$$\Delta(r) = \begin{vmatrix} 1 & x & n+1 \\ r & y & \frac{n(n+1)}{2} \\ 2r-1 & z & n^2-1 \end{vmatrix} \text{, then } \sum_{r=0}^n \Delta(r) \text{ is equal to:}$$

## Solution:

$$\sum_{r=0}^{n} \Delta(r) = \begin{vmatrix} \sum_{r=0}^{n} 1 & x & n+1 \\ \sum_{r=0}^{n} (r) & y & \frac{n(n+1)}{2} \\ \sum_{r=0}^{n} (2r-1) & z & n^2-1 \end{vmatrix}$$

$$= \begin{vmatrix} n+1 & x & n+1 \\ \frac{n(n+1)}{2} & y & \frac{n(n+1)}{2} \\ n^2 - 1 & z & n^2 - 1 \end{vmatrix}$$

$$= 0$$



$$\frac{n^2(n+1)}{2}$$



 $n^3$ 



$$\frac{n(2n+1)(3n+1)}{2}$$



0