

If $y(x) = \begin{vmatrix} \sin x & \cos x & \sin x + \cos x + 1 \\ 23 & 17 & 13 \\ 1 & 1 & 1 \end{vmatrix}$, $x \in \mathbb{R}$, then $\frac{d^2y}{dx^2} + y$ is equal to :

Solution:

$$y(x) = \begin{vmatrix} \sin x & \cos x & \sin x + \cos x + 1 \\ 23 & 17 & 13 \\ 1 & 1 & 1 \end{vmatrix}, \text{ differentiate w.r.t } x$$

$$y'(x) = \begin{vmatrix} \cos x & -\sin x & -\sin x + \cos x \\ 23 & 17 & 13 \\ 1 & 1 & 1 \end{vmatrix}$$

$$y'(x) = \begin{vmatrix} \cos x & -\sin x & -\sin x + \cos x \\ 23 & 17 & 13 \\ 1 & 1 & 1 \end{vmatrix}, \text{ differentiate w.r.t } x$$

$$y''(x) = \begin{vmatrix} -\sin x & -\cos x & -\cos x - \sin x \\ 23 & 17 & 13 \\ 1 & 1 & 1 \end{vmatrix}$$

$$y(x) + y''(x) = \begin{vmatrix} 0 & 0 & 1 \\ 23 & 17 & 13 \\ 1 & 1 & 1 \end{vmatrix} = 6$$

A

6

B

4

C

-10

D

0