

Inverse of a matrix (Reciprocal matrix)

• If A, B are square matrices of order n and $|A| \neq 0$,

 $AB = I_n = BA$, then B is multiplicative inverse of A i.e. $B = A^{-1}$

$$\Rightarrow AA^{-1} = I = A^{-1}A$$

To find inverse of a matrix:

We know, $A adj(A) = |A|I_n = adj A \cdot A$

$$\Rightarrow A \cdot \left(\frac{adj A}{|A|}\right) = I_n = \left(\frac{adj A}{|A|}\right) \cdot A$$

$$\Rightarrow A \cdot A^{-1} = I_n = A^{-1} \cdot A \Rightarrow A^{-1} = \frac{adj(A)}{|A|}$$

Note: For a matrix to be invertible, it must be non – singular.