

If
$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -2 & 4 \end{bmatrix}$$
 & $I = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ and $A^{-1} = \frac{1}{6}(A^2 + cA + dI)$, then the ordered pair (c, d) is:



Solution:

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -2 & 4 \end{bmatrix}$$

$$A^3 - 6A^2 + 11A - 6I = 0$$

$$A^{-1}A^3 - 6A^{-1}A^2 + 11A^{-1}A - 6A^{-1}I = 0$$

+

$$6A^{-1} = A^2 - 6A + 11I$$

$$\Rightarrow A^{-1} = \frac{1}{6}(A^2 - 6A + 11I)$$

$$(c,d) \equiv (-6,11)$$



$$(-6, -11)$$



$$(6, -11)$$



$$(-6,11)$$

