

System of linear equations (Cramer's rule):

Two variables:

Consider system of equations

$$a_1x + b_1y = c_1$$

$$a_2x + b_2y = c_2$$

$$\Delta = \begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix} = a_1b_2 - a_2b_1$$

$$\Delta_1(\Delta_x) = \begin{vmatrix} c_1 & b_1 \\ c_2 & b_2 \end{vmatrix} = c_1 b_2 - c_2 b_1$$

$$\Delta_2(\Delta_y) = \begin{vmatrix} a_1 & c_1 \\ a_2 & c_2 \end{vmatrix} = a_1c_2 - a_2c_1$$

Solution:
$$x = \frac{\Delta_x}{\Delta}$$
; $y = \frac{\Delta_y}{\Delta}$