# Interpretação e Compilação de Linguagens (de Programação) Part 2: Basic Expressions 21/22 Luís Caires (http://ctp.di.fct.unl.pt/~lcaires/)

Mestrado Integrado em Engenharia Informática Departamento de Informática

Faculdade de Ciências e Tecnologia

Universidade Nova de Lisboa

#### Operational Semantics

Interpreters and compilers are language processors that accept syntactically correct programs in a source language and produce denotations (values, effects, or other larger programs).

An interpreter produces a value or effect (executes source program directly)

A compiler produces a program in a (lower level) target language (typically, a machine language). The target program then implements the source program.

How do we define the semantics of a language?

#### Let's look at a simple example (the CALC language)

- We construct a **compositional** definition
  - Interpreter for CALC: implementation using an OO language (Java) the evaluation function is defined "in pieces", one case for each constructor of the AST
  - Compiler for CALC: implementation using an OO language (Java) the compilation function is defined "in pieces", one case for each constructor of the AST, we target the JVM (Java virtual machine)

#### The CALC Language (arithmetic expressions)

The abstract syntax of CALC is given by the following constructors

```
num: Integer → CALCadd: CALC × CALC → CALC
```

mul:  $CALC \times CALC \rightarrow CALC$ 

div:  $CALC \times CALC \rightarrow CALC$ 

sub:  $CALC \times CALC \rightarrow CALC$ 

- Each constructor represents an operator for building a new expression of CALC given already defined expressions.
- The concrete syntax of a language:
  - defines the form how expressions and programs are effectively written in terms off formatting, sequences of (ascii / unicode) characters, etc...
- The abstract syntax of a language:
  - defines the deep structure of expressions and programs in terms of a composition of abstract constructors (like the functions above).

#### Abstract Syntax vs. Concrete Syntax (examples)

#### Numeral literals

- decimal notation: 12
- hexadecimal notation : 0x0C
- abstract syntax: num(12)

#### Identifiers

- C: xpto
- bash: %A
- abstract syntax: id("A")

#### Assignment

- C: x = 2
- OCAML: x := 2
- abstract syntax: assign(id("x"),num(2))

#### Abstract Syntax vs. Concrete Syntax (examples)

#### Algebraic Expressions

```
C: 2*3+2
RPN: 2 3 * 2 +
Lisp: (+ (* 2 3) 2)
abstract syntax: add(mul(num(2),num(3)),num(2))
```

#### Block

- C:{S1 S2 ... Sn }
- Python: \tab SI \tab S2 ... \tab Sn
- abstract syntax: block(\$1,\$2,...,\$n) or seq(\$1, seq(\$2, seq(...))

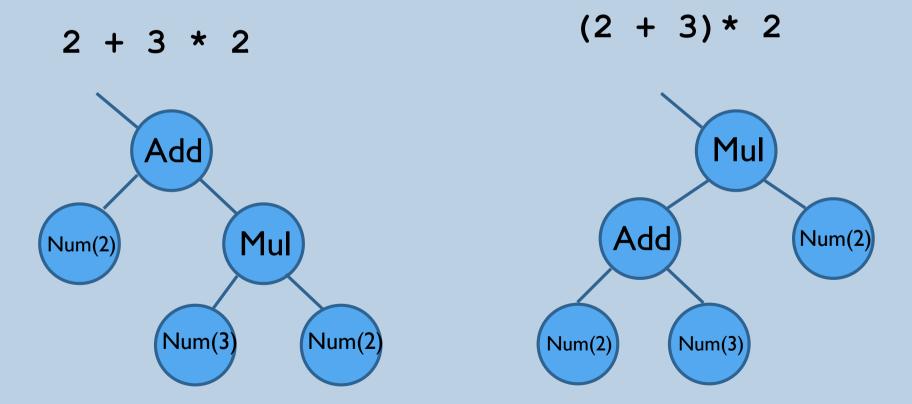
#### while loop:

- C: while (C) S
- Pascal: while C do S
- abstract syntax: while(C,S)

5

#### **Abstract Syntax Tree**

- Represents the structure of expressions and programs in terms of a composition of abstract constructors, depicted as a tree-like structure.
- Abstract Syntax Tree (AST)



#### Semantics of CALC

The semantics of a PL may be defined by giving a computable function I which assigns a definite meaning to each program (fragment)

$$I:CALC \rightarrow DENOT$$

CALC = set of all programs (as syntactical structures)

DENOT = set of all meanings (denotations)

The denotation (value) of a CALC program is an integer value, so we may set

 $I:CALC \rightarrow Integer$ 

CALC = set of all programs (as syntactical structures)

DENOT = Integer = set of all meanings (denotations)

#### CALC Interpreter (evaluation map)

 Algorithm eval(E) that computes the denotation (integer value) of any CALC expression:

#### eval : CALC → Integer

```
if E has the form num(n):
                                   eval(E) = n
if E has the form add(E',E"):
                                   v1 = eval(E'); v2 = eval(E'');
                                   eval(E) \triangleq v1+v2
if E has the form mul(E',E"):
                                  v1 = eval(E'); v2 = eval(E");
                                   eval(E) ≜ v1*v2
if E has the form sub(E',E"):
                                   v1 = eval(E'); v2 = eval(E");
                                   eval(E) ≜ v1-v2
if E has the form div(E',E"):
                                   v1 = eval(E'); v2 = eval(E'');
                                   eval(E) \triangleq v1/v2
```

#### CALC Interpreter (evaluation map)

 Algorithm eval(E) that computes the denotation (integer value) of any CALC expression:

#### eval : CALC → Integer

```
\begin{array}{ll} \text{eval}(\text{num}(\text{n}) \ ) & \triangleq \ \text{n} \\ \\ \text{eval}(\text{add}(\text{E}',\text{E}'') \ ) & \triangleq \ \text{eval}(\text{E}') + \text{eval}(\text{E}'') \\ \\ \text{eval}(\text{mul}(\text{E}',\text{E}'') \ ) & \triangleq \ \text{eval}(\text{E}') * \text{eval}(\text{E}'') \\ \\ \text{eval}(\text{sub}(\text{E}',\text{E}'') \ ) & \triangleq \ \text{eval}(\text{E}') - \text{eval}(\text{E}'') \\ \\ \text{eval}(\text{div}(\text{E}',\text{E}'') \ ) & \triangleq \ \text{eval}(\text{E}') / \text{eval}(\text{E}'') \end{array}
```

#### CALC AST as an (OCAML) inductive data type

```
type calc = Num of int

| Add of calc * calc

| Mul of calc * calc

| Div of calc * calc

| Sub of calc * calc
```

#### CALC eval map as an (OCAML) recursive function

```
let rec eval e =
   match e with
      Num(n) -> n

| Add(e1,e2) -> (eval e1)+(eval e2)

| Mul(e1,e2) -> (eval e1)*(eval e2)

| Sub(e1,e2) -> (eval e1)-(eval e2)

| Div(e1,e2) -> (eval e1)/(eval e2)
```

#### Structural Operational Semantics (Plotkin81)

 Algorithm eval(E) that computes the denotation (integer value) of any CALC expression:

#### eval : CALC → Integer

- The semantic map eval(-) is recursively defined in the structure of the source abstract syntax.
- For each constructor, the semantics of the compound expression only depends on the meaning of each component.

- Compositional Semantics: the meaning of the whole results from the meaning of parts (in particular, it does not depend on the context).
- The same does not depend on "natural" languages
  - time flies like an arrow
  - fruit flies like a banana
- Compositionality is a very important property of a principled formal semantics, it allows us to define the semantics modular and manageable!

- In a OO language, an inductive data type may be represented by an interface type (opaque) and a collection of classes, where each class represents a particular constructor
- The interface declares operations over the inductive data type, for instance::

```
public interface CALC {
    int eval();
}
```

This represents the map eval: CALC → Integer

- Each class represents a particular constructor
- For each operation / map f: T → V defined over the inductive data type T, each class provides the implementation for f on the respective constructor, e.g.;

```
eval(num(n)) ≜ n
```

```
public class ASTNum implements CALC {
    private int value ;
    ASTNum(int v) { value = v; }
    int eval() { return value; }
}
```

- Each class represents a particular constructor
- For each operation / map  $f: T \rightarrow V$  defined over the inductive data type T, each class provides the implementation for f on the respective constructor, e.g.;

```
public class ASTAdd implements CALC {
  CALC lhs, rhs;
  ASTAdd(CALC e1,e2) { lhs=e1, rhs=e2; }
  int eval() {
  return lhs.eval()+rhs.eval(); }
}
```

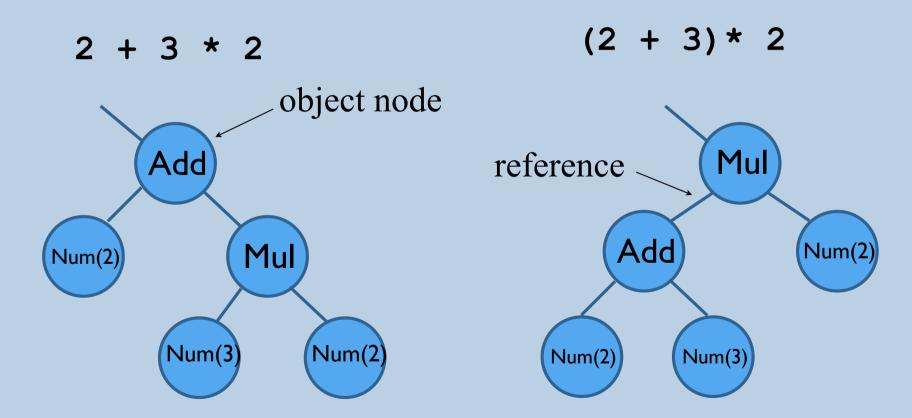
- Each expression of the language is thus represented by an (n-ary) tree of objects (the AST)
- Constructors of the AST are the constructors of the inductive data type,
   and implemented by the AST classes's constructors

```
CALC expr1 = new Add(new Num(2), new Num(3));
int result1 = expr1.eval();

CALC expr2 =
    new Add(new Sub(new Num(2), new Num(3)), new Num(3));
int result2 = expr2.eval();
```

#### **Abstract Syntax Tree**

- Represents the structure of a program expression in terms of the application of the abstract constructors, implemented as a data structure
- Abstract Syntax Tree (AST)



Luís Caires

17

- In our example, classes ASTNum, ASTAdd, ASTSub, ASTMul e ASTDiv, implement the language construtors num, add, sub, mul and div.
- The definition of any function f: CALC→ V becomes dispersed by the several classes of the abstract syntax.
- This makes it easier to add new constructs to the language, we just need to add a new AST class type and the associated implementation of the evaluation maps.

```
public class ASTNeg implements CALC {
  private CALC exp;
  ASTNeg(CALC e) { exp = e;}
  int eval() { return -exp.eval(); }
}
```

#### Compilers

- A compiler produces a program in a (lower level) target language (typically, a machine language).
- The target program then implements the source program.
- The target of the compiler may be code in another language (example javacc compiles grammars into Java, gcc compiles C into LLVM).
- The compiler of a source language S into a target language T preserves the meaning, that is the denotation of the source and target program should be the same. that is,

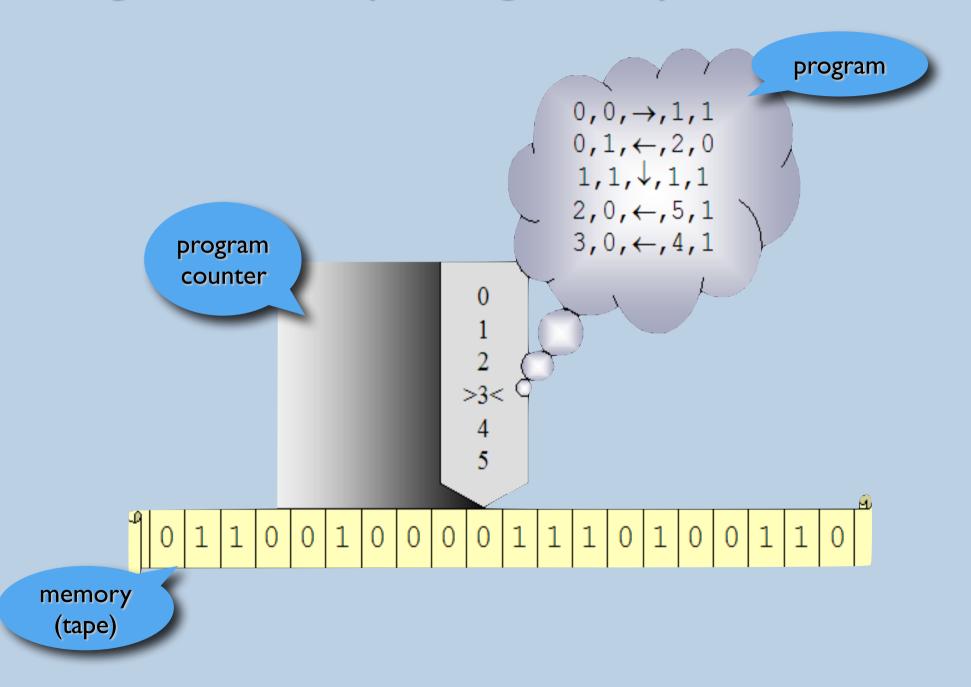
```
evalt(comp(P)) = evals(P)
evalt: T \rightarrow V
evals: S \rightarrow V
```

- Like an interpreter, a compiler may be conveniently defined by recursion on the abstract syntax (AST) of the language
- The target machine of a compiler may be physical (eg., Intel A7) or virtual (eg., JVM, CLR). We will use virtual machines as targets in our course.

#### Virtual Machines (software processors)

- Turing Machine (Turing, 1931)
  - The first one ...
- SECD (Landin, 1962)
  - Stack, Environment, Code, Dump
- P-code machine (Wirth 1972)
  - Stack machine, Pascal p-code compiler
- JVM (Sun, 1995)
  - Type safe, Multi-threaded, focusing on the Java Language
- CLR (Microsoft, 2000)
  - Type safe, Multi-threaded, multi-language (C#, Eiffel, Ada, Python, F#, ... etc)

# Turing Machine (Turing, 1931)



#### SECD - machine (Landin, 1962)

- The first designed to implement the lambda calculus (basis of all functional languages)
- 4 registers holding linked lists
  - S: stack
  - E: Environment
  - C: Code
  - D: Dump



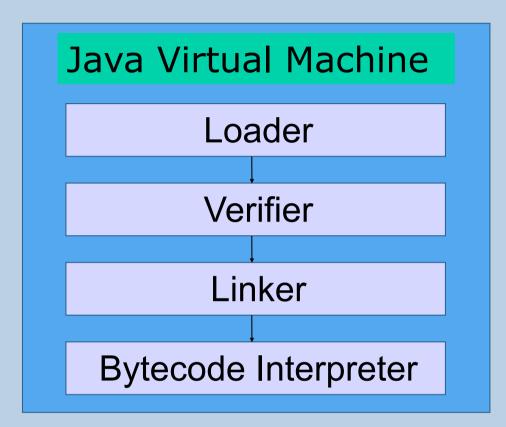
- 9 instructions: nil, ldc, ld, sel, join, ap, ret, dum, rap
- This can implement any computable function (like the Turing machine), but is much higher level

#### P-code machine (Wirth 1972)

- Stack machine devoted to run code for a block structured imperative language (algol like)
- Designed specifically for the Pascal Language, a language very popular in the 70s 80s.
- Pascal was used widely for teaching introductory programming world wide (UCSD Pascal
- The first Apple Mac software (1984)
   was entirely written in Pascal

```
procedure interpret;
   const stacksize = 500:
   var
      p,b,t: integer; {program-, base-, topstack-registers}
      i: instruction; {instruction register}
      s: array [1..stacksize] of integer; {datastore}
   function base(1: integer): integer;
      var b1: integer:
  begin
      b1 := b; {find base 1 levels down}
     while 1 > 0 do
         begin b1 := s[b1]: 1 := 1 - 1
         end:
      base := b1
   end {base};
begin
  writeln(' start pl/0');
  t := 0; b := 1; p := 0;
   s[1] := 0; s[2] := 0; s[3] := 0;
   repeat
      i := code[p]; p := p + 1;
      with i do
      case f of
      lit: begin t := t + 1; s[t] := a end;
      opr: case a of {operator}
           0: begin {return}
                 t := b - 1; p := s[t + 3]; b := s[t + 2];
              end;
           1: s[t] := -s[t];
           2: begin t := t - 1; s[t] := s[t] + s[t + 1] end;
```

# Java Virtual Machine (Sun, 1995)



```
// Bytecode stream: 03 3b 84
// 00 01 1a 05 68 3b a7 ff f9
// Disassembly:
iconst_0 // 03
istore_0 // 3b
iinc 0, 1 // 84 00 01
iload_0 // 1a
iconst_2 // 05
imul // 68
istore_0 // 3b
goto -7 // a7 ff f9
```

method area

heap

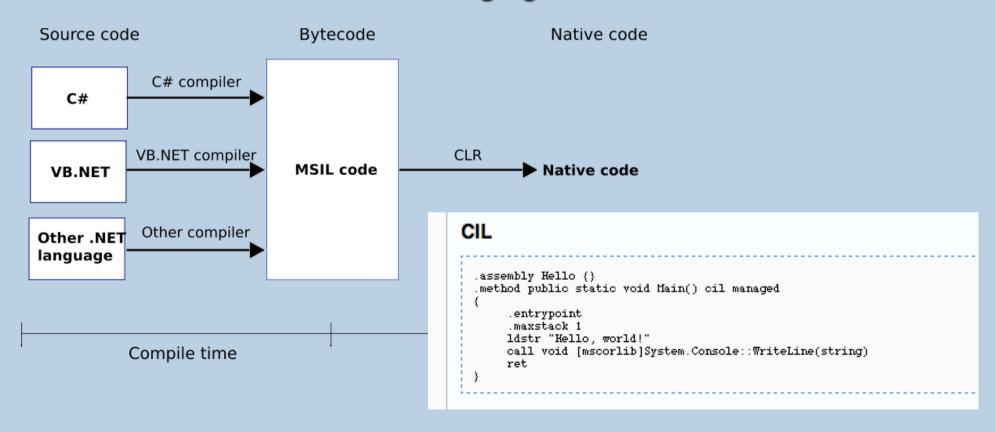
Java stacks PC registers

native method stacks



# Common Language Runtime (Microsoft, 2000)

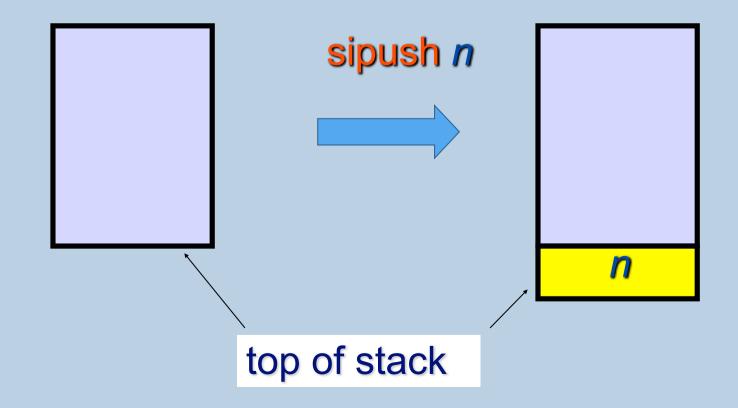
- Stack Machine designed for Microsoft .NET
- Quite independent of the source language, unlike the JVM.
- CIL Common Intermediate Language



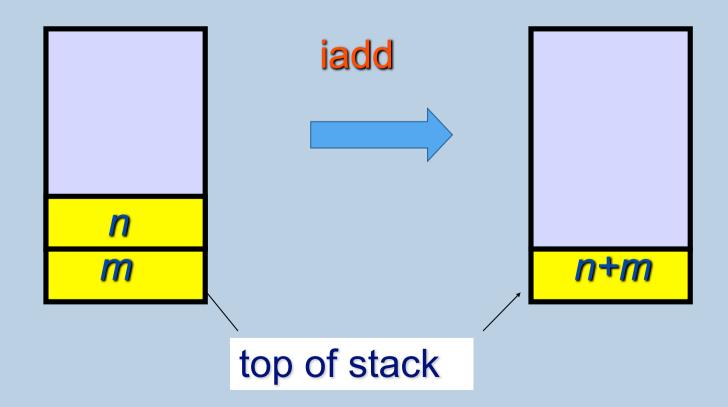
#### Java Virtual Machine

- Stack Machine: all instructions consume their arguments from the top of the stack and leave a result in the top of the stack
- "first" (5) machine instructions of the JVM:
  - sipush n: pushes the integer n on the top of the stack (tos)
  - iadd: Pops two integer values from the tos and pushes their sum
  - imul: likewise for their multiplication
  - idiv: likewise for their division
  - isub: likewise for their subtraction

- first" (5) machine instructions of the JVM:
- sipush n, iadd, imul, idiv, isub.
- (short integer) push (sipush n)



- first" (5) machine instructions of the JVM:
- sipush n, iadd, imul, idiv, isub.
- iadd



- first" (5) machine instructions of the JVM:
- sipush n, iadd, imul, idiv, isub.
- iadd

# bottom of stack unchanged iadd n+m top of stack

- first" (5) machine instructions of the JVM:
- sipush n, iadd, imul, idiv, isub.
- iadd

# bottom of stack unchanged iadd top of stack

ICLP 2009-2010

 algorithm comp(E) that translates CALC expression E into a sequence of JVM instructions

comp : CALC → CodeSeq

```
if E is of the form num( n ):
                                   comp(E) \triangleq < sipush n >
if E is of the form add(E',E"):
                                   s1 = comp(E'); s2 = comp(E'');
                                   comp(E) \triangleq s1 @ s2 @ < iadd >
if E is of the form mul(E',E"):
                                  v1 = comp(E'); v2 = comp(E'');
                                   comp(E) \triangleq s1 @ s2 @ < imul >
if E is of the form sub(E',E"):
                                  v1 = comp(E'); v2 = comp(E'');
                                   comp(E) \triangleq s1 @ s2 @ < isub >
if E is of the form div(E',E''):
                                   v1 = comp(E'); v2 = comp(E'');
                                   comp(E) \triangleq s1 @ s2 @ < idiv >
```

 algorithm comp(E) that translates CALC expression E into a sequence of JVM instructions

comp : CALC → CodeSeq

```
\begin{split} & comp(\textbf{num}(\ n\ )) \triangleq < \textbf{ldc.i4}\ \textbf{n} > \\ & comp(\textbf{add}(E',E'')) \triangleq comp(E') \ @\ comp(E'') \ @\ < \textbf{add} > \\ & comp(\textbf{mul}(E',E'')) \triangleq comp(E') \ @\ comp(E'') \ @\ < \textbf{mul} > \\ & comp(\textbf{sub}(E',E'')) \triangleq comp(E') \ @\ comp(E'') \ @\ < \textbf{sub} > \\ & comp(\textbf{div}(E',E'')) \triangleq comp(E') \ @\ comp(E'') \ @\ < \textbf{div} > \end{split}
```

 algorithm comp(E) that translates CALC expression E into a sequence of JVM instructions

comp : CALC → CodeSeq

```
let rec comp e = match e with
        Num(n) -> ["sipush "^(string_of_int n)]
        | Add(e1,e2) -> (comp e1)@(comp e2)@["iadd"]
        | Mul(e1,e2) -> (comp e1)@(comp e2)@["imul"]
        | Sub(e1,e2) -> (comp e1)@(comp e2)@["isub"]
        | Div(e1,e2) -> (comp e1)@(comp e2)@["idiv"]
```

#### OCAML code

## Compiler correction property

 algorithm comp(E) that translates CALC expression E into a sequence of JVM instructions

comp : CALC → CodeSeq

- Correction invariant for the compiler map:
- execution of comp(E) code starting in a JVM state with stack p always terminates in a JVM state push(v,p), where v = eval(E).

- first" (5) machine instructions of the JVM:
- sipush *n*, iadd, imul, idiv, isub.
- Comp("2+2\*(7-2)") =
- Comp(add(num(2),mul(num(2),sub(num(7),num(2)))))

```
sipush 2
sipush 2
sipush 7
sipush 2
isub
imul
iadd
```

Comp(add(num(2),mul(num(2),sub(num(7),num(2))))) =

# Java Virtual Machine (Sun, 1995)

https://docs.oracle.com/javase/specs/jvms/se9/html/index.html

