

Calculus

Limits

1. $\lim_{x \rightarrow 3} (x^2 - 2x + 3)$

2. $\lim_{x \rightarrow -2} \frac{x^2 - x + 5}{x - 2}$

3. $\lim_{x \rightarrow 1} \frac{x^2 - x + 3}{x + 1}$

4. $\lim_{x \rightarrow 3} \frac{(x^2 + 6x)^{\frac{3}{2}}}{\sqrt{5x + 1}}$

5. $\lim_{x \rightarrow 3} \frac{2\sqrt{x} + x^{\frac{3}{2}}}{\sqrt[4]{x} + 5}$

6. $\lim_{x \rightarrow +\infty} x^2 + 1000x$

7. $\lim_{x \rightarrow +\infty} x^3 - 1000x^2$

8. $\lim_{x \rightarrow -\infty} x^2 - 1000x$

9. $\lim_{x \rightarrow -\infty} x^3 - 1000x^2$

10. $\lim_{x \rightarrow +\infty} \frac{3x + 2}{2x + 1}$

11. $\lim_{x \rightarrow +\infty} \frac{3x^2 + 2}{2x + 1}$

12. $\lim_{x \rightarrow +\infty} \frac{3x + 2}{2x^2 + 1}$

13. $\lim_{x \rightarrow +\infty} \frac{3x^2 + 2}{2x + 1}$

14. $\lim_{x \rightarrow -\infty} \frac{3x^2 + 1}{2x - 1}$

15. $\lim_{x \rightarrow +\infty} \frac{x^2 - 1}{x^2 + 1}$

16. $\lim_{x \rightarrow +\infty} \frac{x^2 + 2x + 2}{x^2 + 3x + 2}$

17. $\lim_{x \rightarrow +\infty} \frac{2x^2 + 5x - 7}{x^3 - 3x^2 + 1}$

18. $\lim_{x \rightarrow -\infty} \frac{2x^2 + 5x - 7}{x^3 - 3x^2 + 1}$

19. $\lim_{x \rightarrow +\infty} \frac{3x^3 - 5x - 10}{x^2 + 6x + 10}$

20. $\lim_{x \rightarrow -\infty} \frac{3x^3 - 5x - 10}{x^2 + 6x + 10}$

21. $\lim_{x \rightarrow +\infty} \sqrt{x^2 - x} - x$

22. $\lim_{x \rightarrow +\infty} \frac{x}{\sqrt{4x^2 + x} - x}$

23. $\lim_{x \rightarrow +\infty} \frac{x}{\sqrt{4x^2 + x} - 2x}$

$$24. \quad \lim_{x \rightarrow +\infty} \frac{x^2}{\sqrt{4x^2 + x} - x}$$

$$25. \quad \lim_{x \rightarrow \infty} \frac{x}{\sqrt{x^2 + 2} + x}$$

$$26. \quad \lim_{x \rightarrow +\infty} \frac{\sqrt{x^4 + 1} - 2x^2 - 1}{x^2}$$

$$27. \quad \lim_{x \rightarrow \infty} \sqrt{x^2 + x + 1} - x$$

$$28. \quad \lim_{n \rightarrow \infty} \sqrt{\frac{4x^2 + 2x + 1}{3x}}$$

$$29. \quad \lim_{n \rightarrow \infty} \frac{\sqrt{4x^2 + x}}{\sqrt{9x^2 - 3x}}$$

$$30. \quad \lim_{x \rightarrow \infty} \frac{\sqrt{9x^2 + x + 3}}{6x}$$

$$31. \quad \lim_{x \rightarrow \pm\infty} \frac{7x^3 + 2x^2}{4x^3 - x}$$

$$32. \quad \lim_{x \rightarrow -\infty} \frac{x^4 + 2x - 3}{x^2 + 100x}$$

$$33. \quad \lim_{x \rightarrow -\infty} \frac{3x + 2}{\sqrt[3]{x^3 - 2}}$$

$$34. \quad \lim_{x \rightarrow \infty} \frac{(x + 1)^3 - (x - 1)^3}{(x + 1)^2 + (x - 1)^2}$$

$$35. \quad \lim_{x \rightarrow \infty} \frac{3x^2 + 2x}{x + 2} - 3x$$

$$36. \quad \lim_{x \rightarrow \infty} \frac{\sqrt{1 + x^2} - \sqrt{1 + x}}{\sqrt{1 + x^3} - \sqrt{1 + x}}$$

$$37. \quad \lim_{x \rightarrow -2} \frac{x^3 + 8}{x + 2}$$

$$38. \quad \lim_{x \rightarrow 1} \frac{x^2 - x}{2x^2 + 5x - 7}$$

$$39. \quad \lim_{x \rightarrow 16} \frac{\sqrt{x} - 4}{x - 16}$$

$$40. \quad \lim_{x \rightarrow \frac{-3}{2}} \frac{2x + 3}{4x^2 + 12x + 9}$$

$$41. \quad \lim_{x \rightarrow 8} \frac{\sqrt{x + 1} - 3}{x - 8}$$

$$42. \quad \lim_{h \rightarrow 1} \frac{h^4 - 1}{h^2 - 1}$$

$$43. \quad \lim_{x \rightarrow -3} \frac{x + 3}{\sqrt{x + 7} - 2}$$

$$44. \quad \lim_{x \rightarrow 5} \frac{\sqrt{x - 1} - 2}{x^2 - 25}$$

$$45. \quad \lim_{x \rightarrow 0} \frac{\sqrt{4 + x^2} - 2}{x^2}$$

$$46. \quad \lim_{x \rightarrow 0} \frac{1}{x} \left\{ \sqrt{1 + \frac{1}{x^2}} - \frac{1}{x} \right\}$$

$$47. \quad \lim_{h \rightarrow 1} \frac{(h - 1)^2}{h^4 - 1}$$

$$48. \quad \lim_{x \rightarrow 3} \left(\frac{x^2}{x-3} - \frac{9}{x-3} \right)$$

$$49. \quad \lim_{x \rightarrow 1} \frac{2x^3 - x^2 - 1}{3x^3 - 3x^2 + 2x - 2}$$

$$50. \quad \lim_{x \rightarrow 1} \frac{x^7 - 1}{x - 1}$$

$$51. \quad \lim_{x \rightarrow -2} \frac{x^5 + 32}{x + 2}$$

$$52. \quad \lim_{x \rightarrow 2} \frac{x^4 - 16}{x - 2}$$

$$53. \quad \lim_{x \rightarrow 2} \frac{x^{-3} - \frac{1}{8}}{x - 2}$$

$$54. \quad \lim_{x \rightarrow 25} \frac{\sqrt{x} - 5}{x - 25}$$

$$55. \quad \lim_{x \rightarrow -27} \frac{\sqrt[3]{x} + 3}{x + 27}$$

$$56. \quad \lim_{x \rightarrow 2} \frac{x^5 - 32}{x^2 - 4}$$

$$57. \quad \lim_{x \rightarrow 3} \frac{x - 3}{x^3 - 27}$$

$$58. \quad \lim_{x \rightarrow -3} \frac{x^4 - 81}{x^3 + 27}$$

$$59. \quad \lim_{x \rightarrow 1} \frac{x^4 - 1}{x^{-2} - 1}$$

$$60. \quad \lim_{x \rightarrow 64} \frac{\sqrt[3]{x} - 4}{\sqrt{x} - 8}$$

$$61. \quad \lim_{x \rightarrow a} \frac{x^{\frac{5}{7}} - a^{\frac{5}{7}}}{x^{\frac{3}{7}} - a^{\frac{3}{7}}}$$

$$62. \quad \lim_{x \rightarrow 0} \frac{\sqrt{1-x} - 1}{x}$$

$$63. \quad \lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{x}$$

$$64. \quad \lim_{x \rightarrow 0} \frac{\sqrt{1+x^3} - \sqrt{1-x^3}}{x^3}$$

$$65. \quad \lim_{x \rightarrow 2} \frac{x^2 - 4}{\sqrt{x+2} - \sqrt{3x-2}}$$

$$66. \quad \lim_{x \rightarrow 0} \frac{\sqrt{x^2 - 1} - \sqrt{x - 1}}{\sqrt{x^3 - 1}}$$

$$67. \quad \lim_{x \rightarrow 2} \frac{\sqrt{x^2 + 5} - 3}{x^2 - 2x}$$

$$68. \quad \lim_{x \rightarrow 0} \frac{\tan 2x}{x}$$

$$69. \quad \lim_{x \rightarrow 0} \frac{\sin 3x}{x}$$

$$70. \quad \lim_{x \rightarrow 0} \frac{\tan 2x}{\sin 5x}$$

$$71. \quad \lim_{x \rightarrow 0} \frac{\sin x^2}{x}$$

72. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\cos x}{\frac{\pi}{2} - x}$
73. $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\sin x - \cos x}{x - \pi/4}$
74. $\lim_{x \rightarrow 0} \frac{\sin 2x - x}{\tan 3x - 2x}$
75. $\lim_{x \rightarrow 0} \frac{\cos 2x - 1}{\sin^2 3x}$
76. $\lim_{x \rightarrow \pi} \frac{\sin x}{x^3 - \pi^3}$
77. $\lim_{x \rightarrow 0} \frac{1 - \cos 3x}{x^2}$
78. $\lim_{x \rightarrow 0} \frac{\sin 2x + 3x}{2x + \sin 3x}$
79. $\lim_{x \rightarrow 0} \frac{\tan x - \sin x}{x(1 - \cos 2x)}$
80. $\lim_{x \rightarrow 0} \frac{x - \sin x}{x^2}$
81. $\lim_{x \rightarrow 0} \frac{1 - \cos 3x}{\tan^2 4x - x^2}$
82. $\lim_{x \rightarrow 0} \frac{\tan x - \sin x}{\sin^3 x}$
83. $\lim_{x \rightarrow 0} \frac{1 - \cos 3x}{\cos 4x}$
84. $\lim_{x \rightarrow 0} \frac{\tan x - \sin x}{x^3}$
85. $\lim_{x \rightarrow 0} \frac{(\sin x + 2)^2 - 4}{x}$
86. $\lim_{x \rightarrow 0} \left(\frac{1}{\sin x} - \frac{1}{\tan x} \right)$
87. $\lim_{x \rightarrow 0} \frac{\sin x - \sin a}{\sqrt{x} - \sqrt{a}}$
88. $\lim_{x \rightarrow 0} \frac{x \tan x}{1 - \cos x}$
89. $\lim_{x \rightarrow 0} \frac{\csc x - \cot x}{x}$
90. $\lim_{x \rightarrow \frac{\pi}{2}} (\sec x - \tan x)$
91. $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\sec^2 x - 2}{\tan x - 1}$
92. $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\sin x - \cos x}{x - \frac{\pi}{4}}$
93. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{1 + \cos 2x}{(\pi - 2x)^2}$
94. $\lim_{x \rightarrow \pi} \frac{1 + \cos x}{\tan^2 x}$
95. $\lim_{x \rightarrow 1} (1 - x) \tan \frac{\pi x}{2}$
96. $\lim_{x \rightarrow 0} \frac{\sqrt{9 + \sin x} - 3}{\sqrt{3 + x} - \sqrt{3}}$
97. $\lim_{x \rightarrow 0} \frac{\sqrt{16 + x^2} - 4}{1 - \cos x}$

$$98. \lim_{x \rightarrow 0} \frac{\sqrt{\cos^2 x + \sin x} - \cos x}{\sqrt{4+x} - 2}$$

$$99. \lim_{x \rightarrow \frac{\pi}{3}} \frac{\tan^3 x - 3 \tan x}{\cos\left(x + \frac{\pi}{6}\right)}$$

$$100. \lim_{x \rightarrow 0} \frac{\sqrt{5+x^2} - \sqrt{5}}{\sqrt{20 + \sin^2 x} - \sqrt{20}}$$

$$101. \lim_{x \rightarrow \frac{\pi}{2}} \frac{\sqrt{1 + \cos 2x}}{\sqrt{\pi} - \sqrt{2x}}$$

$$102. \lim_{x \rightarrow 0} \frac{1 - \cos^2(2 \sin x)}{1 - \cos 2x}$$