

MATHEMATICS 2014

Time: 20 Minutes

Max. Marks: 20

SECTION "A" (MULTIPLE CHOICE QUESTIONS)

1. Choose the correct answer for each from the given options:

(i) The real part of $(2i - 3)i$ is:

- ♦ 2 ♦ -2 ♦ -3 ♦ 3

(ii) $\tan(180^\circ - \theta) =$

- ♦ $\tan\theta$ ♦ $-\tan\theta$ ♦ $\cot\theta$ ♦ $-\cot\theta$

(iii) The value of 8P_2 is:

- ♦ 66 ♦ 76 ♦ 56 ♦ 86

(iv) The multiplication inverse of $(-3, 8)$ is:

- ♦ $(3, -8)$ ♦ $\left(-\frac{1}{3}, \frac{1}{8}\right)$ ♦ $\left(\frac{1}{3}, -\frac{1}{8}\right)$ ♦ $\left(-\frac{3}{73}, -\frac{8}{73}\right)$

(v) $\cos(90^\circ - \alpha)$ is equal to:

- ♦ $\sin\alpha$ ♦ $\cos\alpha$ ♦ $-\cos\alpha$ ♦ $-\sin\alpha$

(vi) If $|x| < 1$, then $1 + 2x + 3x^2 + 4x^3 + \dots$ is equal to:

- ♦ $(1-x)^{-2}$ ♦ $(1+x)^{-2}$ ♦ $(1-x)^{-1}$ ♦ $(1+x)^{-1}$

(vii) $\binom{5}{3, 2} = 1$

- ♦ 8 ♦ 9 ♦ 10 ♦ 20

(viii) If ω is a complex cube root of unity then $(1 + \omega + \omega^2)^2$ will be equal to:

- ♦ 0 ♦ 1 ♦ ω^2 ♦ 4

(ix) If order of matrices A and B respectively are 2×3 and 3×4 than order of AB:

- ♦ 2×2 ♦ 3×3 ♦ 2×4 ♦ 4×2

(x) If $\begin{bmatrix} 4 & 2 \\ 3 & \lambda \end{bmatrix}$ is a singular matrix, then $\lambda =$:

- ♦ 6 ♦ ± 5 ♦ $\frac{3}{2}$ ♦ $\frac{2}{3}$

(xi) $\frac{n!}{(n+1)!}$ is equal to:

- ♦ n ♦ $n+1$ ♦ $\frac{1}{n}$ ♦ $\frac{1}{n+1}$

(xii) The period of $\tan x$ is:

- ♦ π ♦ $\frac{\pi}{2}$ ♦ 2π ♦ none of these

(xiii) $\sum n^3 =$

- ♦ $\frac{n^2(n+1)^2}{4}$ ♦ $\frac{n^3(n+1)^3}{8}$ ♦ $\frac{n(n+1)}{2}$ ♦ none of these

(xiv) The middle term in the expansion of $\left(x - \frac{1}{x}\right)^{20}$ is:

- ♦ 9th ♦ 10th ♦ 11th ♦ 12th

(xv) If a balanced die is rolled, then the probability of getting 3 is:

- ♦ $\frac{2}{3}$ ♦ $\frac{3}{2}$ ♦ $\frac{1}{3}$ ♦ $\frac{1}{6}$

(xvi) $\frac{1}{1 + \tan^2 \theta} =$

- ♦ $\sec^2 \theta$ ♦ $\cos^2 \theta$ ♦ $\sin^2 \theta$ ♦ $\cot^2 \theta$

(xvii) If $\sin \theta > 0$ and $\sec \theta < 0$, then $\rho(\theta)$ lies in this quadrant:

- ♦ First ♦ Second ♦ Third ♦ Fourth

(xviii) The total number of terms in the binomial expansion of

$\left(y^2 + \frac{b^2}{y^2}\right)^n$ is:

- ♦ n ♦ $n-1$ ♦ $n+1$ ♦ $2n$

(xix) The roots of a quadratic equation are equal if:

- ♦ $b^2 - 4ac > 0$ ♦ $b^2 - 4ac < 0$
♦ $b^2 - 4ac = 0$ ♦ $b^2 - 4ac$ is a perfect square

(xx) The H.M. of 2 and 5 is:

- ♦ $\frac{7}{2}$ ♦ $\pm \sqrt{10}$ ♦ 0 ♦ $\frac{20}{7}$

MATHEMATICS 2014

Time: 2 Hours 40 Minutes

Marks: 80

SECTION "B" (SHORT-ANSWER QUESTIONS)

ALGEBRA (35 MARKS)

NOTE: Answer 7 questions from this section.

141

Q.2(i) Determine the value of 'k' for which the root of the

equation $(k+1)x^2 + 2(k+3)x + (2k+3) = 0$ are equal.

(ii) Solve the equation $x^4 + x^3 - 4x^2 + x + 1 = 0$

OR Solve the system of equations:

$$x^2 + y^2 = 34$$

$$xy + 15 = 0$$

(iii) Using the properties of determinants, prove that:

$$\begin{vmatrix} a+y & a & a \\ a & a+y & a \\ a & a & a+y \end{vmatrix} = y^2(3a+y)$$

OR Find the value λ if $\begin{bmatrix} 5 & 8 & 2 \\ 0 & 2 & 2 \\ 9 & 8 & 4 \end{bmatrix}$ is a singular matrix.

(iv) If $|x| < 1$ prove that: $\frac{\sqrt{1+x} + (1-x)^{2/3}}{(1+x) + \sqrt{1+x}} = 11 - \frac{5}{6}x$ nearly.

(v) Which term of the sequence 18, 12, 8, is $\frac{512}{729}$?

(vi) Prove by Mathematical induction:

$10^n + 3 \cdot 4^{n+2} + 5$ is completely divisible by 9, $\forall n \in \mathbb{N}$.

(vii) Write the term independent of x is the expansion of

$$\left(2x + \frac{1}{3x^2}\right)^9$$

(viii) $A = \{1, -1, i, -i\}$, construct the multiplication table for (\bullet)

in A, also show that (\bullet) is commutative in A.

(ix) Into how many distinct ways can the letters of the word PAKPATTAN be arranged?

(x) Find the value of 'n' so that $\frac{a^{n+1} + b^{n+1}}{a^n + b^n}$ may become the

H.M. between 'a' and 'b'.

OR If $\frac{1+3+5+\dots+n \text{ term}}{2+4+6+\dots+n \text{ term}} = 0.95$, find 'n'.

TRIGONOMETRY (15)

Note: Attempt 3 questions from this Section.

Q.3(i) if $\operatorname{cosec} \theta = -\frac{3}{2}$ and $\rho(\theta)$ is in fourth quadrant, then find

the remaining trigonometric functions using the

definition of radius function with $x^2 + y^2 = 1$.

(ii) If a point on the rim of a 21 cm diameter flywheel travels

5040 meters in a minute, through how many radians does

the wheel turn in one second?

(iii) Prove any Two of the following:

$$(a) \frac{1}{1 - \sin \theta} + \frac{1}{1 + \sin \theta} = 2 \sec^2 \theta$$

$$(b) \tan 57^\circ = \frac{\sqrt{3} \cos 3^\circ - \sin 3^\circ}{\cos 3^\circ + \sqrt{3} \sin 3^\circ}$$

$$(c) \cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$$

(iv) Draw the graph of $\sin \theta$, when $-\pi \leq \theta \leq \pi$.

(v) Find the general solution of $\tan 2\theta \cdot \cot \theta = 3$.

OR The three sides of a triangular have lengths 10m, 11m

and 13m respectively. Find the measure of the largest

angle and area of the building.

SECTION C (DETAILED-ANSWER QUESTIONS) (30)

NOTE: Answer 2 questions from this section.

Q.4(a) Solve the following system of equations by Cramer's

rule:

$$x + y = 5 \quad y + z = 7 \quad z + x = 6$$

(b) If α, β are the roots of $y^2 - 2y + 3 = 0$, then find the

equation whose roots are $\frac{1}{\alpha^2}$ and $\frac{1}{\beta^2}$.

Q.5(a) Show that $\sqrt[3]{4} = 1 + \frac{1}{4} + \frac{1.3}{4.6} + \frac{1.3.5}{4.6.8} + \dots$

(b) If sum of 8 terms of an A.P. is 64 and sum of 19 terms is

361, find the 9th term of A.P.

OR (i) The sum of four term of an A.P. is 4. The sum of the

products of the first and the last terms and of the two

middle terms is -38. Find the numbers.

(ii) Find the G.Ms. between 2 and -16.

Q.6(a) Without using calculator, verify

$$\tan^{-1} \frac{1}{13} + \tan^{-1} \frac{1}{4} = \tan^{-1} \frac{1}{3}$$

(b) Prove that $R = \frac{abc}{4\Delta}$. OR Drive Law of cosine.

(c) Prove that $\frac{1}{r^2} + \frac{1}{r_1^2} + \frac{1}{r_2^2} + \frac{1}{r_3^2} = \frac{a^2 + b^2 + c^2}{\Delta^2}$.