



FEATURE SCALING

FEATURE AND PARAMETER VALUES

$b = 0$ { simplicity }

$$w_1 x_1 + w_2 x_2 + b$$

$$x_1 = 2 ; \quad x_2 = 35000 ; \quad y = 50 \quad \checkmark$$

$$w_1 = 100 , \quad w_2 = 100$$

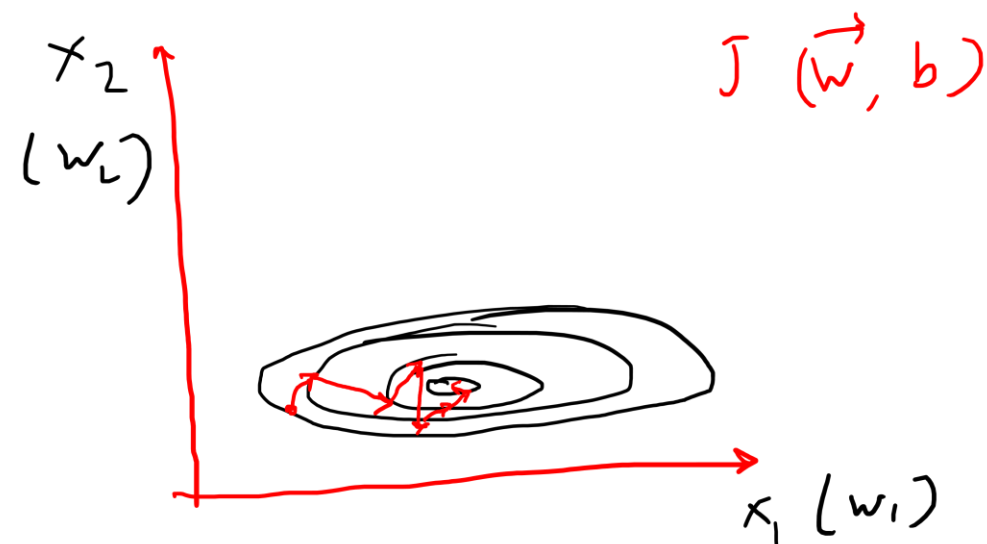
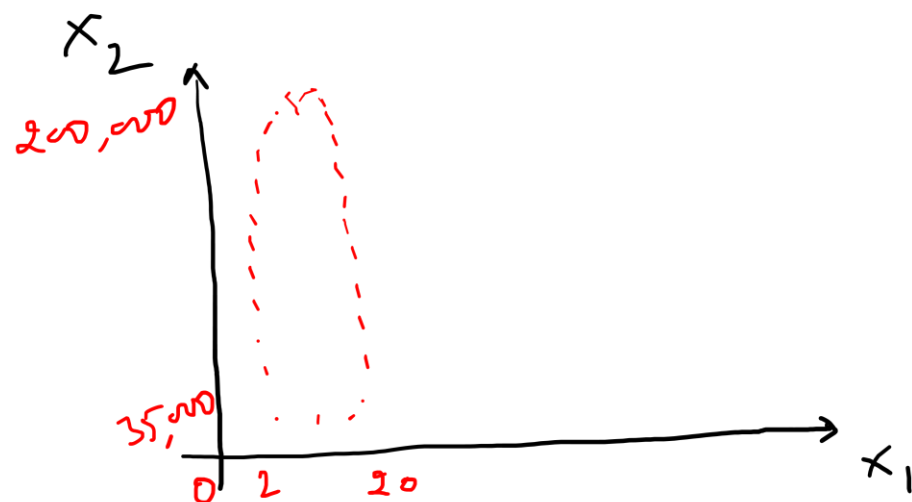
$$\hat{y} = 3500200 \quad \checkmark$$

$$v_1 = 10 , \quad v_2 = 0.001$$

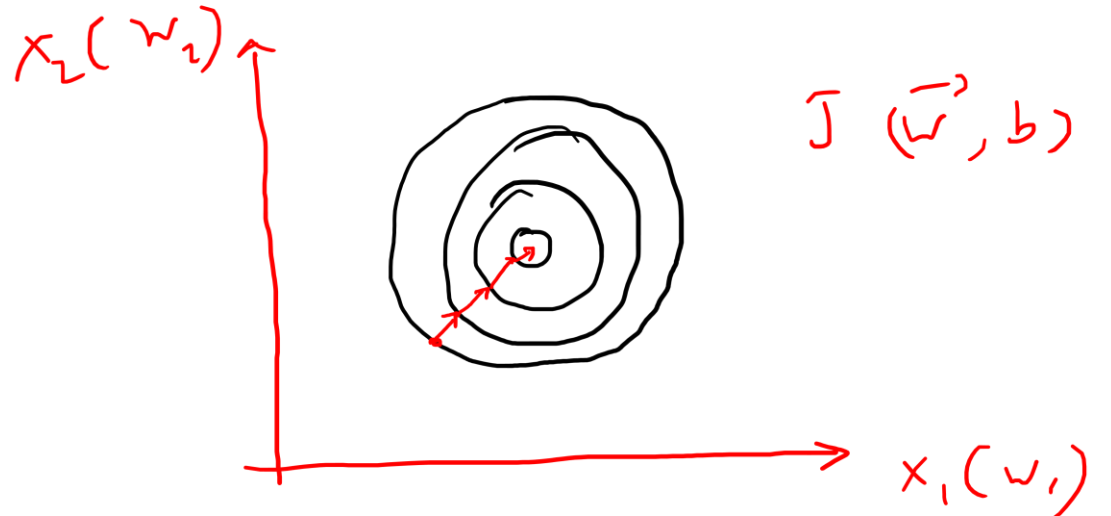
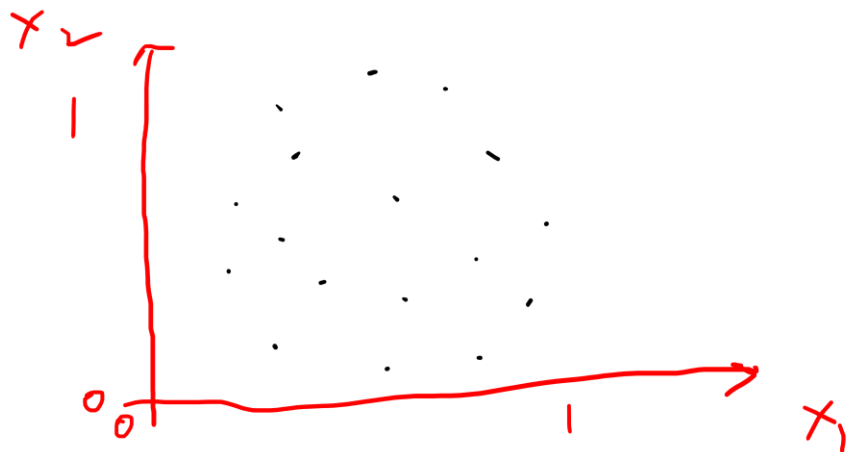
$$\hat{\hat{y}} = 55 \quad \checkmark$$

FEATURE SIZE AND PARAMETER SIZE

| | Size of feature (x_i) | Size of parameter (w_i) |
|----------------|------------------------------|--------------------------------|
| x_1 (Exp) | Small | Large |
| x_2 (Salary) | Large | Small |



FEATURE SIZE AND GRADIENT DESCENT





FEATURE SCALING

- Feature range is either very large or very small



FEATURE SCALING

- Division by Max number in the feature
- Mean Normalization
- Z-Score Normalization



DATASET

Performance Score (Target Variable): Represents an employee's expected performance on a **scale of 0 to 100**, based on past data.

| Experience (Years) | Salary (\$) | Performance Score (Target) |
|--------------------|-------------|----------------------------|
| 2 | 35,000 | 50 |
| 5 | 50,000 | 55 |
| 7 | 80,000 | 70 |
| 3 | 45,000 | 52 |
| 10 | 120,000 | 85 |
| 15 | 200,000 | 95 |
| 20 | 150,000 | 92 |
| 12 | 90,000 | 80 |
| 6 | 60,000 | 65 |
| 18 | 170,000 | 90 |

DIVISION BY MAX NUMBER IN THE FEATURE (MIN-MAX SCALING)

$$35,000 \leq X_2 \leq 2,00,000$$

$$2 \leq X_1 \leq 20$$

$$X_2 = 45,000$$

$$X_{2,s} = \frac{45,000}{2,00,000} = 0.225$$

$$X_1 = 3$$

$$X_{1,s} = \frac{3}{20} = 0.15$$

$$0.175 \leq X_{2,s} \leq 1$$

$$0.1 \leq X_{1,s} \leq 1$$

MEAN NORMALIZATION

$$\mu_1 = 9.8$$

$$x_1 = 3$$

$$x_{1,s} = \frac{x_1 - \mu_1}{\text{Max} - \text{Min}}$$

$$x_{1,s} = -0.37$$

$$-0.43 \leq x_{1,s} \leq 0.56$$

$$\mu_2 = 1,00,000$$

$$x_2 = 45,000$$

$$x_{2,s} = \frac{x_2 - \mu_2}{\text{Max} - \text{Min}}$$

$$x_{2,s} = -0.33$$

$$-0.39 \leq x_{2,s} \leq 0.60$$

Z-SCORE NORMALIZATION

$$\sigma_1 = ? \text{ std. Deviation } (x_1)$$

$$\sigma_2 = ? \text{ std. Deviation } (x_2)$$

$$\mu_1 = \text{Avg}(x_1)$$

$$\mu_2 = \text{Avg}(x_2)$$

$$x_{1,s} = \frac{x_1 - \mu_1}{\sigma_1} \quad ; \quad x_{2,s} = \frac{x_2 - \mu_2}{\sigma_2}$$