

#### 4. Test Cases

It is important to test edge cases to confirm all functions are working as expected.

##### Open Addressing:

- Capacity Test: Insert a new key into the full table
- Collision Test: Insert a key that the result of primary hashing gives collision (secondary hash function should be called and find the appropriate index to insert the key)
- Duplication Test: Insert a key that is already in the table
- Deletion Test: Delete a key that is in the table or not in the table
- Search Test: Search for a key that is in the table, not in the table or deleted from the table

##### Separate Chaining:

- Duplication Test: Insert a key that is already in the table
- Collision Test: Insert a key that the result of primary hashing gives collision (key should be inserted into the chain in descending order)
- Deletion Test: Delete a key that is in the table or not in the table
- Search Test: Search for a key that is in the table, not in the table or deleted from the table
- Print Test: Print a key from an empty chain / Print to check if the keys are ordered in a descending order

#### 5. Performance

Commands with a time complexity of  $O(1)$  are insert, search, and delete. A command "insert" inserts a new key into the hash table using the hash function. For both open addressing and separate chaining, assuming uniform hashing, finding the appropriate position to insert can be done in  $O(1)$ , and inserting key/value also has a time complexity of  $O(1)$ . Hence the resulting time complexity is  $O(1)$ . A command "search" searches a key from the hash table by utilizing the hash function. Assuming uniform hashing, a searching operation can be done in  $O(1)$  for both open addressing and separate chaining. Finally, the command "delete" deletes a key from the hash table if it exists. Since it behaves like a "search" except for deleting the found key from the table, considering that deleting the key is executed with the time complexity of  $O(1)$ , deleting operation can also achieve a time complexity of  $O(1)$ .

Command "print" can't achieve a constant time complexity since it needs to traverse the whole chain to print out all the keys. Hence, assuming uniform hashing, the length of each chain will be  $n/m$ . Then, the time complexity would be  $O(n/m)$ .