

Note: In this document,  $\alpha$  refers exclusively to the fine-structure constant ( $\alpha$ -in) used as input for calibration. The symbols  $\beta$  and  $\gamma$  refer only to standard Post-Newtonian (PPN) parameters relevant to external validation protocols. No structural potential terms  $\{\alpha_V, \beta, \gamma\}$  appear in this document.

## Limitations & Validation Plan — Structural Field Theory (SFT)

**Purpose.** This note consolidates current limitations of SFT and the corresponding validation plan. It is written as a self-contained section to be included in the manuscript bundle.

Language guardrail (recommended): prefix validation items with (C) calibrated/CI-synthetic/methodology vs (P) prediction/REAL-ready inputs required. Use (C) for pipeline auditability and (P) only when REAL solver outputs are in play.

### 1) Experimental validation is pending

**Concern.** While SFT makes concrete predictions, direct tests (e.g., sub-millimeter torsion measurements; CMB/FRB birefringence) are not yet completed.

**Response.** We treat this as an opportunity and commit to a short, testable roadmap:

- **(I) Static Coulomb calibration ( $\alpha$ -in):** use  $\alpha_{\text{ref}}$  as INPUT for calibration; report only consistency with  $\alpha_{\text{ref}}$ . Any  $\alpha$ -out estimation, if executed, lives in a pre-registered appendix with a PASS/FAIL threshold (e.g.,  $\tau = 1\%$ ) and does not affect RC validity.
- **Astrophysical cross-checks.** Recast SFT's birefringence/dispersion predictions against existing CMB TB/EB bounds and FRB/GRB polarization catalogs; declare pass/fail criteria ex ante.
- **Quantitative acceptance bands.** For each test we publish numerical thresholds (energy conservation  $\Delta E/E$ , phase-speed dispersion  $|v_{\text{phase}} - c|/c$ , PPN  $\gamma, \beta$ ), so that third parties can reproduce and decide independently.

### 2) Scope relative to the Standard Model is limited (for now)

**Concern.** Weak interactions, flavor, and the full hadronic spectrum are not modeled yet.

**Response.** SFT's present claims are deliberately scoped to the EM+gravity sector and to the emergent spin- $\frac{1}{2}$  route. The extension path is explicit:

- **Dirac/Wilson appendix completion.** Add numerical checks (no doublers,  $\gamma_5$ -hermiticity, convergence) with tolerances.
- **Internal-texture routes to non-Abelian structure.** "Route B" remains historical/optional, not required for the mainline; we will report negative results as such.
- **Scope discipline.** Until the above milestones are met, we avoid over-reach and label out-of-scope items as future work.

### 3) Initial calibration may look like tuning

**Concern.** The three- step calibration of  $q^*$ ,  $\hbar^*$ ,  $\epsilon^*$ ,  $\mu^*$  could be perceived as parameter- tuning.

**Response.** We operate a single-pass calibration pipeline (already stated across the corpus): calibrate emergent scales once from  $\{\alpha_{em}, c\}$  via a static Coulomb test, freeze them, and then run all demonstrations without per-observable retuning. To make this audit-proof we will:

- **Leave-one-out stress test.** Drop  $\alpha_{em}$  from calibration  $\rightarrow$  predict it back; report residual.
- **Traceability table.** Each figure/number lists precisely which frozen scales it consumes. This turns “tuning” into a reproducible metrology step with cross-validation, rather than free fitting.

Mini-example (illustrative, no numbers):

Item	Consumes frozen scales	Retuning allowed?
Static Coulomb calibration	$\{q^*, \hbar^*, \epsilon^*, \mu^*\}$ frozen from $\{\alpha_{em}, c\}$	No (single-pass)
Demo observable X	Frozen scales only (no per-observable fit)	No
$\alpha$ -out appendix	Separate preregistered $gate\_id$ family	No post-hoc

### 4) Discrete vs. continuum tension

**Concern.** Even with a clean continuum limit, discreteness can jar with traditional QFT/GR.

**Response.** Our mainline Lagrangian is Lorentz-invariant in the continuum; discretization induces  $O((a k)^2)$  corrections that we measure and report (slope  $\xi/2$  in the dispersion-fit). We provide: (I) a convergence scan in a ( $2^{nd}$ -order as claimed); (II) an explicit gauge-fixed Noether construction showing that the Maxwell sector carries no extra DOF ( $A$  is a functional of  $S$  + lattice operators). This reframes discreteness as a numerical regularization with controlled systematics, not as an alternative kinematics.

Audit anchor: the convergence/EOC scan is operationalized in Doc 6 (EOC/CI) and reported via the standard SCAN/REGION/REPORT artifacts where applicable. Reviewers should look for the reported  $O((ak)^2)$  slopes and resolution tags in those artifacts.

### Reviewer Checklist (one page)

1. **Build & Repro:** Docker image builds; pytest passes.
2. **Calibration:** Run once, record  $q^*$ ,  $\hbar^*$ ,  $\epsilon^*$ ,  $\mu^*$ ; no retuning afterward.
3. Numerics: Acceptance bands (preregistered targets): report  $\Delta E/E \leq 1e-3$ ; continuity residual  $\leq 1e-4$ ; dispersion error  $\leq 1\%$ .

4. **PPN:** State convention (signature  $- , + , + , +$ ,  $S = -U$ ), show  $\gamma = 1$  (linear), and  $\beta = 1 + c_\beta \lambda_4 + O(\lambda_4^2)$  with the DSM protocol to extract  $c_\beta$ .
5. **EM emergence:** Cite the Noether $\rightarrow$ Maxwell pipeline and uniqueness/gauge-fixing note (no extra DOF).
6. **Scope:** Label weak/flavor/hadrons as future work; list milestones and negative-result policy.
7. **Experiments:** Define pass/fail bands for (I) sub-mm torsion, (II) CMB/FRB birefringence, (III) lab dispersion.

*Cross-links. See Integrated Technical — Unified Notation & Units (PPN convention), Appendix B (Emergent EM from S), and the Simulation Supplement (Reproducibility summary; defaults; checklist).*

Reviewer Checklist — language guardrail: use labels (C) calibrated / (P) prediction; avoid “predicts/reproduces  $\alpha$ ” wording in the RC body.

## APPENDIX A

### External Break Test #01 — Field Rescaling (Invariance vs Scaling Law)

*Audit protocol (Doc9/Doc15-style) to detect hidden scale dependence and post-hoc tuning*

**Status:** CI / Methodology. Break test intended for external verification.

**Non-claim:** Does not assume  $S \rightarrow \lambda S$  is a physical symmetry. It evaluates (i) representation invariances when applicable and (ii) expected scaling laws when not.

#### 1. Objective

Detect whether the pipeline (estimators, normalizations, gates, and reports) contains hidden scale dependence or compensatory calibration. This test attempts to break the system with a simple field rescaling to reveal: (a) leakage through normalization, (b) adaptive gates, and (c) undeclared sensitivity to amplitude.

## 2. Definitions

Base field:  $S(x)$  generated or imported for a test case with a fixed seed.

Rescaling:  $S_{\lambda}(x) = \lambda \cdot S(x)$ , with  $\lambda \in \{0.5, 1, 2\}$  (minimum).

The  $\lambda$  set used for evaluation MUST be declared in `DECISION_RULE.json` (and hashed) before any run; changing  $\lambda$  post-hoc invalidates the run.

`DECISION_RULE.json`: preregistered definition of operators (stencil/BC), normalization, metrics, and thresholds. Must be hashed (`decision_rule_sha256`) and referenced by `gate_id`.

## 3. Preconditions (prereg / anti-post-hoc)

- Freeze `DECISION_RULE.json` before running (`gate_id + decision_rule_sha256`).
- Deterministic seeds (seed) and version/commit recorded in the report.
- Same grid, same BCs, same dt/CFL (if applicable), same configuration except for the rescaling  $\lambda$ .
- JSON sanitization: NaN/Inf  $\rightarrow$  null before hashing artifacts.
- No threshold/window adjustments after seeing results (post-hoc loosening is forbidden).

## 4. Two complementary tests

### Test A — Representation invariance (if applicable)

Use this when field rescaling is a representational redundancy (e.g.,  $S$  defined up to a multiplicative factor), or when a preregistered parameter transform exists that leaves the model equivalent.

If Test A is used, the exact remap  $p \rightarrow p(\lambda)$  (and any unit/normalization conventions) MUST be stated in `DECISION_RULE.json` and included in the manifest via `decision_rule_sha256`.

Expectation: invariance of outputs explicitly declared as “representation-level” under  $S \rightarrow \lambda S$ .

The list of representation-level outputs MUST be declared in `DECISION_RULE.json` (and hashed), to prevent post-hoc relabeling.

### Test B — Physical scaling law (if A does NOT apply)

Use this when  $S \rightarrow \lambda S$  is not a symmetry. In this case invariance is NOT required; instead, require a preregistered expected scaling law (e.g., energies  $\sim \lambda^2$ , amplitudes/gradients  $\sim \lambda$ , etc., depending on the model).

*For each observable  $y$ , `DECISION_RULE.json` must specify  $y_{\text{expected}}(\lambda)$  (functional form or exponent), the evaluation domain/window, and any masking/exclusions used.*

Expectation: metrics follow the declared scaling law; otherwise FAIL (or “unknown”).

## 5. Procedure (step-by-step)

1. Choose a base case ( $S$ , configuration, seed) and produce/obtain the input artifacts.
2. Create three variants:  $\lambda = 0.5, 1, 2$  (or  $1/3, 1, 3$  if you prefer larger separation).
3. For each  $\lambda$ : run the full pipeline WITHOUT changing anything else.
4. Save the standard artifacts (SCAN/REGION/REPORT if applicable) and the SHA-256 manifest.
5. Compare metrics across  $\lambda$  and evaluate gates according to Test A or Test B.

## 6. Expected artifacts

Note (naming): artifact filenames may be prefixed with BREAKTEST01\_\* for cross-pack reuse, provided the internal schema fields (gate\_id, decision\_rule\_sha256, inputs\_sha256) are unchanged.

Minimum (per  $\lambda$ ):

- ALPHA\_\*\_REPORT.json (includes: suite\_version, gate\_id, decision\_rule\_ref, decision\_rule\_sha256, provenance, GLOBAL\_PASS).
- Optional: COMPATIBILITY\_SCAN\_\*.json and EXISTENCE\_REGION\_\*.json (if the pack uses them).
- MANIFEST\_SHA256.txt (includes hashes for the report + DECISION\_RULE.json + inputs).
- Optional plots: sensitivity\_sweep.png, confusion\_matrix.png (non-authoritative).

## 7. Recommended metrics and gates

Record (per  $\lambda$ ):

- alpha\_like (if applicable) and/or alpha\_out (if applicable), with relative drift vs  $\lambda=1$ .
- Intermediate metrics feeding alpha (e.g., invariants, energy, gradients, fits).
- Scale-sensitivity score per observable:  $s = \max(|\Delta \log y|) / |\Delta \log \lambda|$  (report per  $y$ ).
- Null/adversarial indicators (if the pack has them): FP\_rate, F1, etc.

Suggested gates (examples; must be preregistered):

- Test A:  $|\Delta y_{\text{rep}}| / (|y_{\text{rep}}| + \epsilon) \leq \tau_{\text{rep}}$  for representation-level outputs.

Example (non-normative): Suggested CI defaults (must still be pre-registered):  $\tau_{\text{rep}} = 1e-3$  and  $\tau_{\text{scale}} = 1e-2$ , unless numerical analysis justifies tighter/looser values.

*Non-normative examples only. Thresholds must be preregistered per pack (gate\_id) and justified or inherited from pack-level numerical analysis.*

- Test B:  $|\log y - \log y_{\text{expected}}(\lambda)| \leq \tau_{\text{scale}}$  for observables with a declared scaling law.
- Anti-compensation: if alpha\_out remains “suspiciously constant” while base metrics change strongly, mark as FAIL or “needs review”.

## 8. Quick interpretation (what PASS/FAIL means)

- PASS (Test A): representation-level outputs invariant within gates; manifests and hashes consistent.
- PASS (Test B): outputs follow the preregistered scaling law; deviations small and explainable.
- FAIL: undeclared scale dependence, adaptive gates, post-hoc window changes, or artifact/hash inconsistency.
- INCONCLUSIVE: neither symmetry nor preregistered scaling law; declare “unknown” and preregister expectations before repeating.

## 9. Where this fits in the corpus

This test is recommended as “External Break Test #01” within the validation plan (e.g., Doc 8 or as an appendix to Doc 15). It is especially useful to audit that normalizations, thresholds, and decision rules do not introduce implicit calibration.

**Structural Field Theory.** Complete theory, documents and runners at: <https://github.com/Xaqu69/sft-theory-and-runners>  
<https://doi.org/10.5281/zenodo.17608314>