

## Ecran

**Service:** Screen

**Observers:** **const** Height: [Screen]  $\rightarrow$  int

**const** Width: [Screen]  $\rightarrow$  int

CellNature: [Screen]  $\times$  int  $\times$  int  $\rightarrow$  Cell

**pre** CellNature(S,x,y) **requires**  $0 \leq y < \text{Height}(S)$  **and**  $0 \leq x < \text{Width}(S)$

**Constructors:** init: int  $\times$  int  $\rightarrow$  [Screen]

**pre** init(h,w) **requires**  $0 < h$  **and**  $0 < w$

**Operators:** Dig: [Screen]  $\times$  int  $\times$  int  $\rightarrow$  [Screen]

**pre** Dig(S,x,y) **requires** CellNature(S,x,y) = **PLT**

Fill: [Screen]  $\times$  int  $\times$  int  $\rightarrow$  [Screen]

**pre** Dig(S,x,y) **requires** CellNature(S,x,y) = **HOL**

**Observations:**

[init]: Height(init(h,w)) = h

Width(init(h,w)) = w

**forall** (x, y) **in**  $[0; \text{Width}(S)[ \times [0; \text{Height}(S)[$ , CellNature(init(h,w),x,y) = **EMP**

[Dig]: CellNature(Dig(S,x,y)),x,y = **HOL**

**forall** (x, y) **in**  $[0; \text{Width}(S)[ \times [0; \text{Height}(S)[$ ,

(x  $\neq$  u **or** y  $\neq$  v) **implies** CellNature(Dig(S,u,v)),x,y) = CellNature(x,y)

[Fill]: CellNature(Fill(S,x,y),x,y) = **PLT**

**forall** (x, y) **in**  $[0; \text{Width}(S)[ \times [0; \text{Height}(S)[$ ,

(x  $\neq$  u **or** y  $\neq$  v) **implies** CellNature(Fill(S,u,v)),x,y) = CellNature(x,y)

## Ecran éditable

<b>Service:</b>	EditableScreen <b>includes</b> Screen
<b>Observers:</b>	Playable: [EditableScreen] $\rightarrow$ bool
<b>Operators:</b>	SetNature: [EditableScreen] $\times$ int $\times$ int $\times$ Cell $\rightarrow$ [EditableScreen] <b>pre</b> SetNature(S,x,y,C) <b>requires</b> $0 \leq y < \text{Height}(S)$ and $0 \leq x < \text{Width}(S)$
<b>Observations:</b>	
[invariant]:	Playable(S) <b>min</b> <b>forall</b> (x, y) <b>in</b> $[0; \text{Width}(S)[ \times [0; \text{Height}(S)[$ , CellNature(S,x,y) $\neq$ <b>HOL</b> <b>and forall</b> x <b>in</b> $[0; \text{Width}(S)[$ , CellNature(S,x,0) = <b>MTL</b>
[SetNature]:	CellNature(SetNature(S,x,y,C)),x,y = C <b>forall</b> (x, y) <b>in</b> $[0; \text{Width}(S)[ \times [0; \text{Height}(S)[$ , (x $\neq$ u or y $\neq$ v) <b>implies</b> CellNature(SetNature(S,u,v,C)),x,y) = CellNature(x,y)

## Environment

<b>Service:</b>	Environment <b>includes</b> Screen
<b>Observers:</b>	CellContent: int $\times$ int $\rightarrow$ Set{Character + Item} <b>pre</b> CellContent(E,x,y) <b>requires</b> $0 \leq y < \text{Height}(S)$ and $0 \leq x < \text{Width}(S)$ toString : [Environnement] $\rightarrow$ String
<b>Constructors:</b>	init: EditableScreen $\rightarrow$ Environment
<b>Observations:</b>	
[invariant] :	<b>forall</b> (x; y) <b>in</b> $[0; \text{Width}(E)[ \times [0; \text{Height}(E)[$ , <b>forall</b> Character c1, c2 <b>in</b> CellContent(E,x,y) <sup>2</sup> , c1 = c2 <b>forall</b> (x; y) <b>in</b> $[0; \text{Width}(E)[ \times [0; \text{Height}(E)[$ , CellNature(E,x,y) <b>in</b> { <b>MTL</b> , <b>PLR</b> , <b>TLP</b> } <b>implies</b> CellContent(x,y) = $\emptyset$ <b>forall</b> (x; y) <b>in</b> $[0; \text{Width}(E)[ \times [0; \text{Height}(E)[$ , <b>exists</b> Treasure t <b>in</b> CellContent(E,x,y) <b>implies</b> (CellNature(E,x,y) = <b>EMP</b> and CellNature(E,x,y-1) <b>in</b> { <b>PLT</b> , <b>MTL</b> , <b>TLP</b> })
[init]:	<b>forall</b> (x; y) <b>in</b> $[0; \text{Width}(E)[ \times [0; \text{Height}(E)[$ , CellNature(init(S),x,y) = EditableScreen::CellNature(S,x,y)

## Character

<b>Service:</b>	Character
<b>Observers:</b>	<b>const</b> Envi: [Character] $\rightarrow$ Environment Hgt: [Character] $\rightarrow$ int Wdt: [Character] $\rightarrow$ int Id : [Character] $\rightarrow$ int
<b>Constructors:</b>	init: Screen $\times$ int $\times$ int $\times$ int $\rightarrow$ [Character] <b>pre</b> init(S,x,y) <b>requires</b> Environment::CellNature(S,x,y) = <b>EMP</b>
<b>Operators:</b>	SetPos : [Character] $\times$ int $\times$ int $\rightarrow$ [Character] <b>pre</b> setPos(C,x,y) <b>requires</b> $0 \leq x < \text{Width}(\text{Envi}(C))$ <b>and</b> $0 \leq y < \text{Height}(\text{Envi}(C))$ <b>and</b> Environment::CellNature(Wdt(C),Hgt(C)) not in {MTL, PLT ,TLP} GoLeft: [Character] $\rightarrow$ [Character] GoRight: [Character] $\rightarrow$ [Character] GoUp: [Character] $\rightarrow$ [Character] GoDown: [Character] $\rightarrow$ [Character]
<b>Observations:</b>	
[invariant]:	Environment::CellNature(Envi(C),Wdt(C),Hgt(C)) <b>in</b> {EMP, HOL, LAD, HDR}
[Init]:	GetWdt(Init(screen, x,y,id)) = x GetHgt(Init(screen, x,y,id)) = y id > -1 <b>implies</b> GetId(Init(screen,x,y,id)) = id
[GoLeft]:	Hgt(GoLeft(C)) = Hgt(C) Wdt(C) = 0 <b>implies</b> Wdt(GoLeft(C)) = Wdt(C) Environment::CellNature(Envi(C),Wdt(C)-1,Hgt(C)) <b>in</b> { <b>MTL</b> , <b>PLT</b> , <b>TLP</b> } <b>implies</b> Wdt(GoLeft(C)) = Wdt(C) Environment::CellNature(Envi(C),Wdt(C),Hgt(C)) <b>not in</b> { <b>LAD</b> , <b>HDR</b> } <b>and</b> Environment::CellNature(Envi(C),Wdt(C),Hgt(C)-1) <b>not in</b> { <b>PLT</b> , <b>MTL</b> , <b>LAD</b> , <b>TLP</b> } <b>and not exists</b> Character c <b>in</b> Environment::CellContent(Envi(C),Wdt(C),Hgt(C)-1) <b>implies</b> Wdt(GoLeft(C)) = Wdt(C) <b>exists</b> Character c <b>in</b> Environment::CellContent(Envi(C),Wdt(C)-1,Hgt(C)) <b>implies</b> Wdt(GoLeft(C)) = Wdt(C) (Wdt(C) $\neq$ 0) <b>and</b> Environment::CellNature(Envi(C),Wdt(C)-1,Hgt(C)) <b>not in</b> { <b>MTL</b> , <b>PLT</b> , <b>TLP</b> } <b>and</b> (Environment::CellNature(Envi(C),Wdt(C),Hgt(C)) <b>in</b> { <b>LAD</b> , <b>HDR</b> } <b>or</b> Environment::CellNature(Envi(C),Wdt(C),Hgt(C)-1) <b>in</b> { <b>PLT</b> , <b>MTL</b> , <b>LAD</b> , <b>TLP</b> } <b>or exists</b> Character c <b>in</b> Environment::CellContent(Envi(C),Wdt(C),Hgt(C)-1) ) <b>and</b> (Id(C) = -1 <b>or</b> ( <b>not exists</b> Character c <b>in</b> Environment::CellContent(Envi(C),Wdt(C)-1,Hgt(C)))) <b>implies</b> Wdt(GoLeft(C)) = Wdt(C)-1

[GoRight]:

$Hgt(GoRight(C)) = Hgt(C)$   
 $Wdt(C) = Width(Envi(C))-1$  **implies**  $Wdt(GoRight(C)) = Wdt(C)$   
 $Environment::CellNature(Envi(C), Wdt(C)+1, Hgt(C))$  **in** {MTL, PLT, TLP }  
**implies**  $Wdt(GoRight(C)) = Wdt(C)$   
 $Environment::CellNature(Envi(C), Wdt(C), Hgt(C))$  **not in** {LAD, HDR}  
**and**  $Environment::CellNature(Envi(C), Wdt(C), Hgt(C)-1)$  **not in** {PLT, MTL, LAD, TLP}  
**and not exists** Character  $c$  **in**  $Environment::CellContent(Envi(C), Wdt(C), Hgt(C)-1)$   
**implies**  $Wdt(GoRight(C)) = Wdt(C)$   
**exists** Character  $c$  **in**  $Environment::CellContent(Envi(C), Wdt(C)+1, Hgt(C))$   
**implies**  $Wdt(GoRight(C)) = Wdt(C)$   
 $(Wdt(C) \neq Width(Envi(C))-1)$   
**and**  $Environment::CellNature(Envi(C), Wdt(C)+1, Hgt(C))$  **not in** {MTL, PLT, TLP }  
**and**  $(Environment::CellNature(Envi(C), Wdt(C), Hgt(C))$  **in** {LAD, HDR}  
**or**  $Environment::CellNature(Envi(C), Wdt(C), Hgt(C)-1)$   
**in** {PLT, MTL, LAD, TLP}  
**or exists** Character  $c$  **in**  $Environment::CellContent(Envi(C), Wdt(C), Hgt(C)-1)$  )  
**and**  $(Id(C) = -1$   
**or** **(not exists** Character  $c$  **in**  $Environment::CellContent(Envi(C), Wdt(C)+1, Hgt(C))$ ))  
**implies**  $Wdt(GoRight(C)) = Wdt(C)+1$

[GoUp]:

$Wdt(GoUp(C)) = Wdt(C)$   
 $Hgt(C) = Environment::Height(Envi(C))-1$  **implies**  $Hgt(GoUp(C)) = Hgt(C)$   
 $Environment::CellNature(Envi(C), Wdt(C)+1, Hgt(C))$  **in** {MTL, PLT, TLP }  
**implies**  $Hgt(GoUp(C)) = Hgt(C)$   
 $Environment::CellNature(Envi(C), Wdt(C), Hgt(C))$  **not in** {LAD}  
**implies**  $Hgt(GoUp(C)) = Hgt(C)$   
**exists** Guard  $g$  **in**  $Environment::CellContent(Envi(C), Wdt(C), Hgt(C)+1)$  **and**  $Id(C) < -1$   
**implies**  $Wdt(GoUp(C)) = Wdt(C)$   
 $(Hgt(C) \neq Environment::Height(Envi(C))-1)$   
**and**  $Environment::CellNature(Envi(C), Wdt(C), Hgt(C)+1)$  **not in** {MTL, PLT, TLP }  
**and**  $Environment::CellNature(Envi(C), Wdt(C), Hgt(C))$  **in** {LAD}  
**and**  $(Id(C) = -1$   
**or** **(not exists** Character  $c$  **in**  $Environment::CellContent(Envi(C), Wdt(C), Hgt(C)+1)$ ))  
**implies**  $Hgt(GoUp(C)) = Hgt(C)+1$

[GoDown]:

$Wdt(GoUp(C)) = Wdt(C)$   
 $Hgt(C) = 1$  **implies**  $Hgt(GoDown(C)) = Hgt(C)$   
 $Environment::CellNature(Envi(C), Wdt(C)+1, Hgt(C))$  **in** {MTL, PLT, TLP }  
**implies**  $Hgt(GoDown(C)) = Hgt(C)$   
**exists** Guard  $g$  **in**  $Environment::CellContent(Envi(C), Wdt(C), Hgt(C)-1)$  **and**  $Id(C) < -1$   
**implies**  $Wdt(GoDown(C)) = Wdt(C)$   
 $(Hgt(C) \neq 1)$   
**and**  $Environment::CellNature(Envi(C), Wdt(C), Hgt(C)+1)$  **not in** {MTL, PLT, TLP }  
**and**  $Environment::CellNature(Envi(C), Wdt(C), Hgt(C))$  **in** {LAD}  
**and**  $(Id(C) = -1$   
**or** **(not exists** Character  $c$  **in**  $Environment::CellContent(Envi(C), Wdt(C), Hgt(C)+1)$ ))  
**implies**  $Hgt(GoDown(C)) = Hgt(C)-1$

[setPos]:

$Hgt(SetHgt(C, y)) = Hgt(C)$  **and**  $Wdt(SetWdt(C, x)) = Wdt(C)$  //remplace celle de setHgt et setWdt

## Guard

**Service:** Guard **includes** Character

**Observers:** **const** Id: [Guard]  $\rightarrow$  int  
Target: [Guard]  $\rightarrow$  Player  
Behaviour : [Guard]  $\rightarrow$  Command  
TimeInHole: [Guard]  $\rightarrow$  int  
Engine: [Guard]  $\rightarrow$  Engine  
HasItem: [Guard]  $\rightarrow$  boolean  
Treasure : [Guard]  $\rightarrow$  Item

**Predicates:** **willFall** : [Guard]  $\rightarrow$  boolean  
willFall(g) **defined by**  
Environment::CellNature(Envi(E),Wdt(g),Hgt(g)) **not in** {LAD,HDR,HOL} **and**  
Environment::CellNature(Envi(E),Wdt(g),Hgt(g)-1) **in** {HDR,HOL,EMP} **and**  
**not exists** Guard gbis **in** Environment::CellContent(Envi(E),Wdt(g),Hgt(g)-1)

**willWaitInHole** : [Guard]  $\rightarrow$  boolean  
willWaitInHole(g) **defined by**  
Environment::CellNature(Envi(E),Wdt(g),Hgt(g)) = **HOL** **and**  
Guard::TimeInHole(g) < 10

**willClimbLeft** : [Guard]  $\rightarrow$  boolean  
willClimbLeft(g) **defined by**  
Environment::CellNature(Envi(E),Wdt(g),Hgt(g)) = **HOL** **and**  
Guard::TimeInHole(g) = 10 **and**  
Guard::Behaviour(g) = **LEFT**

**willClimbRight** : [Guard]  $\rightarrow$  boolean  
willClimbRight(g) **defined by**  
Environment::CellNature(Envi(E),Wdt(g),Hgt(g)) = **HOL** **and**  
Guard::TimeInHole(g) = 10 **and**  
Guard::Behaviour(g) = **RIGHT**

**willClimbNeutral** : [Guard]  $\rightarrow$  boolean  
willClimbNeutral(g) **defined by**  
Environment::CellNature(Envi(E),Wdt(g),Hgt(g)) = **HOL** **and**  
Guard::TimeInHole(g) = 10 **and**  
Guard::Behaviour(g) = **NEUTRAL**

**willFollowBehaviour** : [Guard]  $\rightarrow$  boolean  
**not willFall** **and not willWaitInHole** **and not willClimbLeft** **and not willClimbRight** **and**  
**not willClimbNeutral**

**Constructors:** init: Screen  $\times$  int  $\times$  int  $\rightarrow$  [Character]  
**pre** init(S,x,y) **requires** Environment::CellNature(S,x,y) = **EMP**

**Operators:** WaitInHole: [Guard]  $\rightarrow$  [Guard]  
**pre** WaitInHole(G) **requires** Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) = **HOL**  
SetTreasure: [Guard]  $\times$  Item  $\rightarrow$  [Guard]  
**pre** SetTreasure(G,t) **requires not** HasItem(G)

ClimbLeft: [Guard]  $\rightarrow$  [Guard]

**pre** ClimbLeft(g) **requires** Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) = **HOL**

ClimbRight: [Guard]  $\rightarrow$  [Guard]

**pre** ClimbRight(g) **requires** Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) = **HOL**

Step: [Guard]  $\rightarrow$  [Guard]

## Observations:

[Invariants]

**//UP**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {**LAD**} **and**

Hgt(G) < Hgt(Target(G)) **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **not in** {**PLT**,**MTL**,**TLP**} **and**

**not exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**

|Environment::Hgt(Target(G)) - Hgt(G)| > |Environment::Wdt(Target(G)) - Wdt(G)| **implies**

Behaviour(G) = Command::**UP**

**//DOWN**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {**LAD**} **and**

Hgt(G) > Hgt(Target(G)) **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **not in** {**PLT**,**MTL**,**TLP**} **and**

**not exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**

|Environment::Hgt(Target(G)) - Hgt(G)| > |Environment::Wdt(Target(G)) - Wdt(G)| **implies**

Behaviour(G) = Command::**DOWN**

**//LEFT**

(Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {**LAD**} **and**

Wdt(G) < Wdt(Target(G)) **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **not in** {**PLT**,**MTL**,**TLP**} **and**

**not exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**

|Environment::Hgt(Target(G)) - Hgt(G)| < |Environment::Wdt(Target(G)) - Wdt(G)|))

**or**

((Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {**HOL**} **or**

(Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **in** {**PLT**,**MTL**,**TLP**} **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **not in** {**LAD**})) **or**

(**exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **not in** {**LAD**})) **and**

Wdt(G) > Wdt(Target(G)) **implies** Behaviour(G) = Command::**LEFT**

**//RIGHT**

(Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {**LAD**} **and**

Wdt(G) > Wdt(Target(G)) **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **not in** {**PLT**,**MTL**,**TLP**} **and**

**not exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**

|Environment::Hgt(Target(G)) - Hgt(G)| < |Environment::Wdt(Target(G)) - Wdt(G)|))

**or**

((Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {**HOL**} **or**

(Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **in** {**PLT**,**MTL**,**TLP**} **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **not in** {**LAD**})) **or**

(**exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **not in** {**LAD**})) **and**

Wdt(G) < Wdt(Target(G)) **implies** Behaviour(G) = Command::**RIGHT**

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {HDR,EMP} **and**  
 Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **in** {PLT,MTL,TLP} **or**  
**exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**  
 Wdt(G) == Wdt(Target(G)) **implies** Behaviour(G) = Command::NEUTRAL

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) **in** {HDR} **and**  
 (Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **in** {PLT,MTL,TLP} **or**  
**exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **or**  
 |Environment::Hgt(Target(G)) - Hgt(G)| < |Environment::Wdt(Target(G)) - Wdt(G)|) **implies**  
 (Wdt(G) > Wdt(Target(G)) **implies** Behaviour(G) = Command::LEFT) **or**  
 (Wdt(G) < Wdt(Target(G)) **implies** Behaviour(G) = Command::RIGHT) **or**  
 (Wdt(G) = Wdt(Target(G)) **implies** Behaviour(G) = Command::NEUTRAL))  
**or**  
 (Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) **not in** {PLT,MTL,TLP} **and**  
**not exists** Guard g **in** Environnement::getCellContent(Envi(G),Wdt(G),Hgt(G)-1) **and**  
 |Environment::Hgt(Target(G)) - Hgt(G)| < |Environment::Wdt(Target(G)) - Wdt(G)|) **implies**  
 [(Wdt(G) > Wdt(Target(G)) **implies** Behaviour(G) = Command::LEFT) **or**  
 (Wdt(G) < Wdt(Target(G)) **implies** Behaviour(G) = Command::RIGHT) **or**  
 (Wdt(G) = Wdt(Target(G)) **implies** Behaviour(G) = Command::NEUTRAL))]  
**or**  
 [(Hgt(G) > Hgt(Target(G)) **implies** Behaviour(G) = Command::DOWN) **or**  
 (Hgt(G) < Hgt(Target(G)) **implies** Behaviour(G) = Command::UP) **or**  
 (Hgt(G) = Hgt(Target(G)) **implies** Behaviour(G) = Command::NEUTRAL))])

**exists** Guard g **in** Environnement::CellContent(Envi(G),Wdt(G),Hgt(G)) **implies** g = G

[Init]

TimeInHole(init(e,h,w,t)) = 0  
 Target(init(e,h,w,t)) = t

[WaitInHole]

TimeInHole(WaitInHole(G)) = TimeInHole(G)+1

[ClimLeft]

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)+1) **not in** {PLT,MTL,TLP} **and**  
 Environment::CellNature(Envi(G),Wdt(G)-1,Hgt(G)+1) **not in** {PLT,MTL,TLP} **and**  
**not exists** Character c **in** Environnement::getCellContent(Envi(G),Wdt(G)-1,Hgt(G)+1)  
**implies** Wdt(ClimbLeft(G)) = Wdt(G)-1 **and** Hgt(ClimbLeft(G)) = Hgt(G)+1

[ClimRight]

Environment::CellNature(Envi(G),Wdt(G),Hgt(G)+1) **not in** {PLT,MTL,TLP} **and**  
 Environment::CellNature(Envi(G),Wdt(G)+1,Hgt(G)+1) **not in** {PLT,MTL,TLP} **and**  
**not exists** Character c **in** Environnement::getCellContent(Envi(G),Wdt(G)+1,Hgt(G)+1)  
**implies** Wdt(ClimbRight(G)) = Wdt(G)+1 **and** Hgt(ClimbRight(G)) = Hgt(G)+1

[SetTreasure]

HasTreasure(SetTreasure(G,t)) = true

[Step]

WillFall(G) **implies** GetBehaviour(G) = Command::DOWN **and**  
 Wdt(Step(G)) = Wdt(G) **and** Hgt(Step(G)) = Hgt(G)-1 **and**  
 TimeInHole(Step(G)) = TimeInHole(G)

WillClimbLeft(G) **implies** GetBehaviour(G) = Command::LEFT **and**  
     ((Wdt(Step(G)) = Wdt(G)-1 **and** Hgt(Step(G))= Hgt(G)+1) **or**  
     (Wdt(Step(G)) ≠ Wdt(G) **and** Hgt(Step(G)) ≠ Hgt(G))) **and**  
     TimeInHole(Step(G)) = TimeInHole(G)

WillClimbRight(G) **implies** GetBehaviour(G) = Command::RIGHT **and**  
     ((Wdt(Step(G)) = Wdt(G)+1 **and** Hgt(Step(G))= Hgt(G)-1) **or**  
     (Wdt(Step(G)) ≠ Wdt(G) **and** Hgt(Step(G)) ≠ Hgt(G))) **and**  
     TimeInHole(Step(G)) = TimeInHole(G)

WillClimbNeutral(G) **implies** GetBehaviour(G) = Command::NEUTRAL **and**  
     Wdt(Step(G)) = Wdt(G) **and** Hgt(Step(G)) = Hgt(G) **and**  
     TimeInHole(Step(G)) = TimeInHole(G)

WillWaitInHole(G) **implies** GetBehaviour(G) = Command::NEUTRAL **and**  
     Wdt(Step(G)) = Wdt(G) **and** Hgt(Step(G)) = Hgt(G) **and**  
     TimeInHole(Step(G)) = TimeInHole(G)+1



## Player

**Service:** Player **includes** Character, use **Coord**

**Observers:** Engine : [Player]  $\rightarrow$  [Engine]  
HasGauntlet : [Player]  $\rightarrow$  boolean  
Gauntlet : [Player]  $\rightarrow$  Item  
ClonePlayer : [Player]  $\rightarrow$  [Player]

**Constructors:** init: Engine  $\times$  Coord  $\rightarrow$  [Character]  
**pre** init(E,c) **requires**  
Environment::CellNature(Envi(E),GetX(c),GetY(c)) = **EMP**  
**and**  $e \neq \emptyset$  **and**  $c \neq \emptyset$  **and**  
 $0 \leq \text{GetX}(c) < \text{Width}(\text{Envi}(C))$  **and**  
 $0 \leq \text{GetY}(c) < \text{Height}(\text{Envi}(C))$

**Operators:** Step : [Player]  $\rightarrow$  [Player]  
HitLeft : [Player]  $\rightarrow$  [Player]  
**pre** HitLeft(P) **requires** HasGauntlet(P)  
HitRight : [Player]  $\rightarrow$  [Player]  
**pre** HitRight(P) **requires** HasGauntlet(P)  
SetGauntlet : [Player]  $\times$  Item  $\rightarrow$  [Player]  
**pre** setGauntlet(g) **requires** Item:Nature(g) = ItemType::Gauntlet **and**  
 $g \neq \emptyset$  **and** (**not** hasGauntlet(P))

### Observations:

[Invariant]

**exists** Character c in Environment::CellContent(Envi(P),Wdt(P),Hgt(P)) **implies**  $c = P$

[Init]

$\text{GetWdt}(\text{Init}(E,c)) = \text{GetX}(c)$  **and**  $\text{GetHgt}(\text{Init}(E,c)) = \text{GetY}(c)$  **and**  $\text{Engine}(P) = E$

[HitLeft]

$\text{HasGauntlet}(\text{HitLeft}(P)) = \text{false}$

[HitRight]

$\text{HasGauntlet}(\text{HitRight}(P)) = \text{false}$

[SetGauntlet]

$\text{HasGauntlet}(\text{SetGauntlet}(P,g)) = \text{true}$   
 $\text{GetGauntlet}(\text{SetGauntlet}(P,g)) = g$

[Step]

clone **defined by** ClonePlayer(P) **in**  
 $\text{Wdt}(\text{Step}(\text{clone})) = \text{Wdt}(\text{Step}(P))$  **and**  $\text{Hgt}(\text{Step}(\text{clone})) = \text{Hgt}(\text{Step}(P))$

Environment::CellNature(Envi(P),Wdt(P),Hgt(P)) **not in** {LAD,HDR} **and**  
Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) **not in** {PLT,MTL,TLP,LAD} **and**  
**not exists** Guard g **in** Environnement::getCellContent(Envi(P),Wdt(P),Hgt(P)-1) **implies**  
Hgt(Step(P)) = Hgt(P)-1

command **defined by** Engine::NextCommand(Engine(P)) **in**  
command = Command::DIGL **and**  
Environment::CellNature(Envi(P),Wdt(P)-1,Hgt(P)-1) **in** {PLT} **implies**  
Environment::CellNature(Envi(Step(clone)),Wdt(P)-1,Hgt(P)-1) = Cell::HOL **and**  
Environment::CellNature(Envi(Step(P)),Wdt(P)-1,Hgt(P)-1) = Cell::HOL

Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) **in** {PLT,MTL,TLP,LAD} **or**  
**exists** Guard g **in** Environnement::getCellContent(Envi(P),Wdt(P),Hgt(P)-1) **and**  
Environment::CellNature(Envi(P),Wdt(P)-1,Hgt(P)) **in** {EMP,LAD,HDR,HOL} **and**  
Environment::CellNature(Envi(P),Wdt(P)-1,Hgt(P)-1) **in** {PLT} **and**  
Environment::CellNature(Envi(P),Wdt(P)-1,Hgt(P)-1) **not in** {HOL} **implies**  
Environment::CellNature(Envi(Step(P)),Wdt(P)-1,Hgt(P)-1) = Cell::HOL

command **defined by** Engine::NextCommand(Engine(P)) **in**  
command = Command::DIGR **and**  
Environment::CellNature(Envi(P),Wdt(P)+1,Hgt(P)-1) **in** {PLT} **implies**  
Environment::CellNature(Envi(Step(clone)),Wdt(P)+1,Hgt(P)-1) = Cell::HOL **and**  
Environment::CellNature(Envi(Step(P)),Wdt(P)+1,Hgt(P)-1) = Cell::HOL

Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) **in** {PLT,MTL,TLP,LAD} **or**  
**exists** Guard g **in** Environnement::getCellContent(Envi(P),Wdt(P),Hgt(P)-1) **and**  
Environment::CellNature(Envi(P),Wdt(P)+1,Hgt(P)) **in** {EMP,LAD,HDR,HOL} **and**  
Environment::CellNature(Envi(P),Wdt(P)+1,Hgt(P)-1) **in** {PLT} **and**  
Environment::CellNature(Envi(P),Wdt(P)+1,Hgt(P)-1) **not in** {HOL} **implies**  
Environment::CellNature(Envi(Step(P)),Wdt(P)+1,Hgt(P)-1) = Cell::HOL

## Engine

**Service:** Engine

**Observers:** Envi : [Engine] → [Environment]  
Player : [Engine] → [Player]  
Guards : [Engine] → **listOf** [Guard]  
Treasures : [Engine] → **listOf** Item  
Status : [Engine] → GameState  
Holes: [Engine] → **listOf** Hole  
Commands: [Engine] → **listOf** Command  
NextCommand: [Engine] → Command  
Teleporteurs: [Engine] → **listOf** Teleporteur  
Gauntlet: [Engine] → Item

**Constructor:** Init: EditableScreen × Coord × **listOf** Coord × **listOf** Item × **listOf** Teleporteur × Item → [Engine]

```
pre init(es,p,guards,treasures,tp,gant) requires
EditableScreen::Playable(es)
and
Coord::X(p) ≠ Item::Col(gant) or Coord::Y(p) ≠ Item::Hgt(gant)
and
forall Coord co in guards
  Coord::X(co) ≠ Coord::X(p) or Coord::Y(co) ≠ Coord::Y(p)
  Coord::X(co) ≠ Item::Col(gant) or Coord::Y(co) ≠ Item::Hgt(gant)
  forall Coord cobis in guards\co
    Coord::X(co) ≠ Coord::X(cobis) or Coord::Y(co) ≠ Coord::Y(cobis)
  forall Item t in treasures
    Coord::X(co) ≠ Item::Col(t) or Coord::GetY(co) ≠ Item::Hgt(t)
and
forall Item t in treasures
  0 ≤ Item::Col(t) < Environment::Width(Envi(E)) and 0 ≤ Item::Hgt(t) <
Environment::Height(Envi(E))
  Item::Col(t) ≠ Coord::X(p) or Item::Hgt(t) ≠ Coord::Y(p)
  Environment::CellNature(Envi(E),Item::Col(t),Item::Hgt(t)) = EMP and
Environment::CellNature(Envi(E),Item::Col(t),Item::Hgt(t)-1) in {MTL,PLT}
  Item::Col(t) ≠ Item::Col(gant) or Item::Hgt(t) ≠ Item::Hgt(gant)
  forall Item tbis in treasures\
    Item::Col(t) ≠ Item::Col(tbis) or Item::Hgt(t) ≠ Item::Hgt(tbis)
and
forall Teleporteur t in tp
  Environment::CellNature(Envi(E),Coord::X(Teleporteur::PosA),Coord::Y(Teleporteur::
PosA)) = PLT
  Environment::CellNature(Envi(E),Coord::X(Teleporteur::PosB),Coord::Y(Teleporteur::
PosB)) = PLT
```

$\text{Coord}::X(\text{Teleporteur}::\text{PosA}) = \text{Coord}::X(p) \text{ implies } \text{Coord}::Y(\text{Teleporteur}::\text{PosA}) \neq \text{Coord}::Y(p)-1$   
 $\text{Coord}::X(\text{Teleporteur}::\text{PosB}) = \text{Coord}::X(p) \text{ implies } \text{Coord}::Y(\text{Teleporteur}::\text{PosB}) \neq \text{Coord}::Y(p)-1$

**Operators:**      Step:  $[\text{Engine}] \rightarrow [\text{Engine}]$   
                      AddCommand:  $[\text{Engine}] \times \text{Command} \rightarrow [\text{Engine}]$

## Observations:

[Invariant]:

$\text{Player}(E) \in \text{Environment}::\text{CellContent}(\text{Envi}(E), \text{Character}::\text{Wdt}(\text{Player}(E)), \text{Character}::\text{Hgt}(\text{Player}(E)))$   
**forall** Guard  $g$  **in**  $\text{Guards}(E)$   
      $g \in \text{Environment}::\text{CellContent}(\text{Envi}(E), \text{Character}::\text{Wdt}(g), \text{Character}::\text{Hgt}(g))$   
**forall** Item  $t$  **in**  $\text{Treasures}(E)$   
      $t \in \text{Environment}::\text{CellContent}(\text{Envi}(E), \text{Item}::\text{Col}(t), \text{Item}::\text{Hgt}(t))$   
**forall** Hole  $h$  **in**  $\text{Holes}(E)$   
      $\text{Environment}::\text{CellNature}(\text{Envi}(E), \text{Hole}::X(h), \text{Hole}::Y(h)) = \mathbf{HOL}$

[Init]:

$\text{Status}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})) = \text{Playing}$   
 $\text{Score}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})) = 0$   
 $\text{Holes}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})) = \mathbf{empty}$   
 $\text{Commands}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})) = \mathbf{empty}$   
 $\text{Player}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})) \in$   
 $\text{Environment}::\text{CellContent}(\text{Envi}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})), \text{Character}::\text{Wdt}(\text{Coord}::X(p), \text{Coord}::Y(p)))$   
**forall** Coord  $gcoord$  **in**  $\text{guards}$   
     **Exists** Guard  $g$  **in**  
 $\text{Environment}::\text{CellContent}(\text{Envi}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})), \text{Character}::\text{Wdt}(\text{Coord}::X(gcoord), \text{Coord}::Y(gcoord)))$   
**forall** Item  $t$  **in**  $\text{treasures}$   
     **Exists** Item  $i$  **in**  
 $\text{Environment}::\text{CellContent}(\text{Envi}(\text{init}(\text{es}, p, \text{guards}, \text{treasures}, \text{tp}, \text{gant})), \text{Item}::\text{Wdt}(\text{Coord}::\text{Col}(t), \text{Coord}::\text{Hgt}(t)))$   
**and**  $i = t$   
**forall** Teleporteur  $t$  **in**  $\text{teleporteurs}$   
      $\text{Environment}::\text{CellNature}(\text{Envi}(E), \text{Coord}::X(\text{Teleporteur}::\text{PosA}), \text{Coord}::Y(\text{Teleporteur}::\text{PosA})) =$   
 $\mathbf{TLP}$  **and**  $\text{Environment}::\text{CellNature}(\text{Envi}(E), \text{Coord}::X(\text{Teleporteur}::\text{PosB}), \text{Coord}::Y(\text{Teleporteur}::\text{PosB})) =$   
 $\mathbf{TLP}$

[Step]:

$\text{NextCommand}(E) = \mathbf{HITR}$  **and**  $\text{Player}::\text{HasGauntlet}(\text{Player}(E))$   
**implies**  
 $(( \text{exists Guard } g \text{ in } \text{Guards}(E) \text{ and } \text{Character}::\text{Wdt}(g) > \text{Character}::\text{Wdt}(\text{Player}(E)) \text{ and } \text{Character}::\text{Hgt}(g) =$   
 $\text{Character}::\text{Hgt}(\text{Player}(E)) \text{ and } ( \text{forall Guard } g_{bis} \text{ in } \text{Guards}(E) \setminus g \text{ Character}::\text{Wdt}(g_{bis}) > \text{Character}::\text{Wdt}(\text{Player}(E))$   
**and**  $\text{Character}::\text{Hgt}(g_{bis}) = \text{Character}::\text{Hgt}(\text{Player}(E)) \text{ and } \text{Character}::\text{Wdt}(g) < \text{Character}::\text{Wdt}(g_{bis}) ) \text{ and } ( \text{forall}$   
 $\text{Integer } i \text{ in } ]\text{Character}::\text{Wdt}(\text{Player}(E)), \text{Character}::\text{Wdt}(g)[$   
 $\text{Environment}::\text{CellNature}(\text{Envi}(E), i, \text{Character}::\text{Hgt}(\text{Player}(E)) \text{ not in } \{\mathbf{PLT}, \mathbf{MLT}, \mathbf{TLP}\} ) \text{ implies } g \notin \text{Guards}(\text{Step}(E))$   
 $)$

NextCommand(E) = **HITL and** Player::HasGauntlet(Player(E))  
**implies**  
 (( **exists** Guard g **in** Guards(E) **and** Character::Wdt(g) < Character::Wdt(Player(E)) **and** Character::Hgt(g) =  
 Character::Hgt(Player(E)) **and** ( **forall** Guard gbis **in** Guards(E)\g Character::Wdt(gbis) < Character::Wdt(Player(E))  
**and** Character::Hgt(gbis) = Character::Hgt(Player(E)) **and** Character::Wdt(g) > Character::Wdt(gbis) ) **and** (**forall**  
 Integer i **in** ]Character::Wdt(g);Character::Wdt(Player())[  
 Environment::CellNature(Envi(E),i,Character::Hgt(Player(E)) **not in** {PLT,MLT,TLP} ) **implies** g  $\notin$  Guards(Step(E))  
 )

**forall** Item t : Treasures(E)  
 (Item::Col(t) = Character::Wdt(Player(Step(E))) **and** Item::Hgt(t) = Character::Hgt(Player(Step(E))))  
**or**  
 ( **exists** Guard g **in** Guards(Step(E))  
 Item::Col(t) = Character::Wdt(g) **and** Item::Hgt(t) = Character::Hgt(g)  
**implies** t  $\notin$  Treasures(Step(E))  
**exists** Guard g **in** Guards((E)) (Character::Wdt(g) = Character::Wdt(Player(E)) **and** Character::Hgt(g) =  
 Character::Hgt(Player(E)) **implies** Status(Step(E)) = Loss  
**forall** Hole h : Holes(E)  
 Hole::T(h) = 14  
**implies** (h  $\notin$  Holes(Step(E))  
**and**  
**exists** Guards g **in** Environment::CellContent(Envi(E),Character::Wdt(g),Character::Hgt(g))  
**implies** g  $\notin$  Guards(Step(E))  
**and**  
**exists** Player p **in**  
 Environment::CellContent(Envi(E),Character::Wdt(Player(E)),Character::Hgt(Player(E))) **implies**  
 Status(Step(E)) = Loss)  
 Hole::T(h) < 14  
**implies** ((h  $\in$  Holes(Step(E))  
**and**  
**exists** Hole hole **in** Holes(Step(E)) h = hole **implies** Hole::T(hole) = Hole::T(h)+1  
 list::size(Commands(Step(E))) = list::size(Commands(E))

[AddCommand]

list::size(Commands(AddCommand(E,c))) = list::size(Commands(E))+1