

Product of two multivariate gaussians is again gaussian.

$$N_x(a, A) N_x(b, B) = N_x(c, C) \frac{N_a(0, A) N_b(0, B)}{N_c(0, C)}$$

for  $C^{-1} = A^{-1} + B^{-1}$  and  $c = C[A^{-1}a + B^{-1}b]$

Etc.:

$$\prod_i N_x(c_i, C_i) = N_x(t, T) \frac{\prod_i N_{c_i}(0, C_i)}{N_t(0, T)}$$

with  $T^{-1} = \sum_i C_i^{-1}$  and  $t = T \sum_i C_i^{-1} c_i$