

If P is a 3×3 matrix such that $P^T = 2P + I$, where P^T is transpose of P and I is the



3 x 3 identity matrix, then there exists a column matrix $X = \begin{bmatrix} x \\ y \\ z \end{bmatrix} \neq \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$ such that

Solution: $P^T = 2P + I$

$$P = 2P^T + I$$

$$= 4P + 3I$$

$$\Rightarrow P = -I$$

$$PX = -X$$



$$PX = X$$



$$PX = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$



$$PX = -X$$



$$PX = 2X$$