STAT 511 FINAL EXAM SOLUTIONS

SPRING 2010

$$|a|$$
 $1+6+2.5=9.5$

b)
$$t = 0.602$$
 df = $60 - 4 = 56$
 p -value = 0.55

The mean response for Treatment 1 was not significantly different from 0.

C) EFFECT DIFF ESTIMATE SE t-stat PE0.05
$$1-2 -4 2.036 -1.965 N_0$$

$$1-3 -6 2.036 -2.948 YES$$

$$2-3 -2 2.036 -2/2.036 N_0$$

d)
$$drug^2 = \sqrt{.2. - 1.1}$$

 $\hat{V}_{av}(drus^2) = \hat{\sigma}_{30}^2 + \hat{\sigma}_{30}^2 = \hat{\sigma}_{15}^2$

Thus,
$$\hat{G}^2 = (1.662 \sqrt{15})^2$$

$$C)\left[\frac{\mathbb{I}\otimes 1}{6\times 6}, \frac{\mathbb{I}\otimes 1}{4\times 1}, \frac{\mathbb{I}\otimes 1}{2\times 12}, \frac{1}{2\times 1}\right]$$

d)
$$\sigma_s^2$$
 = Variance of subject random effects

 σ_r^2 = Variance of ear vandom effects

 σ_e^2 = Error Variance.

e)
$$65 + 67 + 62$$

$$f) \frac{\sigma_s^2 + \sigma_r^2}{\sigma_s^2 + \sigma_r^2 + \sigma_e^2}$$

- $\frac{25}{\sigma_s^2 + \sigma_r^2 + \sigma_e^2}$
- 2 h) There is a Mean for each combination of heaving aid and test. We should expect the pre-test means to be identical across hearing aid types because the pretest data is collected before the heaving aids are placed. Thus, rather than 6 means, we should have only 4 (pretest and postest for each of the 3 hearing aid types).

3. a) Model 2

b) $128.10 - 2(11) + \log(20)(11)$

c) i. 42.834-14.397

ic. 11-1=10

iii. Model 2 does fit significantly better. The test stat is far bigger than 18.307 = 2,0(.95).

d) i. 38.69 - 14,397

ii. 11-2=9

iii. Again Model 2 fits significantly better. 3 e) The mean number of infected cells for plants of Genotype 2 was estimated to be exp? 0.224503 times the mean number of infected cells for plants of genotype 1.

3+) exp { 2.68785 + 0.22450}

4. (x'X + x^D) - 1 X'Y where D = [89]

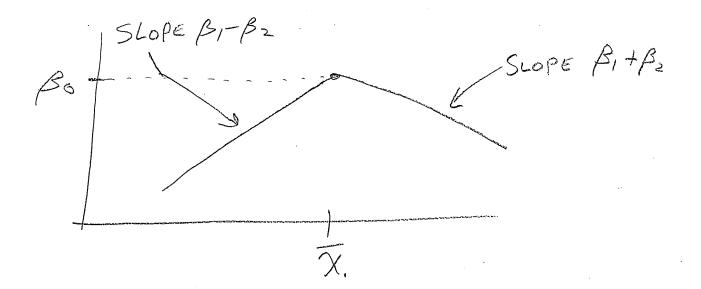
 $\chi'\chi = \left\{ \begin{array}{c} \gamma \\ \gamma \\ \gamma \end{array} \right\} \left(\gamma_i - \overline{\chi}_i \right)^2$

 $\frac{1}{2} = \frac{1}{2} \frac{$

 $\sum_{i=1}^{N} (x_i - \overline{x}_i) y_i$ $\sum_{i=1}^{N} (x_i - \overline{x}_i)^2 + \lambda^2$

5.
$$\beta_0 + \beta_1 (x_i - \overline{x}_i) + \beta_2 | x_i - \overline{x}_i |$$

$$= \begin{cases} \beta_0 + (\beta_1 - \beta_2) (x_i - \overline{x}_i) & \text{if } x_i \leq \overline{x}_i \\ \beta_0 + (\beta_1 + \beta_2) (x_i - \overline{x}_i) & \text{if } x_i > \overline{x}_i \end{cases}$$



This is a continuous, piecewise linear spline function with a knot at X.

- 6 a) 0.1142
 - b) 0.0128
 - (2) (0.113 0.1142)
 - d) 0.1142 (0.1113 0.1142)
 - = 2(0.1142) 0.1113
 - e) 0.0898 to 0.1323