

Key Takeaways

Properties of Inverse of a matrix

If matrix A is invertible, then

- $(kA)^{-1} = \frac{1}{k}A^{-1}$, Where k is a scalar

Proof: $(kA)(kA)^{-1} = I$

$$AA^{-1} = I$$

$$\Rightarrow A \cdot (kA)^{-1} = \frac{1}{k} \cdot I \quad (\because |A| \neq 0) \quad \text{Premultiply by } A^{-1}$$

$$\Rightarrow A^{-1} \cdot A \cdot (kA)^{-1} = \frac{1}{k} \cdot (A^{-1} \cdot I)$$

$$(kA)^{-1} = \frac{1}{k}A^{-1}$$