

Section-B

Note: Solve any TEN of the following questions.

- Q.2 State the De-Morgan's law verify De-Morgan's law when $U =$ The set of the english alphabets.
 $A = \{x | x \text{ is a vowel}\}$ $B = \{y | y \text{ is a consonant}\}$
- Q.4 Drive the Quadratic Formula. standard form of quadratic equation is $px^2 + qx + r = 0, p \neq 0$
- Q.5 Solve the equation $2^2x - 3 \cdot 2^{x-2} + 32 = 0$
- Q.6 When $x^4 + 2x^3 + kx^2 + 3$ is divided by $x - 2$, the remainder is 1. Find the value of k .
- Q.7 Find the sum to 10 terms of an A.P whose 4th term is 7 and 7th term is 13
- Q.8 Prove that ${}^nC_r + {}^nC_{r-1} = {}^nC_r$
- Q.9 A pair is to be chosen from a group of 4 boys and 3 girls. Find the probability that the pair consists of one boy and one girl
- Q.10 Prove by mathematical induction $a^n - b^n$ is divisible by $a - b$ for $n \in \mathbb{N}$
- Q.11 Show that $(\mathbb{R} - \{0\}, *)$ is a group where $*$ is defined on $a * b = a + b + ab$
- Q.12 An arc subtends an angle of 70° at the center of a circle and its length is 132 mm. Find the radius of the circle.
- Q.13 Solve the equation $2^2x - 3 \cdot 2^{x-2} + 32 = 0$
- Q.14 When $x^4 + 2x^3 + kx^2 + 3$ is divided by $x - 2$, the remainder is 1. Find the value of k

Section-C

Note: Solve any THREE of the following questions. Each question carries 10(6 + 4) marks.

- Q.15 (a) A geometric progression, for which the common ratio is positive, has a second term of 18 and a fourth term of 8. Find the sum to infinity of progression
 (b) If there are 3 children in family, what is the probability that the third child is a girl and the two children are boys and one child is girl?
- Q.16 (a) Solve: $\sqrt{x^2 - 3x + 9} = \sqrt{x^2 - 3x + 36} - 3$
 (b) Express the recurring decimal 1.428 as a common fraction.
- Q.17 (a) If $Z = \frac{1}{3} + \frac{13}{3.6} + \frac{13}{3.6.7} + \frac{13.5.7}{3.6.9.12} + \dots$ prove that $Z^2 + 2Z - 2 = 0$
 (b) Show that: $\frac{1}{r^2} + \frac{1}{r_1^2} + \frac{1}{r_2^2} + \frac{1}{r_3^2} = \frac{a^2 + b^2 + c^2}{\Delta^2}$
- Q.18 (a) Solve the system of equations: $2x^2 + xy + y^2 = 8, 6xy + 2y^2 = 20$
 (b) Solve $5^{\sin^{-1} \cos^{-1} x} = 1$