

MONASH BUSINESS SCHOOL

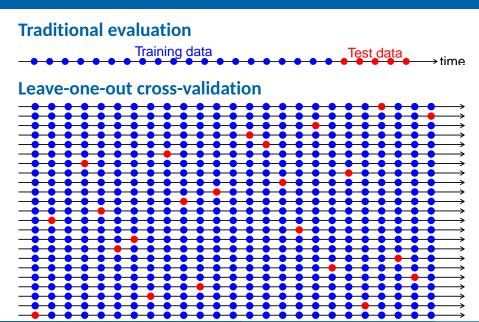
# Forecasting using R

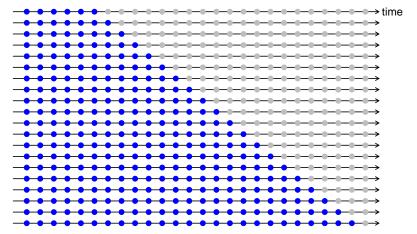
**Rob J Hyndman** 

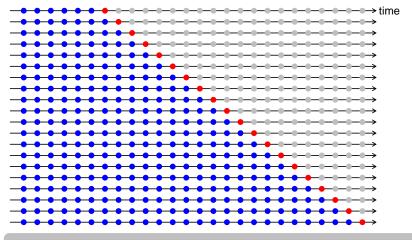
# **Outline**

1 Time series cross-validation

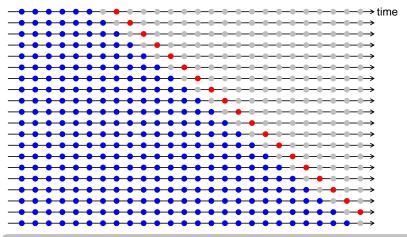
2 Lab session 13



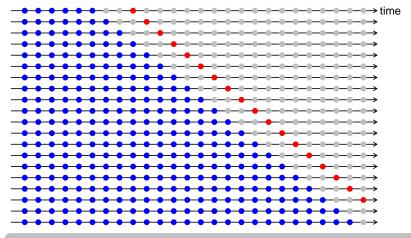




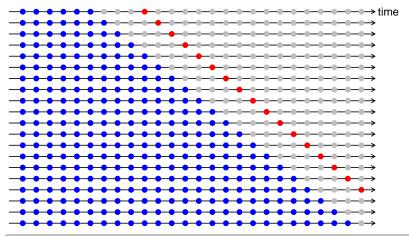
$$h = 1$$



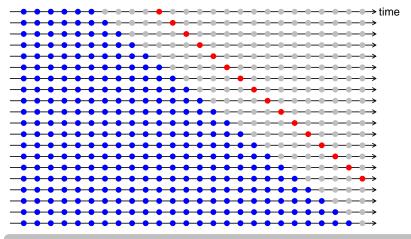
$$h = 2$$



$$h = 3$$

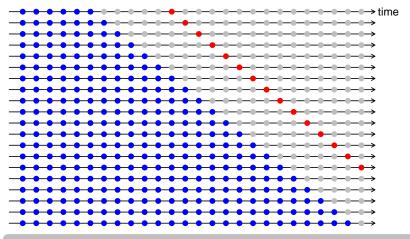


$$h = 4$$



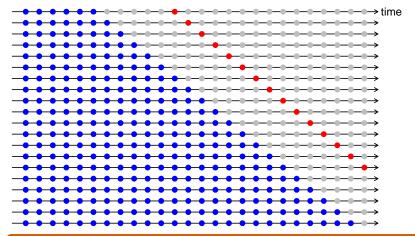
$$h = 5$$

## Time series cross-validation



$$h = 6$$

## Time series cross-validation



Also known as "Evaluation on a rolling forecast origin"

## Some connections

#### **Cross-sectional data**

Minimizing the AIC is asymptotically equivalent to minimizing MSE via leave-one-out cross-validation. (Stone, 1977).

## Time series cross-validation

Minimizing the AIC is asymptotically equivalent to minimizing MSE via one-step cross-validation. (Akaike, 1969, 1973).

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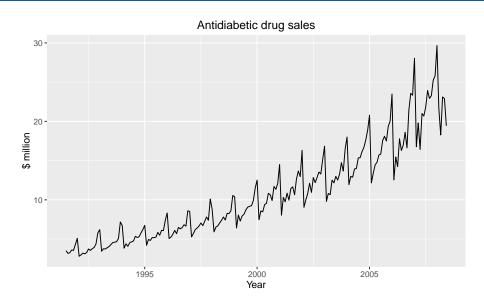
### Time series cross-validation

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## Time series cross-validation

Assume *k* is the minimum number of observations for a training set.

- Select observation k + i for test set, and use observations at times 1, 2, ..., k + i 1 to estimate model.
- Compute error on forecast for time k + i.
- Repeat for i = 0, 1, ..., T k where T is total number of observations.
- Compute accuracy measure over all errors.

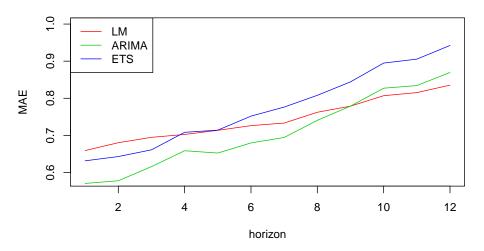


## Which of these models is best?

- Linear model with trend and seasonal dummies applied to log data.
- ARIMA model applied to log data
- ETS model applied to original data
- Set k = 48 as minimum training set.
- Forecast 12 steps ahead based on data to time k+i-1 for  $i=1,2,\ldots,156$ .
- Compare MAE values for each forecast horizon.

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- Compare MAE values for each forecast horizon.



```
k < -48
n <- length(a10)
mae1 <- mae2 <- mae3 <- matrix(NA,n-k-12,12)
for(i in 1:(n-k-12))
  xshort \leftarrow window(a10.end=1995+(5+i)/12)
  xnext < -window(a10, start=1995+(6+i)/12, end=1996+(5+i)/12)
  fit1 <- tslm(xshort ~ trend + season, lambda=0)
  fcast1 <- forecast(fit1,h=12)</pre>
  fit2 <- auto.arima(xshort,D=1, lambda=0)
  fcast2 <- forecast(fit2.h=12)</pre>
  fit3 <- ets(xshort)
  fcast3 <- forecast(fit3,h=12)</pre>
  mae1[i,] <- abs(fcast1[['mean']]-xnext)</pre>
  mae2[i,] <- abs(fcast2[['mean']]-xnext)</pre>
  mae3[i,] <- abs(fcast3[['mean']]-xnext)</pre>
plot(1:12,colMeans(mae1),type="l",col=2,xlab="horizon",ylab="MAE",
     vlim=c(0.58,1.0)
lines(1:12,colMeans(mae2),type="l",col=3)
lines(1:12,colMeans(mae3),type="l",col=4)
legend("topleft",legend=c("LM","ARIMA","ETS"),col=2:4,lty=1)
```

#### Variations on time series cross validation

Keep training window of fixed length.

```
xshort <- window(a10,start=i+1/12,end=1995+(5+i)/12)
```

■ Compute one-step forecasts in out-of-sample period.

```
for(i in 1:(n-k))
  xshort <- window(a10,end=1995+(5+i)/12)
  xlong \leftarrow window(a10, start=1995+(6+i)/12)
  fit2 <- auto.arima(xshort,D=1, lambda=0)
  fit2a <- Arima(xlong,model=fit2)</pre>
  fit3 <- ets(xshort)
  fit3a <- ets(xlong,model=fit3)</pre>
  mae2a[i,] <- abs(residuals(fit3a))</pre>
```

# **Outline**

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2 Lab session 13

Forecasting using R Lab session 13

# **Lab Session 13**

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