

1 Problema 1

PROBLEMA 1

a. Posición: $(0, 150\text{ m})$

Velocidad: (1.0 m/s)

Velocidad =

$$\rightarrow v_x + v_{0x} + at$$

$$v_x = 5\text{ m/s} - (9.8\text{ m/s}^2)(1\text{ s})$$

$$v_x = 4.8\text{ m/s}$$

Posición =

$$\rightarrow v_{iy} = 5\text{ m/s} - (9.8\text{ m/s}^2)(0.150\text{ s})$$

$$v_{iy} = 5\text{ m/s} - 2.45\text{ m/s}$$

$$v_{iy} = 2.55\text{ m/s}$$

$$x(t) = x_0 + v_{0x}t + \frac{1}{2}at^2$$

$$y(t) = 40.0\text{ m} + (2.55\text{ m/s})(0.150\text{ s}) - \frac{1}{2}(9.8\text{ m/s}^2)(0.150\text{ s})^2$$

$$y(t) = 40.0\text{ m} + 0.6375\text{ m} - 0.3\text{ m}$$

$$y(t) = 40.3\text{ m}$$

b.
$$x(t) = x_0 + v_{0x}t + \frac{1}{2}at^2$$
$$0 = 40.0\text{ m} + (5\text{ m/s})t - \frac{1}{2}at^2$$
$$0 = -(4.9)t^2 + 5t + 40$$
$$-0 = 4.9t^2 - 5t - 40$$
$$t_1 = 3.4\text{ s}$$
$$t_2 = -2.39\text{ s}$$

c.
$$v_x = v_{0x} + at$$
$$v_x = 5\text{ m/s} + (9.8\text{ m/s}^2)(3.4\text{ s})$$
$$v_x = 38.32\text{ m/s}$$

d. 40.1 m

2 Problema 2

HA 1

$$\begin{aligned} a. \quad x(t) &= v_0 \cos 50^\circ t \\ y(t) &= h + v_0 \sin 50^\circ t - \frac{1}{2} g t^2 \\ v_y(t) &= v_{0y} - g t \end{aligned} \quad \longrightarrow \quad \begin{aligned} v_y(t) &= v_{0y} - g t \\ 0 &= v_{0y} - g t \\ v_{0y} &= g t \\ \frac{v_{0y}}{g} &= t \end{aligned}$$

$$\frac{x}{v_0 \cos 50^\circ} = t$$

$$\frac{v_0 \sin 50^\circ}{g} = t$$

$$\begin{aligned} y(t) &= h + v_0 \sin 50^\circ t - \frac{1}{2} g t^2 \\ 0 &= h + v_0 \sin 50^\circ \left(\frac{x}{v_0 \cos 50^\circ} \right) - \frac{1}{2} g \left(\frac{x^2}{v_0^2 \cos^2 50^\circ} \right) \\ h + \cancel{v_0 \sin 50^\circ} \left(\frac{x}{\cancel{v_0 \cos 50^\circ}} \right) &= \frac{1}{2} g \left(\frac{x^2}{v_0^2 \cos^2 50^\circ} \right) \\ h + x \tan 50^\circ &= \frac{1}{2} g \left(\frac{x^2}{v_0^2 \cos^2 50^\circ} \right) \end{aligned}$$

$$h = \frac{1}{2} g \left(\frac{x^2}{v_0^2 \cos^2 50^\circ} \right) - x \tan 50^\circ$$

$$y(t) = v_0 + v_{0y} t - \frac{1}{2} g t^2$$

$$\cancel{h_{\max}} = \cancel{x} + v_0 \sin 50^\circ \left(\frac{v_0 \sin 50^\circ}{g} \right) - \frac{1}{2} g \left(\frac{v_0^2 \sin^2 50^\circ}{g^2} \right)$$

$$h_{\max} = \frac{v_0^2 \sin^2 50^\circ}{g} - \frac{1}{2} \frac{(v_0^2 \sin 50^\circ)}{g}$$

$$h_{\max} = \frac{1}{2} \frac{v_0^2 \sin^2 50^\circ}{g}$$

$$gh_{\max} = \frac{v_0^2 \sin^2 50^\circ}{2}$$

$$\cancel{2gh_{\max}} = \cancel{v_0^2 \sin^2 50^\circ}$$

$$v_0^2 = \frac{2gh_{\max}}{\sin^2 50^\circ}$$

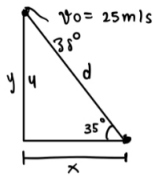
$$v_0 = \sqrt{\frac{2gh_{\max}}{\sin^2 50^\circ}}$$

$$v_0 = \sqrt{\frac{(2)(9.8 \text{ m/s}^2)(0.624 \text{ m})}{0.586}}$$

$$v_0 = 1.50 \text{ m/s}_0$$

3 Problema 3

PROBLEMA 3.



$$\tan 35^\circ = \frac{y}{x} \quad x = \frac{y}{\tan 35^\circ}$$

$$y = \tan 35^\circ x$$

$$y = y - \frac{1}{2} g t_v^2 \rightarrow t_v = \frac{\sqrt{2y}}{g}$$

$$x = v_0 t_v \rightarrow t_v = \frac{x}{v_0} \uparrow$$

$$d = \sqrt{x^2 + y^2}$$

$$d = \sqrt{(v_0^2 \frac{2}{g})^2 + (v_0^2 \frac{2}{g} \tan 35^\circ)^2}$$

$$x = v_0 \frac{\sqrt{2y}}{g}$$

$$\left(\frac{y}{\tan 35^\circ} \right)^2 = v_0^2 \frac{2y}{g}$$

$$t_v = v_0 \frac{2}{g}$$

$$\frac{y^2}{\tan^2 35^\circ} = v_0^2 \frac{2y}{g}$$

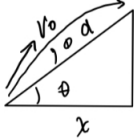
$$v_0^2 = v_0^2 \sin^2 35^\circ - 2g \left(v_0^2 \frac{2}{g} \tan 35^\circ \right)$$

$$y = v_0^2 \frac{2}{g} \tan 35^\circ$$

$$v_0^2 = v_0^2 \sin^2 35^\circ - 2(v_0^2 \frac{2}{g} \tan 35^\circ)$$

4 Problema 4

PROBLEMA 4.



$$a. h = v_0 \sin \phi + v_0 \sin \phi t - \frac{1}{2} g t^2 \rightarrow$$

$$x = v_0 \cos \phi + v_0 \cos \phi t$$

$$\frac{x}{v_0 \cos \phi} = t$$

$$h = v_0 \sin \phi + v_0 \sin \phi \left(\frac{x}{v_0 \cos \phi} \right) - \frac{1}{2} g \left(\frac{x^2}{v_0^2 \cos^2 \phi} \right)$$

$$h = x \tan \phi + \frac{g x^2}{2 v_0^2 \cos^2 \phi}$$

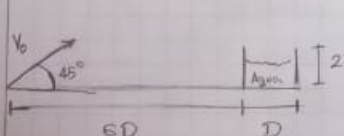
$$b). 45^\circ + \phi = \phi$$

$$d = \sqrt{\left(x \tan \phi + \frac{g x^2}{2 v_0^2 \cos^2 \phi} \right)^2 + v_0^2 \cos^2 \phi t^2}$$

5 Problema 5,6 y 7

Día: Mes: Año:

Problema 5

Diagrama: 

$$H_{\text{total}} = 6D + D = 7D$$

$$H = 2D$$

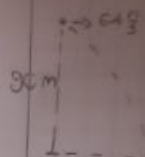
$$V_0^2 = \frac{gD}{2 \cos^2 45^\circ (D \tan 45^\circ + H)}$$

$$V_0^2 = \frac{(9,8 \frac{\text{m}}{\text{s}^2}) 7D}{2 \cos^2 45^\circ (7D \tan 45^\circ + 2D)}$$

$$V_0^2 = \frac{9,8 \frac{\text{m}}{\text{s}^2} 7D}{\frac{2}{2} \cdot (7D + 2D)}$$

$$V_0 = \sqrt{\frac{9,8 \frac{\text{m}}{\text{s}^2}}{\frac{1}{2} \cdot 2D}} ; D \in \mathbb{R} > 0$$

Problema 6

Diagrama: 

$$V_0 = 64 \frac{\text{m}}{\text{s}}$$

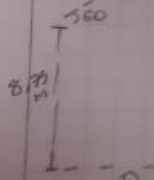
$$y = 90,0 \text{ m}$$

$$90 \text{ m} = 9,8 \frac{\text{m}}{\text{s}^2} t^2 \quad t = \frac{90 \text{ m}}{9,8 \frac{\text{m}}{\text{s}^2}} = 9,18 \text{ s}$$

$$g = 9,8 \frac{\text{m}}{\text{s}^2} \quad x = vt$$

$$x = 64 \frac{\text{m}}{\text{s}} \cdot 9,18 \text{ s} = 587,52 \text{ m}$$

Problema 7

Diagrama: 

$$V_0 = 15,0 \frac{\text{m}}{\text{s}} \sin 60^\circ = \frac{15\sqrt{3}}{2} \frac{\text{m}}{\text{s}}$$

$$V_y = \frac{15\sqrt{3}}{2} \frac{\text{m}}{\text{s}} - (9,8 \frac{\text{m}}{\text{s}^2}) t$$

$$V_x = 15,0 \frac{\text{m}}{\text{s}} \cos 60^\circ = \frac{15}{2} \frac{\text{m}}{\text{s}}$$

$$0 \frac{\text{m}}{\text{s}} = \frac{15\sqrt{3}}{2} \frac{\text{m}}{\text{s}} - (9,8 \frac{\text{m}}{\text{s}^2}) t$$

$$y = \frac{15\sqrt{3}}{2} \frac{\text{m}}{\text{s}} t - \frac{1}{2} (9,8 \frac{\text{m}}{\text{s}^2}) t^2 = \frac{15\sqrt{3}}{2} \frac{\text{m}}{\text{s}} t - 4,9 \frac{\text{m}}{\text{s}^2} t^2$$

$$y_1 = 25,6 \text{ m}$$

$$6,35 + 25,6 \text{ m} = y = 31,95 \text{ m}$$

$$t = \frac{31,95 \text{ m}}{9,8 \frac{\text{m}}{\text{s}^2}} = 3,26 \text{ s}$$

$$t = 2,32 + 3,51 = 5,83 \text{ s}$$

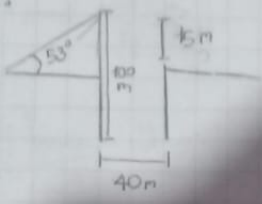
$$D = \frac{15}{2} \frac{\text{m}}{\text{s}} \cdot 4,93 \text{ s} = 36,975 \text{ m}$$

tuffy

6 Problema 8

Dia: _____ Mes: _____ Año: _____

8.



$$\hat{y} = y_0 + v_{0y}t + \frac{1}{2}at^2$$

$$0 = 15\text{m} - \frac{1}{2}gt^2$$

$$\sqrt{\frac{2 \cdot 15\text{m}}{(9,8\frac{\text{m}}{\text{s}^2})}} = t$$

$$1,74\text{s} = t$$

$$\hat{x} = v_0 \cos \theta t$$

$$\frac{\hat{x}}{t \cos \theta} = v_0$$

$$\frac{40\text{m}}{1,74\text{s} \cos 53} = 38,19 \frac{\text{m}}{\text{s}}$$

b.

$$\frac{38,19 \frac{\text{m}}{\text{s}}}{2} = 19,09 \frac{\text{m}}{\text{s}}$$

$$\hat{x} = 19,09 \frac{\text{m}}{\text{s}} \cos 53 \cdot 1,74\text{s} = 19,99 \approx 20\text{m}$$

7 Problema 9

PROBLEMA 9.

Pelota 1

$$y(t) = y_0 + v_{0y}t - \frac{1}{2}gt^2$$

$$y(t) = 40\text{m} + 20\text{m/s} \sin 53^\circ - \frac{1}{2}9,8\text{m/s}^2 t^2 =$$

$$40\text{m} + 20\text{m/s} \sin 53^\circ t - \frac{1}{2}9,8\text{m/s}^2 t^2 = 30\text{m/s} \sin 37^\circ t - \frac{1}{2}gt^2$$

$$15,97t - 4,9t^2 - 18,05t - 4,9t^2 = -40\text{m}$$

$$2,08t$$

$$\frac{40\text{m}}{2\text{m/s}} = t$$

$$20\text{s} = t$$

$$y(t) = 40\text{m} + 20\text{m/s} \sin 53^\circ - \frac{1}{2}9,8\text{m/s}^2 t^2 =$$

$$y(t) = 40\text{m} + 15,97\text{m/s}(20\text{s}) - 4,9\text{m/s}^2 (20\text{s})^2$$

Pelota 2.

$$y(t) = y_0 + v_{0y}t - \frac{1}{2}gt^2$$

$$y(t) = 0 + 30\text{m/s} \sin 37^\circ - \frac{1}{2}gt^2$$