question5

June 29, 2021

```
[]: import cv2
import numpy as np

from scipy.ndimage.filters import convolve

from tqdm import trange
```

0.1 Computing Energy

The energy is computed by $e_i(I) = \left| \frac{\partial I}{\partial x} \right| + \left| \frac{\partial I}{\partial y} \right|$.

Using Sobel Filters,

$$p'_u = \begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix} \circledast I \text{ and } p'_v = \begin{bmatrix} +1 & 0 & -1 \\ +2 & 0 & -2 \\ +1 & 0 & -1 \end{bmatrix} \circledast I, \text{ we compute the derivative as } e_i(I) = |p'_u| + |p'_v|.$$

Source

0.2 Finding the Seam with least Energy

To compute the seam with the least energy, we dynamically compute $M(i,j) = e(i,j) + \min(M(i-1,j-1), M(i-1,j), M(i-1,j+1))$ where M(i,j) stores the minimum energy value stored upto the pixel (i,j).

The minimum energy thus will be stored in the last row of M and backtrack stores the list of pixels present in this s

Inspired from

0.3 Deleting the Minimum Seam

We recursively remove the seam with minimum energy till we reach the image of required size.

```
[]: class Seam():
    def __init__(self, path):
        self.image = cv2.imread(path)
        self.name = path.split('.')[0]

def findEnergy(self, image):
```

```
filter_du = np.array([ [1.0, 2.0, 1.0], [0.0, 0.0, 0.0], [-1.0, -2.0,_{\sqcup}
-1.0],])
       filter_dv = np.array([[1.0, 0.0, -1.0], [2.0, 0.0, -2.0], [1.0, 0.0,  
\rightarrow -1.0],])
       filter_du = np.stack([filter_du] * 3, axis=2)
       filter_dv = np.stack([filter_dv] * 3, axis=2)
       convolved = np.absolute(convolve(image, filter_du)) + np.
⇒absolute(convolve(image, filter_dv))
       energy = convolved.sum(axis=2)
       return energy
   def minimum_seam(self, image):
       row, column, _ = image.shape
       energy = self.findEnergy(image)
       M = energy.copy()
       backtrack = np.zeros_like(M, dtype=np.int)
       for i in range(1, row):
           for j in range(0, column):
               if j == 0:
                   idx = np.argmin(M[i-1, j:j+2])
                   backtrack[i, j] = idx + j
                   min_energy = M[i-1, idx+j]
               else:
                   idx = np.argmin(M[i-1, j-1:j+2])
                   backtrack[i, j] = idx + j-1
                   min_energy = M[i-1, idx+j-1]
               M[i, j] += min_energy
       return M, backtrack
   def carve(self, image):
       row, column, _ = image.shape
       M, backtrack = self.minimum_seam(image)
       mask = np.ones((row, column), dtype=np.bool)
       j = np.argmin(M[-1])
```

```
for i in reversed(range(row)):
                 mask[i, j] = False
                 j = backtrack[i, j]
             mask = np.stack([mask] * 3, axis=2)
             image = image[mask].reshape((row, column-1, 3))
             return image
         def crop(self, image, scale):
             row, column, _ = image.shape
             new = int(scale * column)
             for i in trange(column - new):
                 image = self.carve(image)
             return image
         def crop_column(self, scale_column):
             image = self.image
             image = self.crop(image, scale_column)
             fname = self.name + "_scaled_column_by_" + str(scale_column) + ".png"
             cv2.imwrite(fname, image)
             return image
         def crop_row(self, scale_row):
             image = self.image
             image = np.rot90(image, 1, (0, 1))
             image = self.crop(image, scale_row)
             image = np.rot90(image, 3, (0, 1))
             fname = self.name + "_scaled_row_by_" + str(scale_row) + ".png"
             cv2.imwrite(fname, image)
             return image
[]: img1 = Seam("Image-1.jpg")
     out1 = img1.crop_column(0.5)
[]: img2 = Seam("Image-2.jpg")
     out2 = img2.crop_column(0.5)
[]:
```