a) 
$$\vec{n}_{1} = \vec{e}_{1} = (1,0,0)$$

$$|\vec{t}_{i,s}|^2 = (1+4+q)-1$$
  $\rightarrow |t_{i,s}| = 3.61 \text{ MPa}$ 
 $|t_{2,s}| = 5.83 \text{ MPa}$ 

c) normal = 
$$\frac{1}{3}(2,2,1)$$
 unit length  $\hat{t} = \hat{r}^{T} \cdot \hat{r} = \frac{1}{3}(\frac{9}{17})$  MPa

a) for which 
$$\hat{h}$$
 is  $\hat{t} = \vec{\Gamma} \cdot \hat{n} = \vec{o}$ ?

$$(n_1, -n_2, 0) = (0, 0, 0)^{?}$$

=> requires 
$$n_1 = n_2 = 0$$
,  $n_3$  free  
=>  $\hat{h} = (0,0,1)$ 

$$\Rightarrow \vec{t} \cdot \hat{n} = (n_1^2 - n_2^2) \stackrel{?}{=} 0$$

$$=> N_1 = N_2 \quad \text{or} \quad N_1 = -N_2 \quad \text{or} \quad N_1 = N_2 = 0$$

$$\hat{h} = \frac{1}{2} \sqrt{2} (1,1,0)$$
 $\hat{h} = (0,0,1)$ 

$$\hat{h} = \frac{1}{2} \sqrt{2} (1, -1, 0)$$

(a) principal stress = eigenvalues
$$-\lambda^{3} + \tau^{2}\lambda = 0 \implies \lambda_{1} = -\tau ; \lambda_{2} = \tau, \lambda_{3} = 0$$
eigenvectors = principal stress directions
$$(\vec{x}, \vec{x}^{(i)}) = -\tau \vec{x}^{(i)}$$

$$= \sum_{j=0}^{\infty} x_{j}^{(i)} = -x_{j}^{(i)} + x_{j}^{(i)} = 0$$
normalised:  $\hat{x}^{(i)} = \frac{1}{2}\sqrt{2}(-1)$ 

$$\hat{X}^{(2)} = \frac{1}{2} \sqrt{2} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$
 => check that right handed  $\hat{X}^{(3)} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$  => System

(6) max. Shear 8tress -> = T

-> original coordinate 8 ystem

which is rotated 45° relative to

principal 8tress directions  $\hat{\chi}^{(1)}$  and  $\hat{\chi}^{(2)}$ (around  $\hat{\chi}^{(3)}$ )

or 
$$\Gamma'_{ns} = \Gamma_{n} \cos \varphi \sin \varphi + \Gamma_{21} \sin^{2}\varphi - \Gamma_{12} \cos^{2}\varphi - \Gamma_{22} \cos \varphi \sin \varphi$$

$$= (\Gamma_{1} - \Gamma_{2}) \cos \varphi \sin \varphi$$

$$= \omega \quad \text{principal stress system}$$

$$\omega \quad \text{maximum when } \frac{\partial \Gamma_{ns}}{\partial \varphi} = 0 \implies \cos^{2}\varphi = 0$$

$$\varphi = 45^{\circ} \text{ or } 135^{\circ}$$

plane 
$$X_{1}=1$$
  $\rightarrow$  normal  $(1,0,0)$   
 $\overrightarrow{t}$  on this plane  $=\begin{pmatrix} X_{1}+X_{2} \\ \Gamma_{12} \end{pmatrix} \begin{pmatrix} X_{1}+X_{2} \\ \Gamma_{12} \end{pmatrix}$ 

$$=> \Gamma_{12} (x_1=1) = 5-x_2$$
take linear in  $x_1 => \Gamma_{12} = \alpha x_1 + c - x_2$ 

$$= 5 \text{ for } x_1=1$$

in 
$$X_2$$
 direction =>  $\frac{\partial \Gamma_{12}}{\partial X_1} + \frac{\partial \Gamma_{22}}{\partial X_2} + \frac{\partial \Gamma_{32}}{\partial X_3} = 0$ 

$$a - 2 + 0 = 0$$

$$\Rightarrow a = 2, c = 3$$

=> 
$$\sigma_{12}(x_1, x_2) = 2x_1 + 3 - x_2$$

(a) write out 
$$\underline{\Gamma}'$$
 and  $8um$  diagonal elements  $\Longrightarrow$  tr  $(\underline{\Gamma}')=0$ 

(b) 
$$\Gamma' = 100 \begin{bmatrix} 0 & 5 & -2 \\ 5 & -3 & 4 \end{bmatrix} | CPa$$

of A transformation that diagonalises 5

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} = A \cdot \begin{bmatrix} 0 & + & 0 & \text{the } \end{bmatrix} \cdot A^{T}$$

$$= A \cdot 0 \cdot A^{T} + \text{Cut } I$$

also diagonalises [