

# Assignment: 03

## Question: 01

$$q_1 = 3 \text{ nC} = 3 \times 10^{-9} \text{ C}$$

$$q_2 = -7 \text{ nC} = -7 \times 10^{-9} \text{ C}$$

$$q_3 = 5 \text{ nC} = 5 \times 10^{-9} \text{ C}$$

$$r_1 = 2 \text{ cm} = 2 \times 10^{-2} \text{ m}$$

$$r_2 = 4 \text{ cm} = 4 \times 10^{-2} \text{ m}$$

$$k = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$$

Sol:-

$$F_{13} = \frac{k q_1 q_3}{r_1^2}$$

$$F_{23} = \frac{k q_2 q_3}{r_2^2}$$

$$F_{13} = \frac{(9 \times 10^9)(3 \times 10^{-9})(5 \times 10^{-9})}{(2 \times 10^{-2})^2}$$

$$F_{13} = 3.375 \times 10^{-4} \text{ N (to the left)}$$

$$F_{23} = \frac{(9 \times 10^9)(-7 \times 10^{-9})(5 \times 10^{-9})}{(0.04)^2}$$

$$= -1.96 \times 10^{-4}$$

$$F_{23} = 1.96 \times 10^{-4} \text{ N (to the right)}$$

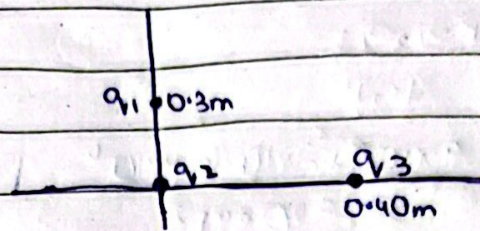
$$\text{Total force} = F_{13} + F_{23}$$

$$F = 1.414 \times 10^{-4} \text{ N}$$



### Question: 02:

$$\begin{aligned}
 q_1 &= 2 \mu\text{C} \\
 \text{at } y &= 0.3 \text{ m} \\
 q_2 &\text{ at origin} \\
 q_3 &= 4 \mu\text{C} \\
 \text{at } x &= 0.40 \text{ m}
 \end{aligned}$$



Soln:-

Acc to question:-

$$\begin{aligned}
 q_1 &= q_2 = 2 \times 10^{-6} \text{ C} \\
 q_3 &= 4 \times 10^{-6} \text{ C}
 \end{aligned}$$

$$r_{23} = 0.40 \text{ m}$$

$$r_{12} = 0.3 \text{ m}$$

$$r_{13} = \sqrt{(r_{12})^2 + (r_{23})^2}$$

$$r_{13} = \sqrt{(0.3)^2 + (0.4)^2}$$

$$r_{13} = 0.5 \text{ m}$$

$$F_{13} = \frac{k q_1 q_3}{(r_{13})^2} \Rightarrow \frac{9 \times 10^9 \times 2 \times 10^{-6} \times 4 \times 10^{-6}}{(0.5)^2}$$

$$F_{13} = 0.288 \text{ N}$$

$$\theta_1 = \tan^{-1}\left(\frac{p}{h}\right)$$

$$= \tan^{-1}\left(\frac{0.3}{0.4}\right)$$

$$\theta_1 = 36.87^\circ$$

$$F_{13x} = F_{13} \cos \theta_1$$

$$F_{13y} = F_{13} \sin \theta_1$$

$$F_{13x} = 0.230 \text{ (right)}$$

$$F_{13y} = 0.172 \text{ (down)}$$



$$F_{23} = k q_2 q_3$$

$$(1.11)^2$$

$$= \frac{9 \times 10^9 \times 2 \times 10^{-6} \times 4 \times 10^{-6}}{(0.4)^2}$$

$$F_{23} = 0.449 \text{ N}$$

∴  $F_{23}$  only applies to right

$$F_{23} = F_{23x} = 0.449 \text{ N} \quad \& \quad F_{23y} = 0$$

$$\text{NOW } \Sigma F = \Sigma F_x + \Sigma F_y$$

$$F_x = F_{13x} + F_{23x}$$

$$= 0.230 + 0.449$$

$$F_x = 0.679 \text{ (downwards)}$$

$$F_y = F_{13y} + F_{23y}$$

$$= 0.172 + 0$$

$$F_y = 0.172 \text{ N}$$

$$F_{\text{net}} = \sqrt{F_x^2 + F_y^2}$$

$$= \sqrt{(0.679)^2 + (0.172)^2}$$

$$F_{\text{net}} = 0.701 \text{ N}$$

$$\theta = \tan^{-1} \left( \frac{F_y}{F_x} \right)$$

$$\theta = 14.25^\circ$$



### Question 03:-

$$\Phi = \frac{\text{total charge}}{\epsilon_0}$$

For S1:-

$$\Phi = \frac{-2Q + Q}{\epsilon_0} = \frac{-Q}{\epsilon_0} \text{ Vm}$$

For S2:-

$$\Phi = \frac{Q - 0}{\epsilon_0} = 0 \text{ Vm}$$

For S3:-

$$\Phi = \frac{-2Q + 0 - 0}{\epsilon_0} = \frac{-2Q}{\epsilon_0} \text{ Vm}$$

For S4:-

$$\Phi = \frac{0}{\epsilon_0} = 0 \text{ Vm}$$

### Question 04:

$$r = 3.2 \times 10^{-2} \text{ m}$$

$$a_1 = 7 \text{ m/s}^2$$

$$a_2 = 9 \text{ m/s}^2$$

$$m_1 = 3.3 \times 10^{-7} \text{ kg}$$

Sol:

∴ Acc to Newton's Second law of motion

$$F = m a$$



$$F_1 = m_1 a_1 \quad F_2 = m_2 a_2$$

$\therefore$  both charges are equal

$$m_1 a_1 = m_2 a_2$$

$$m_2 = \frac{m_1 a_2}{a_1}$$

$$m_2 = \frac{(6.3 \times 10^{-7}) 7}{9}$$

$$m_2 = 4.9 \times 10^{-7} \text{ kg}$$

Acc to Coulomb's law:-

$$F = k_e \times \frac{q_1 q_2}{r^2} \quad \therefore q_1 = q_2$$

$$F = k \frac{q^2}{r^2}$$

$$\text{but } F = ma$$

$$ma = \frac{kq^2}{r^2}$$

$$q^2 = \frac{ma r^2}{k}$$

$$q = \sqrt{\frac{ma r^2}{k}} = \sqrt{\frac{(6.3 \times 10^{-7})(7)(9 \times 10^{-3})^2}{9 \times 10^9}}$$

$$q = \pm 7.1 \times 10^{-11} \text{ C}$$



### Question: 05

$$q_1 + q_2 = 5 \times 10^{-5} \text{ C}$$

$$F = 1 \text{ N} \quad , \quad r = 2 \text{ m}$$

Sol:

$$F = \frac{k q_1 q_2}{r^2}$$

$$q_1 q_2 = \frac{F r^2}{k}$$

$$q_1 q_2 = \frac{(1)(2)^2}{9 \times 10^9}$$

$$q_1 q_2 = 4.4 \times 10^{-10}$$

$$\therefore q_1 + q_2 = 5 \times 10^{-5}$$

$$\text{let } q_1 = x \quad \& \quad q_2 = 5 \times 10^{-5} - x$$

substitute value

$$x (5 \times 10^{-5} - x) = 4.4 \times 10^{-10}$$

$$x^2 - 5 \times 10^{-5} x + 4.4 \times 10^{-10} = 0$$

by quadratic formula

$$x_1 = 3.84 \times 10^{-5} \text{ C} \quad x_2 = 4.25 \times 10^{-5}$$

$$x_2 = 1.16 \times 10^{-5} \text{ C} \quad x_1 = 7.5 \times 10^{-6}$$

smaller charge

$$1.16 \times 10^{-5} \text{ C} \text{ @ } 7.5 \times 10^{-6}$$