

If the matrix
$$A = \begin{bmatrix} 0 & a & -3 \\ 2 & 0 & -1 \\ b & 1 & 0 \end{bmatrix}$$
 is skew-symmetric, then



Solution:

Given:
$$A = \begin{bmatrix} 0 & a & -3 \\ 2 & 0 & -1 \\ b & 1 & 0 \end{bmatrix}$$
 is skew-symmetric

$$A^{T} = \begin{bmatrix} 0 & 2 & b \\ a & 0 & 1 \\ -3 & -1 & 0 \end{bmatrix}$$

We know that A is skew symmetric if $A = -A^T$

$$\begin{bmatrix} 0 & a & -3 \\ 2 & 0 & -1 \\ b & 1 & 0 \end{bmatrix} = - \begin{bmatrix} 0 & 2 & b \\ a & 0 & 1 \\ -3 & -1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & -2 & -b \\ -a & 0 & -1 \\ 3 & 1 & 0 \end{bmatrix}$$

+

$$a = -2$$

$$\Rightarrow -3 = -b$$

$$\therefore b = 3$$

$$a = -2$$



$$a = 2$$



$$b = 3$$



$$b = -3$$