

# 浙江大学宁波理工学院 2017-2018 学年 1 学期

## 《数据结构(A)》课程期末考试试卷 (A)

开课分院: 数据与计算机工程学院 , 考试形式: 闭 卷, 允许带\_\_\_\_\_入场

考试日期: 2018 年 1 月 23 日, 考试所需时间: 120 分钟

考生姓名\_\_\_\_\_学号\_\_\_\_\_考生所在分院: 数据学院 专业班级: \_\_\_\_\_.

术语表:

|                             |                            |
|-----------------------------|----------------------------|
| binary search tree 二叉搜索树    | quick sort 快速排序            |
| quadratic probing 平方探测法     | AOV Activity On Vertex 活动图 |
| preorder traversal 先序遍历     | binary tree 二叉树            |
| inorder traversal 中序遍历      | dummy head node 空表头结点      |
| singly linked list 单向链表     | linear list 线性表            |
| time complexities 时间复杂度     | linked list 链表             |
| Circular Queue 循环队列         | postfix expression 后缀表达式   |
| circularly linked list 循环链表 | complete binary tree 完全二叉树 |
| circular array 循环数组         | average search time 平均查找时间 |
| hash table 散列表              | adjacency matrix 邻接矩阵      |
| hash value 散列值              | BFS 宽度优先搜索                 |
| adjacency lists 邻接表         | Huffman code 哈夫曼编码         |
| connected graph 连通图         | Heap sort 堆排序              |
| topological ordering 拓扑排序   | separate chaining 分离链接法    |

命题 (组) 老师签名: \_\_\_\_\_ 年 月 日

分院主管教学院长或首席主讲教授签名: \_\_\_\_\_ 年 月 日

**1. Answer the following questions with True or False, and make it on your answer sheet. (15 Points)**

- (        ) 1. The major task of algorithm analysis is to analyze the time complexity and the space complexity.
- (        ) 2.  $N^2 \log N$  and  $N \log N^2$  have the same speed of growth.
- (        ) 3. In a singly linked list of  $N$  nodes, the time complexities for query and insertion are  $O(1)$  and  $O(N)$ , respectively.
- (        ) 4. If the most commonly used operations are to visit a random position and to insert and delete the last element in a linear list, then sequential storage works the fastest.
- (        ) 5. If keys are pushed onto a stack in the order  $\{a, b, c, d, e\}$ , then it is impossible to obtain the output sequence  $\{c, d, a, b, e\}$ .
- (        ) 6. If the postorder and inorder traversal sequences of a binary tree are the same, then none of the nodes in the tree has a right child.
- (        ) 7. The time complexity of searching in a binary search tree is the same as that of binary search.
- (        ) 8. To find 63 from a binary search tree, one possible searching sequence is  $\{39, 125, 101, 80, 70, 59, 63\}$ .
- (        ) 9. If the depth of an AVL tree with nodes  $\{1, 2, 3, 4, 5\}$  is 3 (the depth of the root is 1), then node 3 must have two children.
- (        ) 10. If a graph is represented by adjacency lists, then the space taken depends only on the number of vertices, not the number of edges.
- (        ) 11. In a connected graph, there exists at least one vertex of which the degree is 1.
- (        ) 12. In a graph  $G$ , if we have to do BFS twice to visit every one of its vertices, then there must be a cycle in  $G$ .
- (        ) 13. In a connected graph, the number of edges must be greater than the number of vertices minus 1.
- (        ) 14. In a hash table, "synonyms"(同义词) means two elements sharing the same hash value.
- (        ) 15. Given a hash table with size 13. If only the positions with odd (奇数) indices are occupied (the index starts from 0), then when the quadratic probing is used, insertion of a new key into this hash table can be successful.

**2. Read each of the following questions carefully; choose the best answer (from among items A, B, C, or D) and make it on your answer sheet. (30 Points)**

- (       ) 1. Given a 2-dimensional array A of size  $N \times N$ . The time complexity for finding the largest entry without changing the array is:  
A.  $O(N^2)$                       B.  $O(N \log N)$                       C.  $O(N)$                       D.  $O(N^2 \log N)$
- (       ) 2. For a singly linked list of N nodes, the time complexity of inserting a new node after the node with key value  $x$  is:  
A.  $O(1)$                       B.  $O(N/2)$                       C.  $O(N)$                       D.  $O(N^2)$
- (       ) 3. To delete a node from a linked stack with ST being its top pointer, and save the key value of the deleted node into X, we must do:  
A.  $X = ST \rightarrow \text{data}$                       B.  $X = ST; ST = ST \rightarrow \text{next}$   
C.  $X = ST \rightarrow \text{data}; ST = ST \rightarrow \text{next}$                       D.  $ST = ST \rightarrow \text{next}; X = ST \rightarrow \text{data}$
- (       ) 4. When is the linked list structure suitable for representing a linear list L?  
A. frequently insert into and delete from L  
B. frequently change the key values of the nodes in L  
C. L contains large amount of nodes  
D. the structure of the nodes in L is complicated
- (       ) 5. Given an empty stack S and an empty queue Q. Push elements {1, 2, 3, 4, 5, 6, 7} one by one onto S. If each element that is popped from S is enqueued onto Q immediately, and if the dequeue sequence is {3, 2, 6, 5, 7, 4, 1}, then the minimum size of S must be:  
A. 2                      B. 3                      C. 4                      D. 5
- (       ) 6. Given a binary tree with 100 leaves and without 1-degree nodes, the number of nodes in the tree is \_\_\_\_ .  
A. 100                      B. 102                      C. 199                      D. 200
- (       ) 7. For a binary tree, given the preorder traversal sequence 12345 and the postorder traversal sequence 32541, the corresponding inorder traversal sequence must be:  
A. 23145                      B. 23154  
C. 24135                      D. cannot be determined
- (       ) 8. Insert {34, 76, 45, 18, 26, 54, 92, 65} one by one into an initially empty binary search tree. The number of nodes on the last two levels of the resulting tree is:  
A. 1                      B. 2                      C. 3                      D. 4
- (       ) 9. Insert 2, 1, 4, 5, 9, 3, 6, 7 into an initially empty AVL tree. Which one of the following statements is FALSE?  
A. 4 is the root

- B. 3 and 7 are siblings
- C. 2 and 6 are siblings
- D. 9 is the parent of 7

(        ) 10. Which of the following sequence corresponds to a heap?

- A. 37, 99, 45, 33, 66, 10, 22, 13
- B. 99, 45, 66, 13, 37, 10, 22, 33
- C. 99, 66, 45, 33, 37, 10, 22, 13
- D. 99, 66, 22, 33, 37, 13, 45, 10

(        ) 11. Construct a Huffman tree from four leaf nodes with weights 9, 2, 5 and 7. Then the weighted path length of this Huffman tree is:

- A. 23
- B. 44
- C. 37
- D. 46

(        ) 12. Given the adjacency matrix of a graph as shown by the figure. Then starting from V1, a possible DFS sequence is:

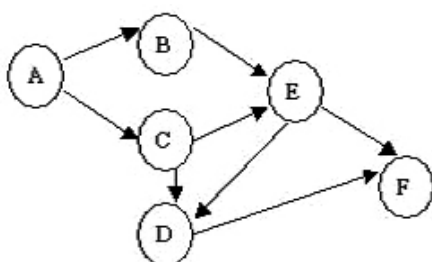
$$\begin{bmatrix} 0 & 1 & 1 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 \end{bmatrix}$$

- A. V1,V2,V3,V4,V5,V6
- B. V1,V2,V4,V5,V6,V3
- C. V1,V3,V5,V2,V4,V6
- D. V1,V3,V5,V6,V4,V2

(        ) 13. What kind of problems can Dijkstra algorithm solve?

- A. critical path
- B. shortest path
- C. topological sort
- D. string matching

(        ) 14. The figure shows an AOV network. Which one of the following is a possible topological order of the network?



- A. ACBDEF
- B. ABCEFD
- C. ABCDFE
- D. ABCEDF

(        ) 15. Given input {46, 79, 56, 38, 40, 84}. After the first partition (with the left most record as the pivot) of quick sort, the resulting sequence is:

- A. {38,46,79,56,40,84}
- B. {38,79,56,46,40,84}
- C. {38,46,56,79,40,84}
- D. {40,38,46,56,79,84}

**3. Read each of the following programs (originate from the textbook) carefully, fill in the blanks and make it on your answer sheet. (2 points for each blank, 20 points total)**

1. Given the following function to initialize a sequentially stored linear list and find an element.

```
typedef int Position;
```

```
typedef struct LNode * PtrToLNode;
```

```
struct LNode {
```

```
    ElementType Data[MAXSIZE];    /* MAXSIZE 为下标，从 0 开始，足够大的整数*/
```

```
    Position Last;
```

```
};
```

```
typedef PtrToLNode List;
```

```
List MakeEmpty()
```

```
{
```

```
    List L;
```

```
    L = (List)malloc(sizeof(____①____));
```

```
    L->Last = -1;
```

```
    return L;
```

```
}
```

```
Position Find(List L, ElementType X)
```

```
{
```

```
    Position i = 0;
```

```
    while(i <= L->Last && ____②____ != X){
```

```
        i++;
```

```
    }
```

```
    if(i > L->Last)
```

```

        return -1;
    else
        return i;
}
2. Given the following function to push an element into stack.

typedef int Position;
typedef struct SNode * PtrToSNode;
struct SNode {
    ElementType * Data;        /*存储元素的数组，Data[MaxSize]下标从 0 开始*/
    Position Top;              /*栈顶指针*/
    int MaxSize;               /*堆栈最大容量*/
};
typedef PtrToSNode Stack;
bool IsFull(Stack S)
{
    return (S->Top == ③);
}
bool Push(Stack S, ElementType X)
{
    if(IsFull(S)){
        printf("Stack is full!");
        return false;
    }else{
        S->Data[④] = X;
        return true;
    }
}

```

3. Given the following program to implement inorder traversal sequences of a binary tree.

```

typedef struct TNode * Position;
typedef Position BinTree;
struct TNode {
    ElementType Data;        /*节点数据*/
    BinTree Left;
    BinTree Right;
};
void InorderTraversal(BinTree BT)

```

```

{
    if(BT){
        InorderTraversal(____⑤____);
        printf("%d", BT->Data);
        InorderTraversal(____⑥____);
    }
}

```

4. Given the following program to resolve conflict using quadratic probing.

```
typedef int Position;
```

```

Position Find(HashTable H, ElementType Key){
    Position CurrentPos, NewPos;
    int CNum = 0;
    NewPos = CurrentPos = Hash(Key, H->TableSize);
    While(H->Cells[NewPos].Info != Empty && H->Cells[NewPos].Data != Key){
        If(++Cum%2){
            NewPos = CurrentPos + ____⑦____;
            If(NewPos >= H->TableSize)
                NewPos = NewPos% H->TableSize;
        }else{
            NewPos = CurrentPos - ____⑧____;
            While(NewPos<0)
                NewPos += NewPos% H->TableSize;
        }
    }
    Return NewPos;
}

```

5. Given the following program to implement bubble sort.

```

void BubbleSort(ElementType A[], int N){
    int P, i;
    bool flag;
    for(P = N-1; P>=0; P--){
        flag = false;
        for(i=0; i<P; i++){
            if(A[i] > A[i+1]){
                Swap(____⑨____);
                flag = true;
            }
        }
    }
}

```

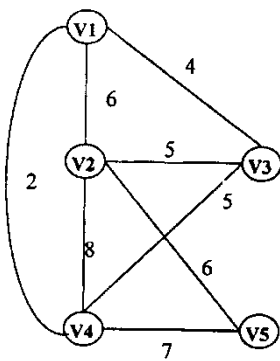
```

    }
}
if(flag==false) ⑩ ;
}

```

**4. Please write or draw your answers for the following problems on the answer sheet. (35 points)**

- (7 points) Given a binary tree, the postorder traversal sequence is: EGFACIJHBD, and the inorder traversal sequence is: EAFGDCBIHJ, please draw the binary tree, and write the preorder traversal sequence.
- (7 points) The following infix-expression:  $(A+B)*C-D/E$ , please write the postfix-expression and draw the content of the Stack while output C and E.
- (7 points) Assume the character set used in the communication message is {a,b,c,d,e,f}, the frequency of each character in the message is {34, 5, 12, 23, 8, 18}, please try to design Huffman code for these 6 characters, draw the Huffman tree you have construct, write the corresponding code for each character.
- (7 points) For the following weighted graph:



Calculate the minimum spanning tree by Prim's algorithm from vertex 1, please draw a construction process step by step while each vertex is added.

- (7 points) Assume keys={47, 7, 29, 11, 16, 92, 22, 8, 3, 50, 37, 89, 94, 21}, hash function is  $h(key)=key\%11$ . The separate chaining is used to resolve collisions. Please try to give the final hash table and calculate the average successful search length (ASL).