

Key Takeaways

Characteristic polynomial and characteristic equation:

Let A be a square matrix.

The polynomial $|A - \lambda I|$ is called characteristic polynomial of A and equation $|A - \lambda I| = 0$ is called characteristic equation of A .

(here λ is called eigen value of A)

$$A = \begin{bmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{bmatrix} \Rightarrow A - \lambda I = \begin{bmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{bmatrix} - \lambda \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$|A - \lambda I| = \begin{vmatrix} a_1 - \lambda & b_1 & c_1 \\ a_2 & b_2 - \lambda & c_2 \\ a_3 & b_3 & c_3 - \lambda \end{vmatrix} = 0 \quad \text{will be the characteristic equation.}$$