WIA / WIB 1002 Graph

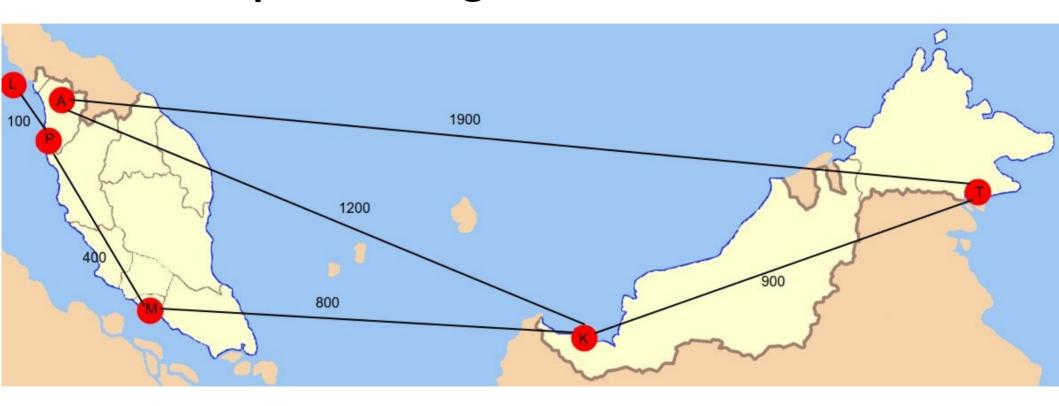
Content

- Concept of Graph
- Modeling Graphs
- Implementation of Graphs
- Graphs Travelsal

Graph

- A concept in mathematics, also a data structure.
- A set of vertices, V and edges, G=(V,E).
- In graph-like problems, these components have natural correspondences to problem elements
 - Entities are nodes and interactions between entities are edges
 - Many complex systems are graph-like.

Example – Flights between cities

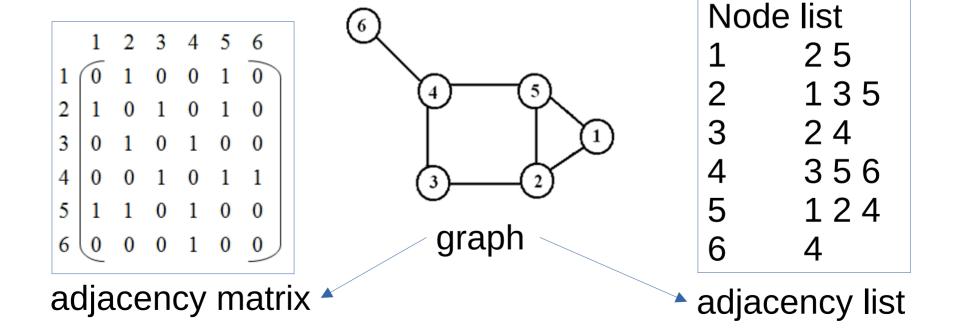


Graph

- 2 vertices are "adjacent" to each other if they share the same edge.
- If, from vertex p, after travel along 1 or more edges, we eventually reach vertex q, we say there is a "path" from p to q.
- Can be directed or undirected.
- Can be unweighted or weighted
 - Each edge in a weighted graph carries a value weight of the edge.

Modelling Graphs

 There are many ways to model graphs in mathematics, among all: adjacency matrix and adjacency list



Representing Vertices

- Vertices can be represented with Array, ArrayList or Linked-list.
- Array implementation is easy but less flexible
- Using ArrayList:

```
// Class City has created before this line
ArrayList<City> vertices = new ArrayList<City>();
vertices.add("Seattle");
vertices.add("San Francisco");
vertices.add("Los Angeles");
........
```

Representing Edges: matrix

- Can be implemented with adjacency matrix or adjacency list.
- For adjacency matrix implementation, a 2D array with value 1 and 0 is used to show the presence of an edge.
- If the graph has n vertices, the size of the matrix is nXn.
- e.g: edge[2][5] =1 and edge[2][6] = 0 means vertices[2] is adjacent to vertices[5] but not vertices[6].
- For weighted graphs, the values are replaced with the weight of the edges

Representing Edges: matrix

1900

1200

800

```
int[][] adjacencyMatrix = {
      { 0, 1, 0, 0, 0, 1}, // Alor Setar
      { 1, 0, 0, 1, 0, 1}, // Kuching
      { 0, 0, 0, 0, 1, 0}, // Langkawi
      { 0, 1, 0, 0, 1, 0}, // Melaka
      { 0, 0, 1, 1, 0, 0}, // Penang
      { 1, 1, 0, 0, 0, 0} // Tawau
}
```

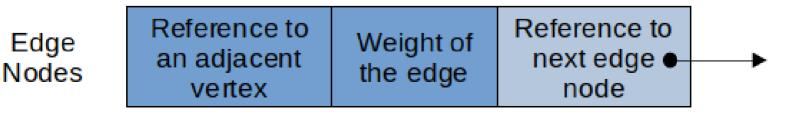
Representing Edges: matrix (directed and weighted)

Representing Edges: matrix

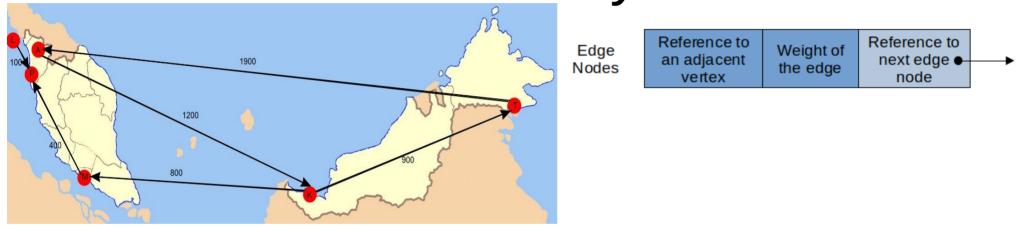
- Adjacency matrix is fast and easy to implement, but it needs large space to hold the matrix if n is large. (imagine a graph that represents "close contacts" for covid-19)
- If the number of edges is also large, we have a dense matrix, and it is justifiable.
- If only a few edges, we have sparse matrix (many elements with value 0), and it is a waste of memory space.
 - Should consider linked-list

Representing Edges: Linked-List

- One linked-list for each vertex.
- Each node in the linked list contains a reference to an adjacency vertex.
- Additional entry for weight if it is a weighted graph.

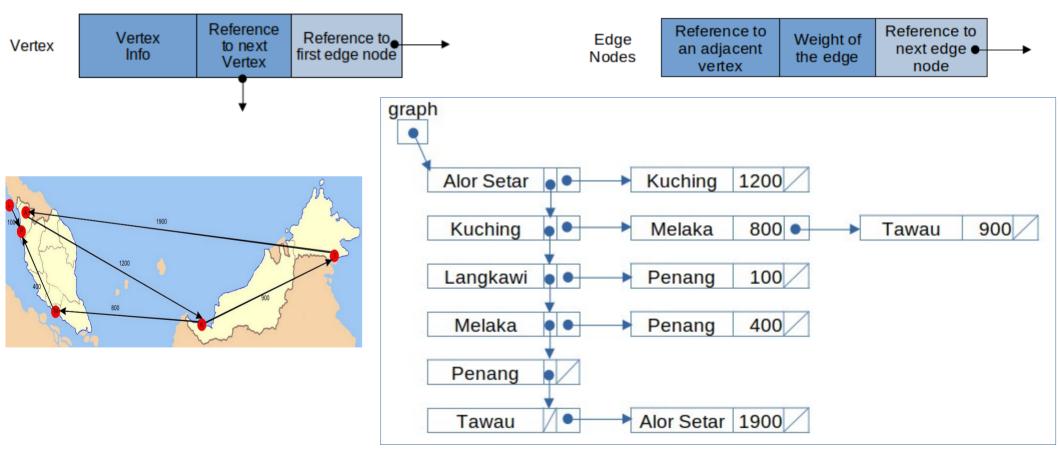


Representing Edges : Linked-List with array





Representing Edges: Linked-List (second way of implementation)



Implementing Graphs - vertex

```
class Vertex<T extends Comparable<T>, N extends Comparable <N>> {
  T vertexInfo;
   int indeg:
   int outdeg;
   Vertex<T,N> nextVertex;
   Edge<T,N> firstEdge:
   public Vertex() {
      vertexInfo=null;
      indeg=0;
      outdeg=0;
      nextVertex = null:
      firstEdge = null;
   public Vertex(T vInfo, Vertex<T,N> next) {
      vertexInfo = vInfo;
      indeg=0;
      outdeg=0;
      nextVertex = next;
      firstEdge = null;
```

Implementing Graphs - vertex

```
class Vertex<T extends Comparable<T>, N extends Comparable <N>> {
   T vertexInfo;
   int indeg:
                         Vertex info
   int outdeg:
   Vertex<T, N> nextVertex; Reference to next vertex
   Edge<T,N> firstEdge;
                          Reference to first edge node
   public Vertex() {
      vertexInfo=null;
      indeg=0;
      outdeg=0;
      nextVertex = null;
      firstEdge = null;
   public Vertex(T vInfo, Vertex<T,N> next) {
      vertexInfo = vInfo;
      indeg=0;
                                                                     Reference
                                                                             Reference to
                                                             Vertex
      outdeg=0;
                                                     Vertex
                                                                              first edge
                                                                      to next
                                                              Info
                                                                      Vertex
                                                                               node
      nextVertex = next:
      firstEdge = null;
```

Implementing Graphs – weighted edge

```
1 pclass Edge<T extends Comparable<T>, N extends Comparable <N>> {
 2
      Vertex<T,N> toVertex:
3
4
5
6
7
8
9
      N weight:
      Edge<T,N> nextEdge;
      public Edge() {
         toVertex = null;
         weight = null;
         nextEdge = null;
10
12 |
      public Edge(Vertex<T,N> destination, N w, Edge<T,N> a) {
13
         toVertex = destination:
14
         weight = w;
         nextEdge = a;
15
16
```

Implementing Graphs – weighted edge

```
1 pclass Edge<T extends Comparable<T>, N extends Comparable <N>> {
       Vertex<T,N> toVertex: ◀
 3
4
5
6
7
8
9
       N weight:
       Edge<T,N> nextEdge; ◀
       public Edge() {
          toVertex = null;
                                               Reference to
                                                                 Reference to
                                        Edge
                                                         Weight of
          weight = null;
                                               an adjacent
                                                                 next edge •
                                        Nodes
                                                         the edge
                                                                   node
                                                 vertex
          nextEdge = null;
10
12 =
       public Edge(Vertex<T,N> destination, N w, Edge<T,N> a) {
13
          toVertex = destination:
          weight = w;
14
          nextEdge = a;
16
```

Implementing Graphs - WeightedGraph

```
class Graph<T extends Comparable<T>, N extends Comparable <N>> {
    Vertex<T,N> head;
    int size;

public Graph() {
    head=null;
    size=0;
}
```

Get number of vertices

```
public int getSize()
  return this.size;
}
```

hasVertex – is this vertex in graph?

```
public boolean hasVertex(T v) {
                                           Compare: to determine whether
   if (head==null)
                                           it is the vertex we are looking for
      return false:
   Vertex<T,N> temp = head;
   while (temp!=null) {
      if ( temp.vertexInfo.compareTo( v ) == 0 )
         return true;
      temp=temp.nextVertex;
   return false;
```

get inDeg of a Vertex

get inDeg of a Vertex

```
public int getIndeg(T v) {
   if (hasVertex(v)==true) {
      Vertex<T,N> temp = head;
      while (temp!=null) {
      if ( temp.vertexInfo.compareTo( v ) == 0 )
           return temp.indeg;
      temp=temp.nextVertex;
   }
}
return -1;  Return -1 if cannot find
}
Get outDeg?
Try to code it!
```

```
public boolean addVertex(T v) {
   if (hasVertex(v)==false) {
      Vertex<T,N> temp=head;
      Vertex<T,N> newVertex = new Vertex<>(v, null);
      if (head==null)
         head=newVertex;
      else {
         Vertex<T,N> previous=head;;
         while (temp!=null) {
            previous=temp;
            temp=temp.nextVertex;
         previous.nextVertex=newVertex;
      size++;
      return true;
   else
      return false;
```

```
public boolean addVertex(T v) {
       if (hasVertex(v)==false) {
          Vertex<T,N> temp=head;
          Vertex<T,N> newVertex = new Vertex<>(v, null);
          if (head==null)
             head=newVertex;
The
          else {
vertex
             Vertex<T,N> previous=head;;
             while (temp!=null) {
is not
                 previous=temp;
in the
                 temp=temp.nextVertex;
graph
              previous.nextVertex=newVertex;
          size++;
          return true;
       else
                            Vertex is already in the graph
          return false;
```

```
public boolean addVertex(T v) {
       if (hasVertex(v)==false) {
          Vertex<T,N> temp=head;
          Vertex<T,N> newVertex = new Vertex<>(v, null);
          if (head==null)
                                          Graph is empty. Point head to this vertex
             head=newVertex;
The
          else {
vertex
             Vertex<T,N> previous=head;;
             while (temp!=null) {
is not
                 previous=temp;
in the
                 temp=temp.nextVertex;
graph
              previous.nextVertex=newVertex;
          size++;
          return true;
       else
                             Vertex is already in the graph
          return false;
```

```
public boolean addVertex(T v) {
       if (hasVertex(v)==false)
          Vertex<T,N> temp=head;
          Vertex<T,N> newVertex = new Vertex<>(v, null);
           if (head==null)
                                           Graph is empty. Point head to this vertex
              head=newVertex;
The
           else {
vertex
              Vertex<T,N> previous=head;;
              while (temp!=null) {
is not
                 previous=temp;
in the
                                                       Use previous to move to the last vertex
                 temp=temp.nextVertex;
graph
              previous nextVertex=newVertex;
                                                 Add the vertex as last in the list
          size++;
           return true;
       else
                              Vertex is already in the graph
           return false;
```

With the node information, find the index of the vertex

```
public int getIndex(T v) {
   Vertex<T,N> temp = head;
   int pos=0;
   while (temp!=null)
      if ( temp.vertexInfo.compareTo( v ) == 0 )
         return pos;
      temp=temp.nextVertex;
      pos+=1;
   return -1;
```

With the node information, find the index of the vertex

```
public int getIndex(T v) {
         Vertex<T,N> temp = head;
         int pos=0;
         while (temp!=null)
Loop
             if ( temp.vertexInfo.compareTo( v ) == 0 ) Vertex is found
to find
                return pos;
the
             temp=temp.nextVertex;
                                         Move temp to next vertex
vertex
             pos+=1;
         return -1;
```

Return all the vertex info to an ArrayList

```
public ArrayList<T> getAllVertexObjects() {
    ArrayList<T> list = new ArrayList<>();
    Vertex<T,N> temp = head;
    while (temp!=null) {
        list.add(temp.vertexInfo);
        temp=temp.nextVertex;
    }
    return list;
}
```

Return all the vertex info to an ArrayList

Return an ArrayList that stores T

```
public ArrayList<T> getAllVertexObjects() {
   ArrayList<T> list = new ArrayList<>();
   Vertex<T,N> temp = head;
   while (temp!=null) {
      list.add(temp.vertexInfo);
      temp=temp.nextVertex;
   }
   return list;
}
```

Use "add" method of ArrayList to add each vertex info

Get vertex info at a specific index/position

```
public T getVertex(int pos) {
   if (pos>size-1 || pos<0)
      return null;
   Vertex<T,N> temp = head;
   for (int i=0; i<pos; i++)
      temp=temp.nextVertex;
   return temp.vertexInfo;
}</pre>
```

Get vertex info at a specific index/position

```
public T getVertex(int pos) {
    if (pos>size-1 || pos<0)
        return null;

    Vertex<T,N> temp = head;
    for (int i=0; i<pos; i++)
        temp=temp.nextVertex;
    return temp.vertexInfo;
}</pre>
```

Check whether there is an edge

```
public boolean hasEdge(T source, T destination) {
   if (head==null)
      return false;
   if (!hasVertex(source) | !hasVertex(destination))
      return false:
  Vertex<T,N> sourceVertex = head;
   while (sourceVertex!=null) {
      if ( sourceVertex.vertexInfo.compareTo( source ) == 0 )
         // Reached source vertex, look for destination now
         Edge<T,N> currentEdge = sourceVertex.firstEdge;
         while (currentEdge != null) {
            if (currentEdge.toVertex.vertexInfo.compareTo(destination)==0)
            // destination vertex found
               return true;
            currentEdge=currentEdge.nextEdge;
      sourceVertex=sourceVertex.nextVertex;
   return false;
```

Check whether there is an edge

```
Graph is public boolean hasEdge(T source, T destination) {
           ▶if (head==null)
empty
               return false:
           if (!hasVertex(source) | !hasVertex(destination))
               return false:
No such
            Vertex<T,N> sourceVertex = head;
vertices
            while (sourceVertex!=null) {
               if ( sourceVertex.vertexInfo.compareTo( source ) == 0 )
                  // Reached source vertex, look for destination now
                  Edge<T,N> currentEdge = sourceVertex.firstEdge;
                  while (currentEdge != null) {
Search
                     if (currentEdge.toVertex.vertexInfo.compareTo(destination)==0)
for the
                     // destination vertex found
                        return true;
edge in
                     currentEdge=currentEdge.nextEdge;
valid
condition
               sourceVertex=sourceVertex.nextVertex;

    Find no such edge

            return false;
                                   in previous loop
```

Check whether there is an edge

```
Source vertex found.
         public boolean hasEdge(T source, T destination) {
                                                                    Create an edge reference
            if (head==null)
                                                                    here and look for
               return false:
                                                                    destination vertex in the
            if (!hasVertex(source) | !hasVertex(destination))
               return false:
                                                                    second while loop
            Vertex<T,N> sourceVertex = head;
            while (sourceVertex!=null) {
               if ( sourceVertex.vertexInfo.compareTo( source ) == 0 )
                  // Reached source vertex, look for destination now
If the
                  Edge<T,N> currentEdge = sourceVertex.firstEdge;
source
                  while (currentEdge != null) {
vertex is not
                     if (currentEdge.toVertex.vertexInfo.compareTo(destination)==0)
                     // destination vertex found
found, go to
                         return true;
next
                     currentEdge=currentEdge.nextEdge;
iteration of
outer while
               sourceVertex=sourceVertex.nextVertex;
loop
            return false;
```

Add a new edge from source to destination, with a weight

```
public boolean addEdge(T source, T destination, N w)
  if (head==null)
      return false:
  if (!hasVertex(source) | !hasVertex(destination))
     return false:
  Vertex<T,N> sourceVertex = head;
  while (sourceVertex!=null) {
      if ( sourceVertex.vertexInfo.compareTo( source ) == 0 )
        // Reached source vertex, look for destination now
        Vertex<T.N> destinationVertex = head;
        while (destinationVertex!=null) {
            if ( destinationVertex.vertexInfo.compareTo( destination ) == 0 ) {
              // Reached destination vertex, add edge here
               Edge<T,N> currentEdge = sourceVertex.firstEdge;
               Edge<T,N> newEdge = new Edge<>(destinationVertex, w, currentEdge);
               sourceVertex.firstEdge=newEdge;
               sourceVertex.outdeg++;
               destinationVertex.indeg++;
               return true;
           destinationVertex=destinationVertex.nextVertex:
      sourceVertex=sourceVertex.nextVertex:
  return false:
```

Add a new edge from source to destination, with a weight

if (!hasVertex(source) | !hasVertex(destination)) return false: Vertex<T.N> sourceVertex = head: while (sourceVertex!=null) { if (sourceVertex.vertexInfo.compareTo(source) == 0) { // Reached source vertex, look for destination now Only this Vertex<T,N> destinationVertex = head; while (destinationVertex!=null) part is if (destinationVertex.vertexInfo.compareTo(destination) == 0) { different // Reached destination vertex, add edge here Edge<T,N> currentEdge = sourceVertex.firstEdge; from Edge<T,N> newEdge = new Edge<>(destinationVertex, w, currentEdge); "hasEdge". sourceVertex.firstEdge=newEdge; sourceVertex.outdeg++; destinationVertex.indeg++; This block return true; loop to find destinationVertex=destinationVertex.nextVertex: destination vertex in sourceVertex=sourceVertex.nextVertex; the nested return false:

public boolean addEdge(T source, T destination, N w)

if (head==null) return false:

while

Add a new edge from source to destination, with a weight

Create

"ref to

edge"

point to

39 / 55

next

list

```
Create an
edge pointer,
and point to
             // Reached source vertex, look for destination now
edges list
              Vertex<T,N> destinationVertex = head;
which the
                                                                                         the edge.
              while (destinationVertex!=null) {
source
                                                                                         Let the
                 if ( destinationVertex.vertexInfo.compareTo( destination ) == 0 )
vertex is
                    // Reached destination vertex, add edge here
pointing to
                    Edge<T,N> currentEdge = sourceVertex.firstEdge;
                    Edge<T,N> newEdge = new Edge<>(destinationVertex, w, currentEdge);
                    sourceVertex.firstEdge=newEdge;
                                                                                         the edges
                  sourceVertex.outdeg++;
                                                          Let the source vertex
                  destinationVertex.indeg++;
Add 1 to in
                                                          point to the new edge
and out
                    return true;
                                                          object
degree
```

destinationVertex=destinationVertex.nextVertex; Reference to Reference to Weight of Edge an adjacent next edge • Nodes the edge node vertex

Retrieve the weight of an Edge

```
public N getEdgeWeight(T source, T destination) {
  N notFound=null;
   if (head==null)
      return notFound;
   if (!hasVertex(source) || !hasVertex(destination))
      return notFound;
  Vertex<T,N> sourceVertex = head;
   while (sourceVertex!=null) {
      if ( sourceVertex.vertexInfo.compareTo( source ) == 0 )
         // Reached source vertex, look for destination now
         Edge<T,N> currentEdge = sourceVertex.firstEdge;
         while (currentEdge != null) {
            if (currentEdge.toVertex.vertexInfo.compareTo(destination)==0)
            // destination vertex found
               return currentEdge.weight;
            currentEdge=currentEdge.nextEdge;
      sourceVertex=sourceVertex.nextVertex;
   return notFound;
```

Retrieve the weight of an Edge

Quite similar to hasEdge

Edge found, return weight

```
public N getEdgeWeight(T source, T destination) {
   N notFound=null;
   if (head==null)
      return notFound;
   if (!hasVertex(source) || !hasVertex(destination))
      return notFound:
   Vertex<T,N> sourceVertex = head;
   while (sourceVertex!=null) {
      if ( sourceVertex.vertexInfo.compareTo( source ) == 0 )
         // Reached source vertex, look for destination now
         Edge<T,N> currentEdge = sourceVertex.firstEdge;
         while (currentEdge != null) {
         if (currentEdge.toVertex.vertexInfo.compareTo(destination)==0)
            // destination vertex found
               return currentEdge.weight;
            currentEdge=currentEdge.nextEdge;
      sourceVertex=sourceVertex.nextVertex;
   return notFound;
```

Return all the neighbours of a vertex to an ArrayList

```
public ArrayList<T> getNeighbours (T v) {
   if (!hasVertex(v))
      return null;
  ArrayList<T> list = new ArrayList<T>();
  Vertex<T,N> temp = head;
  while (temp!=null)
      if ( temp.vertexInfo.compareTo( v ) == 0 )
         // Reached vertex, look for destination now
         Edge<T,N> currentEdge = temp.firstEdge;
        while (currentEdge != null) {
            list.add(currentEdge.toVertex.vertexInfo);
            currentEdge=currentEdge.nextEdge;
      temp=temp.nextVertex;
   return list;
```

Return all the neighbours of a vertex to an ArrayList

Outer
while: loop
to find the
vertex, and
create a ref
to edge if
found

```
public ArrayList<T> getNeighbours (T v) {
   if (!hasVertex(v))
      return null;
  ArrayList<T> list = new ArrayList<T>();
   Vertex<T,N> temp = head;
  while (temp!=null)
      if ( temp.vertexInfo.compareTo( v ) == 0 )
         // Reached vertex, look for destination now
         Edge<T,N> currentEdge = temp.firstEdge;
        while (currentEdge != null) {
            list.add(currentEdge.toVertex.vertexInfo);
            currentEdge=currentEdge.nextEdge;
      temp=temp.nextVertex;
   return list;
```

Nested while: read edges and add to ArrayList

Print graph

```
public void printEdges() {
  Vertex<T,N> temp=head;
   while (temp!=null) {
      System.out.print("# " + temp.vertexInfo + " : " );
      Edge<T,N> currentEdge = temp.firstEdge;
      while (currentEdge != null) {
         System.out.print("[" + temp.vertexInfo + ","
            + currentEdge.toVertex.vertexInfo +"] " );
         currentEdge=currentEdge.nextEdge;
      System.out.println();
      temp=temp.nextVertex;
```

Print graph

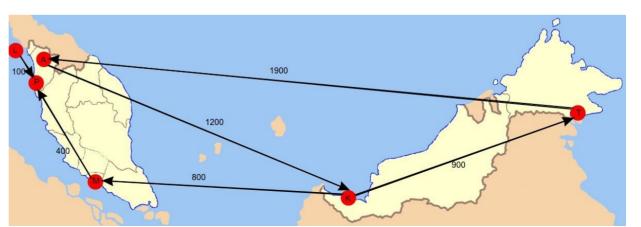
```
public void printEdges() {
                Vertex<T,N> temp=head;
Print a vertex
                while (temp!=null) {
                 System.out.print("# " + temp.vertexInfo + " : " );
                   Edge<T,N> currentEdge = temp.firstEdge;
  Print edges
                   while (currentEdge != null) {
                    System.out.print("[" + temp.vertexInfo + ","
  in a nested
                         + currentEdge.toVertex.vertexInfo +"] " );
  loop
                      currentEdge=currentEdge.nextEdge;
                   System.out.println();
                   temp=temp.nextVertex;
```

Test Program

```
public class TestWeightedGraph {
  public static void main(String[] args) {
     WeightedGraph<String, Integer> graph1 = new WeightedGraph<>();
     String[] cities = {"Alor Setar", "Kuching", "Langkawi", "Melaka", "Penang", "Tawau"};
     for (String i : cities)
        graph1.addVertex(i):
     System.out.println("The number of vertices in graph1: " + graph1.getSize());
     System.out.println("Cities and their vertices ");
     for (int i = 0; i<=graph1.getSize()-1; i++)</pre>
        System.out.print( i + ": " + graph1.getVertex(i) + "\t");
     System.out.println();
     System.out.println("Is Melaka in the Graph? " + graph1.hasVertex("Melaka"));
     System.out.println("Is Ipoh in the Graph? " + graph1.hasVertex("Ipoh"));
     System.out.println();
     System.out.println("Kuching at index: " + graph1.getIndex("Kuching"));
     System.out.println("Ipoh at index: " + graph1.getIndex("Ipoh"));
     System.out.println();
     System.out.println("add edge Kuching - Melaka: " + graph1.addEdge("Kuching", "Melaka", 800) );
     System.out.println("add edge Langkawi - Penang : " + graph1.addEdge("Langkawi", "Penang", 100) );
     System.out.println("add edge Melaka - Penang : " + graph1.addEdge("Melaka", "Penang", 400) );
     System.out.println("add edge Alor Setar - Kuching: " + graph1.addEdge("Alor Setar", "Kuching", 1200) );
     System.out.println("add edge Tawau - Alor Setar : " + graph1.addEdge("Tawau", "Alor Setar", 1900) );
System.out.println("add edge Kuching - Tawau : " + graph1.addEdge("Kuching", "Tawau", 900) );
     System.out.println("add edge Langkawi - Ipoh : " + graph1.addEdge("Langkawi", "Ipoh", 200) );
     Svstem.out.println();
                                                                                                                     46 / 55
```

Test Program

```
" + graph1.hasEdge("Kuching", "Melaka") );
" + graph1.hasEdge("Melaka", "Kuching") );
System.out.println("has edge from Kuching to Melaka?
System.out.println("has edge from Melaka to Langkawi?
System.out.println("has edge from Ipoh to Langkawi? " + graph1.hasEdge("Ipoh", "Langkawi"));
System.out.println():
System.out.println("weight of edge from Kuching to Melaka? " + graph1.getEdgeWeight("Kuching", "Melaka") );
System.out.println("weight of edge from Tawau to Alor Setar? " + graph1.getEdgeWeight("Tawau", "Alor Setar") );
System.out.println("weight of edge from Semporna to Ipoh? " + graph1.getEdgeWeight("Semporna", "Ipoh"));
System.out.println();
System.out.println("In and out degree for Kuching is " + graph1.getIndeg("Kuching") + " and " + graph1.getOutdeg("Kuching") );
System.out.println("In and out degree for Penang is " + graph1.getIndeg("Penang") + " and " + graph1.getOutdeg("Penang"));
System.out.println("In and out degree for Ipoh is " + graph1.getIndeg("Ipoh") + " and " + graph1.getOutdeg("Ipoh") );
System.out.println();
System.out.println("Neighbours of Kuching : " + graph1.getNeighbours("Kuching"));
System.out.println("\nPrint Edges : " );
graph1.printEdges();
```

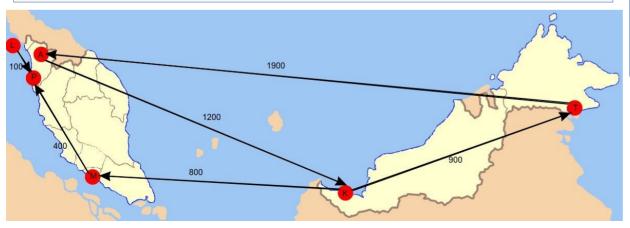


Test Program - output

```
The number of vertices in graph1: 6
Cities and their vertices
0: Alor Setar 1: Kuching 2: Langkawi 3: Melaka 4: Penang 5: Tawau
Is Melaka in the Graph? true
Is Ipoh in the Graph? false

Kuching at index: 1
Ipoh at index: -1

add edge Kuching - Melaka: true
add edge Langkawi - Penang : true
add edge Melaka - Penang : true
add edge Alor Setar - Kuching : true
add edge Tawau - Alor Setar : true
add edge Kuching - Tawau : true
add edge Langkawi - Ipoh : false
```



```
has edge from Kuching to Melaka? true
has edge from Melaka to Langkawi? false
has edge from Ipoh to Langkawi? false
weight of edge from Kuching to Melaka? 800
weight of edge from Tawau to Alor Setar? 1900
weight of edge from Semporna to Ipoh? null
In and out degree for Kuching is 1 and 2
In and out degree for Penang is 2 and 0
In and out degree for Ipoh is -1 and -1
Neighbours of Kuching : [Tawau, Melaka]
Print Edges :
# Alor Setar : [Alor Setar, Kuching]
# Kuching : [Kuching, Tawau] [Kuching, Melaka]
# Langkawi : [Langkawi, Penang]
# Melaka : [Melaka,Penang]
# Penang:
# Tawau : [Tawau,Alor Setar]
```

Graph Traversals

- Also called graph search.
- The process of visiting (checking and/or updating) each vertex in a graph
- Depth-first search and breadth-first search
- Both traversals result in a spanning tree, which can be modeled using a class.

Depth-First Search

- The search can start at any vertex.
- Algorithm:
 - 1. Start by putting any one of the graph's vertices on top of a stack.
 - 2. Take the top item of the stack and add it to the visited list.
 - 3. Create a list of that vertex's adjacent nodes. Add the ones which aren't in the visited list to the top of the stack.
 - 4. Keep repeating steps 2 and 3 until the stack is empty.

Applications of the DFS

- Detecting whether a graph is connected. Search the graph starting from any vertex. If the number of vertices searched is the same as the number of vertices in the graph, the graph is connected.
 Otherwise, the graph is not connected.
- Detecting whether there is a path between two vertices.
- Finding a path between two vertices.
- Detecting whether there is a cycle in the graph.

Breadth-First Search

 With breadth-first traversal of a tree, the nodes are visited level by level. First the root is visited, then all the children of the root, then the grandchildren of the root from left to right, and so on.

Breadth-First Search

Algorithm:

- 1. Start by putting any one of the graph's vertices at the back of a **queue**.
- 2. Take the front item of the queue and add it to the visited list.
- 3. Create a list of that vertex's adjacent nodes. Add the ones which aren't in the visited list to the back of the queue.
- 4. Keep repeating steps 2 and 3 until the queue is empty.

Applications of the BFS

- Quite similar to DFS, but:
 - BFS able to find the path with smallest edges count (not weight/cost/distance) between 2 vertices.
 - It is easy to use BFS to check whether a graph is bipartite. A graph is bipartite if the vertices of the graph can be divided into two disjoint sets such that no edges exist between vertices in the same set.
 - BFS is inefficient in terms of memory consumption, compared to DFS.

End