

LINEAR REGRESSION USING GRADIENT DESCENT

Multiple features



SINGLE FEATURE

Data table

size in feet ²	price in ₹1000's
2104	400
1416	232
1534	315
852	178
...	...
3210	870

MULTIPLE FEATURES

$x_j = j^{\text{th}}$ feature

$n = \text{number of features}$

$\vec{x}^{(i)} = \text{feature of } i^{\text{th}} \text{ training example}$

$x_j^{(i)} = \text{Value of } j^{\text{th}} \text{ feature in } i^{\text{th}} \text{ training example.}$

Size in feet ² x_1	Number of bedrooms x_2	Number of floors x_3	Age of home in years x_4	Price (₹) in ₹ 1000's y
2104	5	1	45	460
1416	3	2	40	232
1534	3	2	30	315
852	2	1	36	178
...

Model

$$f_{w,b}(x) = wx + b \rightarrow f_{\vec{w},b}(\vec{x}) = \vec{w} \cdot \vec{x} + b$$

$$f_{w,b}(x) = w_1 x_1 + w_2 x_2 + w_3 x_3 + w_4 x_4 + b$$

$$f_{\vec{w},b}(\vec{x}) = w_1 x_1 + w_2 x_2 + \dots + w_n x_n + b$$

$$\text{Parameters } \begin{cases} \vec{w} = [w_1 \ w_2 \ w_3 \ \dots \ w_n] \\ b = \text{single number} \end{cases}$$

$$\vec{x} = [x_1 \ x_2 \ x_3 \ \dots \ x_n]$$

SIGNIFICANCE OF VECTORIZATION (PROGRAMMING PYTHON & NUMPY)

Declaration

```
w = np.array([2.0, 6.5, -3.2])
```

```
b = 3
```

```
x = np.array([15, 35, 24])
```

Without Vectorization

```
f = 0
```

```
for j in range (n) :
```

```
    f = f +w[j] * x[j]
```

```
f = f + b
```

Without Vectorization

```
f = w[0] * x[0] +
```

```
    w[1] * x[1] +
```

```
    w[2] * x[2] + b
```

Vectorization

```
f = np.dot(w,x) + b
```

SIGNIFICANCE OF VECTORIZATION (PROGRAMMING PYTHON & NUMPY)

Without vectorization

```
for j in range(0,16):  
    f = f + w[j] * x[j]
```

t_0
 $f + w[0] * x[0]$

t_1
 $f + w[1] * x[1]$

...

t_{15}
 $f + w[15] * x[15]$

Vectorization

```
np.dot(w,x)
```

