



If  $A$  is  $3 \times 3$  non singular matrix such that  $AA^T = A^T A$  and  $B = A^{-1}A^T$ , then  $BB^T$  equals:

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Solution:

$$\begin{aligned} BB^T &= A^{-1}A^T(A^{-1}A^T)^T \\ &= A^{-1}A^T A(A^{-1})^T \\ &= A^{-1}AA^T(A^{-1})^T \\ &= IA^T(A^{-1})^T \\ &= I \end{aligned}$$

$$\begin{aligned} A^{-1}A &= I = AA^{-1} \\ (A^{-1})^T &= (A^T)^{-1} \end{aligned}$$

A

$$B^{-1}$$

B

$$(B^{-1})^T$$

+

C

$$I + B$$

D

$$I$$

+