



Solution: $P^3 = \begin{bmatrix} 1 & 0 & 0 \\ 8 & 1 & 0 \\ 48 & 8 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 4 & 1 & 0 \\ 16 & 4 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 12 & 1 & 0 \\ 96 & 12 & 1 \end{bmatrix}$

Similarly,

$$P^n = \begin{bmatrix} 1 & 0 & 0 \\ 4n & 1 & 0 \\ 16 \frac{n(n+1)}{2} & 4n & 1 \end{bmatrix}$$

$$\therefore P^{50} = \begin{bmatrix} 1 & 0 & 0 \\ 200 & 1 & 0 \\ 8 \cdot 50 \cdot 51 & 200 & 1 \end{bmatrix}$$

$$P^{50} - I = \begin{bmatrix} 0 & 0 & 0 \\ 200 & 0 & 0 \\ 8 \cdot 50 \cdot 51 & 200 & 0 \end{bmatrix}$$

$$\Rightarrow Q = \begin{bmatrix} 0 & 0 & 0 \\ 200 & 0 & 0 \\ 8 \cdot 50 \cdot 51 & 200 & 0 \end{bmatrix} \therefore \frac{q_{31} + q_{32}}{q_{21}} = \frac{400 \cdot 51 + 200}{200} = 103$$

A

52

B

103

C

201

D

205