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# Flexible reservation scheme for urban transportation network management in a multimodal context

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# 1. INTRODUCTION

## INTRODUCTION



### How to alleviate urban traffic congestion?

- Traffic congestion, a persistent and critical challenge in the global urbanization process, leading to tremendous economic losses and environmental pollution
  - A typical US driver wasted **42 hours** due to congestion in 2023, while the average UK driver endured even more, spending **61 hours** in traffic jams. The economic loss of congestion was estimated **at \$70.4 billion** in the U.S. and **£7.5 billion** in the U.K.
- Rapid increase in the number of private cars is a primary contributor to traffic congestion
  - **Private car (PC)**: convenience and privacy
  - **Public transit (PT)**: lower travel cost, more environmentally friendly

**Promote public transit and implement effective management strategies for PC**

## INTRODUCTION



### Reservation-based TDM

- Reservation-based TDM schemes have shown promise in **balancing the capacity of transportation infrastructure and the travel demand of commuters**
  - **Reduction of the cost** of implementing reservation-based strategies due to advances in technology (Monitoring the traffic flow & Collecting the travel demand and preferences)
  - **Absence of direct monetary payment** makes it less likely to be perceived as disguised tax (More welcomed by the public)
- **However**
  - Administrative enforcement required for implementing such strategy
  - Absence of flexibility impedes public acceptance (**inherent**)
- **Critical challenge in the implementation: Noncompliance**



# INTRODUCTION



## Motivations

- **Road capacity partition for two modes** (to serve PT and PC commuters, respectively) would introduce more flexibility into the scheme -> **Multimodal context**
- The combination of the **reservation scheme** and **auction mechanism** represents a hybrid TDM scheme that integrates the pricing and quantity instruments (Liu et al., 2015; Su & Park, 2015) -> **Auction-based reservation**
  - Allowing commuters to **self-select according to their personal preferences**, thereby inducing a shift in demand from the central peak to the shoulder peaks, enhancing the effectiveness of TDM schemes
- Road resource is **scarce and perishable**, which imposes stringent requirements on the stability of demand and accuracy of information. Demand fluctuations **lead to underutilization of road capacity or scramble**. Consider **the underlying noncompliance** due to expected scheduling conflicts -> **Reallocation and penalty mechanisms**

**Flexible reservation scheme for urban transportation network management in a multimodal context**

## INTRODUCTION



This work focuses on

- (1) Introducing a **reservation-based TDM strategy** for congestion management during the morning commute in a **multimodal transportation context**
- (2) **Characterizing and analyzing the noncompliance** in the proposed reservation scheme
- (3) Exploring an efficient approach to **mitigate the adverse effects of noncompliance**

## Main contributions

- (1) A **flexible reservation scheme is proposed** to reduce traffic congestion during the morning commute in a multimodal transportation context
- (2) Noncompliance of commuters, **including cancellation and no show**, is characterized and analyzed
- (3) The **reallocation mechanism** is introduced and incorporated into the reservation scheme to mitigate the negative influence of noncompliance
- (4) The system cost under the implementation of the proposed reservation scheme is analyzed



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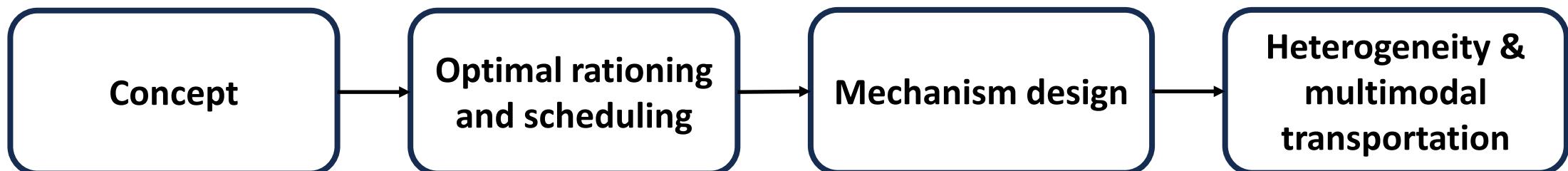


## 2. LITERATURE REVIEW



## Highway reservation

- Concept of the highway use reservation system was **initially proposed by Wong (1997)**
- **Highway space inventory control system** (Teodorović et al., 2005; Edara & Teodorovic, 2008) and the **token-based transportation reservation system** (Liu et al., 2013) were developed
- Liu et al. (2015) examined the design and the efficiency of a highway use reservation system, and they **explored the auction-based reservation** to mitigate the efficiency loss caused by user heterogeneity
- Su and Park (2015) introduced an **auction-based traffic management scheme** and conducted an agent-based simulation to illustrate the application potential of this strategy.





## Road capacity reservation

### Auction theory

- Liu et al. (2015) examined the design and the efficiency of a highway use reservation system, and they explored the **auction-based reservation** to mitigate the efficiency loss caused by user heterogeneity
- Su and Park (2015) introduced an **auction-based traffic management scheme** and conducted an **agent-based simulation** to illustrate the application potential of this strategy

### Autonomous vehicles

- Lamotte et al. (2017) investigated capacity allocation in a single bottleneck dynamic framework with a **booking mechanism for autonomous vehicles**
- Narayanan et al. (2022) formulated a bilevel game-theoretic model integrating Dynamic User Equilibrium with **SAV (Shared Autonomous Vehicles)** chain formation
- Xu et al. (2024) addressed the network design problem for **autonomous truck dedicated lanes**, optimizing the trade-off between safety-related network impacts and carbon emissions using a specialized two-stage algorithm

### Transportation network analysis

- Li et al. (2023) introduced a **linear programming framework** for a combined **booking and rationing** strategy, aiming to secure efficient traffic flow patterns without compromising user equity and flexibility
- Ye et al. (2024) developed a **disaggregated spatiotemporal traffic assignment** method with a system-optimal orientation, employing a novel reverse feasible route searching algorithm to **ensure reliable reservation services** and analyze supply-demand matching.



## Other reservation schemes in the transportation field

### Parking services

- Shao et al. (2016) proposed a **reservation and allocation model of shared parking lots** that maximizes the use of private resources to benefit the community as a whole
- Shao et al. (2020) proposed an **auction-based parking reservation scheme** **considering demand disturbance**, which achieves incentive compatibility, and efficient allocation
- Cheng et al. (2023) proposed a **parking-sharing mechanism** that amends the Vickrey-Clarke-Groves auction with the notion of scale control, where IC and IR are guaranteed.

### Public transit services

- Tang et al. (2024) developed an entry reservation strategy to **optimize the commuter flow during morning peak hours** on a metro line and constructed a **multi-objective passenger flow joint optimization model** to minimize the total trip cost at the reservation station.
- Zhang et al. (2024) **analyzed and optimized the reserved inbound services** of metro stations in Beijing and modeled the congestion and choices of travelers using the Vickrey bottleneck approach.

### Charging services

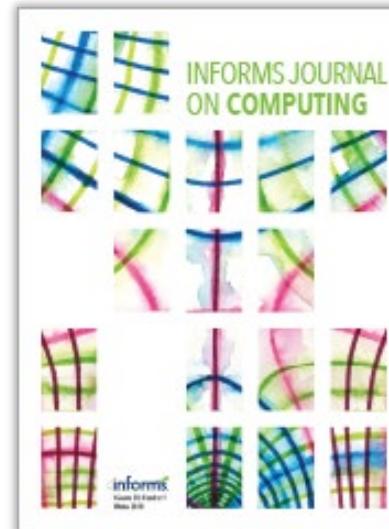
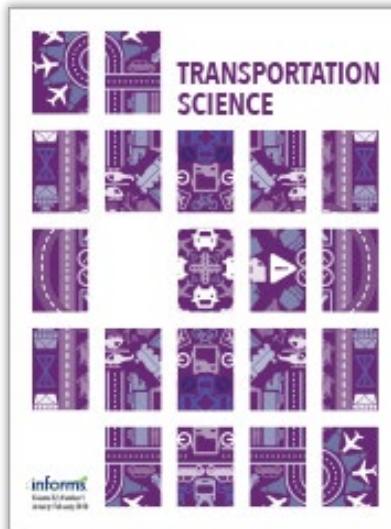
- Conway (2017) described a **simulation model on the charging infrastructure** deployed in Ireland, quantitatively revealing the advantages of a routing and charge point reservation system.
- Zhang et al. (2020) designed an **intelligent mobile charging system for electric vehicles by promoting charging reservations**. Results show superior performance gains by promoting the reservation-based mobile charger selection, especially for mobile chargers equipped with sufficient power capacity.

## LITERATURE REVIEW



### Noncompliance management

- Noncompliance is comprehensively investigated in airline industry and other operations management fields
- Management strategy can be classified into the following types
  - **Active – Overbooking:** Subramanian et al. (1999); Bertsimas and Popescu (2003); Alexandrov and Lariviere (2012)
  - **Passive – Penalty:** Huang and Matsubara (2007); Constantin et al. (2008); Alexandrov and Lariviere (2012)
  - **Hybrid – Two Stage Planning (First stage – Improving strategic slack; Second stage – Dynamic adjustment):** Cummings et al. (2025)





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### 3. MODEL FORMULATION

# MODEL FORMULATION

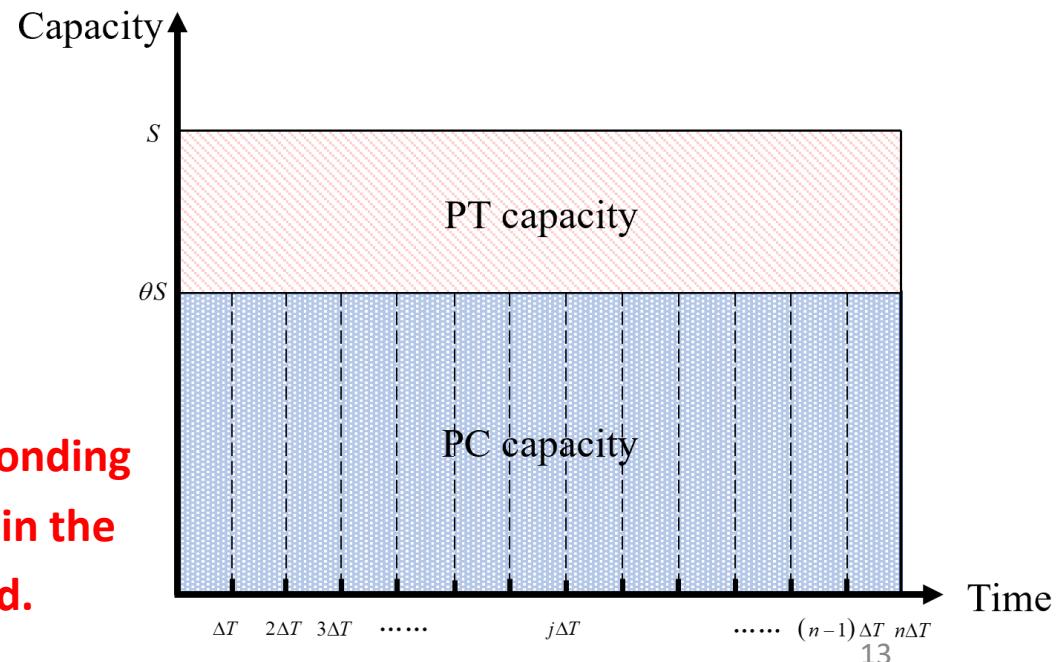


## Initial allocation

- The bottleneck capacity  $S$  is divided into two parts: PC capacity  $\theta S$  and PT capacity  $(1 - \theta)S$
- The travel demand  $N$  is fixed and the set containing all  $N$  commuters is denoted by  $\Omega$
- The morning peak is discretized into finite  $n$  time intervals with identical length  $\Delta T = \frac{N}{nS}$ ; The set contains all time intervals is  $\mathcal{T}$

- Before the start of the morning peak, each commuter  $i \in \Omega$  submits the bid prices  $\mathbf{v}_i = (v_{i1}, v_{i2}, \dots, v_{in})^T$
- The authority would allocate the PC travel right to commuters to maximize the social welfare  $\sum_{i \in N} \sum_{j \in \mathcal{T}} v_{ij} x_{ij}$ ,

**Commuters who want to utilize PC capacity must have corresponding travel right for a specific time interval; Those who do not obtain the PC travel right in any time interval can only take PT instead.**



# MODEL FORMULATION



## Initial allocation

- $x_{ij}$  indicate the allocation status of the PC travel right in time interval  $j$  to commuter  $i$ :  $x_{ij} = 1$  signifies that commuter  $i$  obtains the corresponding travel right and vice versa ( $x_{ij} = 0$ )
- The efficient allocation that maximizes the total social welfare is formulated as

$$\max_{\mathbf{X}} V(\mathbf{X}) = \sum_{i \in \Omega} \sum_{j \in \mathcal{T}} v_{ij} x_{ij}, \quad \text{Social welfare maximization}$$

s.t.

$$\sum_{j \in \mathcal{T}} x_{ij} \leq 1, \text{ for } i \in \Omega,$$

Each commuter obtains at most one PC travel right

$$\sum_{i \in \Omega} x_{ij} \leq \frac{\theta |N|}{n}, \text{ for } j \in \mathcal{T},$$

PC capacity of each interval is completely utilized without being wasted or overallocated

$$x_{ij} \in \{0,1\}, \text{ for } i \in \Omega, j \in \mathcal{T}. \quad \text{Binary variable}$$

The problem is solved by Scip solver via Python interface;

## MODEL FORMULATION



### VCG payment

- After completing the initial allocation, payment of winners for PC travel right is determined based on **VCG payment rule**
- $W(\Omega)$  is the optimal value of the objective function and  $W(\Omega \setminus i)$  is the optimal value where commuter  $i$  is excluded
- The VCG payment for commuter  $i$  is stated as

$$P_i^{VCG} = W(\Omega \setminus i) - \left( W(\Omega) - \sum_j v_{ij} x_{ij}^* \right), \quad \forall i \in \Omega,$$

- $x_{ij}^*$  is the component of the **optimal solution  $\mathbf{X}^*$**
- Winners who obtain the PC travel right should pay **non-negative VCG payment**, as their participation bring negative externality to others  
The VCG payment is zero for those who do not win in the initial allocation
- Such VCG payment rule guarantees **incentive compatibility and individual rationality** of the scheme (Vickrey, 1961; Clarke, 1971; Groves, 1973)

## MODEL FORMULATION



### Formulation of travel cost

- We treat commuters as homogeneous
- The travel cost of PC commuter departing in time interval  $j$ , denoted by  $c_j^{PC}$ , is formulated as

$$c_j^{PC} = \max \left\{ \beta(t_j - t^*), \gamma(t^* - t_j) \right\},$$

- The travel cost of PT commuters, denoted by  $c^{PT}$ , is formulated as

$$c^{PT} = \pi g(N^{PT}) + f^{PT},$$

where  $\pi$  is the unit cost of body congestion and  $g(N^{PT})$  is an increasing function with respect to the total PT travel demand  $N^{PT}$  that describes the discomfort experienced by a PT commuter, and  $f^{PT}$  is the transit fare

- The travel time and the scheduling of bus departures are not included in this study
- The travel cost that a PT commuter incurred is mode-dependent, i.e., closely related to the mode choice of other commuters

## MODEL FORMULATION



### Logit-based model

- We adopt the logit-based model to formulate the mode choice behavior, namely reservation behavior of commuters
- Let mode 1 and mode 2 represent PC and PT, respectively; and the generalized utility of mode  $r = 1,2$ , which is denoted by  $u_r$ , is formulated as

$$u_r = U - c_r + \xi_r, \quad r = 1,2$$

- where  $U$  is the utility achieved by completing the trip on this day;  $\xi_r$  follows an independently and identically distributed Gumbel distribution with mean zero
- The modal split at the aggregate travel demand level is governed by a logit formula

$$N_r = N \frac{e^{-\omega c_r}}{e^{-\omega c_1} + e^{-\omega c_2}}, \quad r = 1,2,$$

- where  $\omega$  is a positive parameter that correlates with the standard deviation of random variables; A larger value of indicates a smaller perception error in travel utility, and an individual is more likely to choose the mode with the minimum travel cost

## MODEL FORMULATION



### Willingness to pay of commuters

- Each commuter selects the mode with a higher utility between PC and PT. While for different time intervals, the willingness to pay (WTP) of commuters is the utility difference (or cost difference) between two distinct travel modes
- The WTP of commuter  $i$  for the PC travel right in interval  $j$ , which is denoted by  $v_{ij}$ , is formulated as

$$v_{ij} = u_{ij}^{PC} - u_i^{PT}$$

- Hence, the bid prices can be obtained accordingly

$$\max_{\mathbf{X}} V(\mathbf{X}) = \sum_{i \in \Omega} \sum_{j \in \mathcal{T}} v_{ij} x_{ij},$$

s.t.

- Once the bid prices of all commuters are determined, the PC travel right is then allocated by completing the initial allocation process

$$\sum_{j \in \mathcal{T}} x_{ij} \leq 1, \text{ for } i \in \Omega,$$

$$\sum_{i \in \Omega} x_{ij} \leq \frac{\theta |N|}{n}, \text{ for } j \in \mathcal{T},$$

$$x_{ij} \in \{0, 1\}, \text{ for } i \in \Omega, j \in \mathcal{T}.$$

## MODEL FORMULATION



### Considering noncompliance

- Considering real-world scenarios, commuters' travel **plans may be disrupted by unforeseen events**
- Commuters who obtained PC travel rights in the initial allocation may cancel the reservation for PC travel and shift to take PT; or they might cancel the trip plans on this day completely
- We consider **two types of noncompliance** in this study:
  - **Cancellation:** Commuters who obtained the PC travel rights cancel the reservation for PC travel before departure and shift to take PT on this day
  - **No show:** Commuters who obtained PC travel rights in the initial allocation cancel the reservation later than the start of the reserved time interval or do not show up for their reservations
- To mitigate **the adverse effect of noncompliance (cancellation)**, this study introduces the **reallocation mechanism** into the reservation scheme, as **no show cannot be identified in advance and managed then**

## MODEL FORMULATION



### Reallocation of PC travel right

- Before introducing and formulating the reallocation process, four sets are introduced as shown below

$C^r = \left\{ i \in N \mid \sum_j x_{ij} = 1 \right\}$ : The set of commuters who have the PC travel rights.

$C^{nr} = \left\{ i \in N \mid \sum_j x_{ij} = 0 \right\} = C \setminus C^r$ : The set of commuters who do not have PC travel rights.

$C^d$ : The set of commuters who have departed from the residential district.

$C^{nd}$ : The set of commuters who have not departed from the residential district.

- These four sets are **dynamically maintained** during the whole morning peak period
- For  $C^{nr}$ , there exist two disjoint subsets:  $C^l$  and  $C^w$ ,
  - $C^l$  contains all commuters who do not get the PC travel right **from the beginning till now**
  - $C^w$  contains commuters who **once had** the PC travel right **but are noncompliant**

## MODEL FORMULATION



### Reallocation of PC travel right

- Assumptions regarding the reallocation
  - No intentional noncompliance    **Implicit assumption in most TDM studies**
  - Commuters in  $C^l$  will be retained as standby candidates in the reallocation process; The released PC travel right of noncompliant commuters will be released and reallocated to **commuter in  $C^l \cap C^{nd}$**
  - Reallocation is conducted **in sequence rather than in batches**
- For commuter  $c$  who has the PC travel right and become noncompliant then, his/her travel right will be released and reallocated
- The reallocation is determined by solving the problem below

$$\max_{(x_{ij}, i \in C^l \cap C^{nd})} \sum_{i \in C^l \cap C^{nd}} v_{ij} x_{ij}, \quad \text{Achieve the max social welfare by reallocating the released PC travel right}$$

s.t.

$$\sum_i x_{ij} = 1, \text{ for } i \in C^l \cap C^{nd}. \quad \text{Only one commuter can win in a reallocation process}$$



## MODEL FORMULATION

### Reallocation of PC travel right

#### Algorithm 1 Reallocation for cancellations

#### Note

#### Inputs

Sets of commuters:  $C^r, C^l, C^w, C^{nd}$   
Time interval  $j$  of the cancellation request

#### Outputs

Noncompliant commuter  $c$   
Bid prices  $b_{ij}$  for all  $i \in C^l \cap C^{nd}$   
Current allocation matrix  $\mathbf{X}_c$

Updated sets  $C^r, C^l, C^w$   
Updated allocation matrix  $\mathbf{X}'_c$

- 1: Move commuter  $c$  from  $C^r$  to  $C^w$  // Update  $C^r$  and  $C^w$
- 2: Generate the optimal solution  $x_{ij}, i \in C^l \cap C^{nd}$  by solving problem (13) to (14); // Winner determination  
 $k \leftarrow \{i \in C^l \cap C^{nd} \mid x_{ij} = 1\}$
- 3: Move commuter  $k$  from  $C^l$  to  $C^r$  // Update  $C^r$  and  $C^l$
- 4: Set  $x_{cj} \leftarrow 0$ ; // Update allocation matrix

- The value of total social welfare before and after reallocation is denoted by  $V(\mathbf{X}_c)$  and  $V(\mathbf{X}'_c)$ , respectively
- It holds  $V(\mathbf{X}'_c) \leq V(\mathbf{X}_c) \leq V(\mathbf{X}^*) = W(\Omega)$ ,
- Reallocation process is accompanied by the **noncompliance of commuters with higher utilities**.
- Hence, it can be easily verified that the noncompliance of commuter  $i$  would pose negative influence on social welfare.

## MODEL FORMULATION



### Identification of no show

- Some commuters may not show up for their reservations without cancelling the reservation in advance
- Such absences of commuters **ultimately lead to the waste of the initially PC capacity**, which **cannot be reallocated** as the authority is not able to know their failure in attending the reservations before the end of the corresponding time interval
- **Identification:**
  - At the end of the time interval  $j$ , commuter  $c$  who has the PC travel right for this time interval and fails to attend the reservation, will be identified as no show

**The reallocation process is not suitable for managing no show**

**The VCG payment of these no show commuters will not be refunded, which can be treated as penalty**

## MODEL FORMULATION



### Determination of penalty for noncompliant commuters

- The loss in social welfare in the reallocation due to the noncompliance of commuter  $c$  is  $V(\mathbf{X}_c) - V(\mathbf{X}'_c)$
- Once commuter  $c$  cancels his/her reservation, **the VCG payment  $P_c^{VCG}$  will be refunded**
- However, this noncompliant commuter  $c$  has to **endure the penalty for the cancellation**
- The penalty fee  $z_c$  is governed by

$$z_c = P_c^{VCG} - P_k^{VCG},$$

- where  **$k$  is the winning standby candidate** in the reallocation process; Such a setting of penalty **fee achieves the consistency of total payment** before and after the reallocation
- The VCG payment of the new winner  $k$  holds  $P_k^{VCG} = v_{pj}$ ,
  - $p$  is the commuter with the **second-highest bid price** for interval  $j$  in the set of available standby candidates
  - The VCG auction reduces to a second-price auction, where  $k$  pays the second-highest submitted bid  $v_{pj}$

## MODEL FORMULATION



### Analytical results of the flexible partial reservation scheme

- For the reservation scheme incorporated with the reallocation and penalty mechanisms, we have the following propositions

**Proposition 1.** *The penalty fee  $z_c$  for a noncompliant commuter  $c$  is non-negative and it is not higher than the VCG payment  $P_c^{VCG}$ , i.e.,  $P_c^{VCG} \geq z_c \geq 0$ .*

**Proposition 2.** *(Incentive compatibility) For any bid prices  $\mathbf{b}_{-i}$  of the other commuters and any true values  $\mathbf{v}_i$ , reporting  $\mathbf{b}_i = \mathbf{v}_i$  weakly maximizes the expected utility  $U_i$  over all possible misreports  $\mathbf{b}'_i$  ( $\neq \mathbf{v}_i$ ).*

**Proposition 3.** *(Individual rationality), under truthful bidding  $\mathbf{b}_i = \mathbf{v}_i$ , the expected utility of commuter  $i$  is non-negative, i.e.,  $U_i \geq 0$ , ensuring that every commuter will participate in the scheme.*

**Proposition 4.** *(Early reporting of noncompliance) For a noncompliant commuter  $i$  who is rational, he/she will cancel the reservation as early as possible once the unforeseen disruption occurs to increase his/her expected utility.*

## MODEL FORMULATION



### Analytical results of the flexible partial reservation scheme

**Proposition 1.** *The penalty fee  $z_c$  for a noncompliant commuter  $c$  is non-negative and it is not higher than*

*the VCG payment  $P_c^{VCG}$ , i.e.,  $P_c^{VCG} \geq z_c \geq 0$ .*

- The max penalty for any noncompliant commuter  $c$  is **non-negative and not greater than his/her VCG payment  $P_c^{VCG}$**
- For no show commuter  $c$ , the penalty  $z_c$  equals the VCG payment  $P_c^{VCG}$
- For cancellation commuter  $c$ , the penalty  $z_c$  depends on  $P_k^{VCG}$  (the payment of new winning commuter  $k$  in the reallocation process)

**Proposition 4.** *(Early reporting of noncompliance) For a noncompliant commuter  $i$  who is rational, he/she will cancel the reservation as early as possible once the unforeseen disruption occurs to increase his/her expected utility.*

- The number of potential standby candidates for reallocation decreases over time
- Noncompliant commuter then has a strong incentive to cancel the reservation at the earliest possible time to reduce the penalty induced



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## 4. NUMERICAL ANALYSES

## NUMERICAL ANALYSES

### Basic setting

- The values of schedule delay early and schedule delay late are denoted  $\beta$  and  $\gamma$ , and it holds  $\gamma > \beta$

Table 1: Parameter settings in the model.

Parameter	$N$	$n$	$S$	$t^*$	$\gamma$
Value	1000	20	500	8.6	8
Parameter	$\theta$	$\omega$	$\pi$	$f^{PT}$	$\beta$
Value	0.6	0.5	0.01	2	2

Note:  $N / S = 2$  indicates the duration of the morning peak is 2 hours.  $\gamma / \beta$  is set to 4, approximates the setting suggested by Arnott et al. (1990b) where  $\beta = 3.9$ ,  $\gamma = 15.21$ , and  $\gamma / \beta \approx 4$ . The specification of in-vehicle congestion function is adopted from Huang (2002). Under such parameter settings, the preferred arrival time  $t^*$  is exactly at the boundary between 16<sup>th</sup> and 17<sup>th</sup> time intervals.

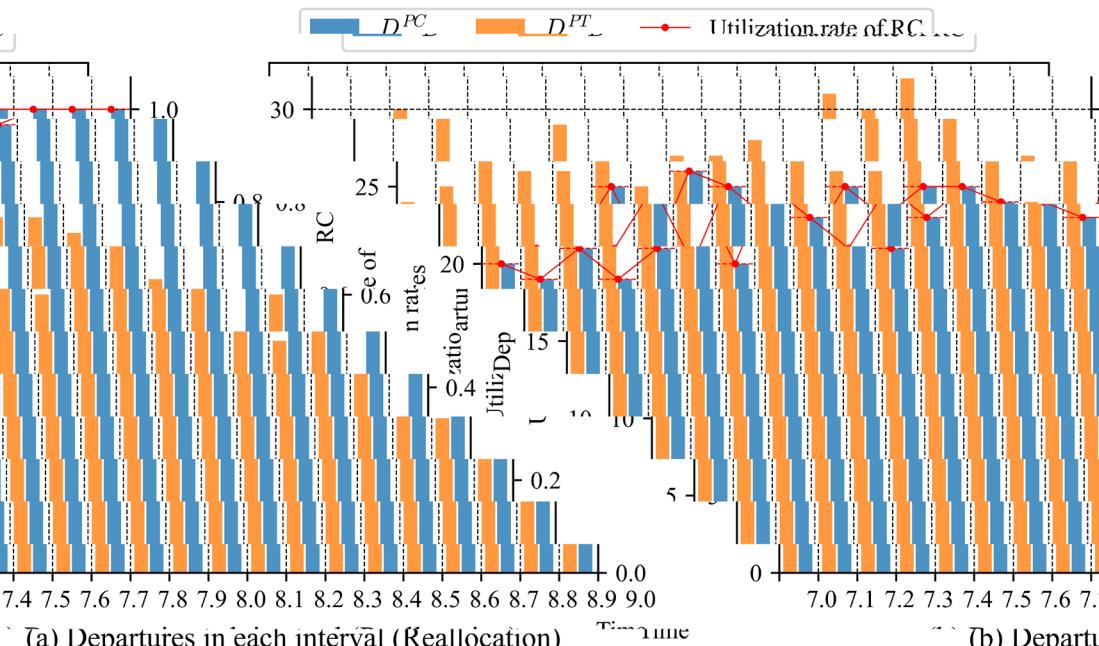
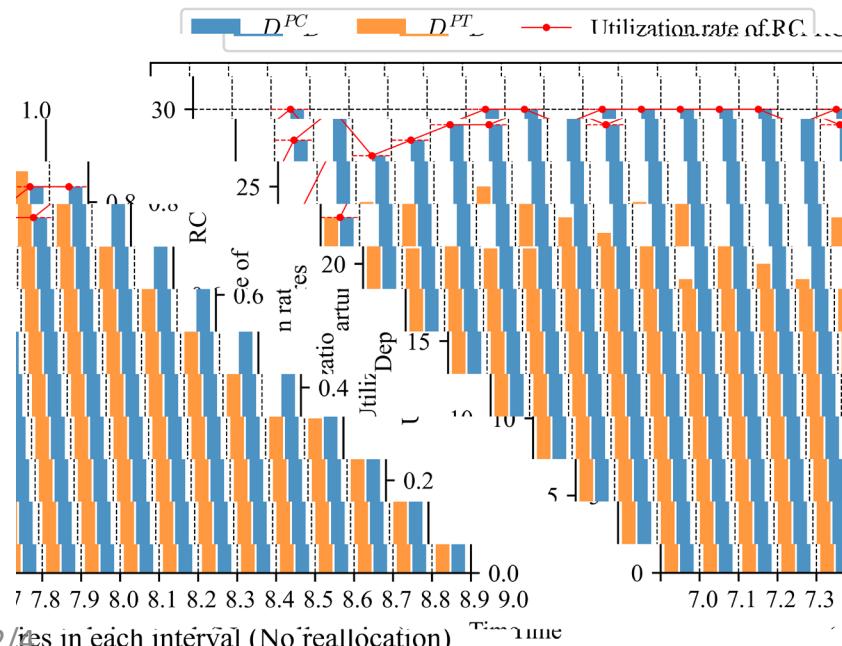
For computational convenience, we adopt the parameter settings in Table 1

# NUMERICAL ANALYSES



## Departures in each time interval

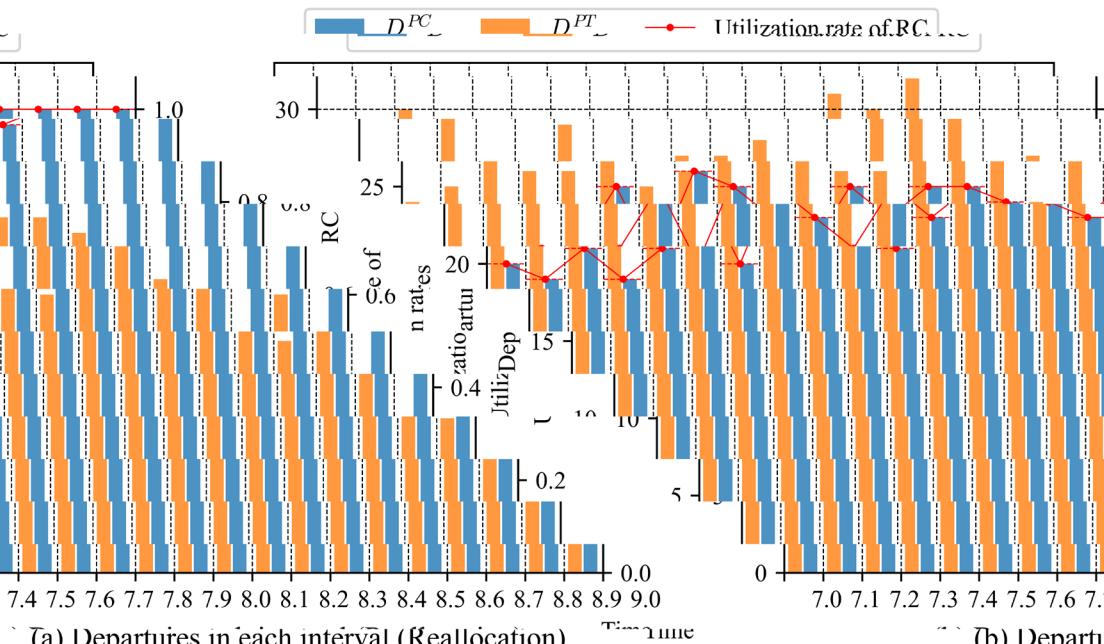
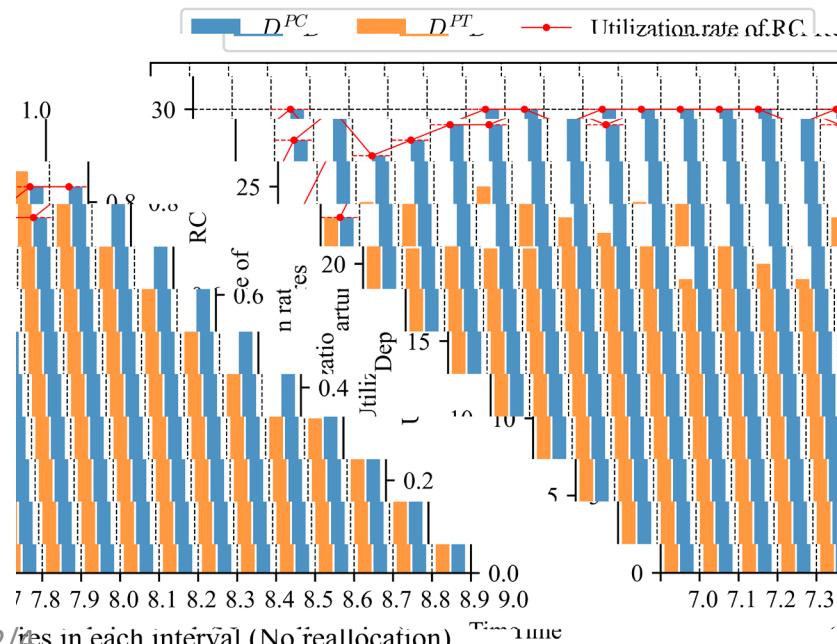
- The utilization rate of PC capacity (denoted by red dashed lines in subplots (a) and (b)), is significantly higher when incorporating the reallocation mechanism in the proposed reservation scheme
- The departures of PC commuters are not sufficient (a proportion of the PC capacity is wasted) in the intervals at the beginning of the morning peak.



## NUMERICAL ANALYSES

### Departures in each time interval

- Although early cancellations provide more standby candidates, the limited buffer period of the other standby candidates leads to a relatively lower reallocation success rate
- The orange bar in subplot (b) signifies that the average commuter load of PT is higher, leading to a further decline in travel experience. The introduction of the reallocation mechanism **improves the utilization rate of PC capacity by 25%** under the given parameter settings.

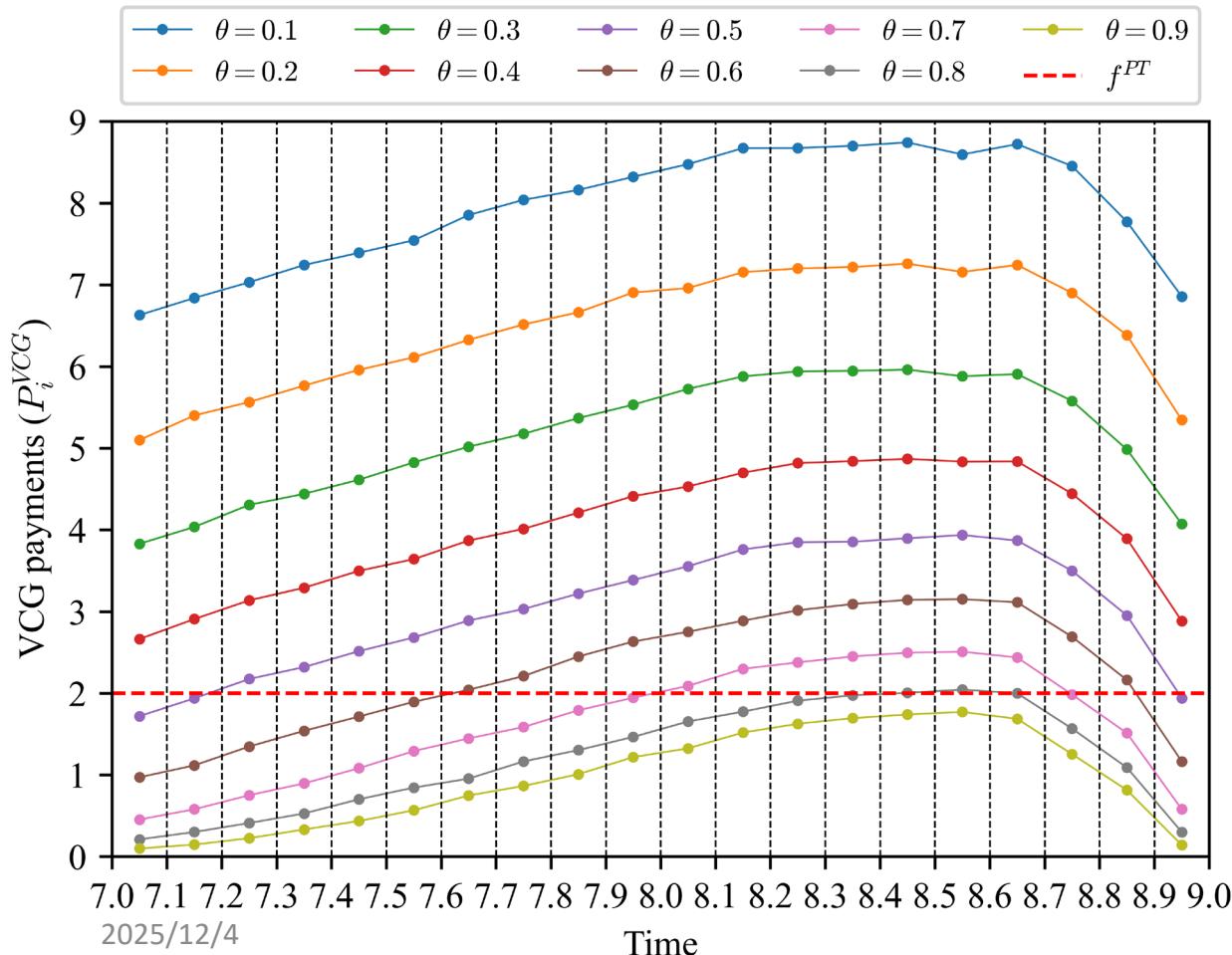


(b) Departure

# NUMERICAL ANALYSES

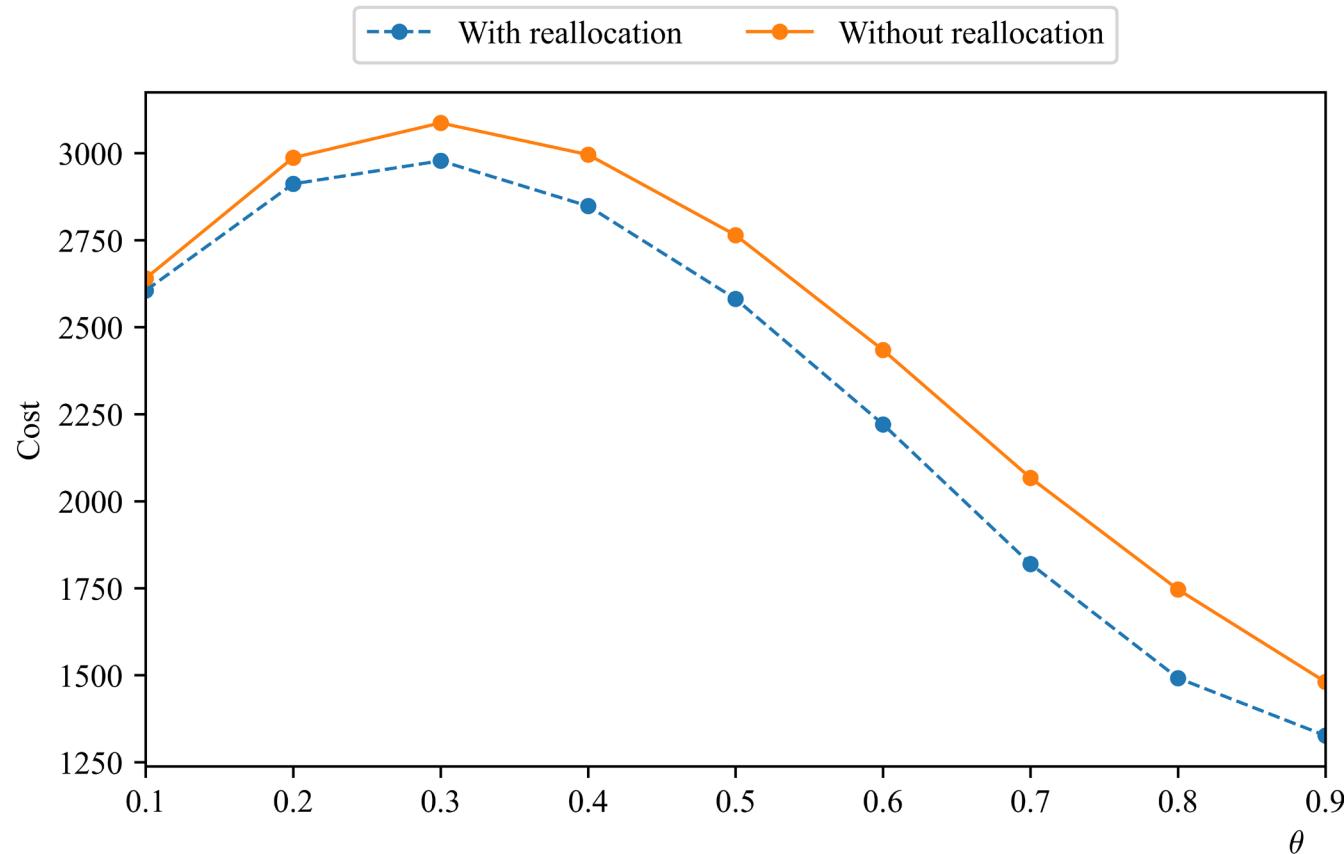


## Average VCG payment for PC travel rights



- The average VCG payment for PC travel is higher for time intervals closer to  $t^*$ , and the trend generally shows an increase first, followed by a decrease across time dimension
- When  $\theta$  is greater than 0.8, the average payment for PC travel for any time interval is lower than the transit fare  $f^{PT}$

## Total revenue of the system

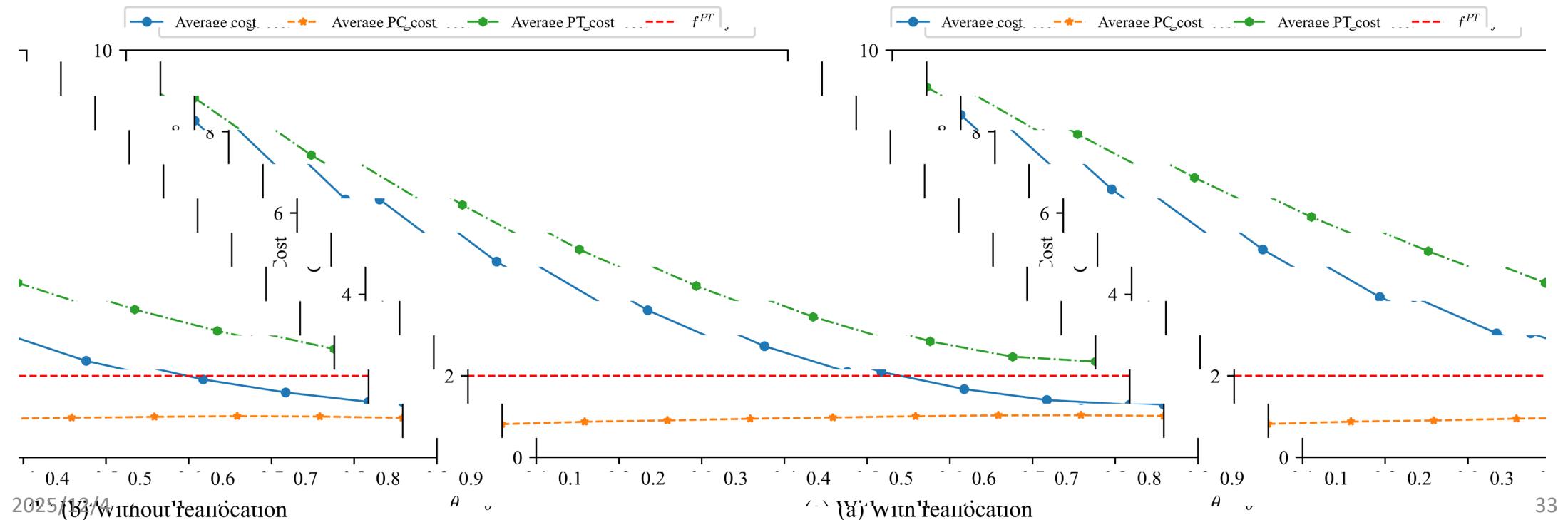


- The total revenue equals the sum of all VCG payments, penalties and public transit fares collected, minus the refund of the VCG payments for noncompliant commuters.
- The introduction of reallocation mechanism leads to a reduction in the authority's total revenue under the implementation of the reservation scheme. From the perspective of revenue maximization, the reasonable range for  $\theta$  should be between 0.2 - 0.4.

## NUMERICAL ANALYSES

### Average system cost, average PC cost, and average PT cost

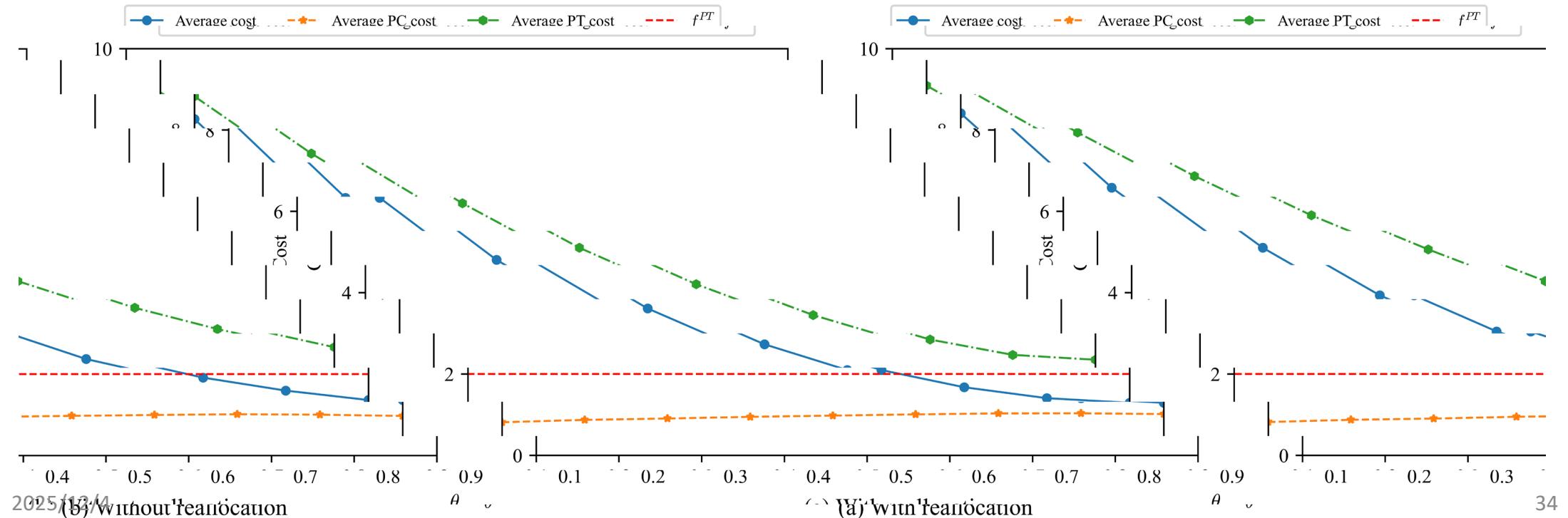
- As  $\theta$  increases, the average system cost significantly decreases
- The average cost of PT is reduced accordingly as body discomfort is mitigated as well
- The average cost of PC commuters does not exhibit substantial variation and consistently remains below the public transit fare



## NUMERICAL ANALYSES

### Average system cost, average PC cost, and average PT cost

- When there is no reallocation mechanism, the average system cost, the average travel cost of PT and PC commuters are all higher than the corresponding cases with the reallocation mechanism
- Although increasing  $\theta$  reduces the average system cost, it lowers the total revenue when considering the authority's perspective alone





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## 5. CONCLUSION & DISCUSSION

## CONCLUSION & DISCUSSION



### Concluding remarks

- The findings in this study demonstrated that **noncompliance has significant influence on the implementation and efficiency of the proposed reservation scheme**; hence incorporating potential noncompliance behavior into such schemes is essential
  - Noncompliance leads to the underutilization of the PC capacity to be reserved, **especially for the time intervals close to the start of rush hour, exacerbating the in-vehicle congestion for PT as well**
  - The average VCG payment made by PC commuters for each time **interval decreases as  $\theta$  increases**
  - When  $\theta$  exceeds 0.8, the average payment drops even below the public transit fare  $f^{PT}$ ; as  $\theta$  decreases, the revenue exhibits a trend of **increasing first and then decreasing** (reaches the maximum when  $\theta$  between 0.2 and 0.4), while the average system cost and the average travel cost of PT commuters are **monotonically decreasing**
  - The introduction of the reallocation mechanism **improves the utilization rate of PC capacity by 25%** under the given parameter settings.

## ***CONCLUSION & DISCUSSION***



### **Future research**

- Heterogeneous scenarios (Values of time, preferred arrival time.....)
- Active noncompliance management: overbooking..... (instead of the passive penalty mechanism)
- Reservation priority based on trip length, values of time, or historical noncompliance records.....

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# Thank you for listening!

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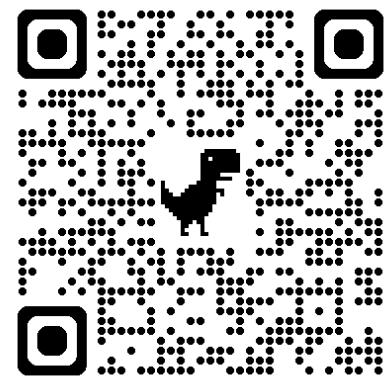
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