



Key Takeaways



Multiplication of Matrix:

- $A_{m \times p} \cdot B_{p \times n} = C_{m \times n} = [c_{ij}]_{m \times n}$, where $c_{ij} = \sum_{k=1}^p a_{mk} b_{kn}$

Example: $A = \begin{bmatrix} 2 & 0 & -1 \\ 3 & -4 & 6 \end{bmatrix}, B = \begin{bmatrix} 1 & -3 \\ 0 & 5 \\ -7 & -2 \end{bmatrix}$

$$C = AB = \begin{bmatrix} 2 & 0 & -1 \\ 3 & -4 & 6 \end{bmatrix}_{2 \times 3} \begin{bmatrix} 1 & -3 \\ 0 & 5 \\ -7 & -2 \end{bmatrix}_{3 \times 2} \quad c_{ij} = \text{Dot product of } i^{\text{th}} \text{ row vector of } A \text{ with } j^{\text{th}} \text{ column vector of } B$$

$$= \begin{bmatrix} 2 \cdot 1 + 0 + (-1) \cdot (-7) & 2(-3) + 0 + (-1) \cdot (-2) \\ 3 \cdot 1 + 0 + 6(-7) & 3(-3) - 4 \cdot 5 + 6(-2) \end{bmatrix}_{2 \times 2}$$

$$= \begin{bmatrix} 9 & -4 \\ -39 & -41 \end{bmatrix}_{2 \times 2}$$