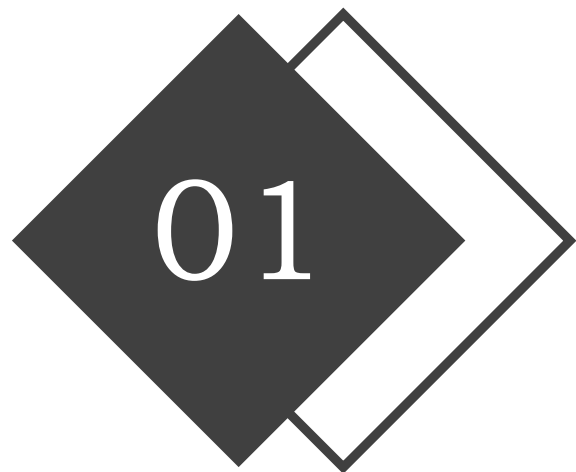


# 无信息搜索

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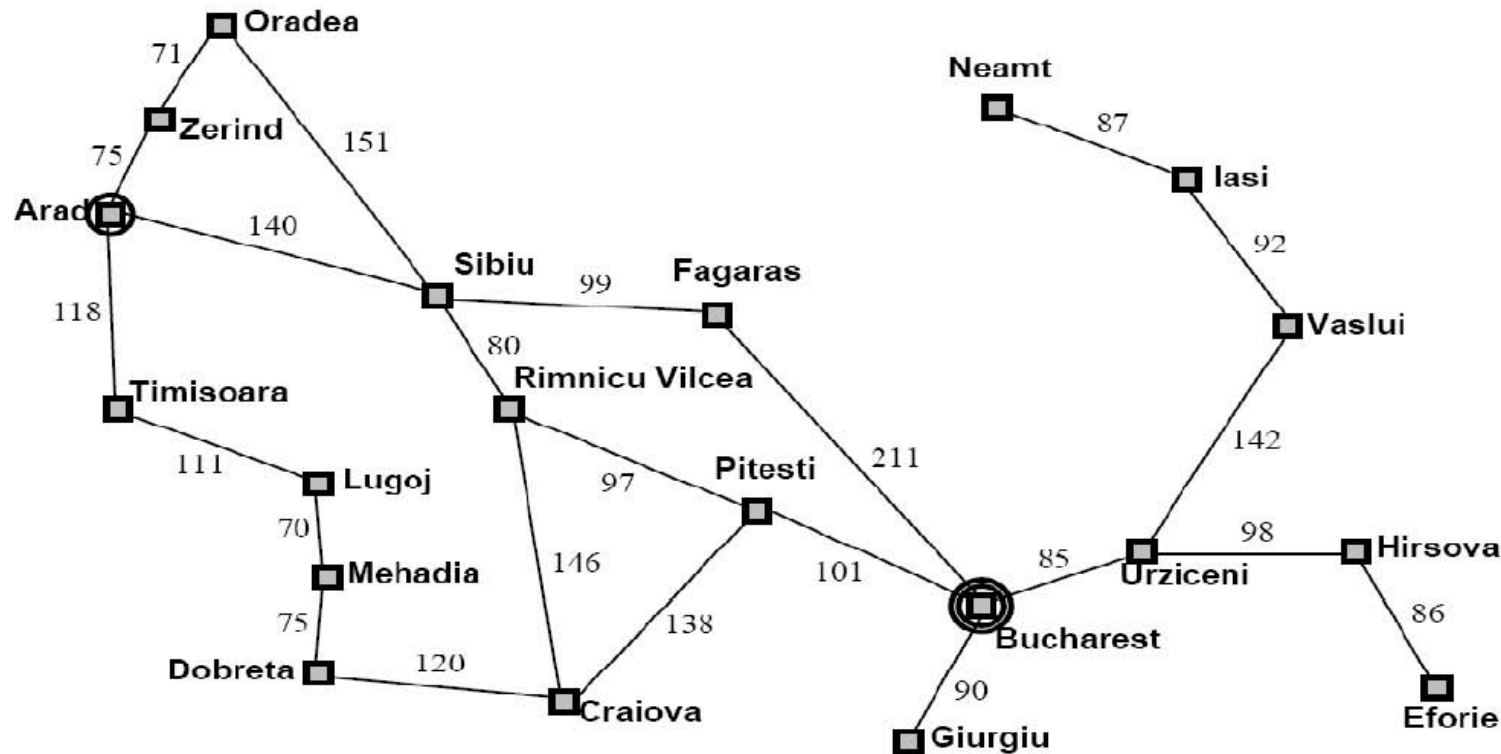


## 搜索问题定义

# 搜索问题定义

## 举例

Currently in Arad, need to get to Bucharest

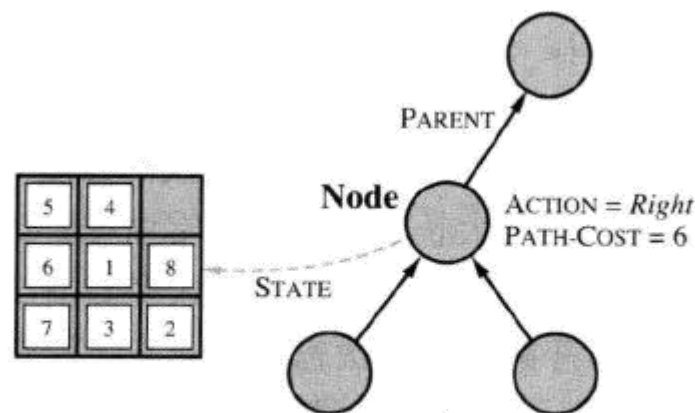


- **States:** the various cities you could be located in.
- **Actions:** drive between neighboring cities.
- **Initial state:** in Arad
- **Goal:** in Bucharest
- **Solution:** the route, the sequence of cities to travel through to get to Bucharest.

## 搜索的数据结构

对树中每个结点 $n$ ，一般定义如下数据结构

- $n.STATE$ : 对应状态空间中的状态;
- $n.PARENT$ : 搜索树中产生该结点的结点 (即父结点);
- $n.ACTION$ : 父结点生成该结点时所采取的行动;
- $n.PATH-COST$ : 代价, 一般用  $g(n)$  表示, 指从初始状态到达该结点的路径消耗;

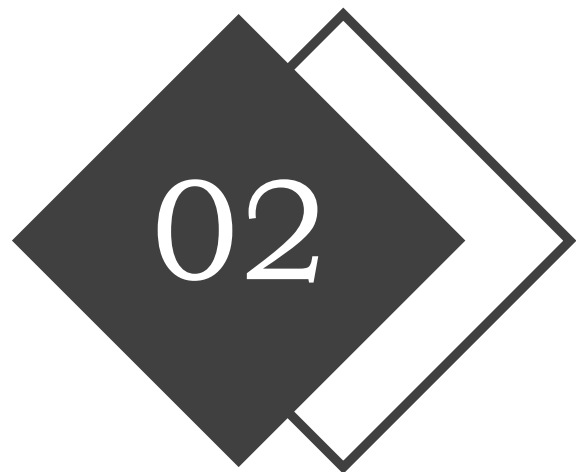


结点数据结构, 由搜索树构造。每个结点都有一个父结点、一个状态和其他域。箭头由子结点指向父结点

## 求解算法的性能

四个方面：

- 完备性：当问题有解时，这个算法能否保证找到解。
- 最优性：搜索策略能否找到最优解。
- 时间复杂度：找到解所需要的时间，也叫搜索代价
- 空间复杂度：执行搜索过程中需要多少内存空间

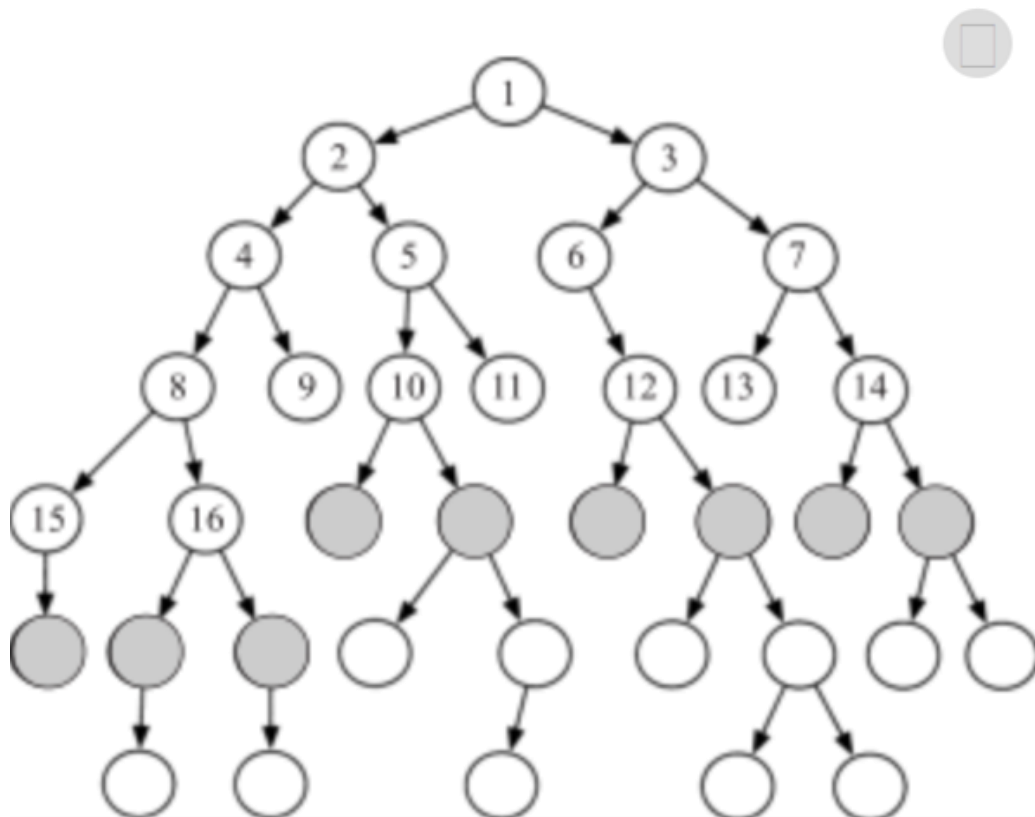


## 无信息搜索策略

- 宽度优先搜索
- 一致代价搜索
- 深度优先搜索
- 深度受限搜索
- 迭代加深搜索
- 双向搜索



## 宽度优先搜索(BFS)



- 完备性;
- 非最优;
- 时间复杂度 $O(b^d)$ ;
- 空间复杂度 $O(b^d)$ ;

- 节点扩展顺序与目标节点的位置无关;
- 用一个先进先出 (FIFO) 队列实现;

## 一致代价搜索Uniform-cost search (UCS)

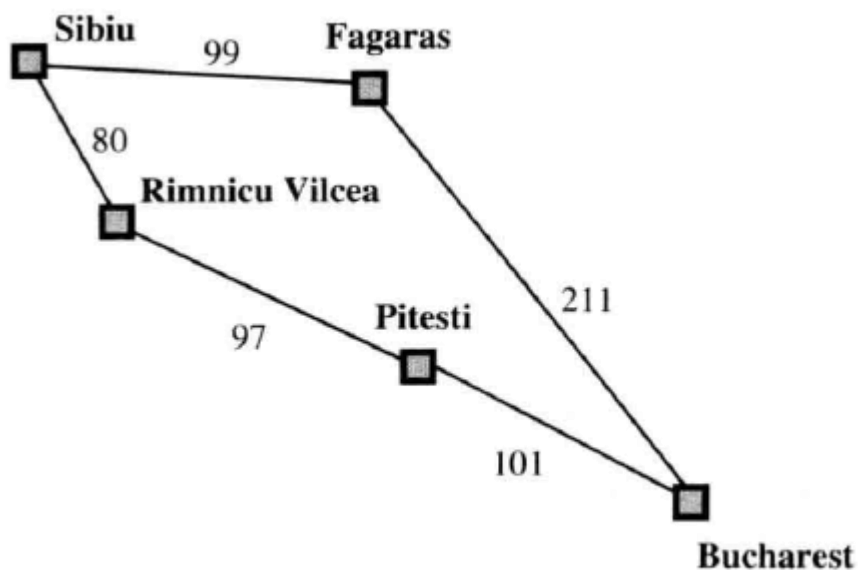


图 3.15 罗马尼亚问题的部分状态空间，  
用于描述一致代价搜索

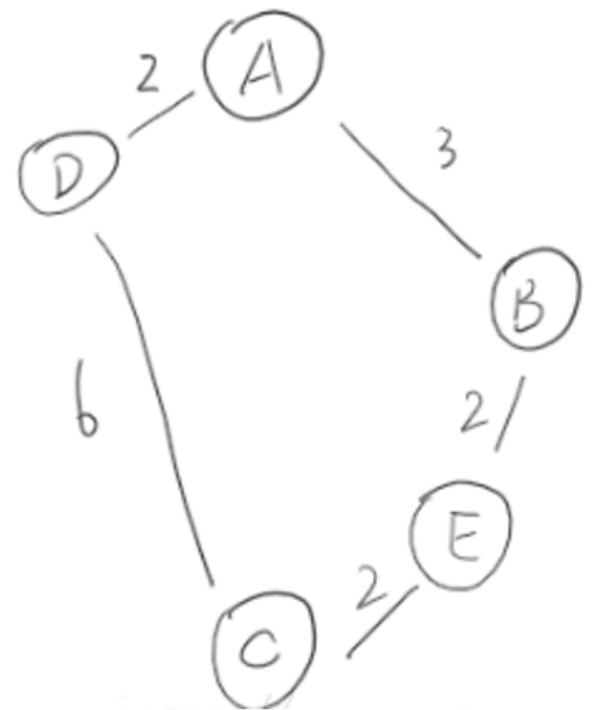
Search Strategy : 扩展最低代价的未扩展节点。

Implementation : 队列，按路径代价排序，最低优先。

Complexity:  $O(b^{1+[C^*/e]})$ ;

# 无信息搜索策略

```
function UNIFORM-COST-SEARCH(problem) returns a solution, or failure
  node  $\leftarrow$  a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  frontier  $\leftarrow$  a priority queue ordered by PATH-COST, with node as the only element
  explored  $\leftarrow$  an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node  $\leftarrow$  POP(frontier) /* chooses the lowest-cost node in frontier */
    if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child  $\leftarrow$  CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        frontier  $\leftarrow$  INSERT(child, frontier)
      else if child.STATE is in frontier with higher PATH-COST then
        replace that frontier node with child
```



# 深度优先搜索 (DFS)

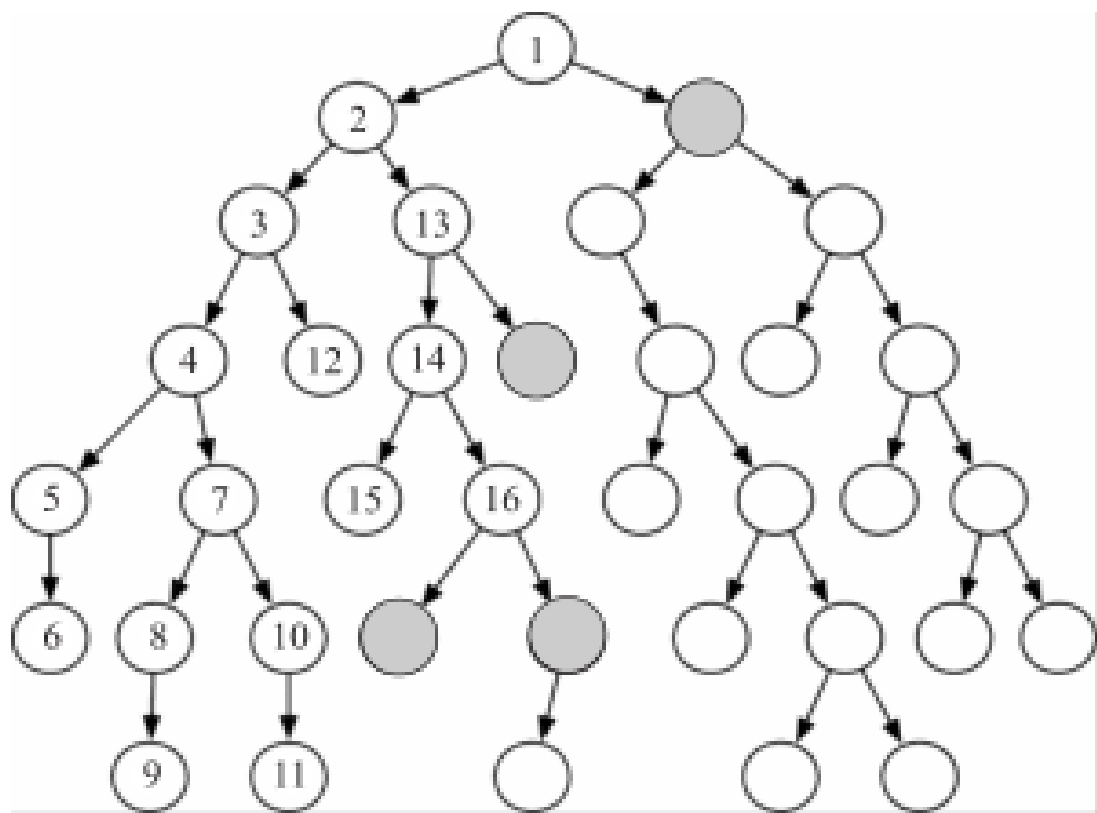


图 3-5 深度优先搜索中节点的扩展顺序

## 深度受限搜索 (Depth-limited Search )

```
1 function Depth-Limited-Search(problem, limit) returns a solution, or failure/cutoff
2   if problem.Goal-Test(node.State) then return Solution(node)
3   if limit = 0 then return cutoff      //no solution
4   cutoff_occurred? ← false
5   for each action in problem.Action(node.State) do
6     child ← Child-Node(problem, node, action)
7     result ← Recursive-DLS(child, problem, limit - 1)
8     if result = cutoff then cutoff_occurred? ← true
9     else if result ≠ failure then return result
10  if cutoff_occurred? then return cutoff    //no solution
11  else return failure
```

## 迭代加深搜索 (Iterative Deepening Search )

```
1 function Iterative-Deepening-Search(problem, limit) returns a solution, or failure
2   for depth = 0 to  $\infty$  do
3     result  $\leftarrow$  Depth-Limited-Search(problem, depth)
4     if result  $\neq$  cutoff then return result
```

## 双向搜索 (Bidirectional search)

它同时进行两个搜索：一个是从初始状态向前搜索，二另一个则从目标向后搜索。当两者在中间相遇时停止。

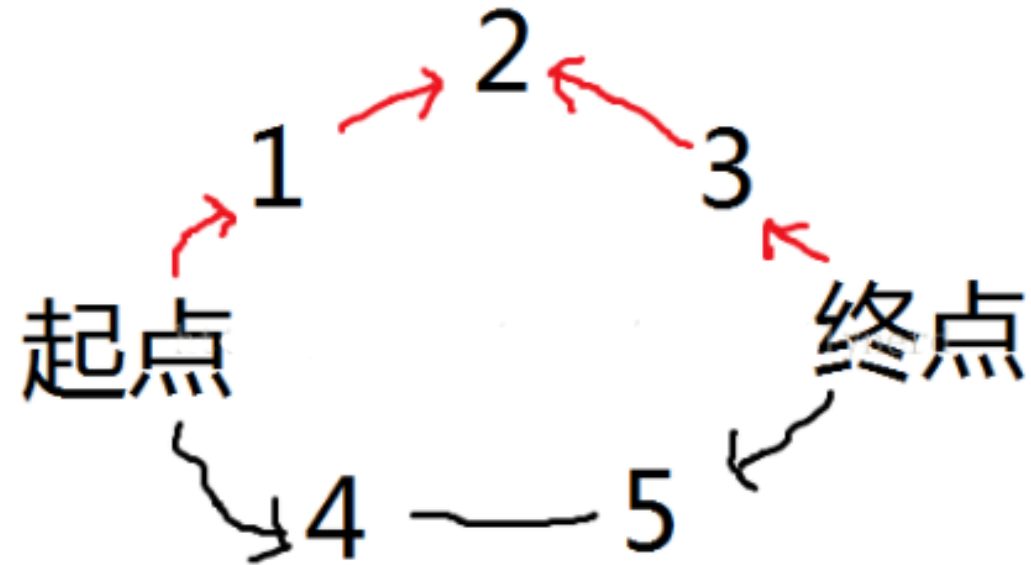
forward tree



backward tree



## 双向搜索 (Bidirectional search)





无信息树搜索策略评价

Evaluation of Uninformed Tree-search Strategies

无信息树搜索策略评价

Criterion	Breadth First	Uniform Cost	Depth First	Depth Limited	Iterative Deepening	Bidirectional
Complete	Yes <sup>a</sup>	Yes <sup>a,b</sup>	No	No	Yes <sup>a</sup>	Yes <sup>a,d</sup>
Time	$O(b^d)$	$O(b^{1+\lfloor C^*/\epsilon \rfloor})$	$O(b^m)$	$O(b^\ell)$	$O(b^d)$	$O(b^{d/2})$
Space	$O(b^d)$	$O(b^{1+\lfloor C^*/\epsilon \rfloor})$	$O(bm)$	$O(b\ell)$	$O(bd)$	$O(b^{d/2})$
Optimal	Yes <sup>c</sup>	Yes	No	No	Yes <sup>c</sup>	Yes <sup>c,d</sup>

- Where
- $b$  -- maximum branching factor of the tree

■  $d$  -- depth of the shallowest solution

■  $m$  -- maximum depth of the tree

■  $l$  -- the depth limit

■  $a$  -- complete if  $b$  is finite

■  $b$  -- complete if step costs  $\epsilon$  for positive

■  $c$  -- optimal if step costs are all identical

■  $d$  -- if both directions use breadth-first search
- <http://blog.csdn.net/c11556913>