

$$\textcircled{1} \quad f(x+h) \approx f(x) + hf'(x)$$

$$h=1 \quad f'(x) \approx f(x+1) - f(x)$$

$$\textcircled{2} \quad f(x-h) \approx f(x) - hf'(x)$$

$$\textcircled{1} - \textcircled{2} \Rightarrow f'(x) \approx \frac{f(x+1) - f(x-1)}{2}$$

$$\begin{aligned}\nabla^2 f(i, j) &= f(i, j-1) + f(i, j+1) \\ &\quad + f(i-1, j) + f(i+1, j) \\ &\quad - 4f(i, j)\end{aligned}$$

|   |    |   |
|---|----|---|
| 0 | 1  | 0 |
| 1 | -4 | 1 |
| 0 | 1  | 0 |

$$f'(x) \approx \frac{f(x+1) - f(x-1)}{2}$$

$h_x$

|                |   |               |
|----------------|---|---------------|
| $-\frac{1}{2}$ | 0 | $\frac{1}{2}$ |
|----------------|---|---------------|

$f$

|   |   |   |   |   |
|---|---|---|---|---|
| 0 | 0 | 2 | 3 | 1 |
| 8 | 8 | 5 | 7 | 4 |
| 1 | 2 | 5 | 3 |   |

1 4 3

1 2 5 3

$y$

|    |      |   |  |
|----|------|---|--|
| 4  |      |   |  |
| -5 | 0    | 1 |  |
|    | -1.5 |   |  |

$h_y$

|               |
|---------------|
| $\frac{1}{2}$ |
| 0             |
| $\frac{1}{2}$ |

} x 1

|      |      |      |      |
|------|------|------|------|
| 1    | 1.5  | -0.5 | -1   |
| -1.5 | -0.5 | -0.5 | -1.5 |
|      | 2    |      |      |

Arctan(-0.5, 0) = 0

X

$$f(x)' = (f(x+1) - f(x-1)) / 2 = [-.5, .0, .5] * [f(x-1), f(x), f(x+1)]$$