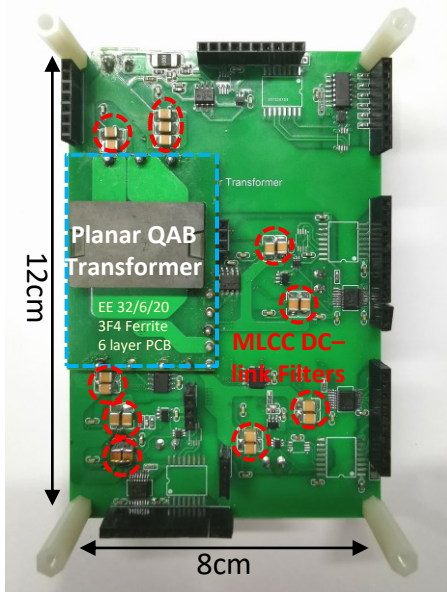
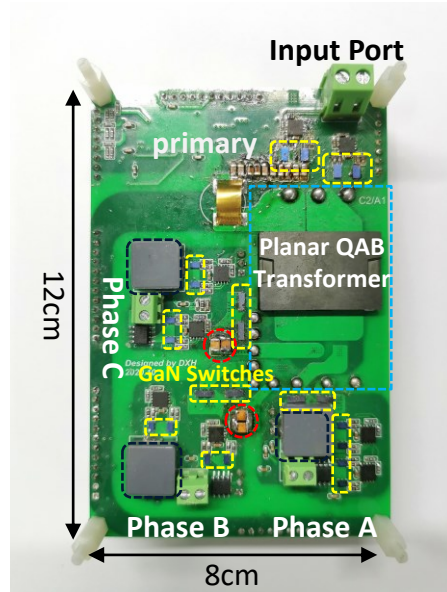
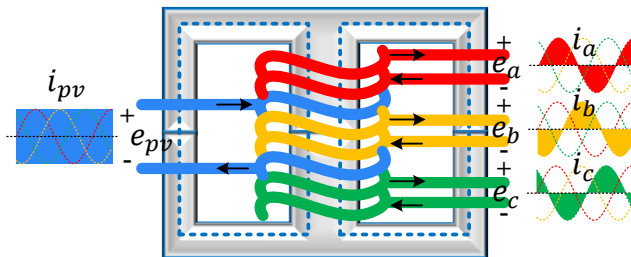
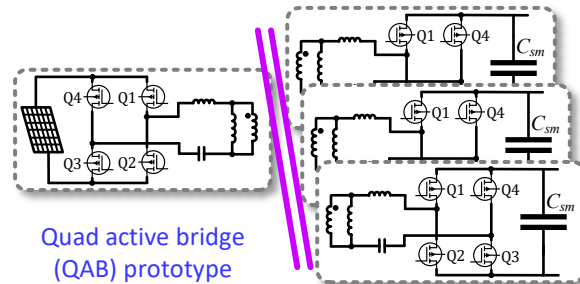
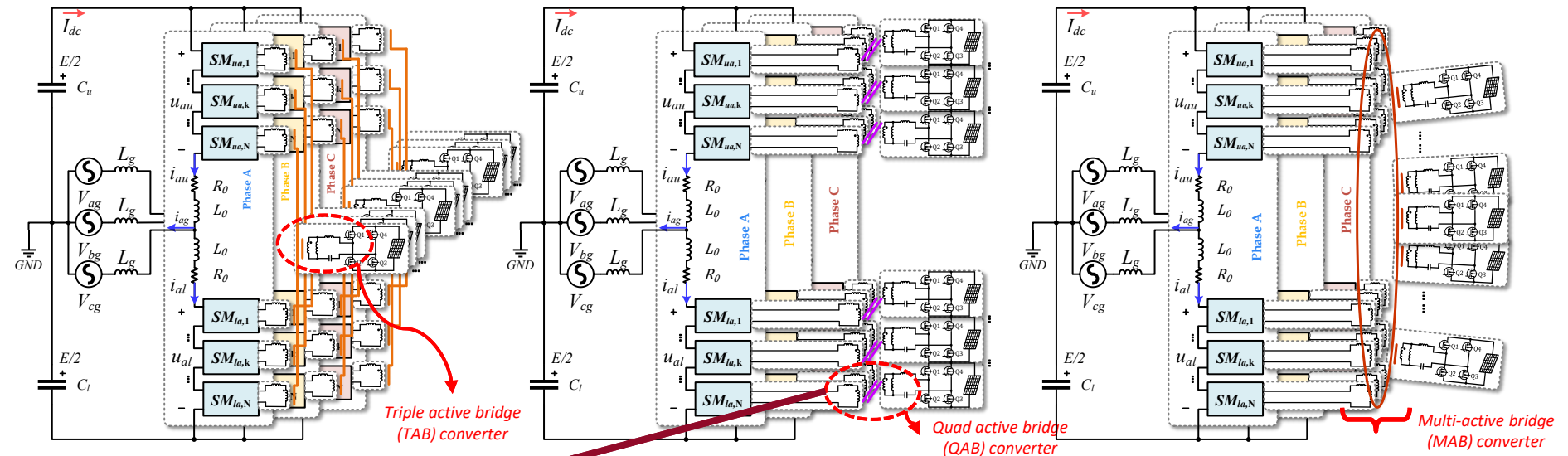


# Research #2: Three-phase MMC PV inverter with Multi-Active Bridge

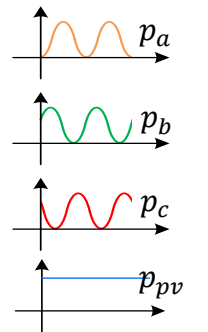


Magnetic Coupled Multilevel-modular Converter (MMC)



$$\begin{cases} p_a = P_a - p_{a2\omega} = \frac{UI}{2} [\cos \varphi - \cos(2\omega t - \beta)] = P_{p,a} - P_{a,b} + P_{c,a} \\ p_b = P_b - p_{b2\omega} = \frac{UI}{2} \left[ \cos \varphi - \cos \left( 2\omega t - \beta + \frac{2}{3}\pi \right) \right] = P_{p,b} + P_{a,b} - P_{b,c} \\ p_c = P_c - p_{c2\omega} = \frac{UI}{2} \left[ \cos \varphi - \cos \left( 2\omega t - \beta - \frac{2}{3}\pi \right) \right] = P_{p,c} + P_{b,c} - P_{c,a} \end{cases}$$

$$p_{pv} = p_a + p_b + p_c = \frac{3}{2} UI$$



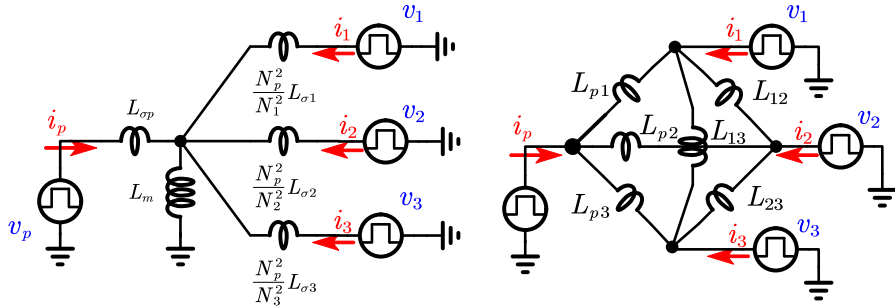
- The fundamental and 2<sup>nd</sup> order harmonic frequency current components in the arm current are 120° phase shifted in three phases.
- From the perspective of instantaneous power, the constant PV power can be inherently distributed to three phases without power fluctuation.

# Research #2: Three-phase MMC PV inverter with Multi-Active Bridge



Queen's  
UNIVERSITY

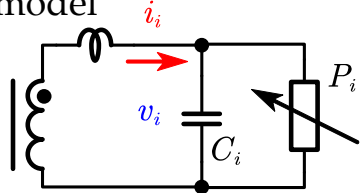
QAB model



$$I_i = \frac{-\sum_{j=1}^n P_{ij}}{V_i} = \sum_{j=1}^n \frac{V_j}{4fL_{ij}} d_{ij} (|d_{ij}| - 1)$$

$$\hat{i}_i = \sum_{j=1}^n G_v(i, j) \hat{v}_j + \sum_{j=1}^n G_d(i, j) \hat{d}_j$$

Submodule model



$$i_i = \frac{v_i}{1/s C_i} + \frac{P_i}{v_i} \text{ (nonlinear constant power load)}$$

$$i_i = \frac{V_i}{1/s C_i} + \frac{P_i}{V_{dc}} + \frac{P_i}{-V_{dc}^2} (v_i - V_{dc}) \text{ (fourier expansion)}$$

$$\hat{i}_i = \left( \frac{1}{1/s C_i} - \frac{P_i}{V_{dc}^2} \right) \hat{v}_i$$

Negative  
Resistance

Small-signal dynamics

$$G_v = \begin{bmatrix} 0 & \dots & \frac{d_{1j}}{4fL_{1j}} (|d_{1j}| - 1) & \dots & \frac{d_{1n}}{4fL_{1n}} (|d_{1n}| - 1) \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \frac{d_{i1}}{4fL_{i1}} (|d_{i1}| - 1) & \dots & \frac{d_{ij}}{4fL_{ij}} (|d_{ij}| - 1) \forall [i \neq j] & \dots & \frac{d_{in}}{4fL_{in}} (|d_{in}| - 1) \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \frac{d_{jn}}{4fL_{jn}} (|d_{jn}| - 1) & \dots & \frac{d_{nj}}{4fL_{nj}} (|d_{nj}| - 1) & \dots & 0 \end{bmatrix}$$

$$G_d = \begin{bmatrix} \sum_{k \neq 1} \frac{V_k}{4fL_{1k}} (2|d_{1k}| - 1) & \dots & \frac{V_j}{4fL_{1j}} (1 - 2|d_{1j}|) & \dots & \frac{V_n}{4fL_{1n}} (1 - 2|d_{1n}|) \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \frac{V_i}{4fL_{i1}} (1 - 2|d_{i1}|) & \dots & \frac{V_j}{4fL_{ij}} (1 - 2|d_{ij}|) \forall [i \neq j] & \dots & \frac{V_n}{4fL_{in}} (1 - 2|d_{in}|) \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ \frac{V_i}{4fL_{n1}} (1 - 2|d_{n1}|) & \dots & \frac{V_j}{4fL_{ni}} (1 - 2|d_{ni}|) & \dots & \sum_{k \neq n} \frac{V_k}{4fL_{nk}} (2|d_{nk}| - 1) \end{bmatrix}$$

$$G_z = G_v = \text{diag} \left[ 1 / \left( \frac{1}{1/s C_1} - \frac{P_1}{V_{dc}^2} \right) \quad \dots \quad 1 / \left( \frac{1}{1/s C_i} - \frac{P_i}{V_{dc}^2} \right) \quad \dots \quad 1 / \left( \frac{1}{1/s C_n} - \frac{P_n}{V_{dc}^2} \right) \right]$$

$$\begin{cases} \hat{i} = G_v \times \hat{v} + G_d \times \hat{d}, \\ \hat{v} = G_z \times \hat{i}. \end{cases}$$

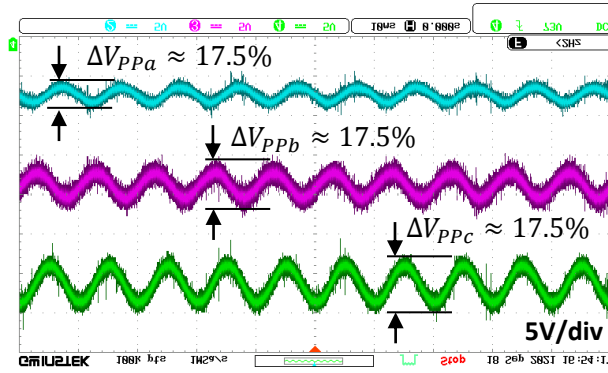
$$\hat{v} = G_z (I - G_v G_z)^{-1} G_d \times \hat{d} = G_s \times \hat{d}$$

$$G_v(i, j) = \frac{d_{ij}}{4fL_{ij}} (|d_{ij}| - 1)$$

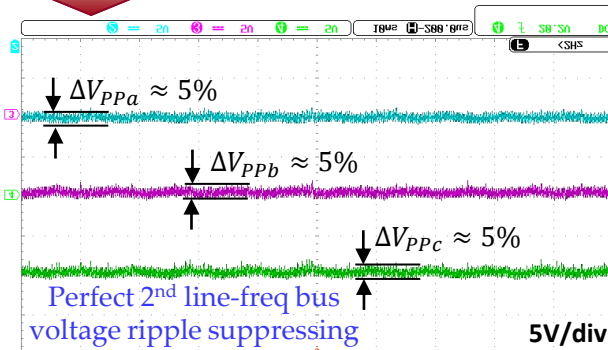
$$G_d(i, j) = \begin{cases} \frac{V_j}{4fL_{ij}} (1 - 2|d_{ij}|) & j \neq i, \\ \sum_{k \neq i} \frac{V_k}{4fL_{ik}} (2|d_{ik}| - 1) & j = i. \end{cases}$$

With system transfer function  $G_s(s)$ , it is possible to design the control system with power decoupling function to trace each phase power.

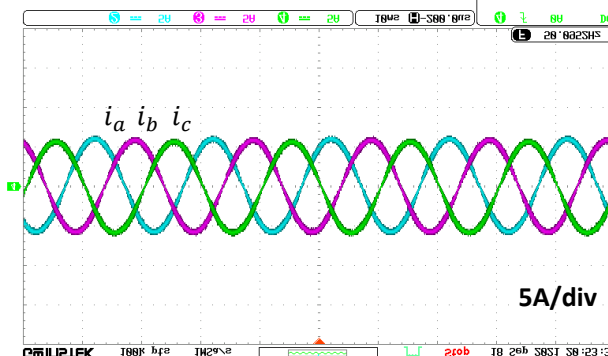
# Research #2: Three-phase MMC PV inverter with Multi-Active Bridge



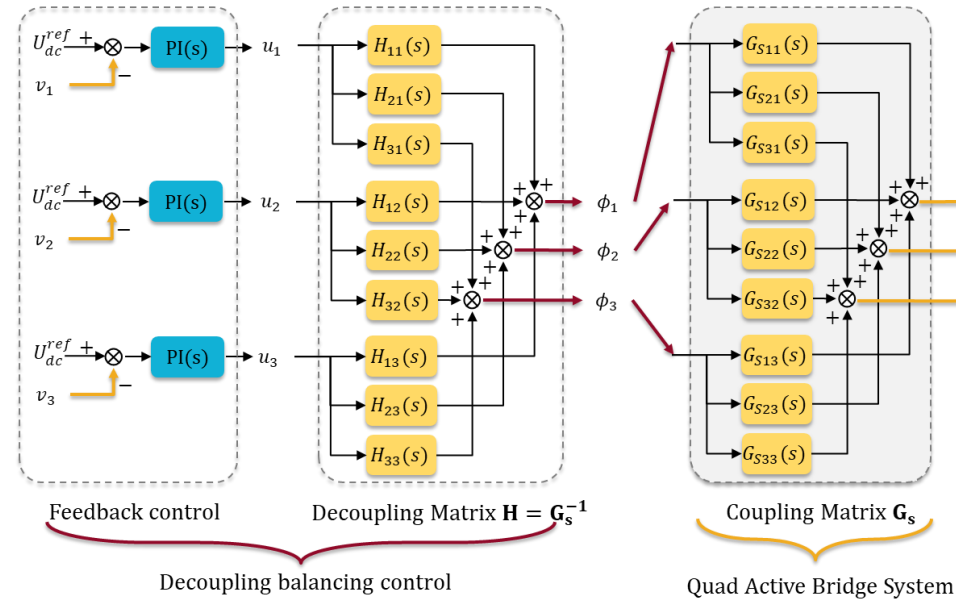
Enable QAB active phase-shift



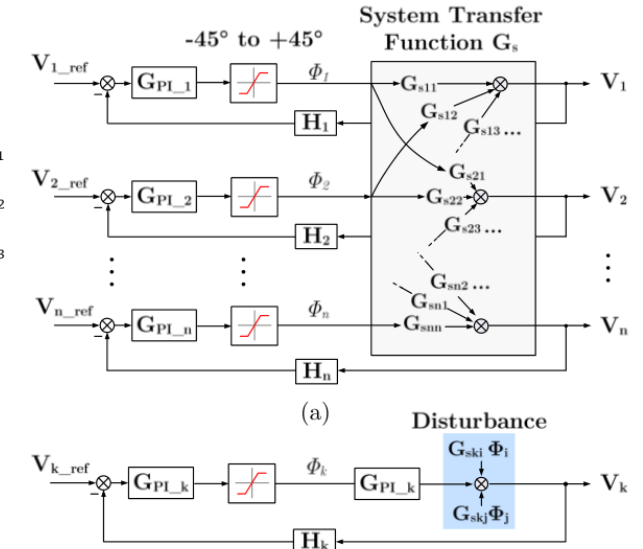
Three-phase dc-link capacitor voltage



Three-phase inverted grid current



Proposed decoupling phase-shifting control



Traditional coupled phase-shifting control

- Compared with non-phase shift QAB, the applying of voltage balancing phase shift have perfect 2<sup>nd</sup> line-frequency voltage ripple reduction.
- The decoupling is implemented by adopting **inverse matrix** of the system dynamic model  $\mathbf{G}_s(s)$ , but the choice of decoupling matrix is not unique.
- Compared with traditional MAB coupled phase-shifting balancing control, the proposed decoupling phase shift control has perfect power distribution on each phase with desired inverted grid current.