$$\sin^2 \alpha + \cos^2 \alpha = 1 \tag{1.1}$$

$$1 + \tan^2 \alpha = \sec^2 \alpha \tag{1.2}$$

$$1 + \cot^2 \alpha = \csc^2 \alpha \tag{1.3}$$

$$\arctan x + \arctan \frac{1}{x} = \begin{cases} \frac{\pi}{2}, & x > 0\\ -\frac{\pi}{2}, & x < 0 \end{cases}$$
 (1.4)

$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta \tag{1.5}$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta \tag{1.6}$$

$$\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta} \tag{1.7}$$

$$\sin 2\alpha = 2\sin \alpha \cos \alpha \tag{1.8}$$

$$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha = 2\cos^2 \alpha - 1 = 1 - 2\sin^2 \alpha \tag{1.9}$$

$$\sin\frac{\alpha}{2} = \sqrt{\frac{1 - \cos\alpha}{2}}\tag{1.10}$$

$$\cos\frac{\alpha}{2} = \sqrt{\frac{1 + \cos\alpha}{2}} \tag{1.11}$$

$$\tan\frac{\alpha}{2} = \sqrt{\frac{1 - \cos\alpha}{1 + \cos\alpha}} = \frac{\sin\alpha}{1 + \cos\alpha} = \frac{1 - \cos\alpha}{\sin\alpha}$$
 (1.12)

$$\sin \alpha = \frac{2\tan\frac{\alpha}{2}}{1 + \tan^2\frac{\alpha}{2}} \tag{1.13}$$

$$\cos \alpha = \frac{1 - \tan^2 \frac{\alpha}{2}}{1 + \tan^2 \frac{\alpha}{2}} \tag{1.14}$$

$$(C)' = 0 (2.1)$$

$$(x^{\mu})^{'} = \mu x^{\mu - 1} \tag{2.2}$$

$$\left(a^{x}\right)' = a^{x} \ln a \tag{2.3}$$

$$\left(e^{x}\right)' = e^{x} \tag{2.4}$$

$$\left(\log_a x\right)' = \frac{1}{x \ln a} \tag{2.5}$$

$$\left(\ln x\right)' = \frac{1}{x} \tag{2.6}$$

$$\left(\sin x\right)' = \cos x \tag{2.7}$$

$$(\cos x)' = -\sin x \tag{2.8}$$

$$(\tan x)' = \frac{1}{\cos^2 x} = \sec^2 x$$
 (2.9)

$$(\cot x)' = -\frac{1}{\sin^2 x} = -\csc^2 x$$
 (2.10)

$$(\sec x)' = \sec x \tan x \tag{2.11}$$

$$\left(\csc x\right)' = -\csc x \cot x \tag{2.12}$$

$$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$
 (2.13)

$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$$
 (2.14)

$$(\arctan x)' = \frac{1}{1+x^2}$$
 (2.15)

$$(\operatorname{arccot} x)' = -\frac{1}{1+x^2}$$
 (2.16)

$$\sin x = x - \frac{x^3}{6} + o(x^5) \tag{3.1}$$

$$\arcsin x = x + \frac{x^3}{6} + o(x^5) \tag{3.2}$$

$$\tan x = x + \frac{x^3}{3} + o(x^5) \tag{3.3}$$

$$\arctan x = x - \frac{x^3}{3} + o(x^5) \tag{3.4}$$

$$e^x = 1 + x + \frac{x^2}{2!} + \dots + \frac{x^n}{n!} + o(x^n)$$
 (4.1)

$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots + (-1)^m \frac{x^{2m+1}}{(2m+1)!} + o(x^{2m+1})$$
(4.2)

$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots + (-1)^m \frac{x^{2m}}{(2m)!} + o(x^{2m})$$
(4.3)

$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots + (-1)^{n-1} \frac{x^n}{n} + o(x^n)$$
(4.4)

$$\frac{1}{1+x} = 1 - x + x^2 + \dots + (-1)^n x^n + o(x^n)$$
(4.5)

$$\frac{1}{1-x} = 1 + x + x^2 + \dots + x^n + o(x^n)$$
 (4.6)

$$(1+x)^{\mu} = 1 + \mu x + \frac{\mu(\mu-1)}{2!}x^2 + \dots + \frac{\mu(\mu-1)\cdots(\mu-n+1)}{n!}x^n + o(x^n)$$
 (4.7)

$$k = \left| \frac{y''}{(1 + y'^2)^{\frac{3}{2}}} \right| \tag{5.1}$$

$$k = \frac{1}{R} \tag{5.2}$$

$$\begin{cases} \xi = x - \frac{y'(1+y'^2)}{y''} \\ \eta = y + \frac{(1+y'^2)}{y''} \end{cases}$$
(5.3)

$$\int 0 \, \mathrm{d}x = C \tag{6.1}$$

$$\int 1 \, \mathrm{d}x = x + C \tag{6.2}$$

$$\int x^{\mu} \, \mathrm{d}x = \frac{1}{\mu + 1} x^{\mu + 1} + C \tag{6.3}$$

$$\int \frac{1}{x} \, \mathrm{d}x = \ln|x| + C \tag{6.4}$$

$$\int a^x \, \mathrm{d}x = \frac{a^x}{\ln a} + C \tag{6.5}$$

$$\int e^x \, \mathrm{d}x = e^x + C \tag{6.6}$$

$$\int \sin x \, \mathrm{d}x = -\cos x + C \tag{6.7}$$

$$\int \cos x \, \mathrm{d}x = \sin x + C \tag{6.8}$$

$$\int \sec^2 x \, \mathrm{d}x = \int \frac{1}{\cos^2 x} \, \mathrm{d}x = \tan x + C \tag{6.9}$$

$$\int \csc^2 x \, \mathrm{d}x = \int \frac{1}{\sin^2 x} \, \mathrm{d}x = -\cot x + C \tag{6.10}$$

$$\int \sec x \tan x \, \mathrm{d}x = \sec x + C \tag{6.11}$$

$$\int \csc x \cot x \, \mathrm{d}x = -\csc x + C \tag{6.12}$$

$$\int \frac{\mathrm{d}x}{\sqrt{1-x^2}} = \arcsin x + C \tag{6.13}$$

$$\int \frac{dx}{1+x^2} = \arctan x + C \tag{6.14}$$

$$\int \tan x \, \mathrm{d}x = -\ln|\cos x| + C \tag{7.1}$$

$$\int \cot x \, \mathrm{d}x = \ln|\sin x| + C \tag{7.2}$$

$$\int \sec x \, \mathrm{d}x = \ln|\sec x + \tan x| + C \tag{7.3}$$

$$\int \csc x \, \mathrm{d}x = \ln|\csc x - \tan x| + C \tag{7.4}$$

$$\int \frac{\mathrm{d}x}{x^2 + a^2} = \frac{1}{a} \arctan \frac{x}{a} + C \tag{7.5}$$

$$\int \frac{\mathrm{d}x}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x - a}{x + a} \right| + C \tag{7.6}$$

$$\int \frac{\mathrm{d}x}{\sqrt{a^2 - x^2}} = \arcsin\frac{x}{a} + C \tag{7.7}$$

$$\int \frac{\mathrm{d}x}{\sqrt{x^2 \pm a^2}} = \ln\left|x + \sqrt{x^2 \pm a^2}\right| + C \tag{7.8}$$

$$\int \sqrt{a^2 - x^2} \, \mathrm{d}x = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \arcsin \frac{x}{a} + C \tag{7.9}$$

$$\int \sqrt{x^2 \pm a^2} \, \mathrm{d}x = \frac{x}{2} \sqrt{x^2 \pm a^2} \pm \frac{a^2}{2} \ln \left| x + \sqrt{x^2 \pm a^2} \right| + C \tag{7.10}$$

$$\int_0^{\frac{\pi}{2}} f(\sin x) \, \mathrm{d}x = \int_0^{\frac{\pi}{2}} f(\cos x) \, \mathrm{d}x \tag{8.1}$$

$$\int_0^{\pi} x f(\sin x) \, dx = \frac{\pi}{2} \int_0^{\pi} f(\sin x) \, dx = \pi \int_0^{\frac{\pi}{2}} f(\sin x) \, dx$$
 (8.2)

$$\int_0^{\frac{\pi}{2}} \sin^n x \, \mathrm{d}x = \int_0^{\frac{\pi}{2}} \cos^n x \, \mathrm{d}x = \begin{cases} \frac{(n-1)(n-3)\cdots 2}{n(n-2)\cdots 3}, & n$$
为奇数
$$\frac{(n-1)(n-3)\cdots 1}{n(n-2)\cdots 2} \cdot \frac{\pi}{2}, & n$$
为偶数 (8.3)

$$S = \int_{a}^{b} y(x) \, \mathrm{d}x \tag{9.1}$$

$$S = \int_{t_1}^{t_2} y(t)x'(t) dt$$
 (9.2)

$$S = \frac{1}{2} \int_{\alpha}^{\beta} r^2(\theta) \, \mathrm{d}\theta \tag{9.3}$$

$$V = \int_{a}^{b} S(x) \, \mathrm{d}x \tag{9.4}$$

$$V_x$$
 (9.5)

若 $f^{(i)}(x_0) = 0, i = 1, 2, \cdots, n-1$,而 $f^{(n)}(x_0) \neq 0$,则: 当 n 为奇数时, x_0 是拐点,但不是极值点; 当 n 为偶数时, x_0 是极值点,但不是拐点。