

## Consider the lines given by



$$L_1$$
:  $x + 3y - 5 = 0$ 

$$L_2$$
:  $3x - ky - 1 = 0$ 

$$L_3$$
:  $5x + 2y - 12 = 0$ 

## Solution:

(A)  $L_1, L_2, L_3$  are concurrent, if

$$\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix} = 0$$

$$L_1: x + 3y - 5 = 0$$

$$L_2$$
:  $3x - ky - 1 = 0$ 

$$L_3$$
:  $5x + 2y - 12 = 0$ 

$$\begin{vmatrix} 1 & 3 & -5 \\ 3 & -k & -1 \\ 5 & 2 & -12 \end{vmatrix} = 0$$

$$\Rightarrow (12k+2) - 3(-36+5) - 5(6+5k) = 0$$

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COLUMN I	COLUMN II
(A) $L_1, L_2, L_3$ are concurrent, if	$(p) \ k = -9$
One of $L_1, L_2, L_3$ is parallel to at least (B) one of the other two, if	$(q) k = -\frac{6}{5}$
(C) $L_1, L_2, L_3$ form a triangle, if	$(r) k = \frac{5}{6}$
(D) $L_1, L_2, L_3$ do not form a triangle, if	(s) $k = 5$