniques
 - Evolutionary algorithm

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Sequencing by Hybridization



- How sequences are identified in the laboratory?
 - DNA sequencing
 - Determine the sequence of nucleotides (A, C, G, and T) in a DNA fragment of length n
- Sequencing by hybridization (SBH)
 - Stage 1: Hybridization experiment (DNA fragment → spectrum)
 - Detect all oligonucleotides (a short sequence of nucleotides) of a given length l that make up the DNA fragment
 - Compare the DNA fragment with the oligonucleotide library (microarray chips)

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Book Reading

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Sequencing by Hybridization



- Sequencing by hybridization (SBH)
 - Stage 2: Reconstructing the original sequence (spectrum → sequence)
 - An ideal spectrum (Stage 1 is performed without errors)
 - Find an ordering of the spectrum elements such that neighboring elements always overlap on *l* -1 nucleotides

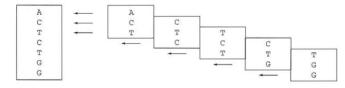
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Example: Reconstruction of Sequence from an Ideal Spectrum



- Original sequence (*n*=7)
 - ACTCTGG
- Oligonucleotide library (*I*=3)
 - AAA, AAC, AAG, AAT, ACA, ..., TTG, TTT
- Ideal spectrum
 - ACT, CTC, TCT, CTG, TGG
- Reconstructed sequence



3.1 FIGURE The reconstruction of the original sequence from the ideal spectrum. Oligonucleotides (in staggered boxes on the right) are ordered in such a way that neighbors always have l-1 nucleotides in common, which leads to the sequence in the box on the left.

Experimental Errors in the Spectrum



- Stage 1 usually produces errors in the spectrum
- Two types of errors
 - Negative errors (a, b)
 - Miss one or more words contained in the original sequence
 - Positive errors (c, d)
 - Contain words that are not found in the original sequence

	Sequence	Spectrum		
(a)	TTACATTA	{ACA, ATT, CAT, TAC, TTA}		
(b)	TTACATTC	{ACA, ATT, TAC, TTA, TTC}		
(c)	TTACAT	{ACA, CAT, TAC, TTA, TTT}		
(d)	TTACAT	{ACA, CAT, GAG, TAC, TTA}		

3.1 TABLE Examples of errors appearing in the spectrum. (a) The italicized fragments are two copies of the same oligonucleotide. The spectrum contains only one such element. (b) An accidental negative error, caused by an incomplete hybridization. (c) The positive error TTT, similar to TTA present in the sequence, appeared in the spectrum according to an imperfect hybridization. (d) An accidental positive

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SECTION II

Formulation of the Sequence Reconstruction Problem

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How About Stage 2?



- During the reconstruction process
 - Negative errors
 - Force overlap between some neighboring oligonucleotides consisting of fewer than I-1 letters
 - Positive errors
 - Force rejection of some oligonucleotides
- Reconstruction with errors
 - A strongly NP-hard combinatorial problem
 - Exact/heuristic methods
 - Restricted/unrestricted model of errors

An Integer Programming Formulation (1)



maximize:

$$\sum_{i=1}^{z} \sum_{j=1}^{z} b_{ij} + 1 \tag{3.1}$$

subject to:

$$\sum_{i=1}^{z} b_{ik} \le 1, \ k = 1, \dots, z$$
 (3.2)

$$\sum_{i=1}^{z} b_{ki} \le 1, \ k = 1, \dots, z$$
(3.3)

$$\sum_{k=1}^{z} \left(\left| \sum_{i=1}^{z} b_{ki} - \sum_{j=1}^{z} b_{jk} \right| \right) = 2$$
 (3.4)

$$\sum_{i=1}^{z} b_{ik} \le 1, \ k = 1, \dots, z$$

$$\sum_{i=1}^{z} b_{ki} \le 1, \ k = 1, \dots, z$$

$$\sum_{k=1}^{z} \left(\left| \sum_{i=1}^{z} b_{ki} - \sum_{j=1}^{z} b_{jk} \right| \right) = 2$$

$$\sum_{k \in S'} \left(\sum_{s \in S'} b_{ik} \cdot \sum_{s \in S'} b_{kj} \right) < |S'|, \ \forall S' \subset S, \ S' \ne \emptyset$$

$$\sum_{i=1}^{z} \sum_{j=1}^{z} c_{ij} b_{ij} \le n - 1,$$
(3.2)
$$(3.2)$$

$$(3.3)$$

$$(3.4)$$

$$(3.5)$$

$$\sum_{i=1}^{z} \sum_{j=1}^{z} c_{ij} b_{ij} \le n - 1, \tag{3.6}$$

An Integer Programming Formulation (2)



The maximized criterion function

maximize:

$$\sum_{i=1}^{z} \sum_{j=1}^{z} b_{ij} + 1 \tag{3.1}$$

= the number of spectrum elements composing the solution

An Integer Programming Formulation (3



Inequalities

subject to:

$$\sum_{i=1}^{z} b_{ik} \le 1, k = 1, \dots, z \tag{3.2}$$

$$\sum_{i=1}^{z} b_{ik} \le 1, \ k = 1, \dots, z$$

$$\sum_{i=1}^{z} b_{ki} \le 1, \ k = 1, \dots, z$$
(3.2)

 Guarantee that every element of the spectrum will be joined in the solution with, respectively, at most one element from the left side and at most one element from the right side

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An Integer Programming Formulation (4



Equation

$$\sum_{k=1}^{z} \left(\left| \sum_{i=1}^{z} b_{ki} - \sum_{j=1}^{z} b_{jk} \right| \right) = 2$$
 (3.4)

- Ensure that in any solution, precisely two elements appear that are connected to other elements from only one side
 - These elements constitute the **beginning** and the **end** of the reconstructed sequence

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An Integer Programming Formulation (5



Inequalities

$$\sum_{s_k \in S'} \left(\sum_{s_i \in S'} b_{ik} \cdot \sum_{s_j \in S'} b_{kj} \right) < |S'|, \ \forall S' \subset S, \ S' \neq \emptyset$$
 (3.5)

- Allow to eliminate solutions including subcycles of elements
 - An element in the solution that is simultaneously a successor and the immediate predecessor of another element in the solution

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An Integer Programming Formulation (6):



Inequality

$$\sum_{i=1}^{z} \sum_{j=1}^{z} c_{ij} b_{ij} \le n - 1, \tag{3.6}$$

• The length of the reconstructed sequence cannot exceed its known length

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Example: Reconstruction of a Sequence from a Spectrum Containing Errors



- Original sequence (*n*=7)
 - ACTCTGG
- Ideal spectrum
 - ACT, CTC, TCT, CTG, TGG
- Erroneous spectrum
 - ACT, CAA, CTG, TCT, TGG, TTG
- Exhaustive search of potential solutions
 - {ACT, TCT, CTG, TGG} → ACTCTGG (the original sequence)
 - {CAA, ACT, CTG, TGG} → CAACTGG

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SECTION III

A Hybrid Genetic Algorithm for Sequence Reconstruction

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A Hybrid Genetic Algorithm for Sequence Reconstruction

Blazewicz et al. (2002)



- Hybridized with a heuristic greedy-improvement method
 - Standard mutation → local search
- Gives surprisingly good results for difficult instances
 - Reconstructed sequences are very similar to the originals
 - · Compared with a tabu search method

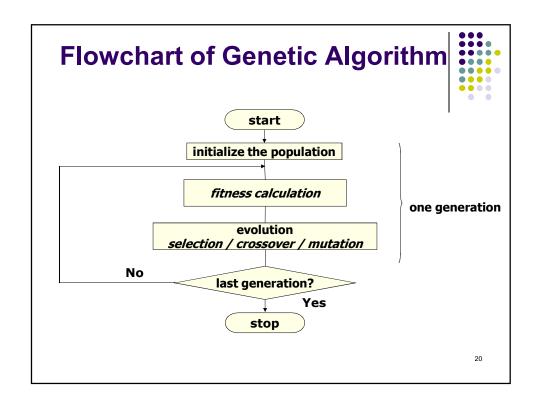
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Criterion Function and Constraint



- Given
 - A spectrum of elements (all of length l)
- To find
 - A solution that maximizes the number of elements
 - An ordering of elements chosen from the spectrum, with a corresponding reconstructed sequence
 - The maximum sequence length n
 - The reconstructed sequence should not be longer than n
 - The general model of errors
 - Nothing is assumed about the types and numbers of the errors that may exist in the spectrum

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Representation



- A candidate solution
 - A permutation of indices of oligonucleotides from the spectrum
 - · Adjacency-based encoding

4	1	5	3	6	2

 $1 \rightarrow 4, 2 \rightarrow 1, 3 \rightarrow 5, 4 \rightarrow 3, 5 \rightarrow 6, 6 \rightarrow 2$

- Example
 - Erroneous spectrum
 - ACT(1), CAA(2), CTG(3), TCT(4), TGG(5), TTG(6)
 - · Resulting cycle of spectrum elements
 - CTG(3), TGG(5), TTG(6), CAA(2), ACT(1), TCT(4), CTG(3)

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Fitness Function



- Evaluate the fitness of a candidate solution
 - Select the best substring of oligonucleotides in the chromosome
 - The largest number of elements
 - The neighboring oligonucleotides are maximally overlapped
 - Include as many elements as possible in the substring
 - Normalized fitness value =
 - the number of oligonucleotides in the substring l (n l + 1)
- Example
 - Evaluate 6 subpaths of the cycle for

CTG(3), TGG(5), TTG(6), CAA(2), ACT(1), TCT(4), CTG(3)

- CTG, TGG, TTG → CTGGTTG
- TGG, TTG → TGGTTG
- TTG, CAA → TTGCAA
- CAA, ACT, TCT → CAACTCT
- ACT, TCT, CTG, TGG → ACTCTGG (the best, fitness = 4)
- TCT, CTG, TGG → TCTGG

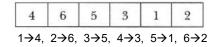
The normalized fitness = 4/(7-3+1)=0.8

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Initial Population



- Randomly generated according to a uniform distribution
 - Each candidate must be a permutation of indices
 - Each candidate must not include any subcycle involving fewer indices than the spectrum's cardinality
 - An infeasible candidate with 2 subcycles



- CTG(3), TGG(5), ACT(1), TCT(4), CTG(3)
- CAA(2), TTG(6), CAA(2)

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Genetic Operators



- Fitness
 - Normalized, and linear scaled
- Selection
 - Stochastic remainder without replacement
 - Elitism
 - Remember the best individual found in each generation
- Crossover
 - Greedy crossover
 - The first oligonucleotide: randomly
 - The next oligonucleotide: the best successor
 - Overlap by the largest number of necleotides

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SECTION IV

Results from Computational Experiments

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Experiment settings



- Compared with the tabu search method
 - The tabu search algorithm + a greedy constructive procedure for generating initial solutions
 - Require similar computation times
- Parameter settings
 - Population size: 50
 - Maximum number of iterations without improvement: 20
- Environment
 - Pentium II 300 MHz CPU, 256 MB RAM, and Linux OS
- Spectrum
 - Derived from DNA sequences coding human proteins taken from GenBank

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