



# **Probabilistic energy forecasting for smart grids and buildings**

Rob J Hyndman

21 March 2017

# Demand forecasting

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# Demand forecasting in the smart grid



Figure: <http://solutions.3m.com>

Energy sources (fossil fuel, wind, solar, wave, ...)

Supply



Energy consumers

Demand

# Demand forecasting in the smart grid

Need demand forecasts for outage planning, energy trading, demand response, system management, ...

## Predictors

- calendar effects
  - Time of day
  - Day of week
  - Time of year
  - Holidays
- prevailing and recent weather conditions
- demand response incentives
- household characteristics

We build a nonlinear nonparametric stochastic model of demand as a function of these predictors.

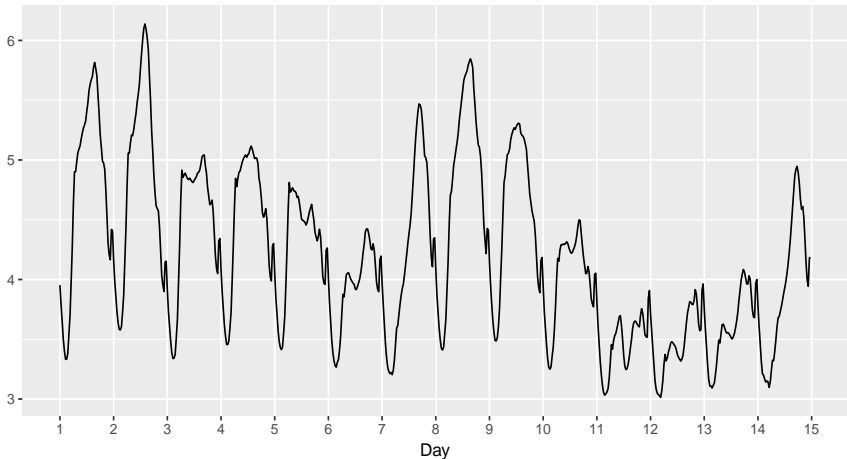
# Probabilistic forecasting

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# Probabilistic forecasting

**Aim: forecast entire probability distribution of demand, not only the average.**

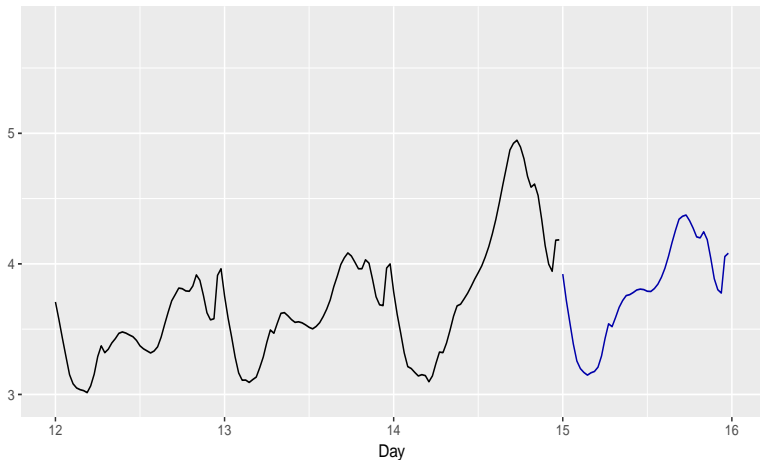
Half-Hourly electricity demand



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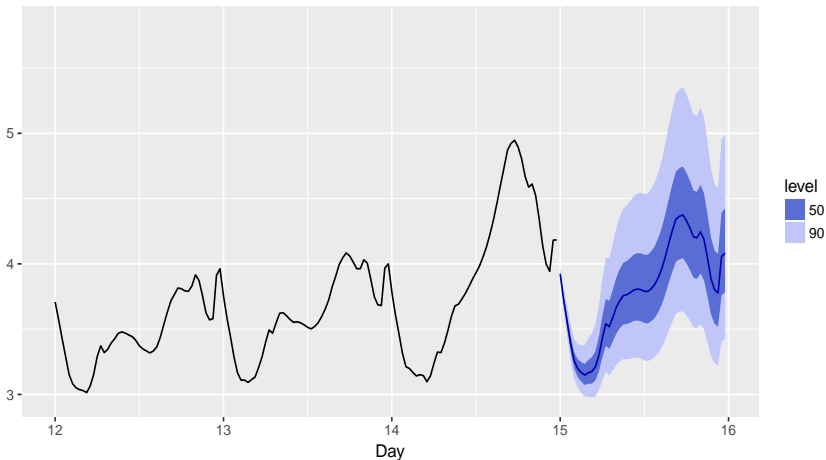
Point (mean) forecasts



# Probabilistic forecasting

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Point forecasts with prediction intervals

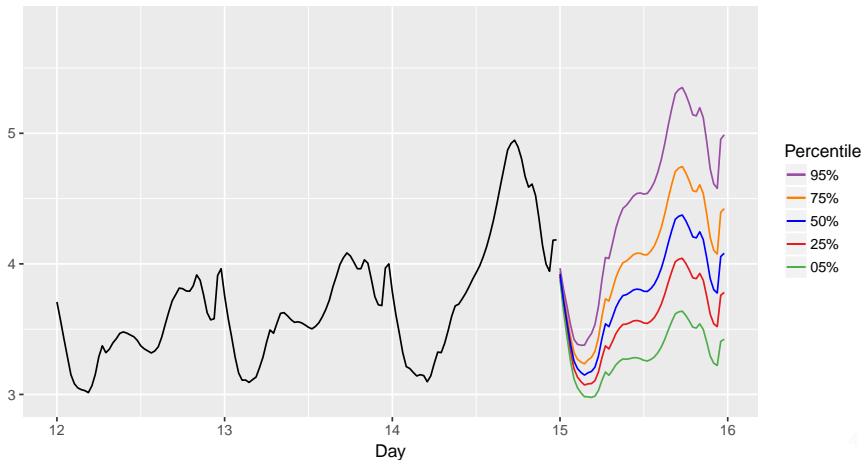




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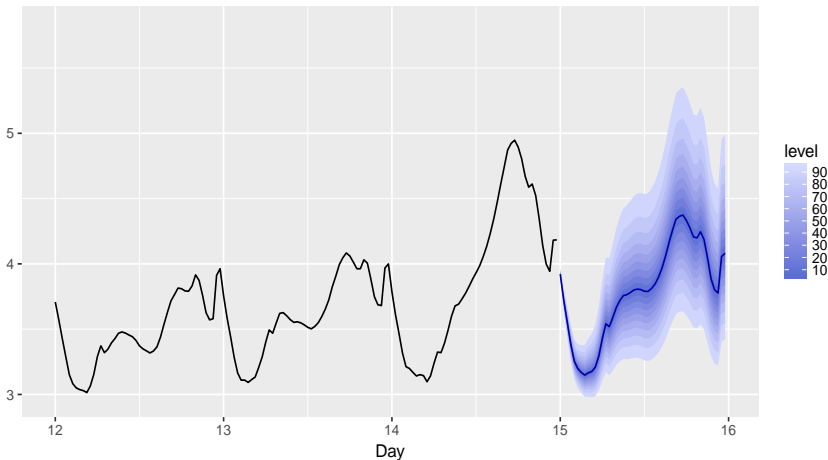
Point forecasts with percentiles



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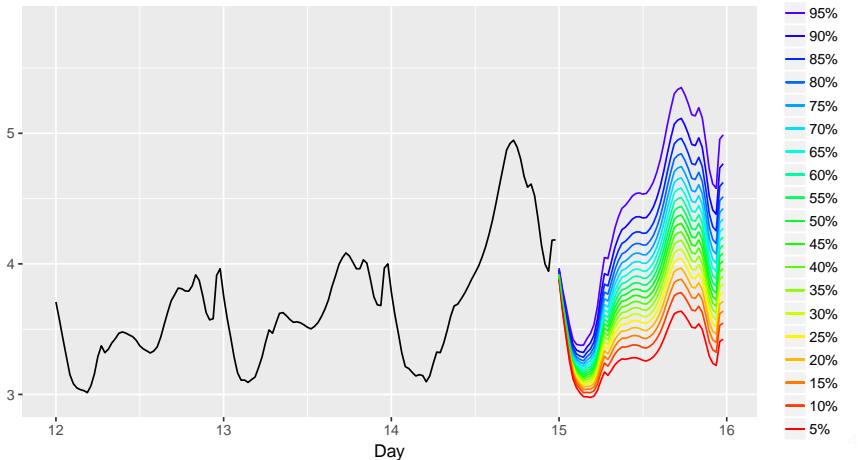
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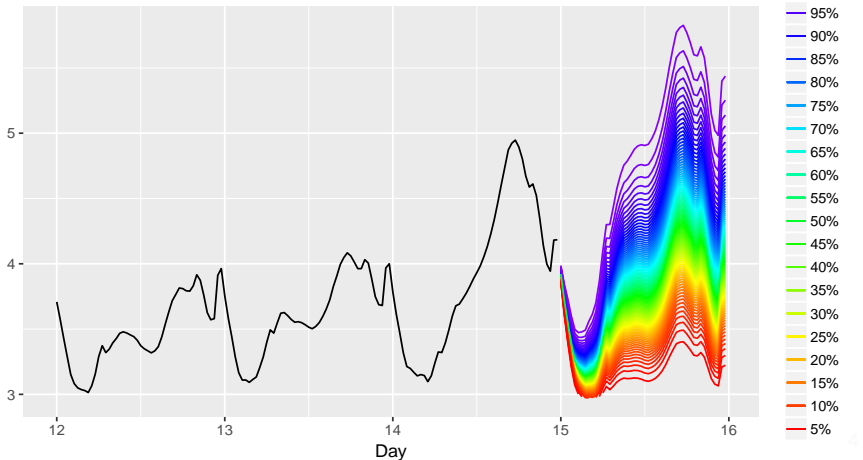
Point forecasts with percentiles



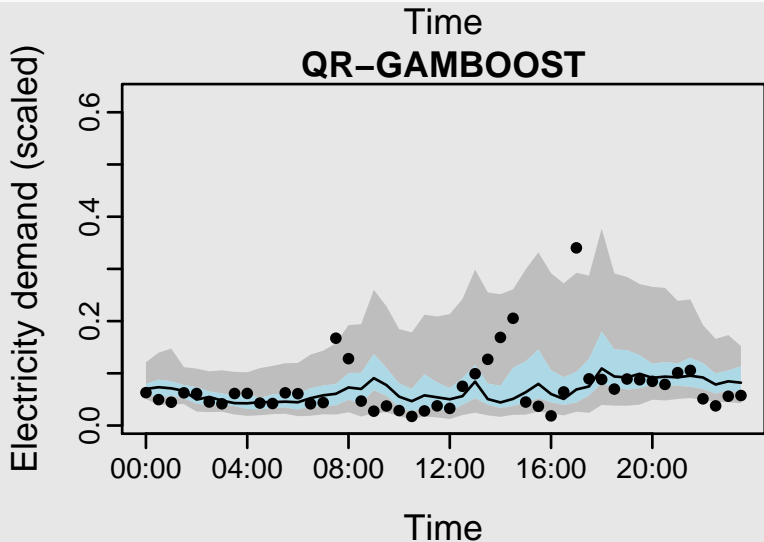
# Probabilistic forecasting

**Aim: forecast entire probability distribution of demand, not only the average.**

Point forecasts with percentiles



## Probabilistic forecasting



Half-hourly data. Blue: 50% region. Grey: 95% region.

## Forecast accuracy measures

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- MSE: Mean squared error
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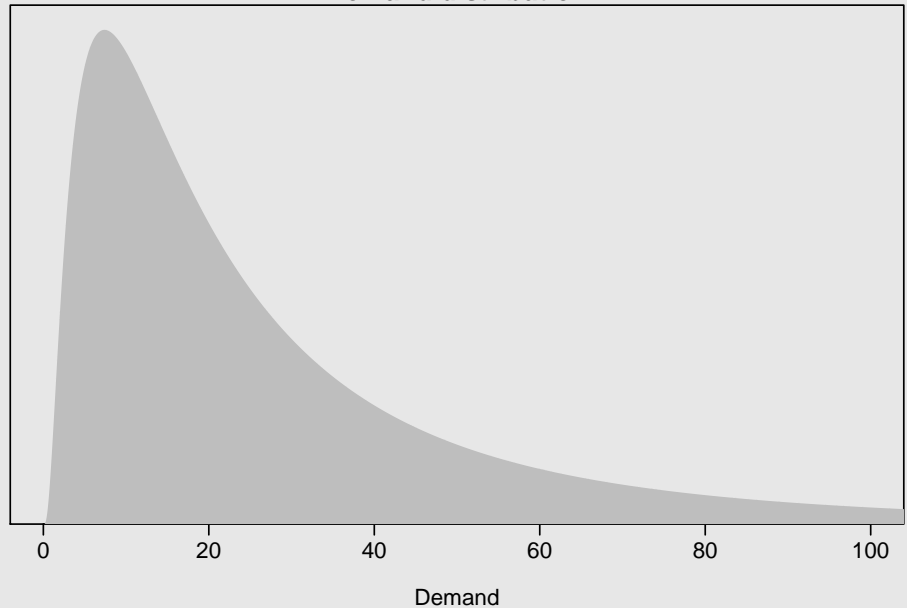
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- ➡ If  $q_t(p)$  is accurate, then  $y_t$  should be less than  $q_t(p)$  about  $100p\%$  of the time.
- ➡ Need to penalize unlikely side more (a “pinball loss” function) 6

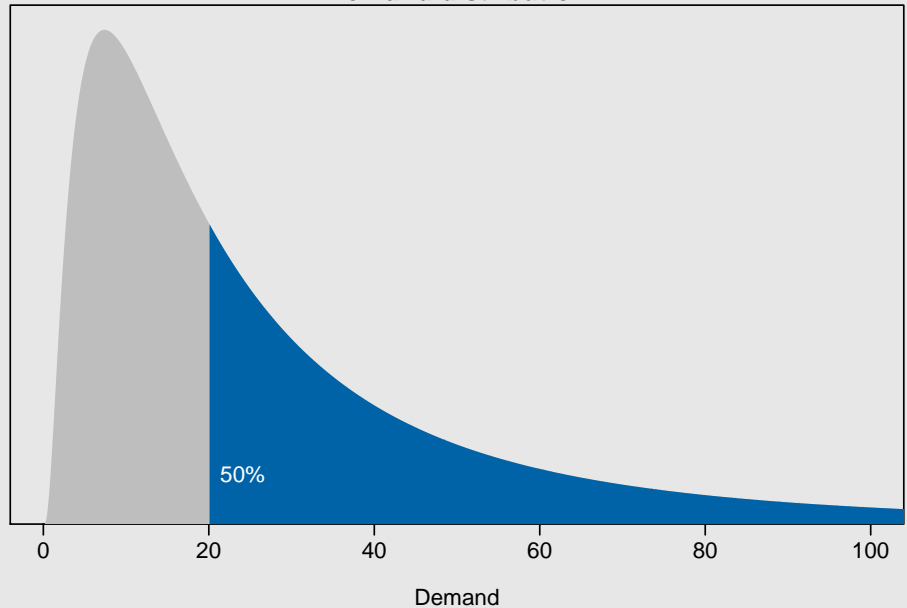
## Forecast scoring

**Demand distribution**



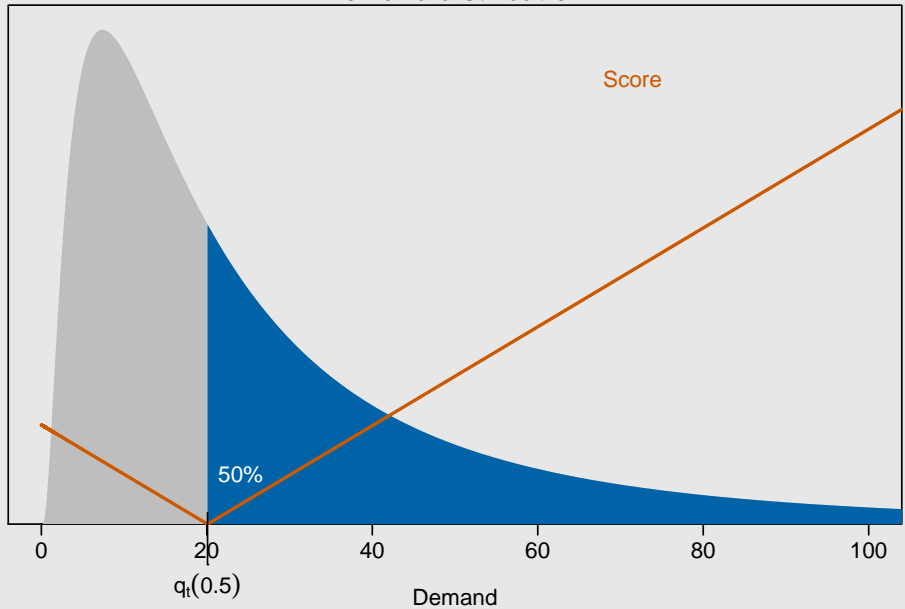
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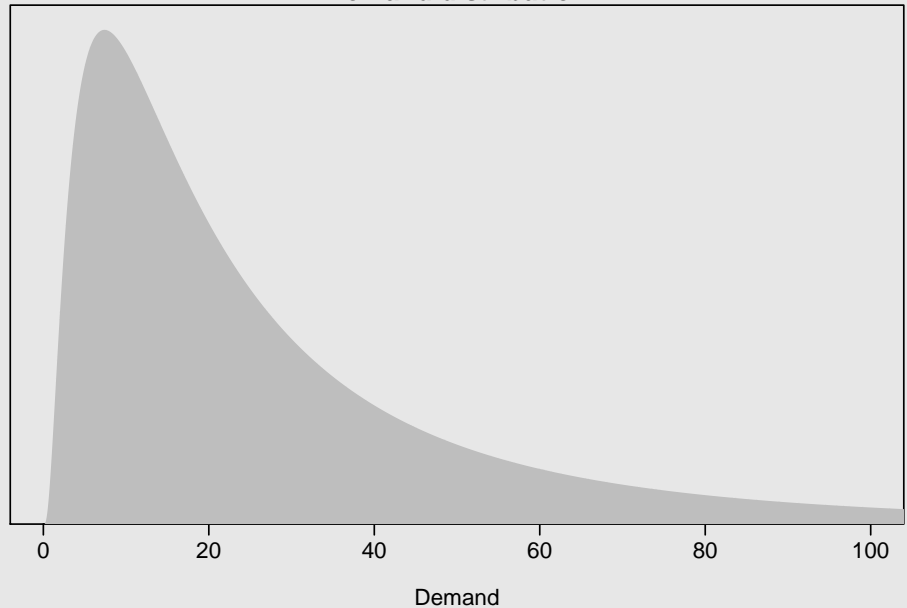
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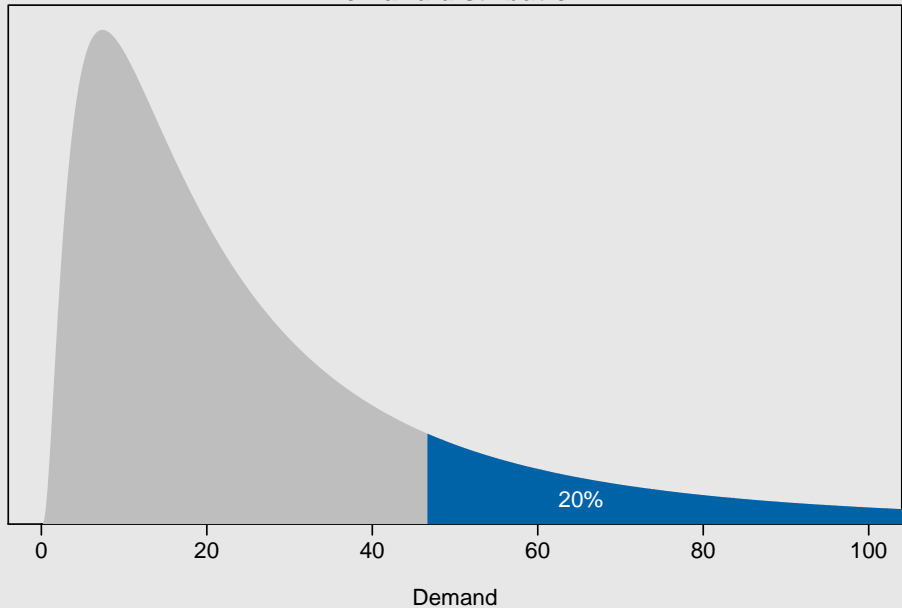
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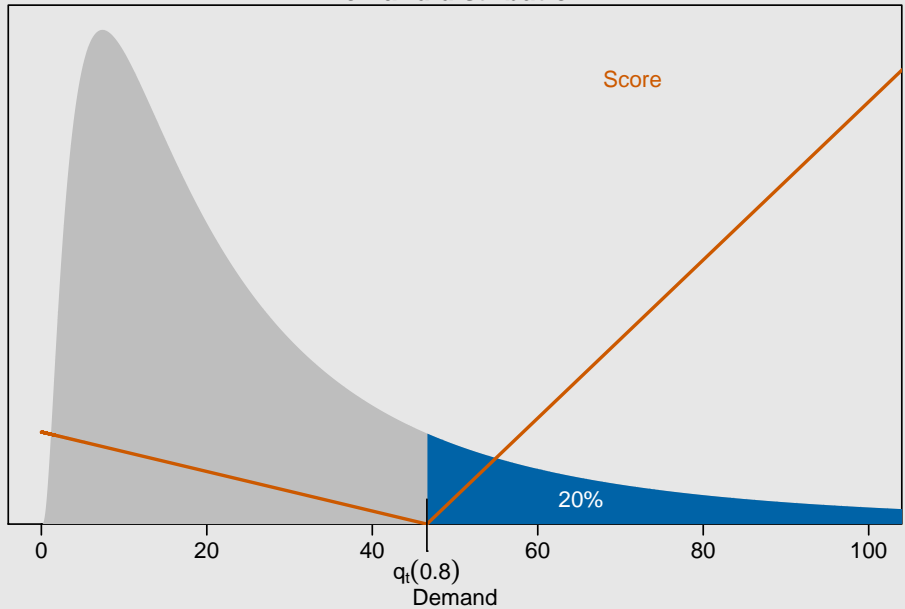
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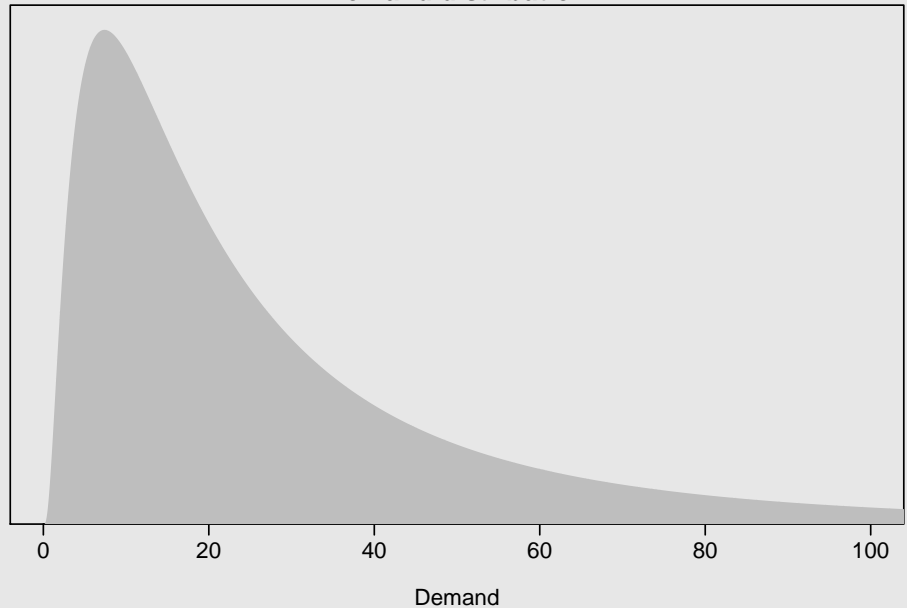
Demand distribution





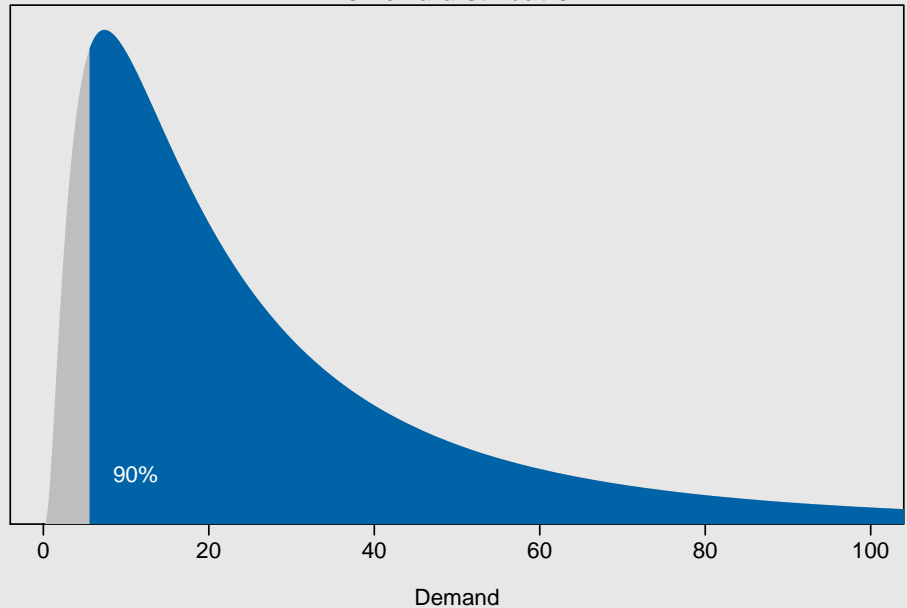
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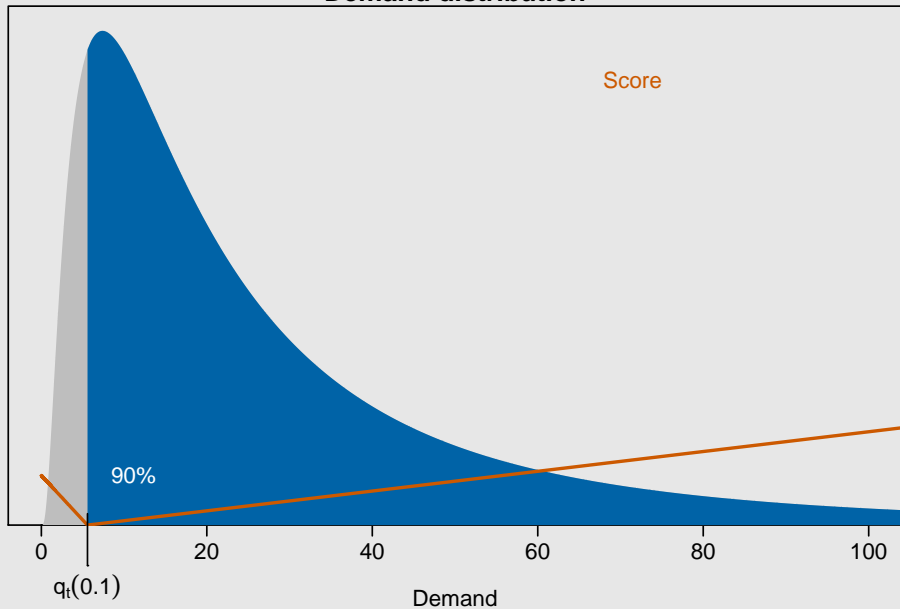
## Forecast scoring

**Demand distribution**



# Forecast scoring

Demand distribution



# Forecast scoring

Quantile Score for observation  $y$ :

For  $0 < p < 1$ :

$$S(y_t, q_t(p)) = \begin{cases} p(y_t - q_t(p)) & \text{if } y_t \geq q_t(p) \\ (1 - p)(q_t(p) - y_t) & \text{if } y_t < q_t(p) \end{cases}$$

- Scores are averaged over all observed data for each  $p$  to measure the accuracy of the forecasts for each percentile.
- Average score over all percentiles gives the best distribution forecast:

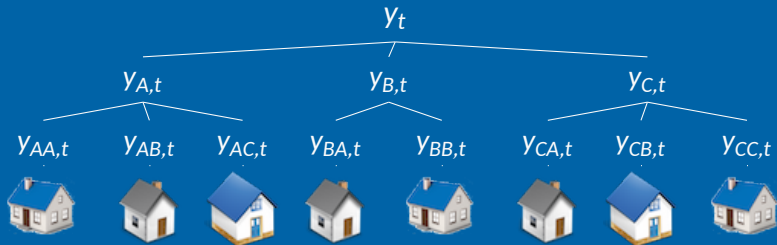
$$QS = \frac{1}{99T} \sum_{p=1}^{99} \sum_{t=1}^T S(q_t(p), y_t)$$

- Equivalent to CRPS (Continuous Rank Probability Score).
- Reduces to MAE if we are only interested in  $p = 0.5$ .

# Hierarchical forecasting

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# Hierarchical electricity demand data



$$y_t = y_{A,t} + y_{B,t} + y_{C,t}$$

$$y_{A,t} = y_{AA,t} + y_{AB,t} + y_{AC,t}$$

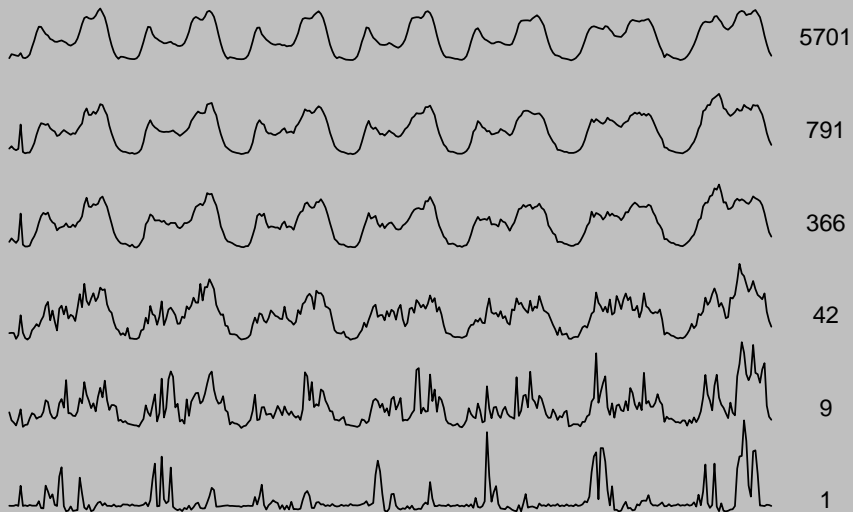
$$y_{B,t} = y_{BA,t} + y_{BB,t}$$

$$y_{C,t} = y_{CA,t} + y_{CB,t} + y_{CC,t}$$

Aggregations may be based on:

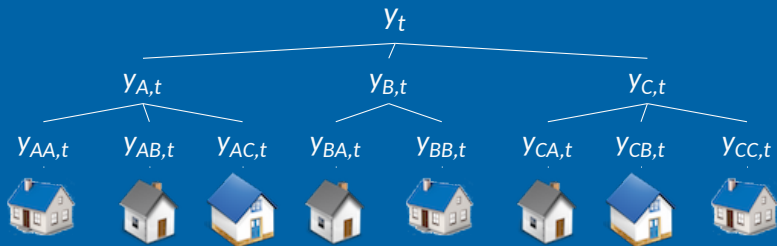
- Geography (suburbs, regions, states)
- Demography (number of people in household, age distributions)
- Appliances (air conditioning, electric heating)

# Hierarchical electricity demand data



Period of Week

# Hierarchical forecasting



- Easier to forecast at more aggregated levels.
- We forecast at every level and reconcile the forecasts.
- Optimal reconciliation algorithm: Hyndman et al (2011, 2016, 2017)
- Forecast means should add up, but percentiles are more complicated
- **Current research topic:** How to reconcile percentiles at all levels?



# Building-level energy forecasting

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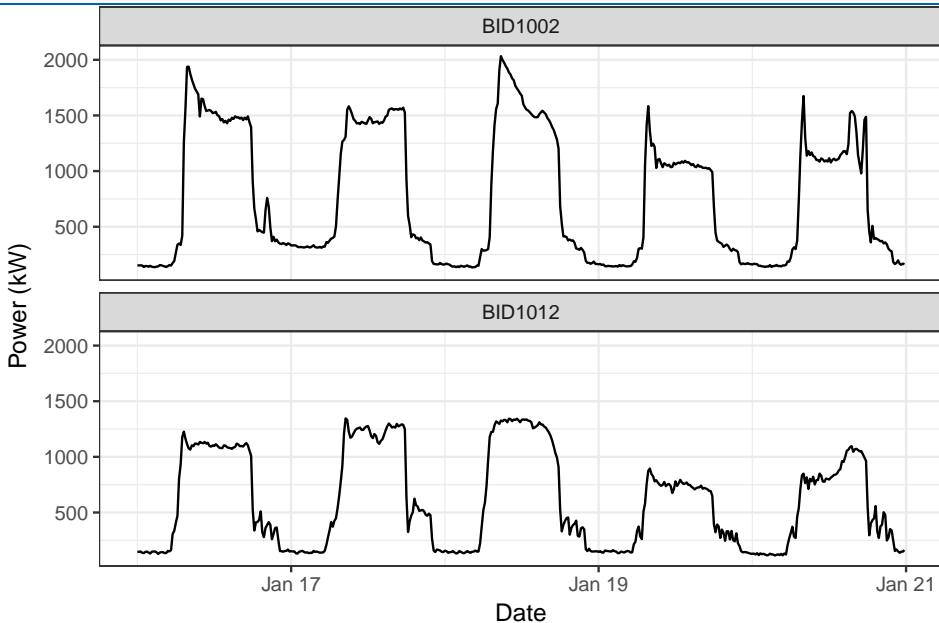
Commercial buildings require energy forecasting to help:

- Manage peak demand.
- Quantify the impacts of building management changes.
- Assess performance and energy efficiency.

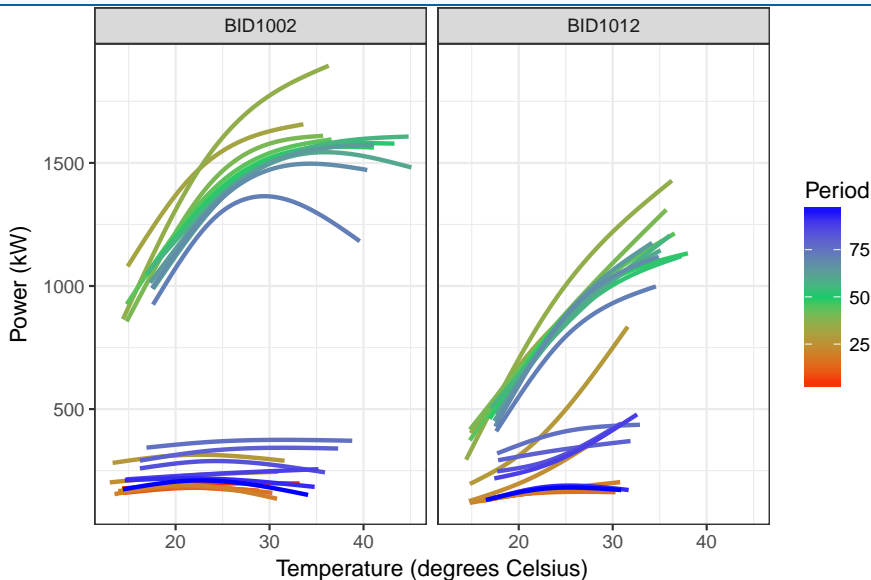
**Buildings Alive** works with 150+ commercial buildings which include supermarkets, hospitals and office blocks.

Each require daily forecasts to inform facilities managers.

# Building Level Data



# Building Level Data



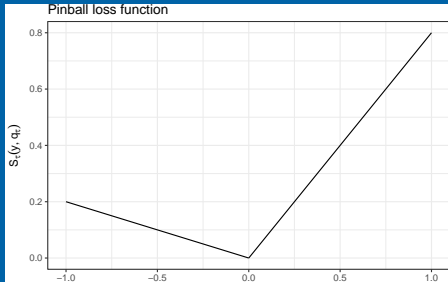
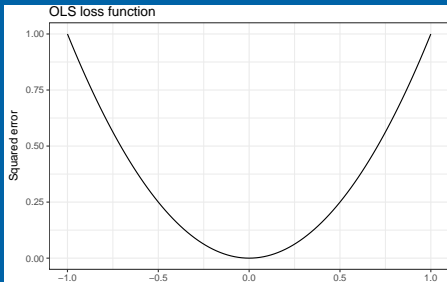
Natural cubic splines for each period of the day ( $df = 2$ ).

# Quantile Regression

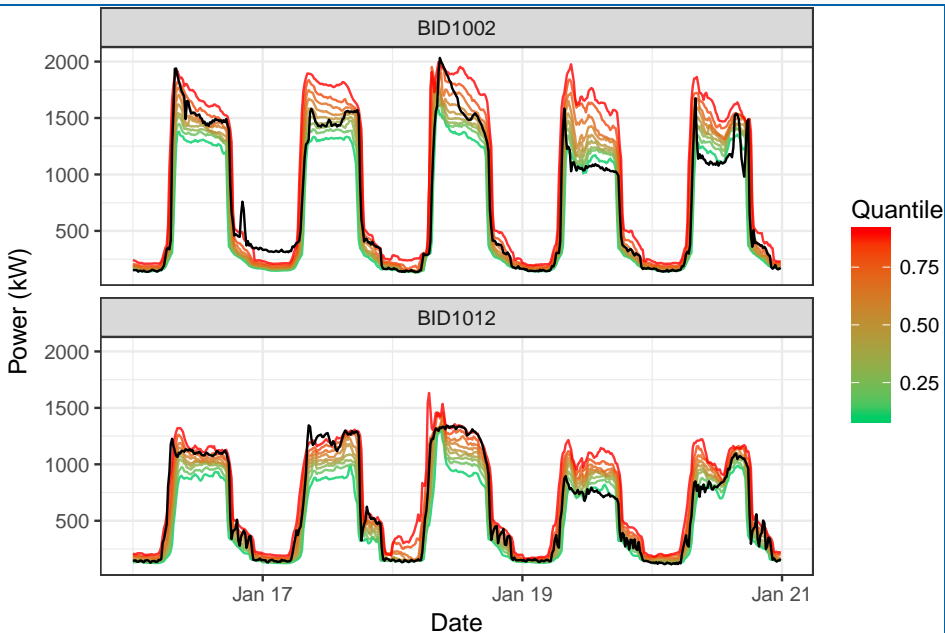
Probabilistic forecasts can be produced using quantile regression.

Use the pinball loss function:

$$S_p(y, q_p) = \begin{cases} p(y - q_p) & \text{for } y \geq q_p, \\ (1 - p)(q_p - y) & \text{for } q_p > y. \end{cases}$$



# Quantile Regression Forecasting



## Assessing performance

- Forecasting a full distribution allows facilities managers to better assess risks and take appropriate actions.
- Allows facilities managers to know the severity **and probability** of demand peaks.
- Can immediately assess if a building's performance was good compared to historical performance under similar conditions.

# Competitions, conferences and resources

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## Global Energy Forecasting Competitions

- Organized by Professor Tao Hong (UNC)
- GEFCom 2012: Load, Wind Forecasting
- GEFCom 2014: Load, Price, Wind, Solar Forecasting
- GEFCom 2017: Hierarchical probabilistic forecasts, real-time, rolling origin.
- **gefcom.org**
- Winning entries published in *International Journal of Forecasting*.
- Huge improvements in forecast accuracy over previously published methods.

# International Symposium on Energy Analytics 2017

## Predictive Energy Analytics in the Big Data World

Proudly sponsored by International Institute of Forecasters

June 22-23, 2017

Cairns, Australia

### Featured speakers

- Yannig Goude, Electricite de France, France
- Rob J Hyndman, Monash University, Australia
- Pierre Pinson, Technical University of Denmark, Denmark
- Richard Povinelli, Marquette University, USA
- Rafal Weron, Wroclaw University of Technology, Poland
- Hamidreza Zareipour, University of Calgary, Canada
- Xun Zhang, Chinese Academy of Sciences, China

# International Symposium on Forecasting 2017



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## PROGRAM NEWS

### Important 2017 Dates:

28 February	Proposals for invited sessions
28 February	Travel grant applications due
17 March	Abstract submission deadline
31 March	Abstract acceptance/rejection
14 April	Early registration deadline

## 37th International Symposium on Forecasting Cairns, Australia | Cairns Convention Centre 25-28 June 2017

The International Symposium on Forecasting (ISF) is the premier forecasting conference, attracting the world's leading forecasting researchers, practitioners, and students. Through a combination of keynote speaker presentations, academic sessions, workshops, and social programs, the ISF provides many excellent opportunities for networking, learning, and fun.

### Blogs

- [robjhyndman.com/hyndsight/](http://robjhyndman.com/hyndsight/)
- [blog.drhongtao.com/](http://blog.drhongtao.com/)

## Some resources

### Blogs

- [robjhyndman.com/hyndsight/](http://robjhyndman.com/hyndsight/)
- [blog.drhongtao.com/](http://blog.drhongtao.com/)

### Organizations

- International Institute of Forecasters:  
[forecasters.org](http://forecasters.org)
- IEEE Working Group on Energy Forecasting:  
[linkedin.com/groups/  
IEEE-Working-Group-on-Energy-4148276](http://linkedin.com/groups/IEEE-Working-Group-on-Energy-4148276)

# References

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