

Let  $S$  be the set of all  $\lambda \in \mathbb{R}$  for which the system of linear equations  $2x - y + 2z = 2$ ;  $x - 2y + \lambda z = -4$ ;  $x + \lambda y + z = 4$ , has no solution. Then the set  $S$

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A

Contains more than two elements

B

Contains exactly two elements

C

Is a singleton

D

Is an empty set

Solution:  $S$  be the set of all  $\lambda \in \mathbb{R}$

$$\left. \begin{array}{l} 2x - y + 2z = 2 \\ x - 2y + \lambda z = -4 \\ x + \lambda y + z = 4 \end{array} \right\} \text{No solution}$$

$$\Delta = \begin{vmatrix} 2 & -1 & 2 \\ 1 & -2 & \lambda \\ 1 & \lambda & 1 \end{vmatrix} = 0$$

$$C_1 \rightarrow C_1 - C_3$$

$$\Delta = \begin{vmatrix} 0 & -1 & 2 \\ 1 - \lambda & -2 & \lambda \\ 0 & \lambda & 1 \end{vmatrix} = 0$$

$$\Rightarrow (\lambda - 1)(-1 - 2\lambda) = 0$$

$$\Rightarrow \lambda = 1, -\frac{1}{2}$$