## Asymptotics II & Search Trees

Exam Prep 7: March 4, 2019

## 1 More, MORE, MOREEEE (Spring 2016, MT2)

For all the methods below, give the runtime in  $\Theta(\cdot)$  notation as a function of N. Your answer should be simple, with no unnecessary leading constants or summations.

```
public static void p1(int N) {
        for (int i = 0; i < N; i += 1) {
            for (int j = 1; j < N; j = j + 2) {
                System.out.println("hi !");
        }
   P1 answer: \Theta(
   public static void p2(int N) {
        for (int i = 0; i < N; i += 1) {
2
            for (int j = 1; j < N; j = j * 2) {
                System.out.println("hi !");
        }
   }
   P2 answer: \Theta(
   public static void p3(int N) {
       if (N <= 1) return;</pre>
       p3(N / 2);
        p3(N / 2);
   }
   P3 answer: \Theta(
```

## 2 A Wild Hilfinger Appears! (Fall 2017, Final)

a. Given the following function definitions, what is the worst-case runtime for p(N)? Assume h is a boolean function requiring constant time.

int p(int M) { return r(0, M); } int r(int i, int M) { if (i >= M) return 0; if (s(i) > 0) return i; return r(i + 1, M);} 9 10 int s(int k) { 11 **if** (k <= 0) **return** 0; 12 if (h(k)) return k; 13 return s(k - 1); 14 } 15

Answer:  $\Theta$ (

b. What is the worse-case runtime for the call p(N)? Assume that calls to h require constant time.

```
void p(int M) {
   int L, U;
   for (L = U = 0; U < M; L += 1, U += 2) {
      for (int i = L; i < U; i+= 1) {
            h(i);
      }
   }
}</pre>
```

Answer:  $\Theta$ (

## 3 Tree Time (Spring 2018, Midterm 2)

a. Draw the 2-3 tree that results from inserting 1, 2, 3, 7, 8, 9, 5 in that order.

b. Draw a valid BST of minimum height containing the keys 1, 2, 3, 7, 8, 9, 5.